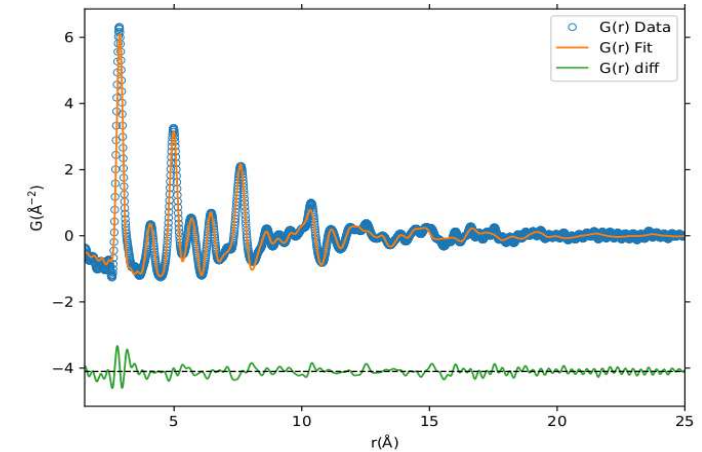
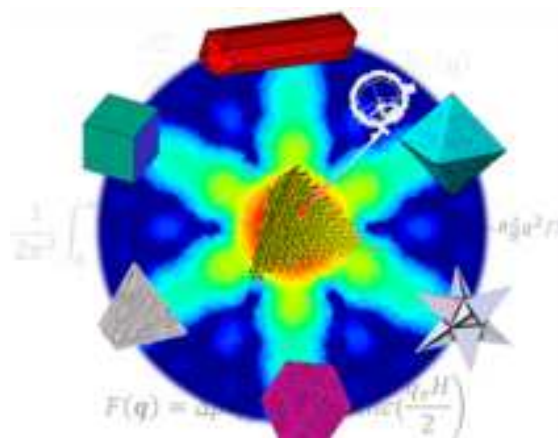
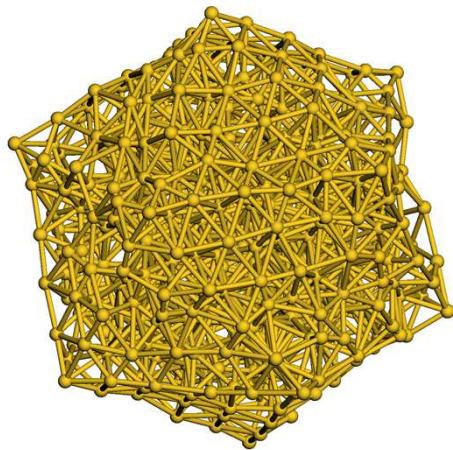




# Machine learning assisted structural characterization of nanoclusters using X Ray scattering



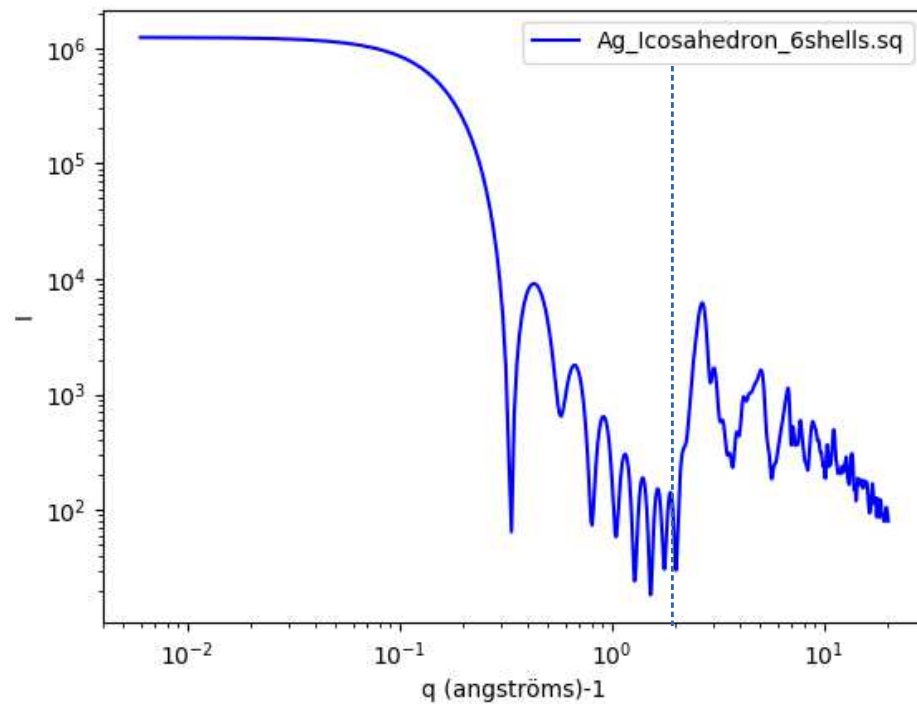
N. Ratel-Ramond – S. Cayez

# X-Ray scattering techniques

$Q < 1 \text{ \AA}^{-1}$ : Small Angle Region (SAXS)

$1$ : Wide Angle Region (WAXS)

- particle size
- particle shape
- arrangement of particles



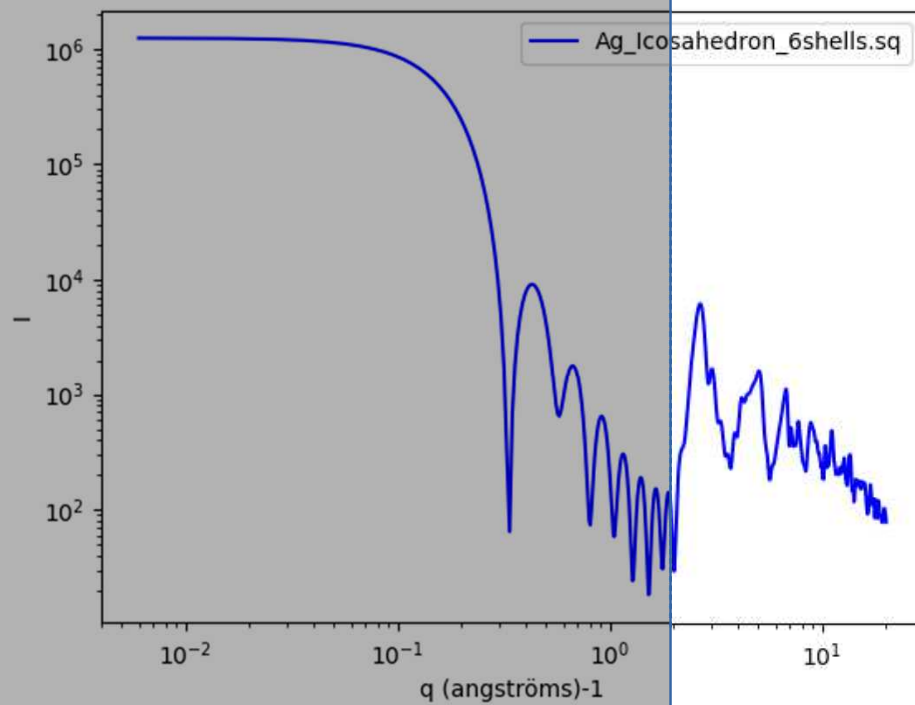
$Q > 1 \text{ \AA}^{-1}$

# X-Ray scattering techniques

$Q < 1 \text{ \AA}^{-1}$ : Small Angle Region (SAXS)

$1 < Q < 10 \text{ \AA}^{-1}$ : Wide Angle Region (WAXS)

