## 1 Non Intrusive Load Monitoring on REDD dataset

#### Version 0.2 Changelog

- Now uses Pandas for resampling, indexing, and most other Time Series operations. This fixes
  a bug earlier, where we downsampled based on the number of samples and not on the basis
  of time
- Added breakdown analysis showing daily variation and 6 hourly variation, also weekday vs weekend

#### 1.1 About the dataset

The datset contains high frequency, low frequency and raw data of 6 households in the USA. We choose House 2 for our analysis as it contains the least number of appliances. Further we choose to do the analysis of **low frequency** data. This house contains the following appliances/circuits:

- Kitchen
- Kitchen 2
- Stove
- Refrigerator
- Dishwasher
- Disposal
- Washer Dryer
- Microwave
- Lighting

These circuits are sampled once every 3-4 seconds. Also the house contains 2 mains which are sampled at 1 Hz.

#### 1.2 Basic imports

In this section we setup the basic imports which shall be required for performing the analysis.

```
import numpy as np
import matplotlib.pyplot as plt
import math
from scipy.cluster.vq import kmeans,vq
import itertools
import matplotlib
#Setting size of figures as 20*10
plt.figsize(20,10)
#Setting font size to be 16
matplotlib.rcParams.update({'font.size': 16})
```

```
import pandas as pd
from pandas import Series,DataFrame
plt.figsize(20,10)
import json
s = json.load( open("/home/nipun/bmh_matplotlibrc.json") )
matplotlib.rcParams.update(s)
matplotlib.rcParams.update({'font.size': 16})
```

### 1.3 Loading and Plotting of Mains Data

```
mains_1_data=np.loadtxt('/home/nipun/study/datasets/MIT/low_freq/house_2/channel_1.dat')
mains_2_data=np.loadtxt('/home/nipun/study/datasets/MIT/low_freq/house_2/channel_2.dat')
```

We can observe that data is missing towards the end. As a part of the data cleansing process we should eliminate the last indices. Next we find the last valid index for which contiguos data is present. This corresponds to epoch timestamp of 1304282291. Now we plot the cleaned data and also use Time for X axis representation.

```
upper=np.where(mains_1_data[:,0]==1304282291.0)[0]
lower=np.where(mains_1_data[:,0]>1303084800.0)[0][0]
mains_1_power=mains_1_data[:,1][lower:upper]
mains_2_power=mains_2_data[:,1][lower:upper]
timestamp=mains_1_data[:,0][lower:upper]
timestamp_mains_date=timestamp.astype('datetime64[s]')
```

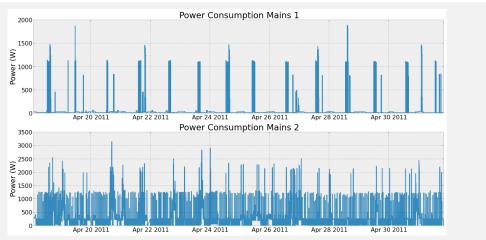
Overall statistics about the dataset.

```
df_mains=DataFrame({'Mains_1_Power':mains_1_power,'Mains_2_Power':mains_2_power},index=
    timestamp_mains_date)
 df_mains.describe()
      Mains_1_Power Mains_2_Power
          1162980.0 1162980.0
count
               43.4
                             187.5
mean
                             213.9
               148.2
std
               12.3
                              21.2
min
25%
               14.8
                              22.5
50%
               15.1
                             218.4
75%
               33.5
                             259.2
max
             1887.4
                             3149.0
```

Plotting overall power consumption for the two main circuits.

```
plt.subplot(2,1,1)
plt.plot(df_mains.index,df_mains.Mains_1_Power);
plt.title('Power Consumption Mains 1');
plt.ylabel('Power (W)');
plt.subplot(2,1,2)
plt.plot(df_mains.index,df_mains.Mains_2_Power);
plt.ylabel('Power (W)');
```

# plt.title('Power Consumption Mains 2');



#### 1.4 Downsampling Mains Data

Energy consumption (KWh) statistics about data.

#### df\_1\_day\_energy.describe()

```
Mains_1_Energy Mains_2_Energy
count
            14.000000
                             14.000000
             1.001500
                              4.326060
mean
std
             0.284175
                              0.739165
             0.739473
min
                              3.243120
25%
             0.766775
                              3.733631
50%
             0.870461
                              4.329253
75%
             1.264915
                              4.907687
max
             1.516066
                              5.567054
```

Plotting daily energy consumption.

```
def correct_labels(ax):
    labels = [item.get_text() for item in ax.get_xticklabels()]
    days=[label.split(" ")[0] for label in labels]
    months=["Jan","Feb","Mar","Apr","May","Jun","Jul","Aug","Sep","Oct","Nov","Dec"]
    final_labels=[]
    for i in range(len(days)):
        a=days[i].split("-")
        final_labels.append(a[2]+"\n"+months[int(a[1])-1])
```

```
ax.set_xticklabels(final_labels)
```

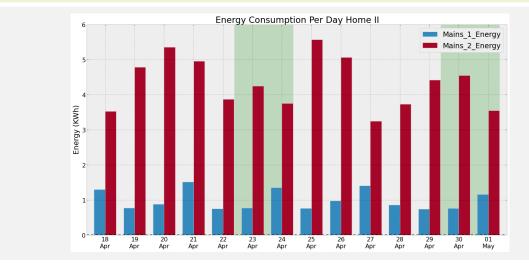
Function to find which of the days are weekdays and their indices

```
def find_weekend_indices(datetime_array):
    indices=[]
    for i in range(len(datetime_array)):
        if datetime_array[i].weekday()>=5:
            indices.append(i)
    return indices

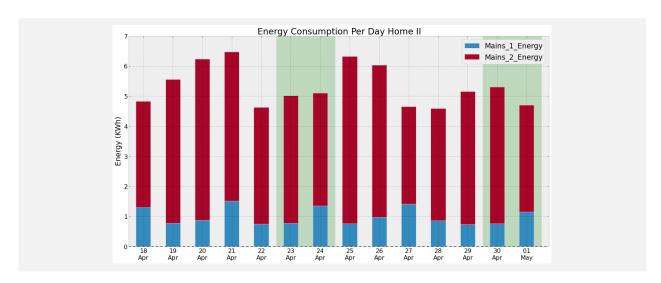
def highlight_weekend(weekend_indices,ax,ymax):
    i=0
    while i<len(weekend_indices):
        ax.fill_between([weekend_indices[i],weekend_indices[i]+2],ymax,facecolor='green',
            alpha=.2)
    i+=2</pre>
```

date\_range=[datetime.datetime(2011,4,18)+datetime.timedelta(days=i) for i in range(14)]
weekend\_indices=find\_weekend\_indices(date\_range)

```
ax=df_1_day_energy.plot(kind='bar',rot=0);
ax.set_title('Energy Consumption Per Day Home II');
ax.set_ylabel('Energy (KWh)');
correct_labels(ax);
highlight_weekend(weekend_indices,ax,6);
```



```
ax=df_1_day_energy.plot(kind='bar',stacked=True,rot=0);
ax.set_title('Energy Consumption Per Day Home II');
ax.set_ylabel('Energy (KWh)');
correct_labels(ax);
highlight_weekend(weekend_indices,ax,7);
```



Now we try to break down the energy consumption into 6 hours slot and see if we can see some patterns amongst the same.

Statistics about Energy data downsampled to 6 hours.

#### df\_6\_hours\_energy.describe()

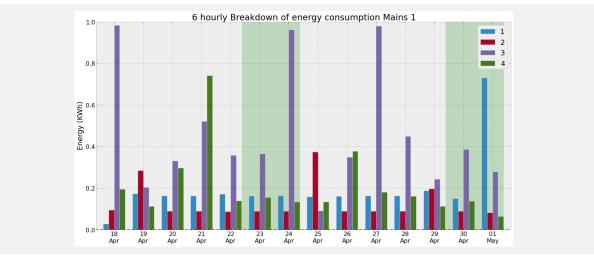
```
Mains_1_Energy Mains_2_Energy
            56.000000
                             56.000000
count
             0.250375
                               1.081515
mean
             0.228078
                               0.439292
std
min
             0.028911
                               0.235619
25%
             0.107926
                               0.762373
50%
             0.162402
                               0.964794
75%
             0.305203
                               1.386838
             0.983501
                               2.117311
max
```

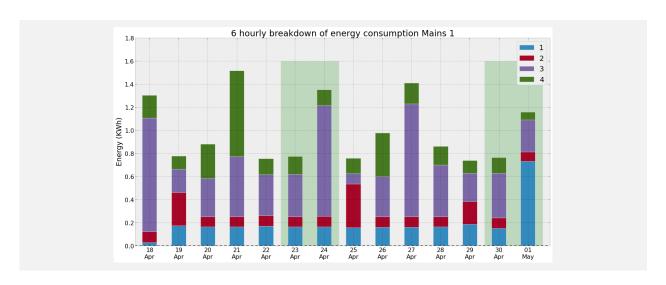
```
days_mains_1=[]
dawn_mains_1=[]
morning_mains_1=[]
dusk_mains_1=[]
night_mains_1=[]
dawn_mains_2=[]
morning_mains_2=[]
morning_mains_2=[]
for i in range(len(df_6_hours_energy.Mains_1_Energy)/4):
```

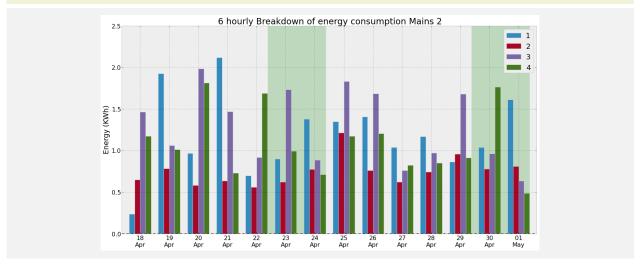
```
days_mains_1.append(df_6_hours_energy.index[4*i])
dawn_mains_1.append(df_6_hours_energy.Mains_1_Energy[4*i+1])
morning_mains_1.append(df_6_hours_energy.Mains_1_Energy[4*i+2])
night_mains_1.append(df_6_hours_energy.Mains_1_Energy[4*i+3])
dawn_mains_2.append(df_6_hours_energy.Mains_2_Energy[4*i])
morning_mains_2.append(df_6_hours_energy.Mains_2_Energy[4*i+1])
dusk_mains_2.append(df_6_hours_energy.Mains_2_Energy[4*i+2])
night_mains_2.append(df_6_hours_energy.Mains_2_Energy[4*i+3])
```

