

HW17

1)

9. 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16
 $O(1)$ $O(1)$ $O(1)$ $O(1)$ $O(1)$ $O(1)$ $O(1)$ $O(1)$ $O(1)$ $O(1)$ $O(1)$ $O(1)$ $O(1)$ $O(1)$ $O(1)$ $O(1)$

So sequence of n inserts

$$O(n) + O(2n) = O(n)$$

Thus amortized runtime is

$$O(n)/n = O(1)$$

Amortised = Actual

b)

Simple ops

$$O(1)$$

$$O(1)$$

Complex ops (i^{th} index)

$$O(10)$$

$$O(1)$$

i) 1 2 3 bank = $3+3+3-1-1-1 = \$6$

ii) 1 2 3 4 Cost = $0-4 = -4 \Rightarrow$ bank = $6-4 = \$2$

iii) 1 2 3 4 5 6 7 bank = $2+6 = \$8$
 $O(1)$ $O(1)$ $O(1)$

iv) 1 2 3 4 5 6 7 8 Cost = $0-8 = -\$8 \Rightarrow$ bank = $\$8 - \$8 = \$0$
 $O(1)$

v) 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 bank = $\$18$

vi) 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 \Rightarrow bank = $\$0$
 $O(1)$ $O(1)$

Thus we can always keep bank non-negative
 Our Assumptions hold \Rightarrow Amortized time for
 each op