

0 - 0,064	0 - 0,44	0,32 - 3,008	2,88 - 4,032	3,504 + 4,915
30	350	2500	1200	400

### 3.2.1 anatype

$$P(\bar{x}) =$$

$$\bar{x} = \frac{2x}{\pi}$$

$$\Rightarrow x = \frac{\pi}{2} \bar{x}$$

$$P(x) = \sin(\quad)$$

$$P(\bar{x}) = a\bar{x} + b\bar{x}^3 + c\bar{x}^5$$

$$P(\bar{x}=1) = a + b + c = P(x = \frac{\pi}{2}) = \sin\left(\frac{\pi}{2}\right) = 1$$

$$x = \frac{\pi}{2}$$

$$a + b + c = 1 \quad (1)$$

$$P'(\bar{x}) = a + 3b\bar{x} + 5c\bar{x}^4$$

$$P'(\bar{x}=2) = a + 3b + 5c = \frac{\pi}{2} \cos\left(\frac{\pi}{2} \bar{x}\right)_{\bar{x}=1} = 0$$

$$a + 3b + 5c = 0$$

$$\begin{cases} a+b+c=1 \\ a+3b+5c=0 \end{cases} \Rightarrow \begin{cases} b=1-a-c \\ a+3(1-a-c)+5c=0 \end{cases}$$

$$\begin{cases} b=1-a-c \\ a+3-3a-3c+5c=0 \end{cases}$$

$$\begin{cases} b=1-a-c \\ 2c=2a-3 \end{cases} \Rightarrow \begin{cases} b=1-a-(a-\frac{3}{2}) \\ c=a-\frac{3}{2} \end{cases}$$

$$\begin{cases} b=-2a+\frac{5}{2} \\ c=a-\frac{3}{2} \end{cases}$$

$$c-) \quad p'(\bar{x}=0) = (a + 3b\bar{x}^2 + 5c\bar{x}^4)_{\bar{x}=0} = \left(\frac{\pi}{2} \cos\left(\frac{\pi}{2}\bar{x}\right)\right)_{\bar{x}=0} = 0$$

$$\Rightarrow \boxed{a = \frac{\pi}{2}}$$

$$\begin{aligned} \int_0^2 p(\bar{x}) d\bar{x} &= \int_0^1 \sin\left(\frac{\pi}{2}\bar{x}\right) d\bar{x} \\ &= \left[ -\frac{\cos\left(\frac{\pi}{2}\bar{x}\right)}{\frac{\pi}{2}} \right]_0^1 \\ &= \frac{(-\cos(\frac{\pi}{2} \cdot 1) + \cos(0))}{\pi/2} \end{aligned}$$

$$\int_0^1 p(\bar{x}) d\bar{x} = \frac{2}{\pi}$$

$$\int_0^1 p(\bar{x}) d\bar{x} = \int_0^1 a\bar{x} + b\bar{x}^3 + c\bar{x}^5 d\bar{x}$$

$$= \left[ \frac{a}{2} \bar{x}^2 + \frac{b}{4} \bar{x}^4 + \frac{c}{6} \bar{x}^6 \right]_0^1$$

$$= \frac{a}{2} + \frac{b}{4} + \frac{c}{6} = \frac{2}{\pi}$$

$$a = \frac{4}{\pi} - \frac{b}{2} - \frac{c}{3}$$

$$a = \frac{4}{\pi} - \left( -a + \frac{5}{4} \right) - \left( \frac{a}{3} - \frac{1}{2} \right)$$