- particle size
- particle shape
- arrangement of particles



$Q > 10 \text{ \AA}^{-1}$

# X-Ray scattering techniques: WAXS

RECIPROCAL SPACE

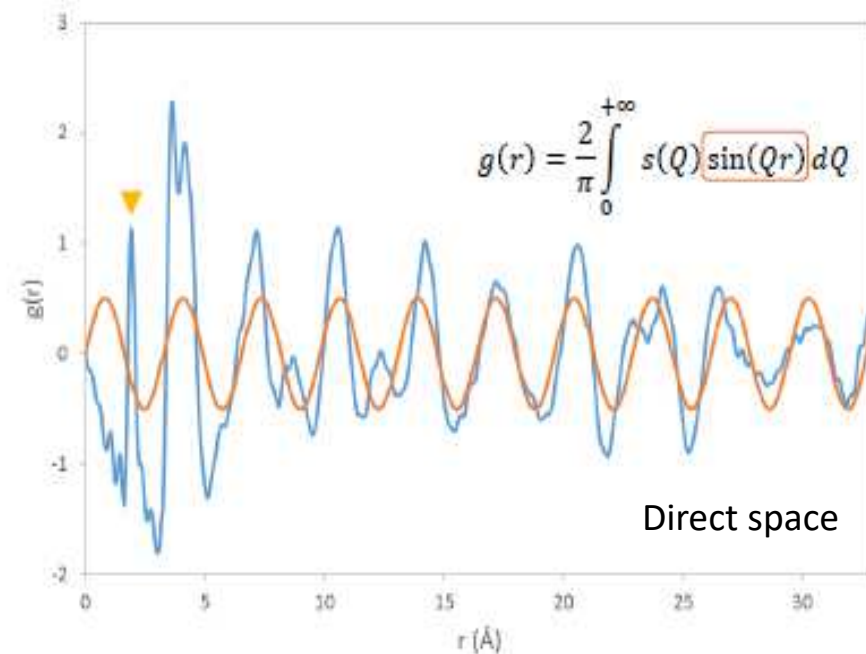
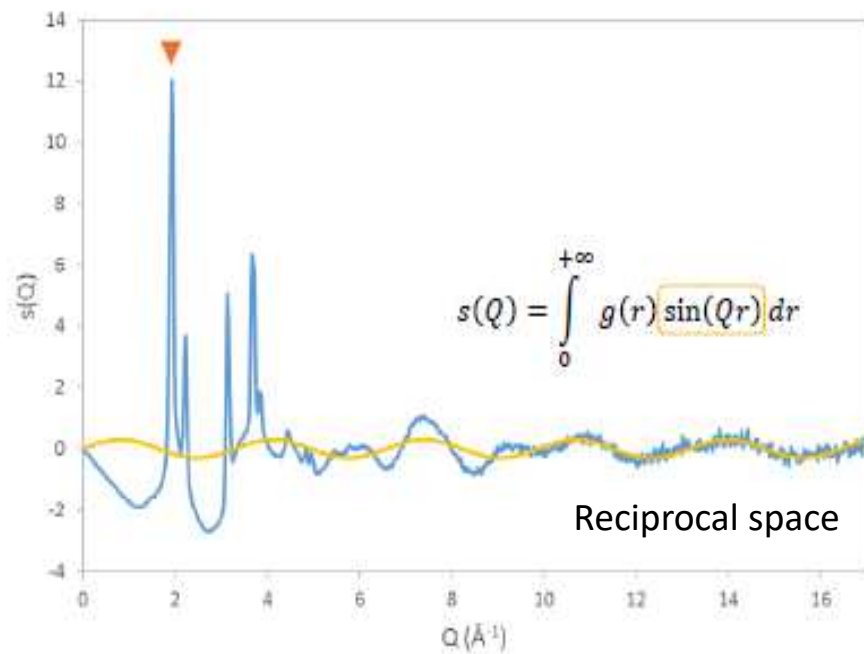
$$\begin{matrix} I(Q) \\ \rightarrow S(Q) \\ F(Q) \end{matrix} = \frac{Q}{4\pi \sin(\theta)} \lambda$$

Fourier transform

REAL SPACE

$g(r)$

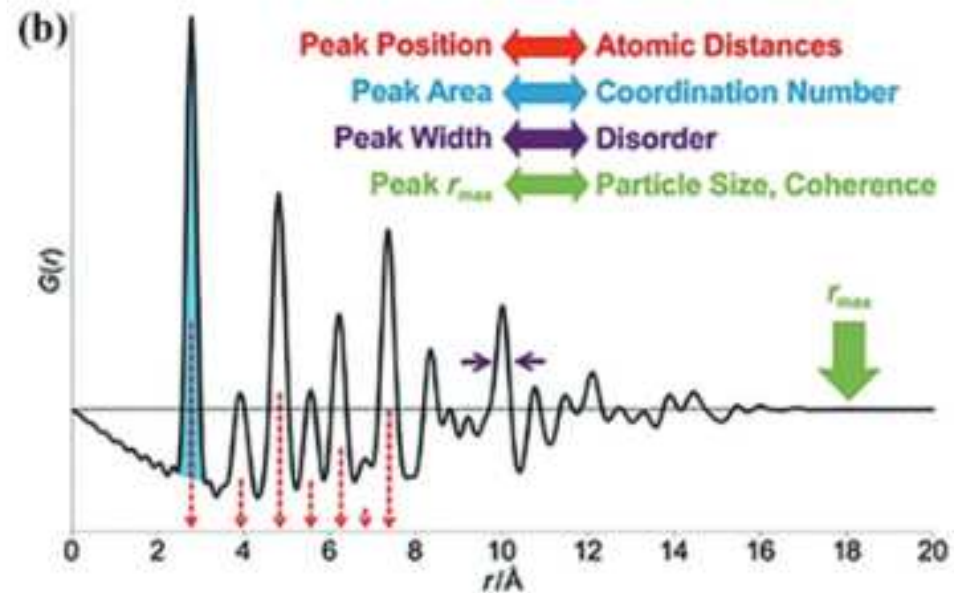
$G(r)$



# X-Ray scattering techniques: WAXS

## ◆ What type of information in a PDF ?

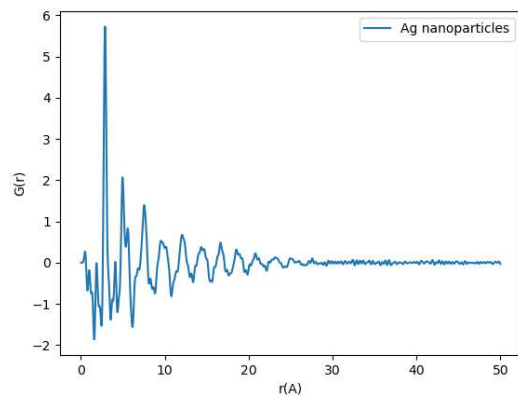
- ◆ Atomic distances
- ◆ Coordination number
- ◆ Disorder
- ◆ Particle size



➡ Structural information at the atomic scale

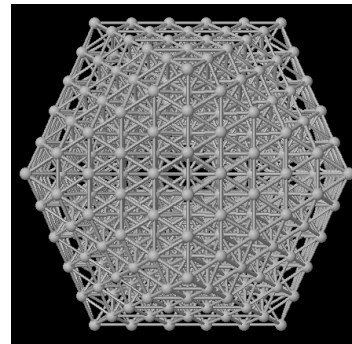
# X-Ray scattering techniques: WAXS

◆ Example: Ag nanoparticles (R. Parmar, L.M. Lacroix, G. Viau)



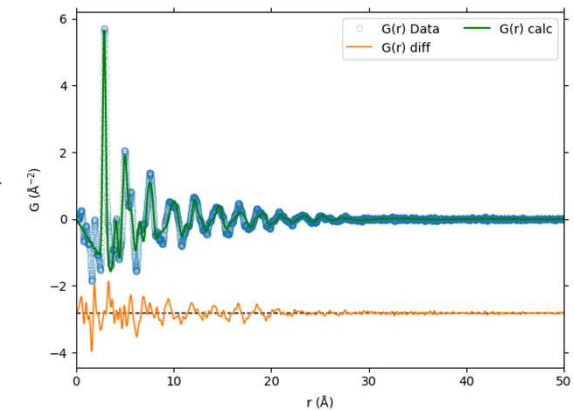
Experimental PDF does not match with cubic structure