#### Plotting 6 hourly breakdown of energy consumption from Mains 1

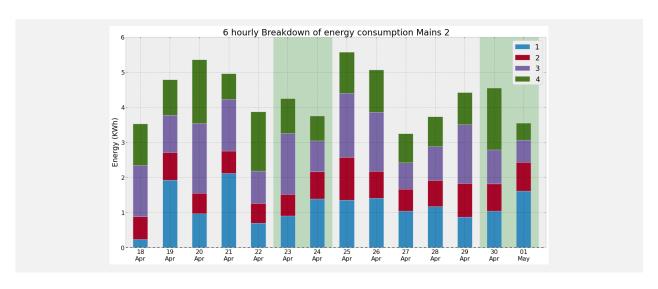
```
df4=DataFrame({'1':dawn_mains_1,'2':morning_mains_1,'3':dusk_mains_1,'4':night_mains_1},
    index=days_mains_1)
ax=df4.plot(kind='bar',stacked=False,legend=False,rot=0);
patches, labels = ax.get_legend_handles_labels();
ax.legend(patches, labels, loc='upper right');
ax.set_title('6 hourly Breakdown of energy consumption Mains 1');
ax.set_ylabel('Energy (KWh)');
correct_labels(ax);
highlight_weekend(weekend_indices,ax,1);
```







```
ax=df5.plot(kind='bar',stacked=True,legend=False,rot=0);
patches, labels = ax.get_legend_handles_labels();
ax.legend(patches, labels, loc='upper right');
ax.set_title('6 hourly Breakdown of energy consumption Mains 2');
ax.set_ylabel('Energy (KWh)');
correct_labels(ax);
highlight_weekend(weekend_indices,ax,6);
```



```
kitchen_data=np.loadtxt('house_2/channel_3.dat')
light_data=np.loadtxt('house_2/channel_4.dat')
stove_data=np.loadtxt('house_2/channel_5.dat')
microwave_data=np.loadtxt('house_2/channel_6.dat')
washer_dry_data=np.loadtxt('house_2/channel_7.dat')
kitchen_2_data=np.loadtxt('house_2/channel_8.dat')
refrigerator_data=np.loadtxt('house_2/channel_9.dat')
dishwasher_data=np.loadtxt('house_2/channel_10.dat')
disposal_data=np.loadtxt('house_2/channel_11.dat')
upper=np.where(kitchen_data[:,0]==1304282291.0)[0]
lower=np.where(mains_1_data[:,0]>1303084800.0)[0][0]
kitchen_power=kitchen_data[:,1][lower:upper]
light_power=light_data[:,1][lower:upper]
stove_power=stove_data[:,1][lower:upper]
microwave_power=microwave_data[:,1][lower:upper]
washer_dryer_power=washer_dry_data[:,1][lower:upper]
kitchen_2_power=kitchen_2_data[:,1][lower:upper]
refrigerator_power=refrigerator_data[:,1][lower:upper]
dishwasher_power=dishwasher_data[:,1][lower:upper]
disposal_power=disposal_data[:,1][lower:upper]
timestamp=kitchen_data[:,0][lower:upper]
timestamp_appliance_date=timestamp.astype('datetime64[s]')
```

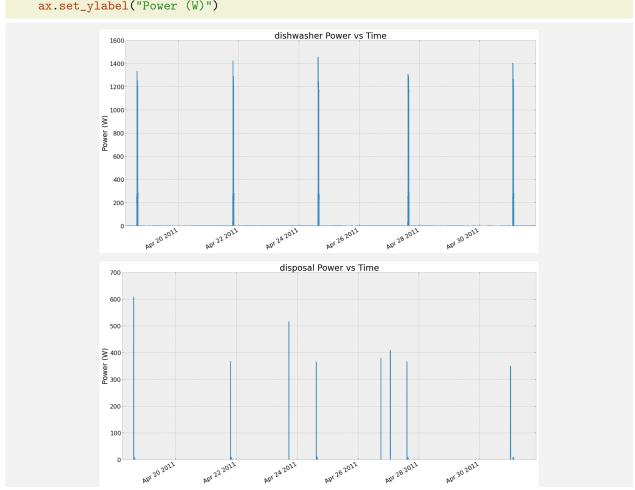
```
df_appliances=DataFrame({'kitchen':kitchen_power,'light':light_power,'stove':stove_power
        ,'microwave':microwave_power,\
'washer_dryer':washer_dryer_power,'kitchen_2':kitchen_2_power,'refrigerator':
        refrigerator_power,'dishwasher':dishwasher_power,\
'disposal':disposal_power},index=timestamp_appliance_date)
pd.set_option('display.precision', 2)
print df.describe().to_string()
```

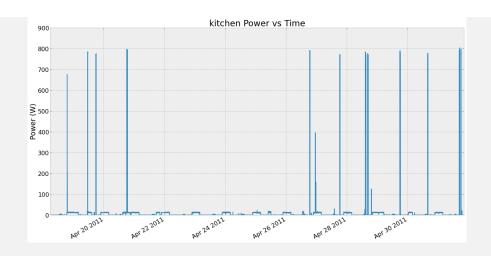
```
dishwasher disposal
                    kitchen kitchen_2
                                         light microwave refrigerator
                                                                         stove washer_dryer
                                                                                         3086
        308612.0 308612.0 308612.0
                                   308612.0 308612.0
                                                       308612.0
                                                                   308612.0 308612.0
count
                                       10.5
mean
            9.2
                    0.1
                              6.1
                                                26.9
                                                          14.4
                                                                       79.6 1.5
```

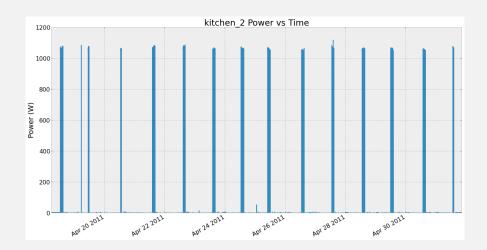
std	97.2	3.4	38.3	99.0	46.2	104.5	87.7	19.2
min	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
25%	0.0	0.0	0.0	1.0	8.0	4.0	6.0	0.0
50%	0.0	0.0	0.0	1.0	8.0	5.0	7.0	0.0
75%	0.0	0.0	13.0	1.0	9.0	5.0	161.0	1.0
max	1457.0	609.0	805.0	1119.0	289.0	1986.0	2246.0	457.0

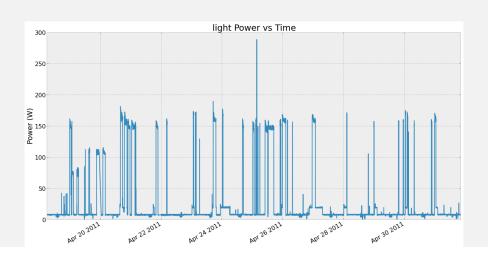
Now we plot all the channels and describe their statistics

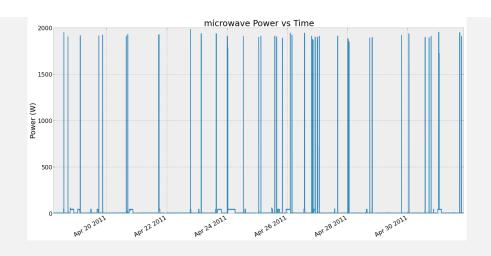
```
for key in df_appliances:
   plt.figure()
   ax=df_appliances[key].plot(title=key+" Power vs Time")
   ax.set_ylabel("Power (W)")
```

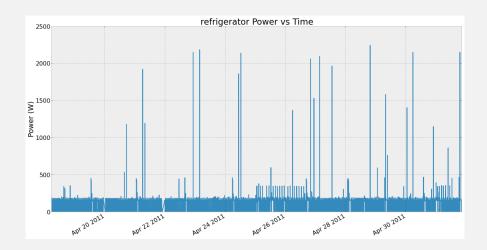


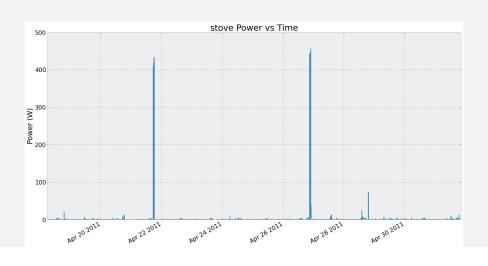


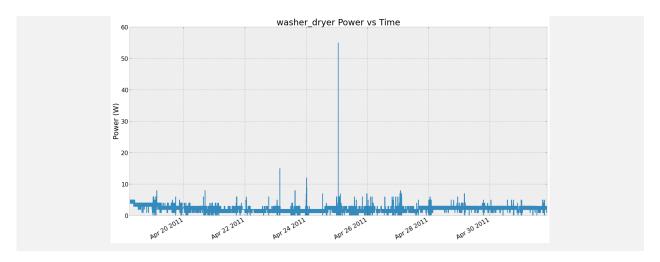












Similarly we load data correspding to different channels (appliances/circuits) and plot them.