$$a = \frac{4}{\pi} + \cancel{a} - \frac{5}{4} - \frac{a}{3} + \frac{1}{2}$$

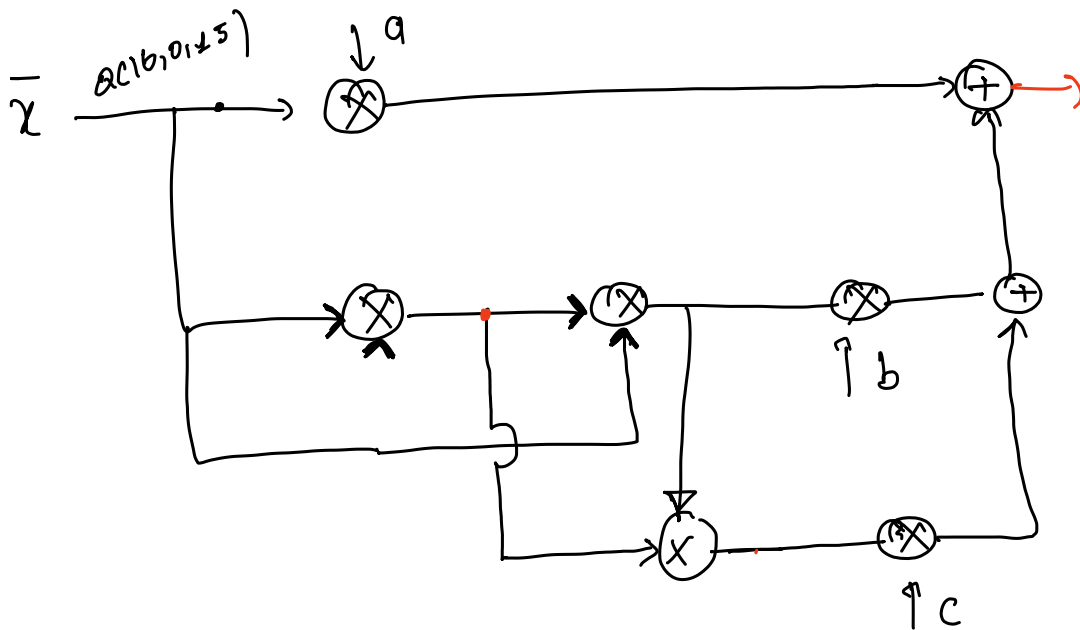
$$\Rightarrow \frac{a}{3} = \frac{4}{\pi} - \frac{5}{4} + \frac{1}{2}$$

$$\Rightarrow a = \frac{12}{\pi} - \frac{15}{4} + \frac{3}{2}$$

$$= \frac{12}{\pi} - \frac{15 + 6}{4}$$

$$a = \frac{12}{\pi} - \frac{9}{4}$$

$$P(\bar{x}) = a\bar{x} + b\bar{x}^3 + c\bar{x}^5 \Rightarrow$$



Dynamique de sortie de  $P(\bar{x})$  :

$$-1 \leq \bar{x} \leq 1$$

$\Rightarrow$

$$-1 \leq \bar{x}^3 \leq 1$$

$$-1 \leq \bar{x}^5 \leq 1$$

$$a \cdot \bar{x} \in [-1,56, 1,56]$$

$$b \bar{x}^3 \in [-0,63, 0,63]$$

$$c \bar{x}^5 \in [-0,69, 0,69]$$

$$\} \Rightarrow P(\bar{x}) \in [-2,95, 2,25]$$

$$\bar{x} \Rightarrow Q(16, 0, 15)$$

$$a = 1,56 \Rightarrow Q_a(16, 1, 14)$$

$$b = -0,63 \Rightarrow Q_b(16, 0, 15)$$

$$c = 90b \Rightarrow Q_c(16, -4, 19)$$

$$\bar{\chi} \cdot a \Rightarrow Q_{\bar{\chi} \cdot a} (32, 2, 29) \Rightarrow Q_{\bar{\chi} \cdot a} (16, 2, 13)$$

$$\bar{\chi}^3 \cdot b \Rightarrow Q_{\bar{\chi}^3 \cdot a} (32, 1, 30) \Rightarrow Q_{\bar{\chi} \cdot b} (16, 1, 14)$$

$$\bar{\chi}^3 \cdot c \Rightarrow Q_{\bar{\chi}^3 \cdot c} (32, 1, 30) \Rightarrow Q_{\bar{\chi}^3 \cdot c} (16, 1, 14)$$