Build model  
using ASE  
Python library



Icosahedral model with 6 layers

Refine model  
using diffpy-cmi  
python library



Adjust the  
parameters  
of the model



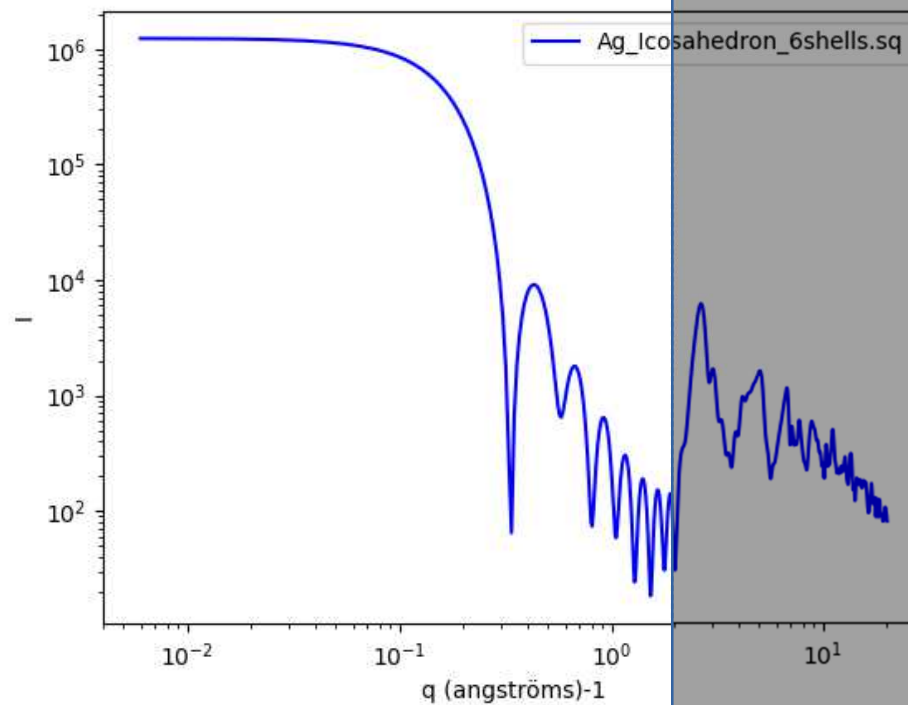
Best  $R_w=0,23$

# X-Ray scattering techniques: SAXS

$Q < 1 \text{ \AA}^{-1}$ : Small Angle Region (SAXS)

$1$ : Wide Angle Region (WAXS)

- particle size
- particle shape
- arrangement of particles

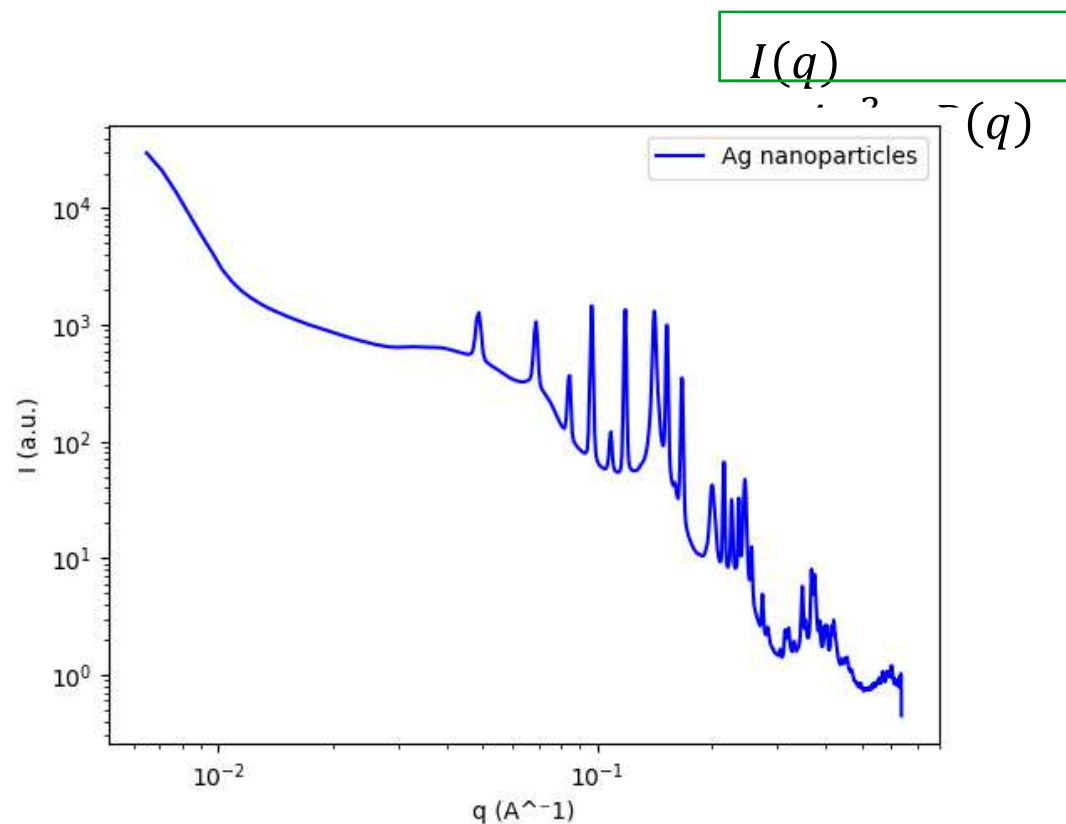


$Q > 1 \text{ \AA}^{-1}$

# X-Ray scattering techniques: SAXS

◆ Theoretical Aspects : the general equation of SAXS has the following expression

◆



- Information about:
  - × Size
  - × Size distribution
  - × Shape
  - × Surface structure
  - × Arrangement of particles