#### 1.5 Assigning loads to different mains circuits

Since there are two mains in the home we need to break down the individual appliance into different mains. Clearly,

- Kitchen\_2 belongs to Mains1
- Kitchen belongs to Mains1
- Refrigerator belongs to Mains 2

Beyond this it is difficult to visually find the mains corresponding to different appliances. We thus decide to iteratively remove the known components. It must be noted that Mains is at 1 Hz and appliance are at lower resolution. Thus we need to align the two. This we do by aligning higher frequency mains to lower resolution appliance resolution. Thus, we downsample both the mains and all the appliances to a minute resolution, taking mean of the values contained within the minute.

```
df_appliances_minute=df_appliances.resample('1Min',how='mean')
pd.set_option('display.precision', 2)
print df_appliances_minute.describe().to_string()
df_appliances_minute.index
```

dishwasher	disposal	kitchen	kitchen_	2 light	microwave	refrigerator	stove	washer.	_dryer
count	19398.0	19398.0	19398.0	19398.0	19398.0	19398.0	19398.0	19398.0	19398.0
mean	9.3	0.1	6.1	10.6	26.9	14.4	79.6	1.5	2.2
std	96.5	1.6	35.0	74.5	46.1	89.7	85.5	18.1	0.6
min	0.0	0.0	0.0	0.0	2.0	1.6	1.6	0.0	0.0
25%	0.0	0.0	0.0	1.0	8.0	4.1	6.1	0.1	2.0
50%	0.1	0.0	0.4	1.0	8.6	4.6	7.0	0.5	2.0
75%	0.1	0.0	13.0	1.0	9.0	5.0	160.8	0.9	2.2
max	1255.6	115.8	794.6	1071.8	185.4	1926.0	598.2	411.0	8.8

<class 'pandas.tseries.index.DatetimeIndex'>
[2011-04-18 05:41:00, ..., 2011-05-01 20:38:00]
Length: 19618, Freq: T, Timezone: None

As a sanity check, we confirm that 19400 minutes correspond to about 14 days, thus our resampling was correct.

```
df_mains_minute=df_mains.resample('1Min',how='mean')
 df_mains_minute.describe()
 print df_mains_minute.index
 print np.where(df_mains_minute.index==df_appliances_minute.index[0])
 df_mains_minute=df_mains_minute[236:]
 print df_mains_minute.index
 df_mains_minute.describe()
<class 'pandas.tseries.index.DatetimeIndex'>
[2011-04-18 01:45:00, ..., 2011-05-01 20:38:00]
Length: 19854, Freq: T, Timezone: None
(array([236]),)
<class 'pandas.tseries.index.DatetimeIndex'>
[2011-04-18 05:41:00, ..., 2011-05-01 20:38:00]
Length: 19618, Freq: T, Timezone: None
       Mains_1_Power Mains_2_Power
count
             19397.0
                            19397.0
                43.5
                               187.7
mean
               130.4
                               204.1
std
                13.4
                                21.4
min
                                22.5
25%
                14.9
50%
                15.1
                               214.4
75%
                33.7
                               259.1
              1312.0
                              2612.5
max
```

We now plot the lower resolution mains 1 and iteratively attempt to take out appliances.

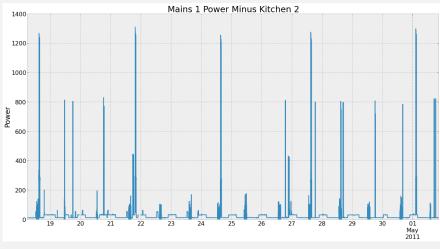


Removing kitchen\_2 from Mains 1

```
temp_1=df_mains_minute.Mains_1_Power-df_appliances_minute.kitchen_2
temp_1[temp_1<0.0]=0.0</pre>
```

```
df_mains_minute_minus_kitchen_2=df_mains_minute.copy()
df_mains_minute_minus_kitchen_2.Mains_1_Power=temp_1
print df_mains_minute_minus_kitchen_2.describe()
print df_mains_minute.describe()
ax=df_mains_minute_minus_kitchen_2.Mains_1_Power.plot(title='Mains 1 Power Minus Kitchen_2')
ax.set_ylabel('Power');
```

Mains_	1_Power Mains_	_2_Power
count	19395.0	19397.0
mean	33.2	187.7
std	107.0	204.1
min	0.0	21.4
25%	13.7	22.5
50%	14.1	214.4
75%	32.4	259.1
max	1312.0	2612.5
	Mains_1_Power	Mains_2_Power
count	19397.0	19397.0
mean	43.5	187.7
std	130.4	204.1
min	13.4	21.4
25%	14.9	22.5
50%	15.1	214.4
75%	33.7	259.1
max	1312.0	2612.5



Now removing Kitchen 1 from mains 1

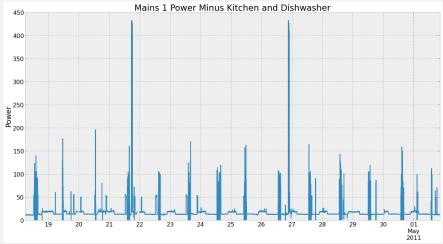
count	_1_Power Mains_ 19395.0	19397.0									
mean	27.1	187.7									
std	100.7	204.1									
min	0.0	21.4									
25%	13.5	22.5									
20% 50%	13.7	214.4									
75%	18.6	259.1									
max	1299.0	2612.5									
	Mains_1_Power	Mains_2_Power									
count	19395.0	19397.0									
mean	33.2	187.7									
std	107.0	204.1 21.4									
min 25%	13.7	22.5									
25% 50%	14.1	214.4									
50% 75%	32.4	259.1									
max	1312.0	2612.5									
шах	1312.0			1611		Lieb L	_				
	1400	Mains	l Power Mir	ius Kitch	en 2 an	a Kitch	ien 1				
				1			ı			1	
	1200										
	1000										
	1000										
	800										
	Power										
	600										
	400					1					
	200		.l	1				,		1	
	0										
		20 21 22	23 24	25	26	27	28	29	30	01	

Now we observe that Dishwasher was used every 3rd day starting from 19th and power consumption was about 1200+ W. Thus, we next remove the dishwasher component from mains 1

```
\label{temp_3=df_mains_minute_minus_kitchen_2_1.Mains_1_Power-df_appliances_minute.dishwasher $$ temp_3[temp_3<0.0]=0.0$
```

```
df_mains_minute_minus_kitchen_dishwasher=df_mains_minute_minus_kitchen_2_1.copy()
df_mains_minute_minus_kitchen_dishwasher.Mains_1_Power=temp_3
```

#### Mains\_1\_Power Mains\_2\_Power 19395.0 19397.0 17.8 187.7 mean 20.9 204.1 std 0.0 21.4 min 25% 13.5 22.5 50% 13.7 214.4 75% 18.5 259.1 2612.5 433.4 max Mains\_1\_Power Mains\_2\_Power count 19395.0 19397.0 mean 27.1 187.7 100.7 204.1 std 0.0 21.4 min 22.5 25% 13.5 214.4 50% 13.7 75% 18.6 259.1 1299.0 2612.5 max 450



#### Removing stove from Mains 1

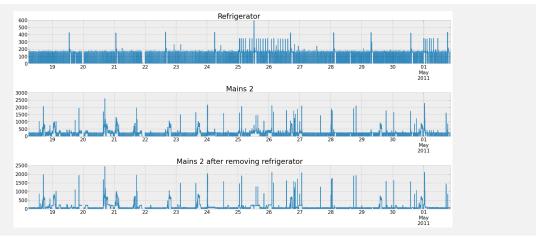
```
df_mains_minute_minus_kitchen_dishwasher_stove=df_mains_minute_minus_kitchen_dishwasher.
    copy()
df_mains_minute_minus_kitchen_dishwasher_stove.Mains_1_Power=temp_4
print df_mains_minute_minus_kitchen_dishwasher_stove.describe()
print df_mains_minute_minus_kitchen_dishwasher.describe()
```

```
ax=df_mains_minute_minus_kitchen_dishwasher_stove.Mains_1_Power.plot(title='Mains 1
    Power Minus Kitchen, Dishwasher and Stove')
ax.set_ylabel('Power');
```

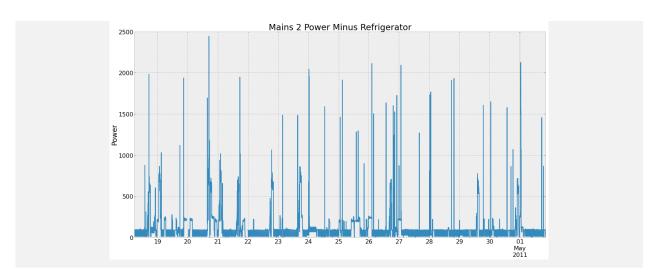
```
Mains_1_Power Mains_2_Power
count
               19395.0
                                 19397.0
                   16.3
                                   187.7
mean
                    9.9
                                   204.1
std
                    0.0
                                    21.4
min
25%
                   12.7
                                    22.5
                   13.4
                                   214.4
50%
75%
                   17.7
                                   259.1
                 196.0
                                  2612.5
max
        Mains_1_Power
                         Mains_2_Power
               19395.0
                                 19397.0
count
mean
                   17.8
                                   187.7
std
                   20.9
                                   204.1
min
                    0.0
                                    21.4
                                    22.5
25%
                   13.5
                                   214.4
50%
                   13.7
                                   259.1
75%
                   18.5
max
                 433.4
                                  2612.5
                                   Mains 1 Power Minus Kitchen, Dishwasher and Stove
                 150
                Power
100
```

We next observe that none of the other appliance can be extracted visually from Mains 1. So we start removing appliances iteratively from Mains 2. From the next plot we can see that there is a slight difference in power seen by the mains and the appliance level monitor, hence there seems to be a need to do this calibration to ensure that we have better results. Moreover, this is an aspect i think no one has yet highlighted in their work.

```
df_mains_minute.Mains_2_Power.plot(title='Mains 2')
plt.subplot(3,1,3)
temp_5.plot(title='Mains 2 after removing refrigerator');
plt.tight_layout()
```



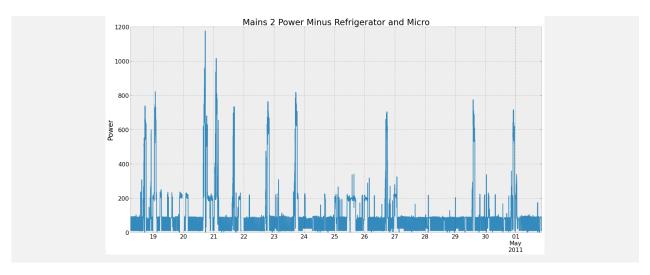
Mains_	1_Power Mains_	2_Power
count	19395.0	19395.0
mean	16.3	108.1
std	9.9	168.1
min	0.0	0.0
25%	12.7	16.3
50%	13.4	89.3
75%	17.7	97.5
max	196.0	2448.5
	Mains_1_Power	Mains_2_Power
count	19395.0	19397.0
mean	16.3	187.7
std	9.9	204.1
min	0.0	21.4
25%	12.7	22.5
50%	13.4	214.4
75%	17.7	259.1
max	196.0	2612.5



