



# HSFM- ΣNN: Combining a Feedforward Motion Prediction Network and Covariance Prediction

A.Postnikov, A.Gamayunov, G.Ferrer

# Approach

**Human** beings tend to be **hardly predictable** on their decisions and motion. But properly predicted motion uncertainties can be used in many other fields.

 $\mathsf{HSFM}\text{-}\mathsf{\Sigma}\mathsf{NN}$  - proposed **method** of pedestrians **motion prediction with uncertainty estimation**.

HSFM- $\Sigma$ NN combines two different approaches: a model-based transition functions - **HSFM\*** and a shallow **Neural Network** (NN) for covariance prediction.

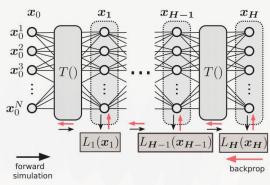


Fig.1 - The initial configuration  $x_0$  propagates through several layers, each representing the transition function T().

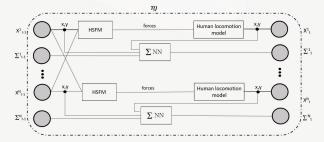


Fig.2 - Diagram of the proposed method, HSFM-ΣNN.

At each time-step the HSFM generates virtual forces, which are then integrated. Our approach combines this with a NN for covariance prediction.

<sup>\*</sup>Mehta, D., Ferrer, G., Olson, E. (2018, May). "Backprop-MPDM(ICRA) (pp. 1740-1746)





### Compared methods

A. Linearization and Covariance Forward-Propagation (FP)

$$x_{t+1} = T(\mu_t) + G_t(x_t - \mu_t)$$

B. Monte-Carlo(MC) Covariance Estimation

$$x_t^i \sim p(x_t), \quad i = 1, \dots, N, \ x_{t+1}^i = T(x_t^i)$$

C. Neural Network(**ΣNN**) Covariance Prediction

#### Shallow NN

Method	percent of predicted values inside $1\sigma$ ( $\Delta$ from expected)	percent of predicted values inside $3\sigma(\Delta \text{ from expected})$
LSTM	47.60 (-16.39)	69.74 (-28.25)
LSTM MC	37.16 (-26.83)	51.33 (-46.66)
HSFM MC	37.11 (-26.88)	60.98 (-37.01)
HSFM FP	6.06 (-57.93)	8.60 (-89.39)
HSFM-ΣNN	58.79 (-5.20)	85.45(-12.54)

Table.1 Comparison of calculated covariances

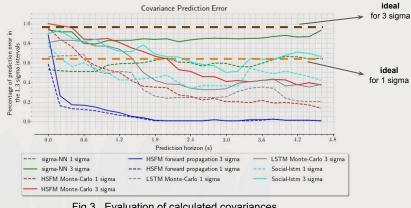


Fig.3 Evaluation of calculated covariances

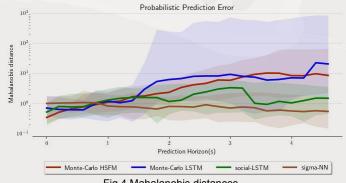


Fig.4 Mahalanobis distances



# Conclusions

- FP collapses linearization error & vanishing gradients
- MC expensive and underestimate uncertainties
- LSTM degrades over time, underestimate uncertainties
- HSFM-ΣNN (proposed) achieves consistent results, best predicted uncertainties

Aleksey Postnikov - postnikov.a.l@sberbank.ru Aleksander Gamayunov gamayunov.a.r@sberbank.ru Gonzalo Ferrer - g.ferrer@skoltech.ru