# X-Ray scattering techniques: SAXS

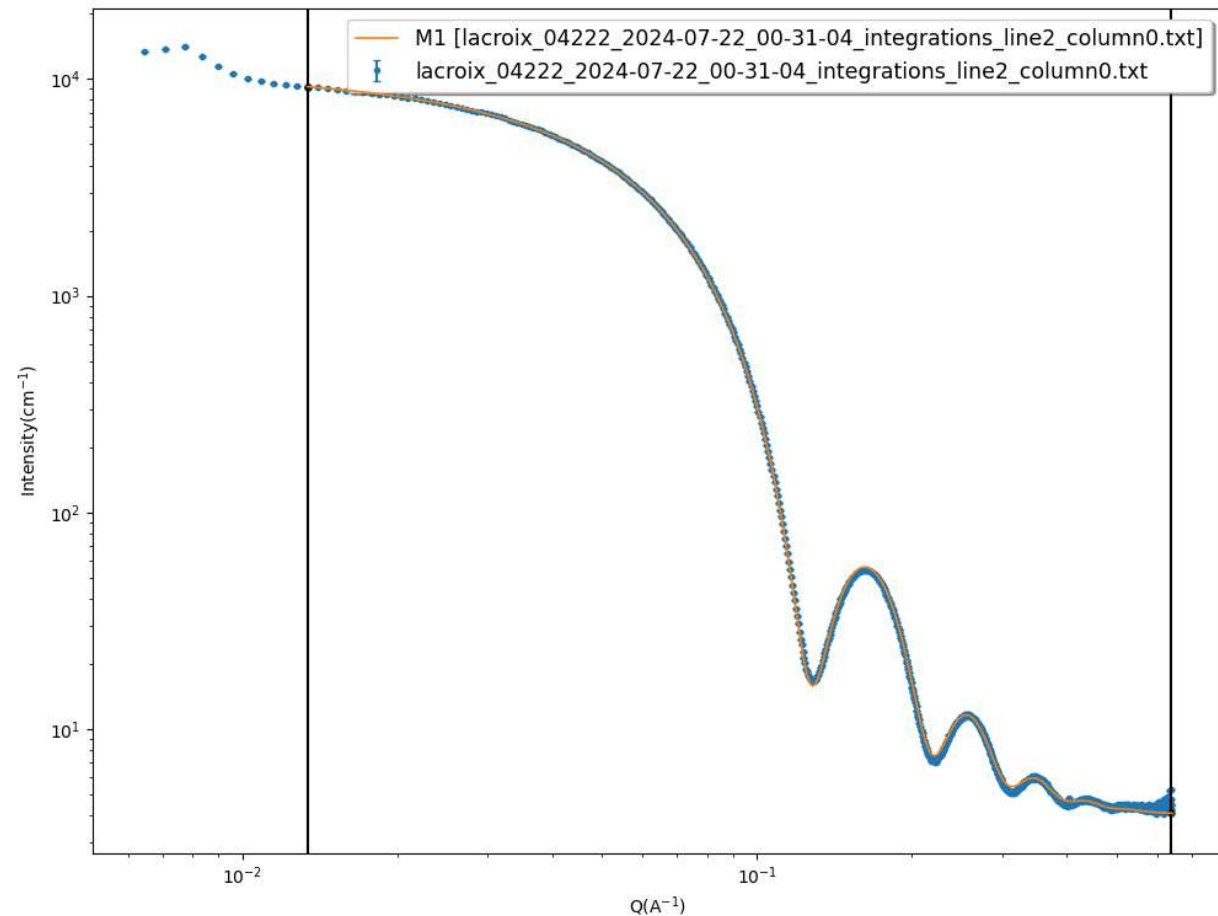
## 1. Form factor analysis

For dilute systems

Example of Au nanoparticles:

Model: sphere

Radius =  $34.907 \pm 0.071 \text{ \AA}$ ,  
polydispersity ratio =  $0.062 \pm 0.004$   
(gaussian)

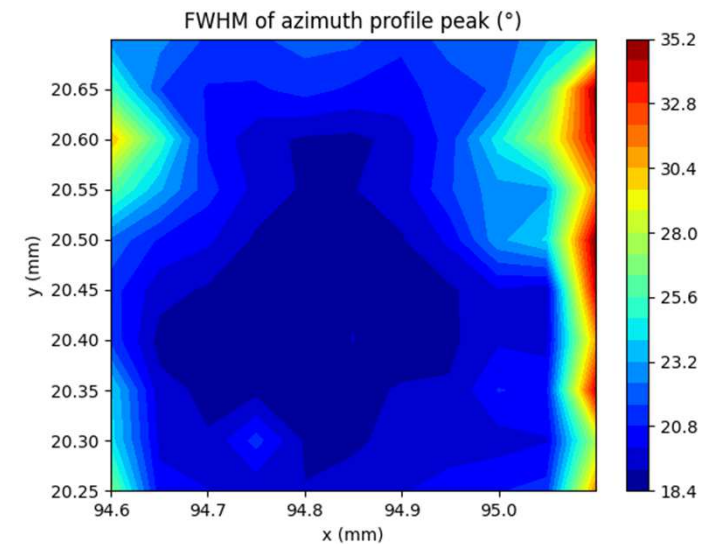
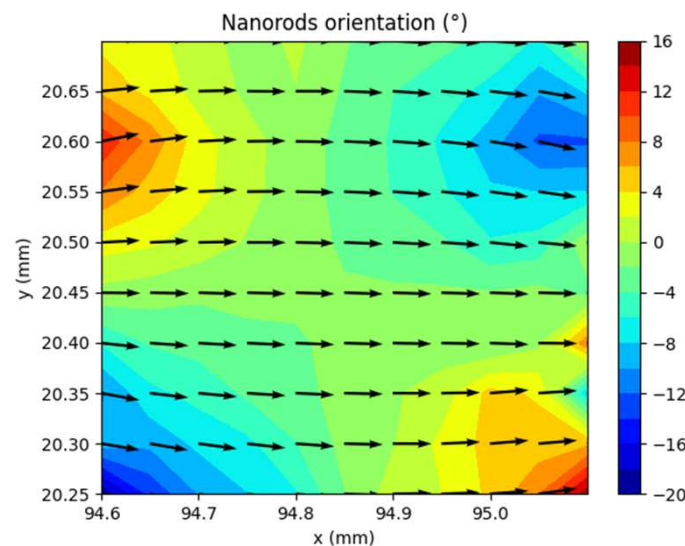
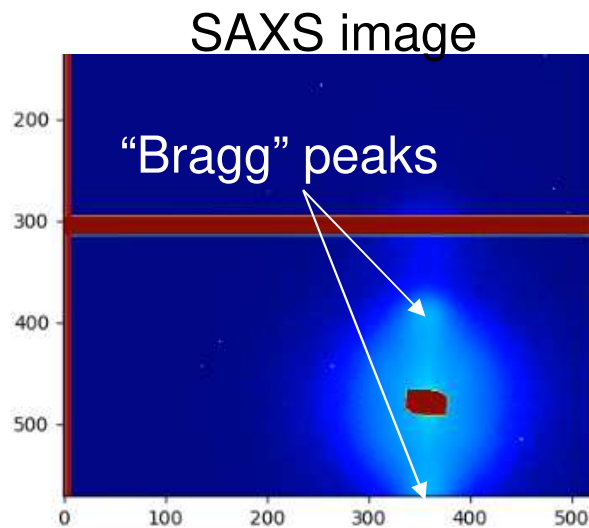


A. Pham, C. Chinaud-Chaix, S. Tricard

# X-Ray scattering techniques: SAXS

## 2. Structure factor analysis: Crystalline assemblies – lattice indexing

Example of  $\mu$ SAXS investigation of micromagnets built by magnetophoresis from Co nanorods (L.M. Lacroix, G. Viau)

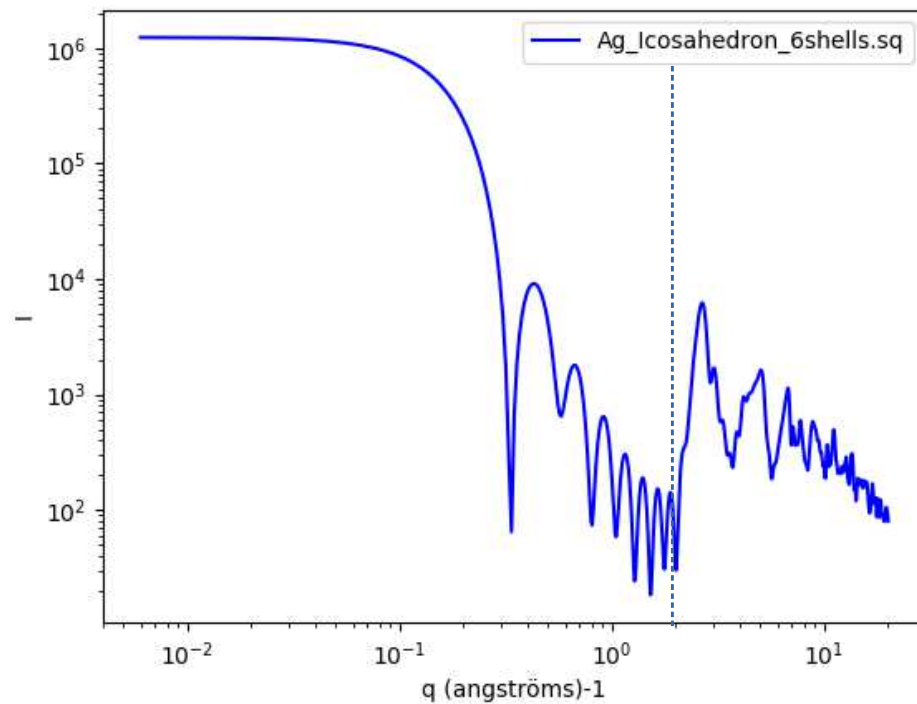


# X-Ray scattering techniques: SAXS

$Q < 1 \text{ \AA}^{-1}$ : Small Angle Region (SAXS)