Since microwave is taking more power than residual power in Mains 1, it has to belong to Mains 2. Next, removing Microwave from Mains 2.

```
temp_6=df_mains_minute_minus_kitchen_dishwasher_stove_ref.Mains_2_Power-
    df_appliances_minute.microwave
temp_6[temp_6<0.0]=0.0</pre>
```

Mains_	1_Power Mains_	2_Power
count	19395.0	19395.0
mean	16.3	93.6
std	9.9	136.0
min	0.0	0.0
25%	12.7	12.2
50%	13.4	80.0
75%	17.7	91.6
max	196.0	1177.5
	Mains_1_Power	Mains_2_Power
count	19395.0	19395.0
mean	16.3	108.1
std	9.9	168.1
min	0.0	0.0
25%	12.7	16.3
50%	13.4	89.3
75%	17.7	97.5
max	196.0	2448.5

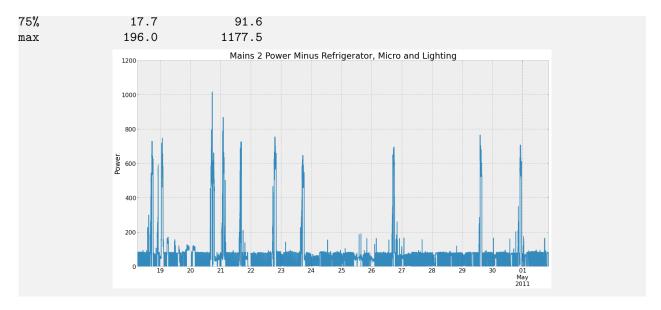


An interesting thing to note is the correlation between **Disposal** and **Dishwasher** both of which occur on the same days. Next, we iteratively start extracting out appliances from Mains 2. Now removing microwave from Mains 2.

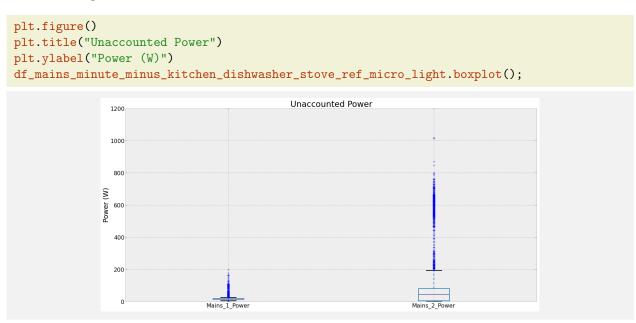
Removing lighting from Mains 2.

```
temp_7=df_mains_minute_minus_kitchen_dishwasher_stove_ref_micro.Mains_2_Power-
    df_appliances_minute.light
temp_7(temp_7<0.0]=0.0</pre>
```

Mains_	1_Power Mains_	2_Power
count	19395.0	19395.0
mean	16.3	66.7
std	9.9	120.2
min	0.0	0.0
25%	12.7	4.2
50%	13.4	45.7
75%	17.7	80.3
max	196.0	1017.3
	Mains_1_Power	Mains_2_Power
count	19395.0	19395.0
mean	16.3	93.6
std	9.9	136.0
min	0.0	0.0
25%	12.7	12.2
50%	13.4	80.0



Thus, we can see that both for Mains 1 and Mains 2 there is still a lot of unaccounted power. This is due to mis calibration between the appliance level loads and also due to absence of complete information. This is an important aspect to address. Next, we draw the boxplot showing unaccounted power.



Remaining load is unaccounted for in the analysis. We now have 2 options:

- To continue with this data as such and not process further
- To filter out data about which not information has been provided.

Option 1 is more realistic and Option 2 is more ideal. We shall be considering the ideal case through the remaining analysis. Thus, we need to filter out the remaining data.

```
df_filtered_mains=pd.DataFrame({'Mains_1_Power':filtered_mains_1_power,'Mains_2_Power':
    filtered_mains_2_power},\
index=df_mains_minute_minus_kitchen_dishwasher_stove_ref_micro_light.index)
```

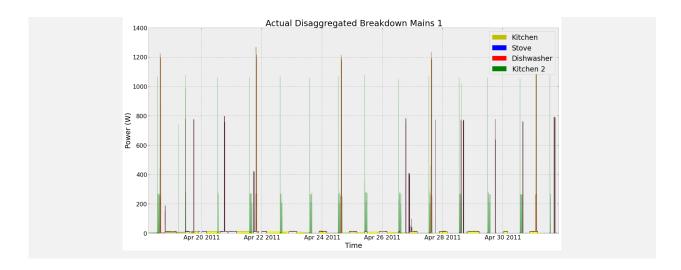
#### df\_filtered\_mains.describe()

	Mains 1 Power	Mains_2_Power
a a 11 m +	19398.0	19398.0
count	19396.0	
mean	27.4	121.0
std	127.4	139.6
min	0.2	9.6
25%	1.5	18.3
50%	2.5	121.3
75%	14.4	177.8
max	1268.6	2252.2

Plotting Disaggregated consumption Mains 1

```
python_datetime=df_filtered_mains.index.to_pydatetime()
```

```
plt.title('Actual Disaggregated Breakdown Mains 1');
plt.xlabel('Time');
plt.ylabel('Power (W)');
y_1=df_appliances_minute.kitchen+df_appliances_minute.stove
y_2=y_1+df_appliances_minute.dishwasher
plt.fill_between(python_datetime,df_appliances_minute.kitchen,np.zeros(len(
    df_appliances_minute.kitchen)),color="yellow")
plt.fill_between(python_datetime,y_1,df_appliances_minute.kitchen,color='blue',label='
   Test')
plt.fill_between(python_datetime,y_2,y_1,color='red',alpha=.6)
plt.fill_between(python_datetime,y_2,df_filtered_mains.Mains_1_Power,color='green',alpha
    =0.4)
p = Rectangle((0, 0), 1, 1, fc="y")
p1=Rectangle((0, 0), 1, 1, fc="b")
p2=Rectangle((0, 0), 1, 1, fc="r")
p3=Rectangle((0, 0), 1, 1, fc="g")
legend([p,p1,p2,p3], ["Kitchen","Stove","Dishwasher","Kitchen 2"]);
```



#### 1.6 State Space

Finding different states for each appliance and the corresponding power consumption using various clustering techniques. Firstly, we start with stove. There are several reasons behind choosing a clustering algorithm, some of them are mentioned at http://scikit-learn.org/stable/modules/clustering.html

```
from sklearn.cluster import MiniBatchKMeans, KMeans
import time
```

Filling missing data (currently NaN) with 0's. CONFIRM: If this is the right thing to do.

```
df_appliances_minute.fillna(0,inplace=True)
times=df_appliances_minute.index.to_pydatetime()
```

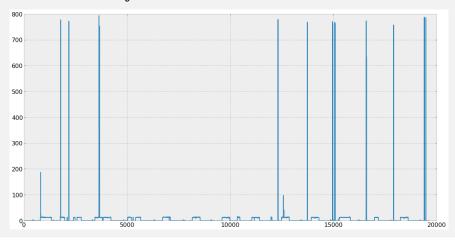
```
def apply_kmeans(n_clusters, n_init,X,init=None):
    if init is None:
        k_means = KMeans(n_clusters=n_clusters, n_init=n_init)
    else:
        k_means=KMeans(init='k-means++',n_clusters=n_clusters, n_init=n_init)
    t0 = time.time()
    k_means.fit(X)
    t_batch = time.time() - t0
    k_means_labels = k_means.labels_
    k_means_cluster_centers = k_means.cluster_centers_
    k_means_labels_unique = np.unique(k_means_labels)
    inertia=k_means.inertia_
    return [t_batch, k_means_labels, k_means_cluster_centers, k_means_labels_unique,
        inertia]
```

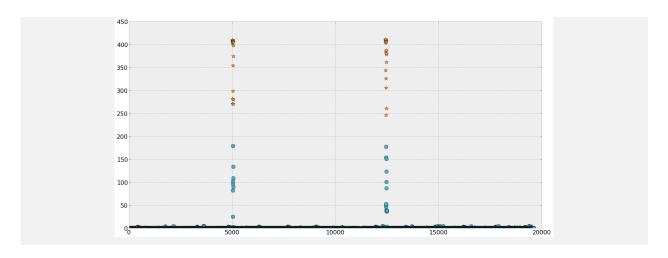
```
def plot_cluster_assignments(X,k_means_labels, k_means_cluster_centers,n_clusters):
    colors = ['#4EACC5', '#FF9C34', '#4E9A06']
    markers=['o','*','.']
```

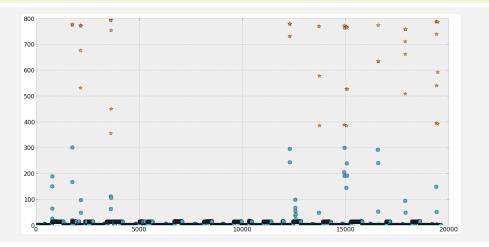
```
x_temp=np.arange(len(X))
for k, col in zip(range(n_clusters), colors):
    my_members = k_means_labels == k
    cluster_center = k_means_cluster_centers[k]
    plt.plot(x_temp[my_members], X[my_members, 0], markers[k], markersize=10,
        markerfacecolor=col)
```

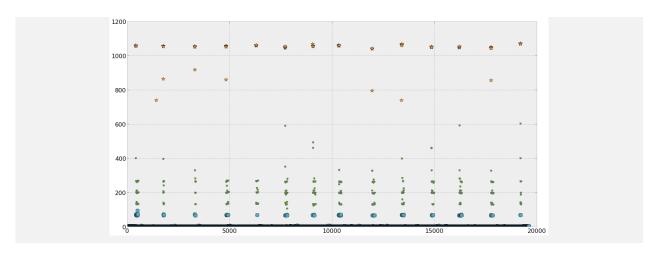
```
raw_data={}
for key in df_appliances_minute:
    raw_data[key]=df_appliances_minute[key].values
    length=len(raw_data[key])
    raw_data[key]=raw_data[key].reshape(length,1)
plt.plot(raw_data["kitchen"])
plt.legend()
```