$1$ : Wide Angle Region (WAXS)

- particle size
- particle shape
- arrangement of particles



$Q > 1 \text{ \AA}^{-1}$

SWAXS techniques are well suited for nano and atomic scale structural characterization of nanoclusters

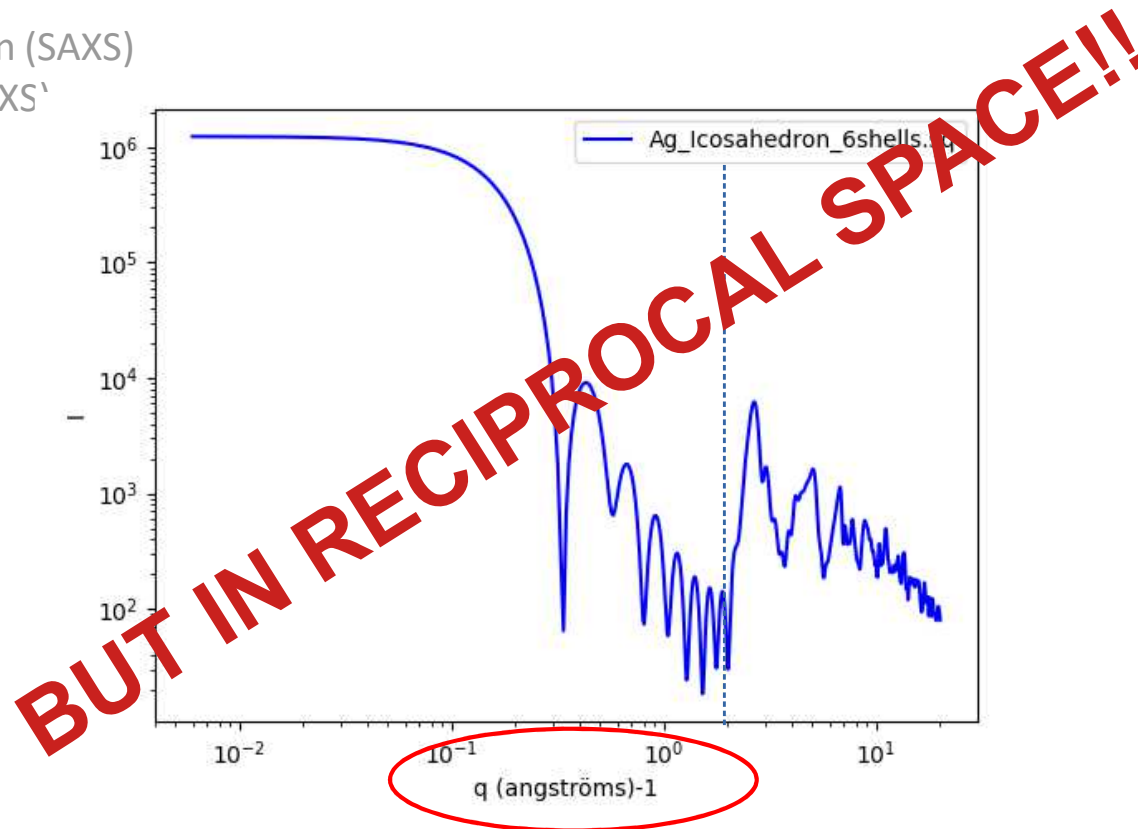
# X-Ray scattering techniques: SAXS

$Q < 1 \text{ \AA}^{-1}$ : Small Angle Region (SAXS)

$1$ : Wide Angle Region (WAXS)

- particle size
- particle shape
- arrangement of particles

$Q > 1 \text{ \AA}^{-1}$



SWAXS techniques are well suited for nano and atomic scale structural characterization of nanoclusters

# Machine learning assisted SWAXS analysis

Purpose: algorithm for the prediction of the size and shape of monometallic nanoparticles from SAXS/WAXS scattering data, particularly for non crystalline structures

## Methodology:

- Create dataset
  - build structural models
  - calculate the corresponding scattering curve
  - store the results with the corresponding labels (shape, size, atom type)

- Choose ML model



- Training

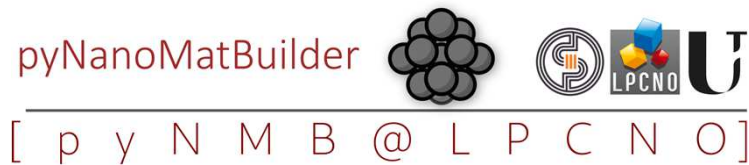
TRAINING

- Testing

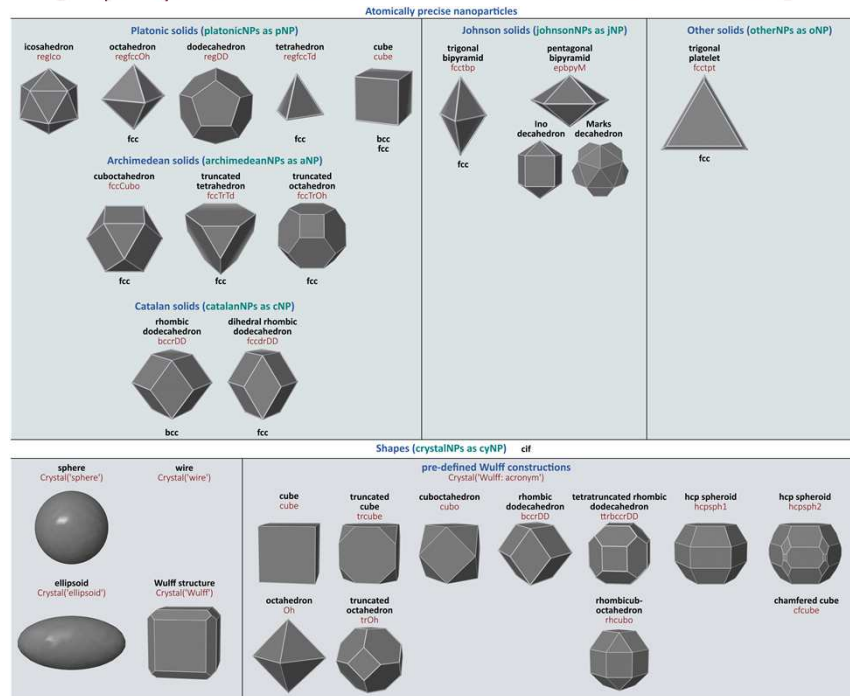


# Machine learning assisted SWAXS analysis

- Create dataset
  - build structural models
  - calculate the corresponding scattering curve
  - store the results with the corresponding labels (shape, size, atom type)



R. Poteau – LPCNO - MCP



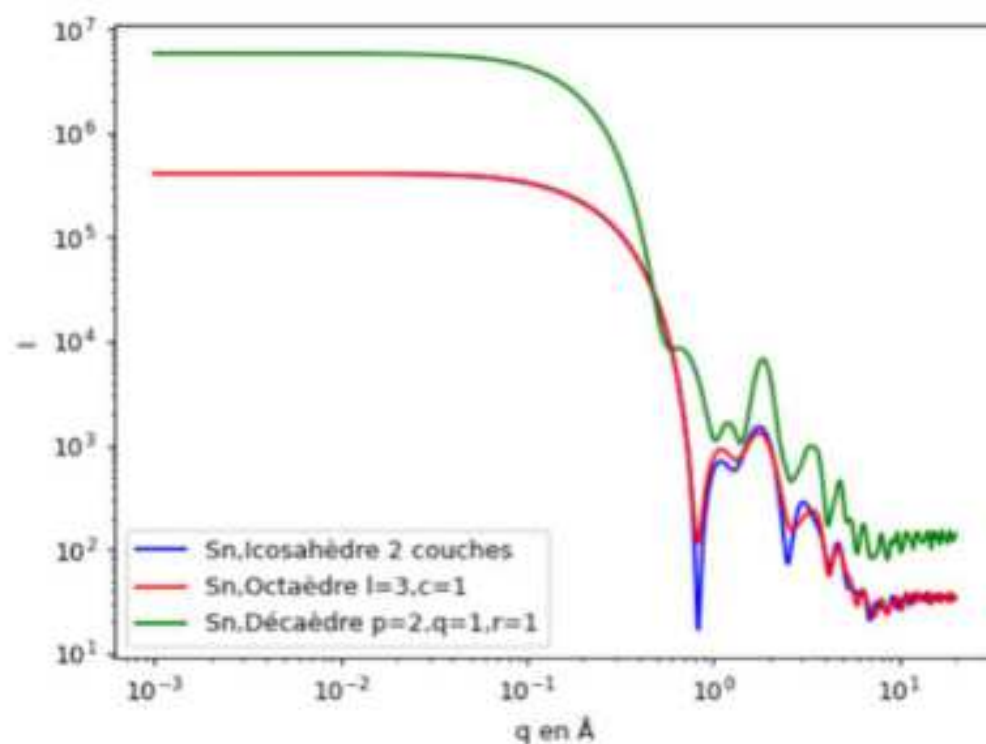
# Machine learning assisted SWAXS analysis