/usr/lib/pymodules/python2.7/matplotlib/axes.py:4486: UserWarning: No labeled objects found. Use label= warnings.warn("No labeled objects found."









```
np.savetxt('stove',downsampled_stove)
centroids,_ = kmeans(downsampled_stove,2)
colors_index=['r','g','b']
idx,_ = vq(downsampled_stove,centroids)
print "Contribution of different states for stove"
for i in range(0,2):
    print "Power: ",centroids[i], "Percent: ",100.0*sum(idx==i)/len(idx)
    print "Variance",np.var(downsampled_stove[np.where(idx==i)])
clustered_stove=np.array([downsampled_stove,idx])
np.savetxt('clustered_stove',clustered_stove)
```

```
np.savetxt('kitchen.arff',downsampled_kitchen)
centroids,_ = kmeans(downsampled_kitchen,2)
idx,_ = vq(downsampled_kitchen,centroids)
print "Contribution of different states for Kitchen"
for i in range(0,2):
    print "Power: ",centroids[i], "Percent: ",100.0*sum(idx==i)/len(idx)
    print "Variance",np.var(downsampled_stove[np.where(idx==i)])
clustered_kitchen=np.array([downsampled_kitchen,idx])
np.savetxt('clustered_kitchen',clustered_kitchen)
```

```
np.savetxt('kitchen_2.arff',downsampled_kitchen_2)
centroids,_ = kmeans(downsampled_kitchen_2,3)
idx,_ = vq(downsampled_kitchen,centroids)
print "Contribution of different states for Kitchen 2"
for i in range(0,3):
    print "Power: ",centroids[i], "Percent: ",100.0*sum(idx==i)/len(idx)
    print "Variance",np.var(downsampled_stove[np.where(idx==i)])
clustered_kitchen_2=np.array([downsampled_kitchen_2,idx])
np.savetxt('clustered_kitchen_2',clustered_kitchen_2)
```

```
np.savetxt('dishwasher.arff',downsampled_dishwasher)
centroids,_ = kmeans(downsampled_dishwasher,3)
idx,_ = vq(downsampled_dishwasher,centroids)
```

```
print "Contribution of different states for Dishwasher"
for i in range(0,3):
    print "Power: ",centroids[i], "Percent: ",100.0*sum(idx==i)/len(idx)
    print "Variance",np.var(downsampled_stove[np.where(idx==i)])
clustered_dishwasher=np.array([downsampled_dishwasher,idx])
np.savetxt('clustered_dishwasher',clustered_dishwasher)
```

```
np.savetxt('refrigerator.arff',downsampled_refrigerator)
centroids,_ = kmeans(downsampled_refrigerator,3)
idx,_ = vq(downsampled_refrigerator,centroids)
print "Contribution of different states for Refrigerator"
for i in range(0,3):
    print "Power: ",centroids[i], "Percent: ",100.0*sum(idx==i)/len(idx)
    print "Variance",np.var(downsampled_stove[np.where(idx==i)])
clustered_refrigerator=np.array([downsampled_refrigerator,idx])
np.savetxt('clustered_refrigerator',clustered_refrigerator)
```

```
np.savetxt('microwave.arff',downsampled_microwave)
centroids,_ = kmeans(downsampled_microwave,3)
idx,_ = vq(downsampled_microwave,centroids)
print "Contribution of different states for Microwave"
for i in range(0,3):
    print "Power: ",centroids[i], "Percent: ",100.0*sum(idx==i)/len(idx)
    print "Variance",np.var(downsampled_stove[np.where(idx==i)])
clustered_microwave=np.array([downsampled_microwave,idx])
np.savetxt('clustered_microwave',clustered_microwave)
```

```
centroids,_ = kmeans(downsampled_lighting,3)
idx,_ = vq(downsampled_lighting,centroids)

print "Contribution of different states for Lighting"
for i in range(0,3):
    print "Power: ",centroids[i], "Percent: ",100.0*sum(idx==i)/len(idx)
    print "Variance",np.var(downsampled_stove[np.where(idx==i)])
clustered_lighting=np.array([downsampled_lighting,idx])
np.savetxt('clustered_lighting',clustered_lighting)
```

Thus, we obtain the following states from cluster analysis.

```
kitchen=[0,19]
lighting=[8,25,150]
stove=[0,304]
micro=[4,52,1220]
kitchen_2=[1,167,992]
ref=[7,161,992]
dish=[0,244,1170]
```

For mains 1, we now draw the state space, which consists of all possible combinations of appliances in their different states. We also show the corresponding histogram which tells how close the

different states are. The closer the states, the more difficult the disaggregation becomes.

```
states_combination=list(itertools.product(kitchen,stove,kitchen_2,dish))
```

```
print "The possible different state combinations are\n Kitchen, Stove, Kitchen 2,
    Dishwasher\n", states_combination
```

```
sum_combination=np.array(np.zeros(len(states_combination)))
for i in range(0,len(states_combination)):
    sum_combination[i]=sum(states_combination[i])
from copy import deepcopy
b=deepcopy(sum_combination)
b.sort()
grid(True)
title('Sorted possible sums of all appliances');
xlabel('Combinations');
ylabel('Power (W)');
plot(b);
```

```
title('Histogram showing relative frequencies of different state combinations');
hist(b,100);
```

Now we basically need to iterate over all our sample and see which of the possible state assignment matches closest to the overall power consumption. We thus create a function to do the same.

```
def find_nearest(array,value):
   idx = (np.abs(array-value)).argmin()
   diff=array[idx]-value
   return [idx,-diff]
```

We thus apply this technique to find the residual power left from the closest state assignment.

```
title('Residual Power Mains 1');
xlabel('Time');
ylabel('Power (W)');
plot(residual_power_mains_1);
```

However we can also impose another condition that the sum of powers of all the appliances is strictly less than the aggregate power observed. Thus, we can create a function for that as follows.

```
def find_nearest_positive(array,value):
    idx_temp = np.where(array-value<=0.0)[0]
    temp_arr=array[idx_temp]
    try:
        idx_in_new=np.abs(temp_arr-value).argmin()
        idx=np.where(array==temp_arr[idx_in_new])[0][0]

        diff=array[idx]-value
    except:
        idx=0
        diff=0
    return [idx,-diff]</pre>
```

```
title('Residual Power Mains 1 considering sum of appliance powers < Aggregate Power');
xlabel('Time');
ylabel('Power (W)');
grid(True);
plot(residual_power_mains_1_positive);</pre>
```

After having applied Total Load Model, we need to assign different states to different appliances.

```
length_sequence=len(filtered_downsampled_mains_1)
co_kitchen_states=np.zeros(length_sequence,dtype=np.int)
co_kitchen_power=np.zeros(length_sequence)
co_stove_states=np.zeros(length_sequence,dtype=np.int)
co_stove_power=np.zeros(length_sequence)
co_kitchen_2_states=np.zeros(length_sequence,dtype=np.int)
co_kitchen_2_power=np.zeros(length_sequence)
co_dish_states=np.zeros(length_sequence,dtype=np.int)
co_dish_power=np.zeros(length_sequence)
```

```
for i in range(length_sequence):
    if int(states_idx[i])/18==0:
        co_kitchen_states[i]=0

else:
        co_kitchen_states[i]=1
    co_kitchen_power[i]=kitchen[co_kitchen_states[i]]

temp=int(states_idx[i])/9
    if temp%2==0:
```

```
co_stove_states[i]=0
else:
   co_stove_states[i]=1
co_stove_power[i]=stove[co_stove_states[i]]
temp=int(states_idx[i])/3
if temp%3==0:
   co_kitchen_2_states[i]=0
elif temp%3==1:
   co_kitchen_2_states[i]=1
else:
   co_kitchen_2_states[i]=2
co_kitchen_2_power[i]=kitchen_2[co_kitchen_2_states[i]]
temp=int(states_idx[i])%3
if temp==0:
   co_dish_states[i]=0
elif temp==1:
   co_dish_states[i]=1
else:
   co_dish_states[i]=2
co_dish_power[i]=dish[co_dish_states[i]]
```

Now we compare the produced output with Ground truth.

```
subplot(2,1,1);

plt.title('Actual Dishwasher Consumption');
plt.xlabel('Time');
plt.ylabel('Power (W)');
subplots_adjust(hspace=.5)
plt.plot(downsampled_timestamp_appliance_date,downsampled_dishwasher);
subplot(2,1,2);
plt.xlabel('Time');
plt.ylabel('Power (W)');
plt.title('Observed Dishwasher Consumption');
plt.plot(downsampled_timestamp_appliance_date,co_dish_power);
```

```
plt.subplot(2,1,1)
plt.title('Actual Kitchen 1 Consumption');
plt.xlabel('Time');
plt.ylabel('Power (W)');
subplots_adjust(hspace=.5);
plt.plot(downsampled_timestamp_appliance_date,downsampled_kitchen)
plt.subplot(2,1,2)
plt.xlabel('Time');
plt.ylabel('Power (W)');
plt.title('Observed Kitchen 1 Consumption')
plt.ylim((0,800))
plt.plot(downsampled_timestamp_appliance_date,co_kitchen_power);
```

```
plt.subplot(2,1,1)
plt.title('Actual Kitchen 2 Consumption')
plt.xlabel('Time');
plt.ylabel('Power (W)');
subplots_adjust(hspace=.5);
plt.plot(downsampled_timestamp_appliance_date,downsampled_kitchen_2)
plt.subplot(2,1,2)
plt.xlabel('Time');
plt.ylabel('Power (W)');
plt.ylabel('Power (W)');
plt.title('Observed Kitchen 2 Consumption')
plt.plot(downsampled_timestamp_appliance_date,co_kitchen_2_power);
```

```
plt.subplot(2,1,1)
plt.title('Actual Stove Consumption')
plt.xlabel('Time');
plt.ylabel('Power (W)');
subplots_adjust(hspace=.5)
plt.plot(downsampled_timestamp_appliance_date,downsampled_stove)
plt.subplot(2,1,2)
plt.xlabel('Time');
plt.ylabel('Power (W)');
plt.title('Predicted Stove Consumption')
plt.plot(downsampled_timestamp_appliance_date,co_stove_power);
```

Calculation of Residual Power and Standard Deviation

```
residual_power_total=sum(np.abs(residual_power_mains_1))
print "Residual Power is: ",residual_power_total," W"
standard_deviation=np.std(residual_power_mains_1)
print "Standard Deviation is ",standard_deviation
```