- Create dataset
  - build structural models
  - calculate the corresponding scattering curve
  - store the results with the corresponding labels (shape, size, atom type)

$$I(Q) = \sum_i \sum_j f_i f_j \frac{\sin(Qr_{ij})}{Qr_{ij}}$$

where

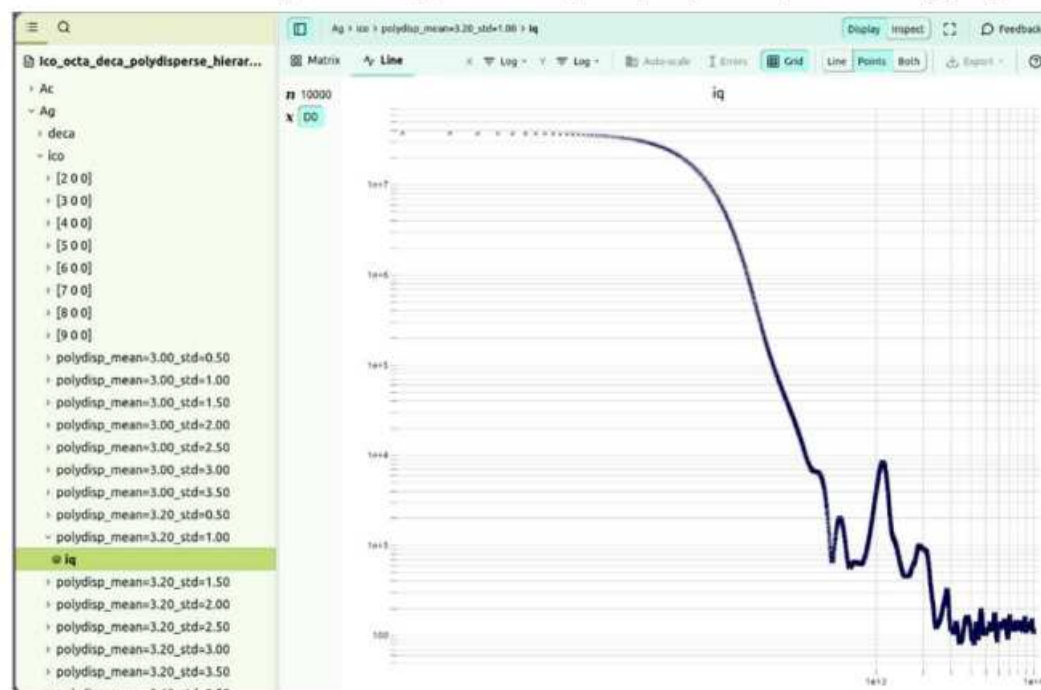
- $Q$  is the scattering vector, called also momentum transfer vector ( $Q = |\mathbf{Q}| = 4\pi \sin \theta / \lambda$ , where  $\theta$  is diffraction half-angle and  $\lambda$  is the wavelength),
- $r_{ij} = |\mathbf{r}_i - \mathbf{r}_j|$  is the distance between atoms  $i$  and  $j$ ,
- and  $f_i$  is the atomic scattering factor of  $i$ -th atom; in general it depends on  $Q$  and we should write it as  $f(Q)$ , but we don't, to keep the notation simple.





# Machine learning assisted SWAXS analysis

- Create dataset
  - build structural models
  - calculate the corresponding scattering curve
  - store the results with the corresponding labels (shape, size, atom type)



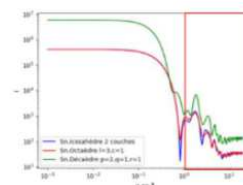
➔ Creation of a large database of scattering data tagged with structural features (labels)



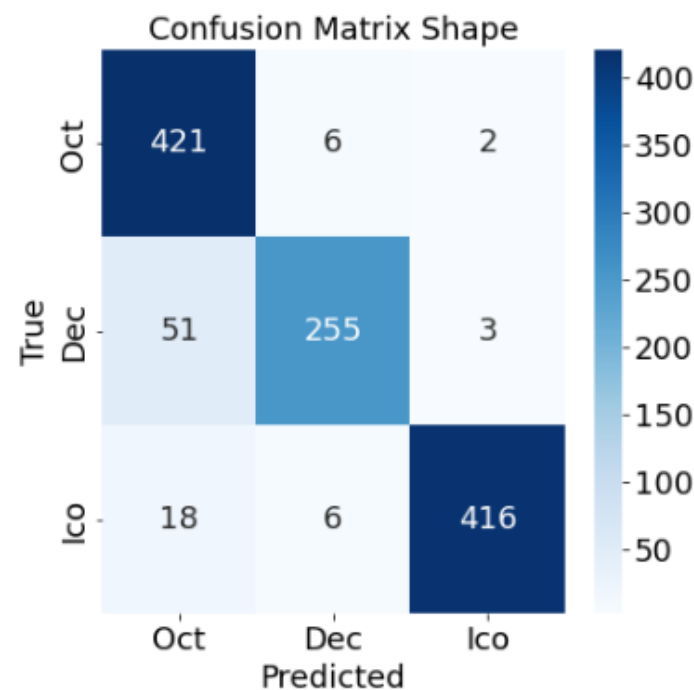
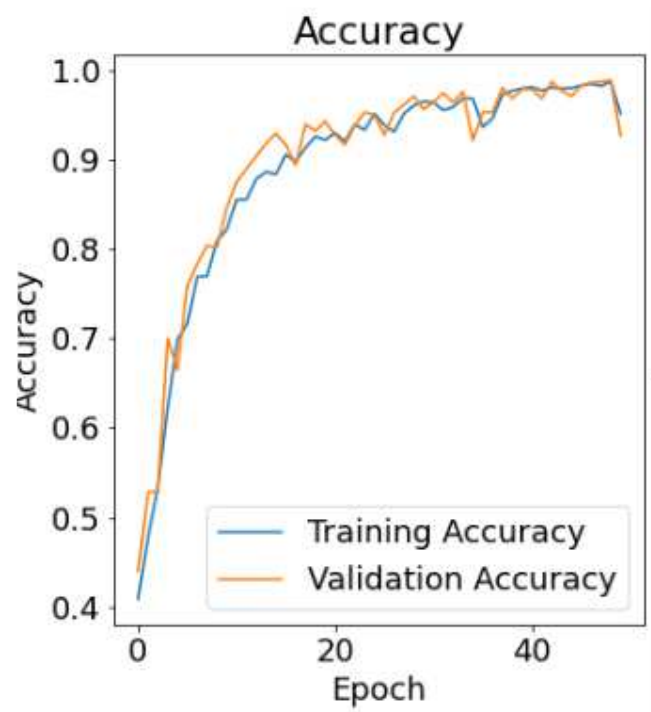
# Machine learning assisted SWAXS analysis

## Shape Prediction

Predictions made in the WAXS domain



**92,6** % accuracy

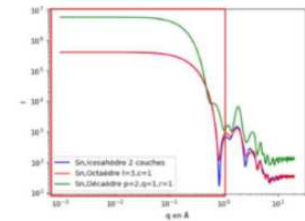
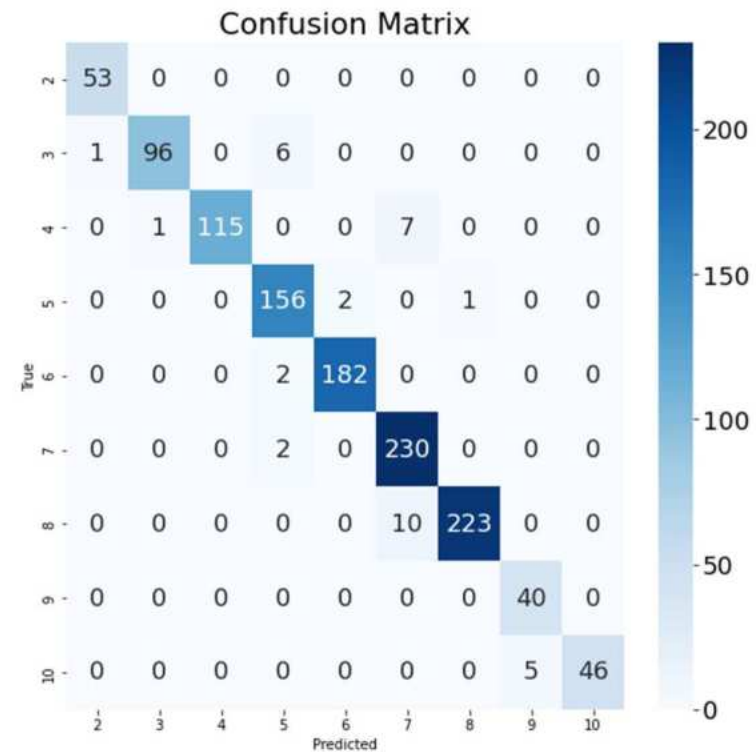
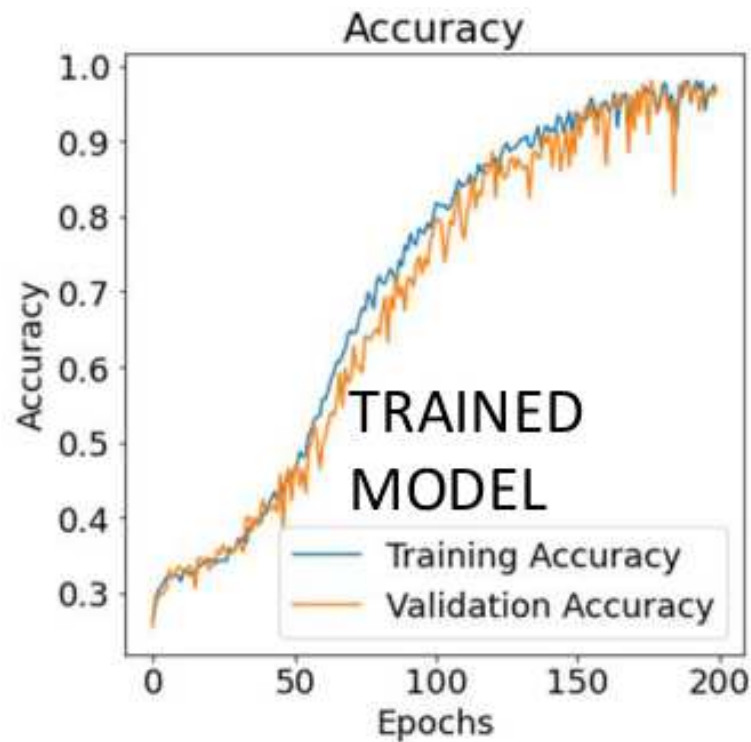


# Machine learning assisted SWAXS analysis

## Size Prediction

- Predictions made in the SAXS domain (Guinier plateau)

**96.8 % accuracy**

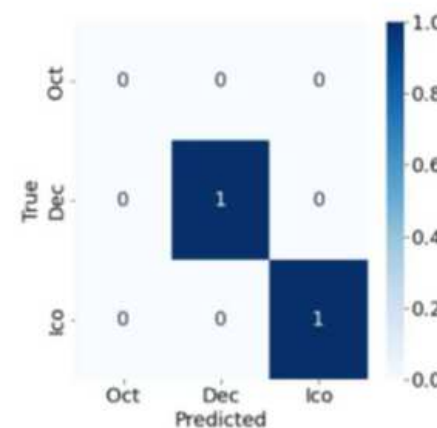
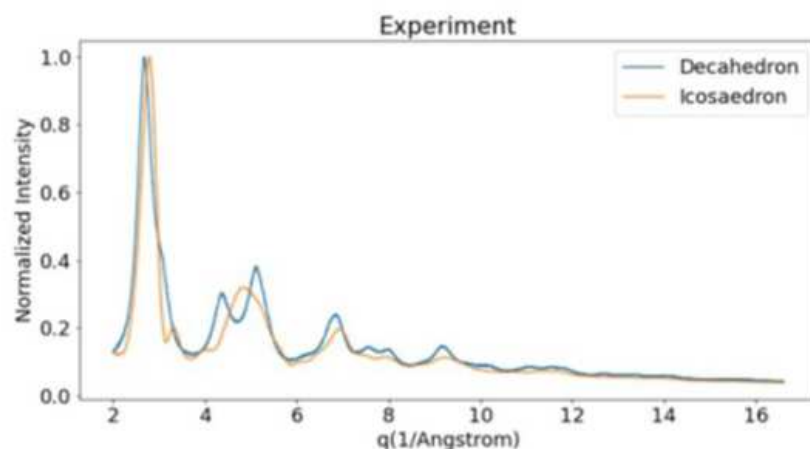


# Machine learning assisted SWAXS analysis

## Shape Prediction

Real systems: Au decahedron - Au icosahedron NPs

$I(q)$  data were corrected from solvent contribution

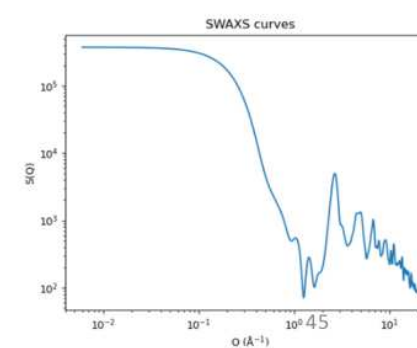
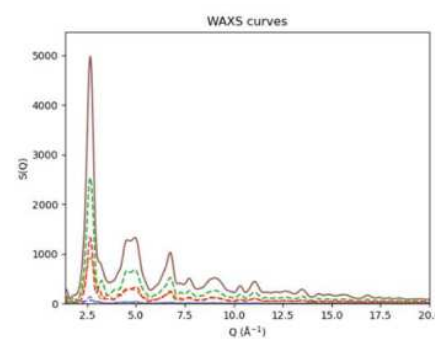
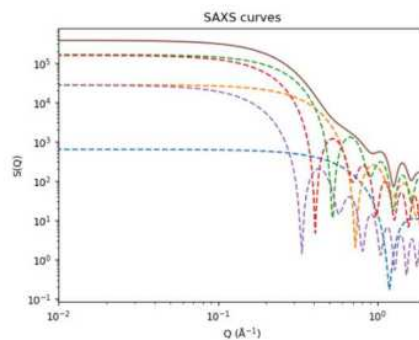
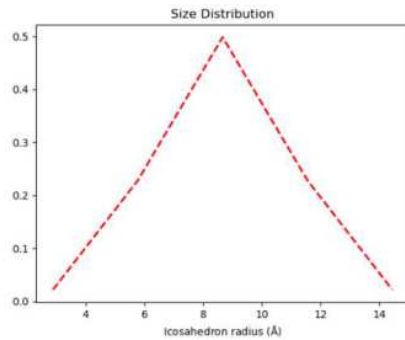
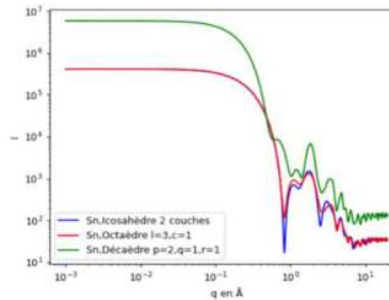


Accuracy 100%  
on ... 2 experimental  
samples 🍊

# Machine learning assisted SWAXS analysis

## Perspectives

- Size and shape predictions from combined SAXS and WAXS domains (rather than separate SAXS for size, WAXS for shape)
- Simultaneous size and shape predictions?
- Introduction of polydispersity in the dataset to mimic real systems (e.g. icosahedral, mean =4 layers, 20% polydisp.)