Reading original labels of different states for different appliances

```
dummy,labels_stove=np.loadtxt('clustered_stove')
dummy,labels_kitchen=np.loadtxt('clustered_kitchen')
dummy,labels_kitchen_2=np.loadtxt('clustered_kitchen_2')
dummy,labels_dish=np.loadtxt('clustered_dishwasher')
dummy,labels_ref=np.loadtxt('clustered_refrigerator')
dummy,labels_micro=np.loadtxt('clustered_microwave')
dummy,labels_lighting=np.loadtxt('clustered_lighting')
```

```
labels_stove=labels_stove.astype(np.int)
labels_kitchen=labels_kitchen.astype(np.int)
labels_kitchen_2=labels_kitchen_2.astype(np.int)
labels_dish=labels_dish.astype(np.int)
labels_ref=labels_ref.astype(np.int)
labels_micro=labels_micro.astype(np.int)
labels_lighting=labels_lighting.astype(np.int)
```

Next, we define a function to plot the confusion matrix.

```
def print_confusion_matrix(appliance,num_states,true_label,observed_label):
   correct_predicted=0
   conf_arr=[]
   for i in range(num_states):
       counts=[]
       for j in range(num_states):
           idx=np.where(true_label==i)[0]
           counts.append(len(np.where(observed_label[idx]==j)[0]))
       correct_predicted+=counts[i]
       conf_arr.append(counts)
   norm_conf = []
   for i in conf_arr:
       a = 0
       tmp_arr = []
       a = sum(i, 0)
       for j in i:
           tmp_arr.append(float(j)/float(a))
       norm_conf.append(tmp_arr)
   fig = plt.figure()
   plt.clf()
   ax = fig.add_subplot(111)
   ax.set_aspect(1)
   res = ax.imshow(np.array(norm_conf), cmap=plt.cm.jet,
              interpolation='nearest')
   width = len(conf_arr)
   height = len(conf_arr[0])
   for x in xrange(width):
       for y in xrange(height):
           ax.annotate(str(conf_arr[x][y]), xy=(y, x),
                  horizontalalignment='center',
                  verticalalignment='center')
   cb = fig.colorbar(res)
   alphabet = ['State 1', 'State 2', 'State 3']
   plt.title('Confusion Matrix for '+appliance)
   plt.xticks(range(width), alphabet[:width])
   plt.yticks(range(height), alphabet[:height])
   plt.show()
   return correct_predicted*1.0/len(true_label)
```

Plotting the confusion matices for different appliances mains 1

We now repeat the same procedure when we take the assumption that the sum of powers of different appliances must be less than or equal to the aggregate power.

```
co_positive_kitchen_states=np.zeros(length_sequence,dtype=np.int)
co_positive_kitchen_power=np.zeros(length_sequence)
co_positive_stove_states=np.zeros(length_sequence,dtype=np.int)
co_positive_stove_power=np.zeros(length_sequence)
co_positive_kitchen_2_states=np.zeros(length_sequence,dtype=np.int)
co_positive_kitchen_2_power=np.zeros(length_sequence)
co_positive_dish_states=np.zeros(length_sequence,dtype=np.int)
co_positive_dish_power=np.zeros(length_sequence)
```

```
for i in range(length_sequence):
   if int(states_idx_positive[i])/18==0:
       co_positive_kitchen_states[i]=0
   else:
       co_positive_kitchen_states[i]=1
   co_positive_kitchen_power[i]=kitchen[co_positive_kitchen_states[i]]
   temp=int(states_idx_positive[i])/9
   if temp%2==0:
       co_positive_stove_states[i]=0
   else:
       co_positive_stove_states[i]=1
   co_positive_stove_power[i] = stove[co_positive_stove_states[i]]
   temp=int(states_idx_positive[i])/3
   if temp%3==0:
       co_positive_kitchen_2_states[i]=0
   elif temp%3==1:
       co_positive_kitchen_2_states[i]=1
   else:
       co_positive_kitchen_2_states[i]=2
   co_positive_kitchen_2_power[i]=kitchen_2[co_positive_kitchen_2_states[i]]
   temp=int(states_idx_positive[i])%3
   if temp==0:
       co_positive_dish_states[i]=0
   elif temp==1:
       co_positive_dish_states[i]=1
   else:
       co_positive_dish_states[i]=2
   co_positive_dish_power[i]=dish[co_positive_dish_states[i]]
```

```
plt.subplot(2,1,1)
plt.title('Actual Stove Consumption')
plt.xlabel('Time');
plt.ylabel('Power (W)');
subplots_adjust(hspace=.5)
plt.plot(downsampled_timestamp_appliance_date,downsampled_stove)
plt.subplot(2,1,2)
plt.xlabel('Time');
plt.ylabel('Power (W)');
plt.title('Predicted Stove Consumption (CO Positive)')
plt.plot(downsampled_timestamp_appliance_date,co_positive_stove_power);
plt.subplot(2,1,1)
plt.title('Actual Dish Washer Consumption')
plt.xlabel('Time');
plt.ylabel('Power (W)');
subplots_adjust(hspace=.5)
plt.plot(downsampled_timestamp_appliance_date,downsampled_dishwasher)
plt.subplot(2,1,2)
plt.xlabel('Time');
plt.ylabel('Power (W)');
plt.title('Predicted Dish Washer Consumption (CO Positive)')
plt.plot(downsampled_timestamp_appliance_date,co_positive_dish_power);
plt.subplot(2,1,1)
plt.title('Actual Kitchen Consumption')
plt.xlabel('Time');
plt.ylabel('Power (W)');
plt.plot(downsampled_timestamp_appliance_date,downsampled_kitchen)
plt.subplot(2,1,2)
plt.title('Predicted Kitchen Consumption (CO Positive)')
plt.xlabel('Time');
plt.ylabel('Power (W)');
subplots_adjust(hspace=.5)
plt.ylim((0,800))
plt.plot(downsampled_timestamp_appliance_date,co_positive_kitchen_power);
plt.subplot(2,1,1)
plt.title('Actual Kitchen 2 Consumption')
plt.xlabel('Time');
plt.ylabel('Power (W)');
subplots_adjust(hspace=.5)
plt.plot(downsampled_timestamp_appliance_date,downsampled_kitchen_2)
plt.subplot(2,1,2)
plt.title('Predicted Kitchen 2 Consumption (CO Positive)')
plt.xlabel('Time');
plt.ylabel('Power (W)');
plt.ylim((0,800))
```

plt.plot(downsampled\_timestamp\_appliance\_date,co\_positive\_kitchen\_2\_power);

```
residual_power_positive_total=sum(np.abs(residual_power_mains_1))
```

```
residual_power_total=sum(np.abs(residual_power_positive_total))
print "Residual Power is: ",residual_power_positive_total," W"
standard_deviation=np.std(residual_power_mains_1_positive)
print "Standard Deviation is ",standard_deviation
```

Now we see if we take actual mains as in case 1 how does it affect the results, that is if we do not filter the data, how would result be affected.

```
co_kitchen_actual_states=np.zeros(length_sequence,dtype=np.int)
co_kitchen_actual_power=np.zeros(length_sequence)
co_stove_actual_states=np.zeros(length_sequence,dtype=np.int)
co_stove_actual_power=np.zeros(length_sequence)
co_kitchen_2_actual_states=np.zeros(length_sequence,dtype=np.int)
co_kitchen_2_actual_power=np.zeros(length_sequence)
co_dish_actual_states=np.zeros(length_sequence,dtype=np.int)
co_dish_actual_power=np.zeros(length_sequence)
```

```
for i in range(length_sequence):
    if int(states_idx_actual[i])/18==0:
        co_kitchen_actual_states[i]=0

else:
        co_kitchen_actual_states[i]=1
    co_kitchen_actual_power[i]=kitchen[co_kitchen_actual_states[i]]

temp=int(states_idx_actual[i])/9
    if temp%2==0:
        co_stove_actual_states[i]=0
    else:
        co_stove_actual_states[i]=1
    co_stove_actual_power[i]=stove[co_stove_actual_states[i]]
```

```
temp=int(states_idx_actual[i])/3
if temp%3==0:
   co_kitchen_2_actual_states[i]=0
elif temp%3==1:
   co_kitchen_2_actual_states[i]=1
else:
   co_kitchen_2_actual_states[i]=2
co_kitchen_2_actual_power[i]=kitchen_2[co_kitchen_2_actual_states[i]]
temp=int(states_idx_actual[i])%3
if temp==0:
   co_dish_actual_states[i]=0
elif temp==1:
   co_dish_actual_states[i]=1
else:
   co_dish_actual_states[i]=2
co_dish_actual_power[i]=dish[co_dish_actual_states[i]]
```

```
plt.subplot(2,1,1)
plt.title('Actual Stove Consumption')
plt.xlabel('Time');
plt.ylabel('Power (W)');
subplots_adjust(hspace=.5)
plt.plot(downsampled_timestamp_appliance_date,downsampled_stove)
plt.subplot(2,1,2)
plt.xlabel('Time');
plt.ylabel('Power (W)');
plt.title('Predicted Stove Consumption')
plt.plot(downsampled_timestamp_appliance_date,co_positive_stove_power);
```

```
plt.subplot(2,1,1)
plt.title('Actual Dish Washer Consumption')
plt.xlabel('Time');
plt.ylabel('Power (W)');
subplots_adjust(hspace=.5)
plt.plot(downsampled_timestamp_appliance_date,downsampled_dishwasher)
plt.subplot(2,1,2)
plt.xlabel('Time');
plt.ylabel('Power (W)');
plt.title('Predicted Dish Washer Consumption (CO Positive)')
plt.plot(downsampled_timestamp_appliance_date,co_positive_dish_power);
```

```
plt.subplot(2,1,1)
plt.title('Actual Kitchen 2 Consumption')
plt.xlabel('Time');
plt.ylabel('Power (W)');
subplots_adjust(hspace=.5)
plt.plot(downsampled_timestamp_appliance_date,downsampled_kitchen_2)
plt.subplot(2,1,2)
plt.title('Predicted Kitchen 2 Consumption (CO Positive)')
```

```
plt.xlabel('Time');
plt.ylabel('Power (W)');
plt.ylim((0,800))
plt.plot(downsampled_timestamp_appliance_date,co_positive_kitchen_2_power);
```