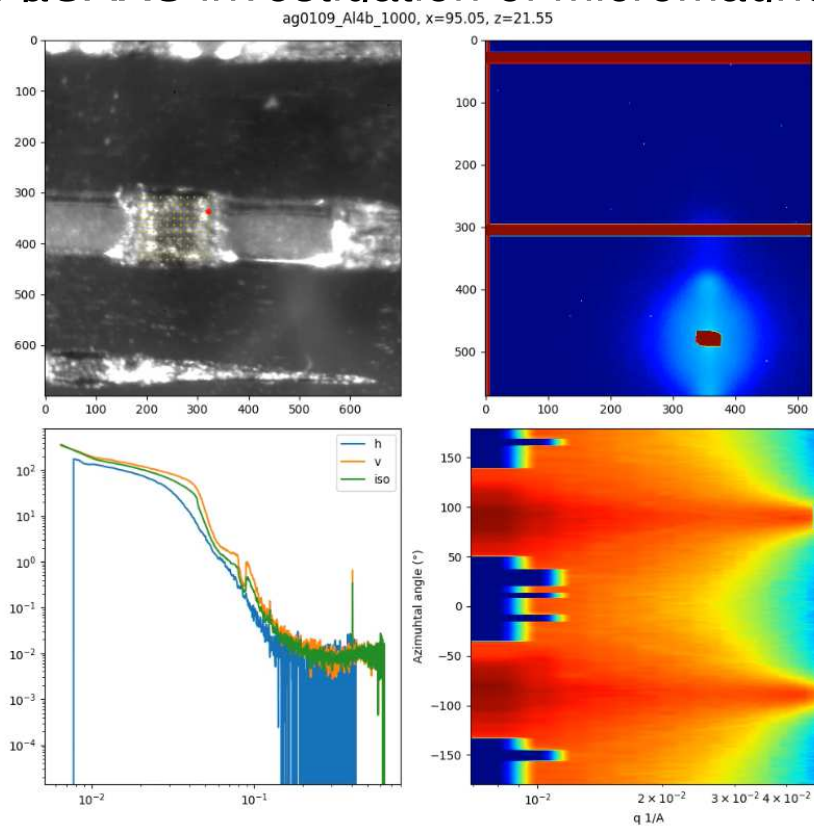
**Thank you for your attention!**



# Applications in SAXS

## 2. Structure factor analysis: Crystalline assemblies – lattice indexing

Example of  $\mu$ SAXS investigation of micromagnets (L.M. Lacroix, G. Viau)

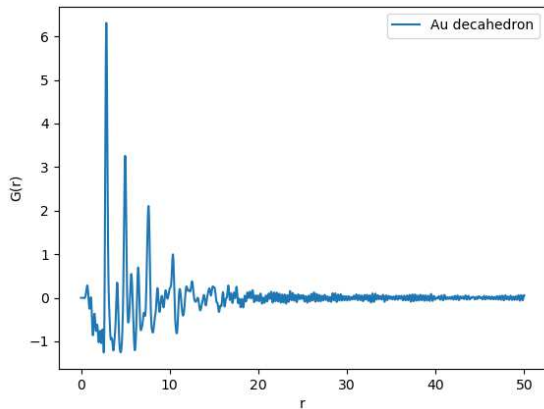


[video](#)

# Applications in WAXS

M. Imperor- LPS Orsay

## ◆ Example 3: Decahedron Au : explore decahedron parameters and find best model



Build models  
using ASE  
Python library



ASE : 3 parameters are used to describe a decahedron :

p: Number of atoms on the (100) facets perpendicular to the five fold axis.

q: Number of atoms on the (100) facets parallel to the five fold axis. q = 1 corresponds

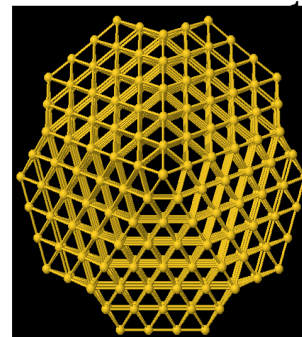
to no visible (100) facets.

r: Depth of the Marks re-entrance at the pentagon corners. r = 0 corresponds to no re-

entrance

The following (p,q,r) were tested :

(3,1,2),(3,1,3),(4,1,0),(4,1,1),(4,1,2),(4,1,3),(5,1,0),(5,1,1),(5,1,2),(5,1,3),(6,1,0),(6,1,1),(6,1,2),(7,1,0),(7,1,1),(7,1,2)

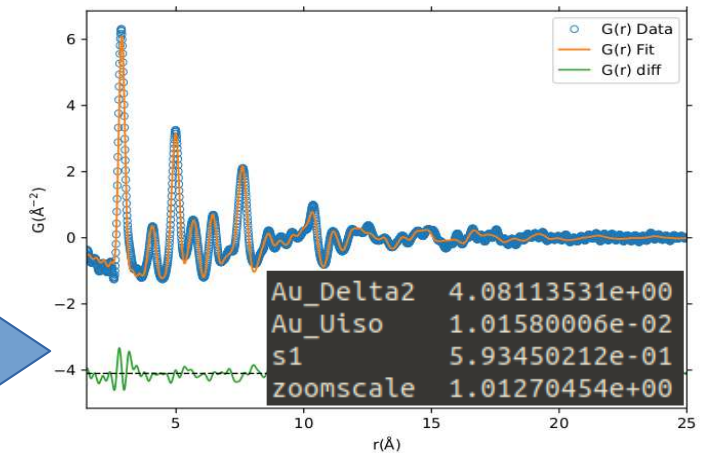
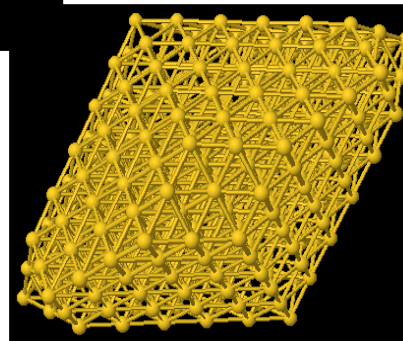


Refine model  
using diffpy-cmi  
python library

(4,1,2)



Adjust the  
parameters  
of the model



Best refinement obtained for (6,1,1)  
decahedron :  $R_w=0,167$

# Applications in WAXS

◆ Example 3: Decahedron Au : optimize structure using ASE

ASE library contains optimizers for atomic structures

BFGS Optimization : ([video](#))





# Applications in WAXS

◆ Example 3: Decahedron Au - optimize structure using ASE

ASE library contains optimizers for atomic structures

BFGS Optimization :



The structure shrinks. Would that improve the PDF refinement ?



Model refinement at each step of the optimization

# Applications in WAXS

## ◆ Example 3: Decahedron Au : optimize structure using ASE

ASE library contains optimizers for atomic structures

## ◆ BFGS Optimization

Improvement of refinement ?

➡ Optimization did not improve the refinement