We now do the same analysis for Mains 2 as we did for Mains 1. Distribution of states space

```
states_combination_2=list(itertools.product(ref,lighting,micro))
print "Possible state combinations for Mains2 are\nRef.,Lighting,Microwave\n",
    states_combination_2
```

```
sum_combination_2=np.array(np.zeros(len(states_combination_2)))
for i in range(0,len(states_combination_2)):
    sum_combination_2[i]=sum(states_combination_2[i])
from copy import deepcopy
b=deepcopy(sum_combination_2)
b.sort()
grid(True);
title('Sorted possible sums of all appliances');
xlabel('Combinations');
ylabel('Power (W)');
plot(b);
```

```
title('Histogram showing relative frequencies of different state combinations');
hist(b,100);
```

```
length_sequence=len(filtered_downsampled_mains_2)
co_ref_states=np.zeros(length_sequence,dtype=np.int)
co_ref_power=np.zeros(length_sequence)
co_micro_states=np.zeros(length_sequence,dtype=np.int)
co_micro_power=np.zeros(length_sequence)
co_lighting_states=np.zeros(length_sequence,dtype=np.int)
co_lighting_power=np.zeros(length_sequence)
```

```
title('Residual Power Mains 2');
xlabel('Time');
ylabel('Power (W)');
plot(residual_power_mains_2);
```

```
for i in range(length_sequence):
   if int(states_idx_2[i])/9==0:
       co_ref_states[i]=0
   elif int(states_idx_2[i])/9==1:
       co_ref_states[i]=1
   else:
       co_ref_states[i]=2
   co_ref_power[i]=ref[co_ref_states[i]]
   temp=int(states_idx_2[i])/3
   if temp%3==0:
       co_lighting_states[i]=0
   elif temp%3==1:
       co_lighting_states[i]=1
   else:
       co_lighting_states[i]=2
   co_lighting_power[i]=lighting[co_lighting_states[i]]
   temp=int(states_idx_2[i])%3
   if temp==0:
       co_micro_states[i]=0
   elif temp==1:
       co_micro_states[i]=1
   else:
       co_micro_states[i]=2
   co_micro_power[i]=micro[co_micro_states[i]]
```

```
plt.subplot(2,1,1)
ylim((0,1000))
plt.title('Actual Ref Consumption')
plt.xlabel('Time');
plt.ylabel('Power (W)');
subplots_adjust(hspace=.5)
plt.plot(downsampled_timestamp_appliance_date,downsampled_refrigerator)
plt.subplot(2,1,2)
plt.xlabel('Time');
plt.ylabel('Power (W)');
plt.ylabel('Predicted Ref Consumption (CO)')
plt.plot(downsampled_timestamp_appliance_date,co_ref_power);
```

```
plt.subplot(2,1,1)
plt.title('Actual Lighting Consumption')
plt.xlabel('Time');
```

```
plt.ylabel('Power (W)');
subplots_adjust(hspace=.5)
plt.plot(downsampled_timestamp_appliance_date,downsampled_lighting)
plt.subplot(2,1,2)
plt.title('Predicted Lighting Consumption (CO)')
plt.xlabel('Time');
plt.ylabel('Power (W)');
plt.ylabel('Power (W)');
plt.ylim((0,200))
plt.plot(downsampled_timestamp_appliance_date,co_lighting_power);
```

```
plt.subplot(2,1,1)
plt.title('Actual Microwave Consumption')
plt.xlabel('Time');
plt.ylabel('Power (W)');
subplots_adjust(hspace=.5)
plt.plot(downsampled_timestamp_appliance_date,downsampled_microwave)
plt.subplot(2,1,2)
plt.xlabel('Time');
plt.ylabel('Power (W)');
plt.title('Predicted Microwave Consumption (CO)')
plt.plot(downsampled_timestamp_appliance_date,co_micro_power);
```

TODO: Violation of switch continuity principle

#### 1.7 Discrete Hidden Markov Model

```
import sys
sys.path.append('/home/nipun/git/PyHMM/src')
from dhmm_em import dhmm_em
```

Using EM algorithm, we try to learn HMM parameters for different appliances.

```
# For Stove which is two state, we try to learn the parameters using Baum
stove_prior=np.array([0.8,0.2])
stove_transmat=np.array([[0.9,0.1],[0.1,0.9]])
stove_emission=np.array([[.9,.1],[0.1,0.9]])
[LL, stove_learnt_prior, stove_learnt_transmat, stove_learnt_obsmat,nr_iter] = dhmm_em([
    labels_stove], stove_prior, stove_transmat, stove_emission, 3500,.0000001);
```

```
title('Log Likelihood vs Iterations for Stove');
xlabel('Iterations');
ylabel('Log Likelihood');
plot(LL);
```

```
def print_hmm_parameters(obsmat,prior,transmat):
   print "Learnt HMM Parameters\nObservation Matrix ",obsmat,"\nPrior ",prior," \
       nTransition Matrix ",transmat
print_hmm_parameters(stove_learnt_obsmat,stove_learnt_prior,stove_learnt_transmat)
# For Stove which is two state, we try to learn the parameters using Baum
ref_prior=np.array([0.9,0.05,0.05])
ref_transmat=np.array([[0.95,0.05,0],[0.05,0.9,0.05],[0.05,0.05,..9]])
ref_emission=np.array([[.99,.01,0],[0.05,0.9,.05],[0.05,0.05,.9]])
[LL, ref_learnt_prior, ref_learnt_transmat, ref_learnt_obsmat,nr_iter] = dhmm_em([
    labels_ref], ref_prior, ref_transmat, ref_emission, 3500,.0000001 );
title('Log Likelihood vs Iterations for Ref.');
xlabel('Iterations');
ylabel('Log Likelihood');
plot(LL);
print_hmm_parameters(ref_learnt_obsmat,ref_learnt_prior,ref_learnt_transmat)
# For Stove which is two state, we try to learn the parameters using Baum
micro_prior=np.array([0.9,0.05,0.05])
micro_transmat=np.array([[0.95,0.05,0],[0.05,0.9,0.05],[0.05,0.05,.9]])
micro_emission=np.array([[.99,.01,0],[0.05,0.9,.05],[0.05,0.05,.9]])
[LL, micro_learnt_prior, micro_learnt_transmat, micro_learnt_obsmat,nr_iter] = dhmm_em([
   labels_micro], micro_prior, micro_transmat, micro_emission, 3500,.0000001 );
title('Log Likelihood vs Iterations for Micro');
xlabel('Iterations');
ylabel('Log Likelihood');
plot(LL);
print_hmm_parameters(micro_learnt_obsmat,micro_learnt_prior,micro_learnt_transmat)
# For Stove which is two state, we try to learn the parameters using Baum
lighting_prior=np.array([0.9,0.05,0.05])
lighting_transmat=np.array([[0.95,0.05,0],[0.05,0.9,0.05],[0.05,0.05,.9]])
lighting_emission=np.array([[.99,.01,0],[0.05,0.9,.05],[0.05,0.05,.9]])
[LL, lighting_learnt_prior, lighting_learnt_transmat, lighting_learnt_obsmat,nr_iter] =
    dhmm_em([labels_lighting], lighting_prior, lighting_transmat, lighting_emission,
    3500,.0000001);
title('Log Likelihood vs Iterations for Lighting');
xlabel('Iterations');
ylabel('Log Likelihood');
```

```
plot(LL);
print_hmm_parameters(lighting_learnt_obsmat,lighting_learnt_prior,
    lighting_learnt_transmat)
# For Stove which is two state, we try to learn the parameters using Baum
dishwasher_prior=np.array([0.9,0.05,0.05])
dishwasher_transmat=np.array([[0.95,0.05,0],[0.05,0.9,0.05],[0.05,0.05,.9]])
dishwasher_emission=np.array([[.99,.01,0],[0.05,0.9,.05],[0.05,0.05,.9]])
[LL, dishwasher_learnt_prior, dishwasher_learnt_transmat, dishwasher_learnt_obsmat,
   nr_iter] = dhmm_em([labels_dish], dishwasher_prior, dishwasher_transmat,
    dishwasher_emission, 3500,.0000001 );
title('Log Likelihood vs Iterations for Dishwasher');
xlabel('Iterations');
ylabel('Log Likelihood');
plot(LL);
print_hmm_parameters(dishwasher_learnt_obsmat,dishwasher_learnt_prior,
    dishwasher_learnt_transmat)
# For Stove which is two state, we try to learn the parameters using Baum
kitchen_2_prior=np.array([0.9,0.05,0.05])
kitchen_2_transmat=np.array([[0.95,0.05,0],[0.05,0.9,0.05],[0.05,0.05,.9]])
kitchen_2_emission=np.array([[.99,.01,0],[0.05,0.9,.05],[0.05,0.05,.9]])
[LL, kichen_2_learnt_prior, kitchen_2_learnt_transmat, kitchen_2_learnt_obsmat,nr_iter]
    = dhmm_em([labels_kitchen_2], kitchen_2_prior, kitchen_2_transmat, kitchen_2_emission
    , 3500,.0000001);
title('Log Likelihood vs Iterations for Kitchen 2');
xlabel('Iterations');
ylabel('Log Likelihood');
plot(LL);
print_hmm_parameters(kitchen_2_learnt_obsmat,kichen_2_learnt_prior,
    kitchen_2_learnt_transmat)
# For Stove which is two state, we try to learn the parameters using Baum
kitchen_prior=np.array([0.95,0.05])
kitchen_transmat=np.array([[0.95,0.05],[0.05,0.95]])
kitchen_emission=np.array([[.99,.01],[0.01,0.99]])
[LL, kitchen_learnt_prior, kitchen_learnt_transmat, kitchen_learnt_obsmat,nr_iter] =
    dhmm_em([labels_kitchen], kitchen_prior, kitchen_transmat, kitchen_emission,
    3500,.0000001);
```

```
title('Log Likelihood vs Iterations for Kitchen');
xlabel('Iterations');
ylabel('Log Likelihood');
plot(LL);
```

```
print_hmm_parameters(kitchen_learnt_obsmat,kitchen_learnt_prior,kitchen_learnt_transmat)
```

#### 1.8 Creating FHMM

Combining different states according to technique used for FHMM. We define functions for combining constituent priors into prior for FHMM and similarly for Transition and Emission matrices. For mains 2

```
def calculate_combined_pie(ordered_list_appliance_pies):
    total_series=len(ordered_list_appliance_pies)
    result=np.array(ordered_list_appliance_pies[0])
    for i in range(total_series-1):
        m=np.vstack(result.flatten())
        size_n=len(ordered_list_appliance_pies[i+1])
        n=np.reshape(ordered_list_appliance_pies[i+1],(1,size_n))
        result=np.dot(m,n)
    return result.flatten()
```

Combining the transition matrices and the emission matrices. It should be seen that it can be done by Kronecker multiplication.

```
def calculate_combined_A(ordered_transmat_list):
    total_series=len(ordered_transmat_list)
    result=ordered_transmat_list[0]
    for i in range(total_series-1):
        result=np.kron(result,ordered_transmat_list[i+1])
    return result
```

Now Viterbi algorithm is used to decode the most likely sequence.

```
from viterbi_path import path;
```

We plot the predicted state sequence and compare against observed state sequence.

```
title('Observed State Sequence');
plot(states_idx_2);
```

We now see the observations and map them from 0 to 26 based on closeness to the total power in those cases.

```
viterbi_produced_path=path(pie_combined,A_combined,B_combined,states_idx_2)
path_produced=viterbi_produced_path[0]
```

```
title('Predicted State Sequence according to Viterbi');
plot(path_produced);
```

```
length_sequence=len(filtered_downsampled_mains_2)
hmm_ref_states=np.zeros(length_sequence,dtype=np.int)
hmm_ref_power=np.zeros(length_sequence)
hmm_micro_states=np.zeros(length_sequence,dtype=np.int)
hmm_micro_power=np.zeros(length_sequence)
hmm_lighting_states=np.zeros(length_sequence,dtype=np.int)
hmm_lighting_power=np.zeros(length_sequence)
```

```
for i in range(length_sequence):
   if int(path_produced[i])/9==0:
       hmm_ref_states[i]=0
   elif int(path_produced[i])/9==1:
       hmm_ref_states[i]=1
   else:
       hmm_ref_states[i]=2
   hmm_ref_power[i]=ref[hmm_ref_states[i]]
   temp=int(path_produced[i])/3
   if temp%3==0:
       hmm_lighting_states[i]=0
   elif temp%3==1:
       hmm_lighting_states[i]=1
   else:
       hmm_lighting_states[i]=2
   hmm_lighting_power[i]=lighting[hmm_lighting_states[i]]
   temp=int(path_produced[i])%3
   if temp==0:
       hmm_micro_states[i]=0
   elif temp==1:
       hmm_micro_states[i]=1
       hmm_micro_states[i]=2
   hmm_micro_power[i]=micro[hmm_micro_states[i]]
```

```
plt.subplot(3,1,1)
ylim((0,1000))
plt.title('Actual Ref Consumption')
subplots_adjust(hspace=.5)
plt.plot(downsampled_timestamp_appliance_date,downsampled_refrigerator)
plt.subplot(3,1,2)
plt.title('Predicted Ref Consumption (FHMM)')
plt.plot(downsampled_timestamp_appliance_date,hmm_ref_power);
plt.subplot(3,1,3)
plt.title('Predicted Ref Consumption (CO)')
plt.plot(downsampled_timestamp_appliance_date,co_ref_power);
```

```
plt.subplot(3,1,1)
plt.title('Actual Lighting Consumption')
subplots_adjust(hspace=.5)
plt.plot(downsampled_timestamp_appliance_date,downsampled_lighting)
plt.subplot(3,1,2)
plt.ylim((0,200))
plt.title('Predicted Lighting Consumption (FHMM)')
plt.plot(downsampled_timestamp_appliance_date,hmm_lighting_power);
plt.subplot(3,1,3)
plt.ylim((0,200))
plt.title('Predicted Lighting Consumption (CO)')
plt.title('Predicted Lighting Consumption (CO)')
plt.plot(downsampled_timestamp_appliance_date,co_lighting_power);
```

```
plt.subplot(3,1,1)
plt.title('Actual Micro Consumption')
subplots_adjust(hspace=.5)
plt.plot(downsampled_timestamp_appliance_date,downsampled_microwave)
plt.subplot(3,1,2)
plt.title('Predicted Micro Consumption (FHMM)')
plt.plot(downsampled_timestamp_appliance_date,hmm_micro_power);
plt.subplot(3,1,3)
plt.title('Predicted Micro Consumption (CO)')
plt.plot(downsampled_timestamp_appliance_date,co_micro_power);
```

```
ref_accuracy=print_confusion_matrix("Ref",len(ref),labels_ref,hmm_ref_states)
micro_accuracy=print_confusion_matrix("Micro",len(micro),labels_micro,hmm_micro_states)
lighting_accuracy=print_confusion_matrix("Lighting",len(lighting),labels_lighting,
    hmm_lighting_states)
```

We do a similar analysis for Mains 1.

```
viterbi_produced_path_1=path(pie_combined_1,A_combined_1,B_combined_1,states_idx)
path_produced_1=viterbi_produced_path_1[0]
```

```
hmm_kitchen_actual_states=np.zeros(length_sequence,dtype=np.int)
hmm_kitchen_actual_power=np.zeros(length_sequence)
hmm_stove_actual_states=np.zeros(length_sequence,dtype=np.int)
hmm_stove_actual_power=np.zeros(length_sequence)
hmm_kitchen_2_actual_states=np.zeros(length_sequence,dtype=np.int)
hmm_kitchen_2_actual_power=np.zeros(length_sequence)
hmm_dish_actual_states=np.zeros(length_sequence,dtype=np.int)
hmm_dish_actual_power=np.zeros(length_sequence)
```

```
for i in range(length_sequence):
   if int(path_produced_1[i])/18==0:
       hmm_kitchen_actual_states[i]=0
   else:
       hmm_kitchen_actual_states[i]=1
   hmm_kitchen_actual_power[i]=kitchen[hmm_kitchen_actual_states[i]]
   temp=int(path_produced_1[i])/9
   if temp%2==0:
       hmm_stove_actual_states[i]=0
   else:
       hmm_stove_actual_states[i]=1
   hmm_stove_actual_power[i]=stove[hmm_stove_actual_states[i]]
   temp=int(path_produced_1[i])/3
   if temp%3==0:
       hmm_kitchen_2_actual_states[i]=0
   elif temp%3==1:
       hmm_kitchen_2_actual_states[i]=1
   else:
       hmm_kitchen_2_actual_states[i]=2
   hmm_kitchen_2_actual_power[i]=kitchen_2[hmm_kitchen_2_actual_states[i]]
   temp=int(path_produced_1[i])%3
   if temp==0:
       hmm_dish_actual_states[i]=0
   elif temp==1:
       hmm_dish_actual_states[i]=1
   else:
       hmm_dish_actual_states[i]=2
   hmm_dish_actual_power[i]=dish[hmm_dish_actual_states[i]]
```

```
plt.subplot(3,1,1)
ylim((0,1000))
plt.title('Actual Kitchen Consumption')
subplots_adjust(hspace=.5)
```

```
plt.plot(downsampled_timestamp_appliance_date,downsampled_kitchen)
plt.subplot(3,1,2)
ylim((0,1000))
plt.title('Predicted Kitchen Consumption (FHMM)')
plt.plot(downsampled_timestamp_appliance_date,hmm_kitchen_actual_power);
plt.subplot(3,1,3)
vlim((0,1000))
plt.title('Predicted Kitchen Consumption (CO)')
plt.plot(downsampled_timestamp_appliance_date,co_kitchen_power);
plt.subplot(3,1,1)
vlim((0,1000))
plt.title('Actual Kitchen 2 Consumption')
subplots_adjust(hspace=.5)
plt.plot(downsampled_timestamp_appliance_date,downsampled_kitchen_2)
plt.subplot(3,1,2)
ylim((0,1000))
plt.title('Predicted Kitchen 2 Consumption (FHMM)')
plt.plot(downsampled_timestamp_appliance_date,hmm_kitchen_2_actual_power);
plt.subplot(3,1,3)
ylim((0,1000))
plt.title('Predicted Kitchen 2 Consumption (CO)')
plt.plot(downsampled_timestamp_appliance_date,co_kitchen_2_power);
plt.subplot(3,1,1)
plt.title('Actual Stove Consumption')
subplots_adjust(hspace=.5)
plt.plot(downsampled_timestamp_appliance_date,downsampled_stove)
plt.subplot(3,1,2)
plt.title('Predicted Stove Consumption (FHMM)')
plt.plot(downsampled_timestamp_appliance_date,hmm_stove_actual_power);
plt.subplot(3,1,3)
plt.title('Predicted Stove Consumption (CO)')
plt.plot(downsampled_timestamp_appliance_date,co_stove_power);
plt.subplot(3,1,1)
plt.title('Actual Dishwasher Consumption')
subplots_adjust(hspace=.5)
plt.plot(downsampled_timestamp_appliance_date,downsampled_dishwasher)
plt.subplot(3,1,2)
plt.title('Predicted Dishwasher Consumption (FHMM)')
plt.plot(downsampled_timestamp_appliance_date,hmm_dish_actual_power);
```

plt.subplot(3,1,3)

plt.title('Predicted Dishwasher Consumption (CO)')

plt.plot(downsampled\_timestamp\_appliance\_date,co\_dish\_power);

```
hmm_kitchen_2_actual_states)
stove_accuracy=print_confusion_matrix("Stove",len(stove),labels_stove,
   hmm_stove_actual_states)
dish_accuracy=print_confusion_matrix("Dish Washer",len(dish),labels_dish,
   hmm_dish_actual_states)
```

We now compare the accuracies of the two approaches across different mains circuits.

```
plt.title('Disaggregation Accuracy for Mains 2');
plt.ylabel('Accuracy')
plt.ylim((50,100))
plt.bar( numpy.arange(3) * 2, [91.03,93.03,82.8], color = 'red' );
plt.bar( numpy.arange(3) * 2 +0.8, [93.29,93.54,82.2], color = 'green' );
locs, labels = xticks();
xticks(locs+1, ('Refrigerator',' ', 'Microwave',' ', 'Lighting'));
plt.legend(('FHMM','CO'),);
```