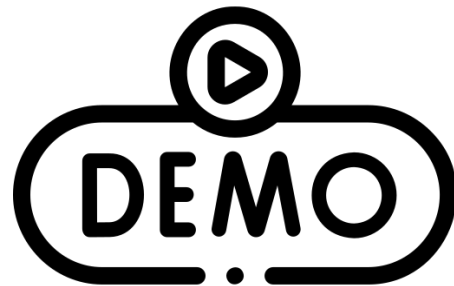
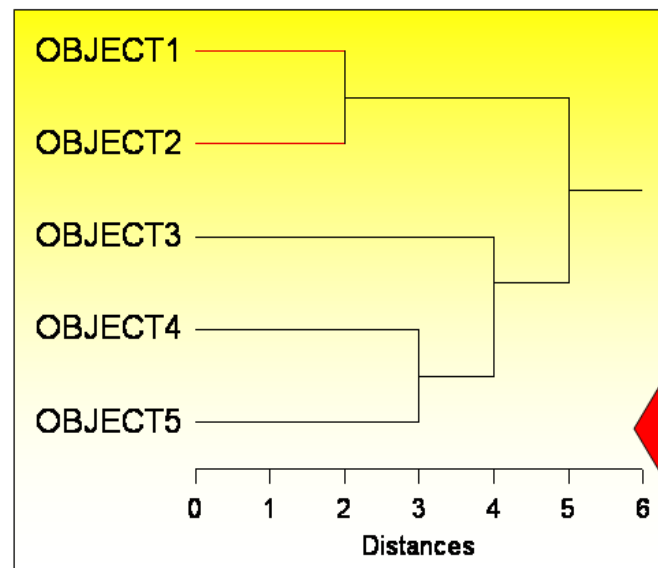


Clustering – hierarchical: An illustration



Simple joining (nearest neighbour)



Object	1	2	3	4	5
1					
2					
3					
4					
5					

Distance matrix

Distance	Cluster
0	1,2,3,4,5
2	(1, 2), 3, 4, 5
3	(1, 2), 3, (4, 5)
4	(1, 2), (3, 4, 5)
5	(1, 2, 3, 4, 5)



Distance matrix

Object	1	2	3	4	5
1					
2	2				
3	6	5			
4	10	9	4		
5	9	8	5	3	

Step 1

group 1 & 2, at the distance of 2

(1,2), 3, 4, 5

(1,2)

3 5
4 9 4
5 8 5 3

$\text{Dist}(2,3) = 5$

$\text{Dist}(1,3) = 6$

$5 < 6$

Step 2 : group 5 & 4 at distance of 3

(1,2), 3, (4,5)

(1,2)

3 5
(4,5) 8 4

$\text{Dist}(1,4) = 10$

$\text{Dist}(1,5) = 9$

$\text{Dist}(2,4) = 9$

$\text{Dist}(2,5) = 8$



Object	1	2	3	4	5
1					
2	2				
3	6	5			
4	10	9	4		
5	9	8	5	3	

Step 3: group 3 & (4, 5), at distance 4
 (1, 2), (3, 4, 5)

(1, 2)

(3, 4, 5) 5 ←

$$\text{Dist}(1, 3) = 6$$

$$\text{Dist}(2, 3) = 5$$

$$\text{Dist}(2, 5) = 8$$

Step 4: group (1, 2) & (3, 4, 5) at distance 5

Done



Object	1	2	3	4	5
--------	---	---	---	---	---

1					
2					
3	6	5			
4	10	9	4		
5	9	8	5	3	

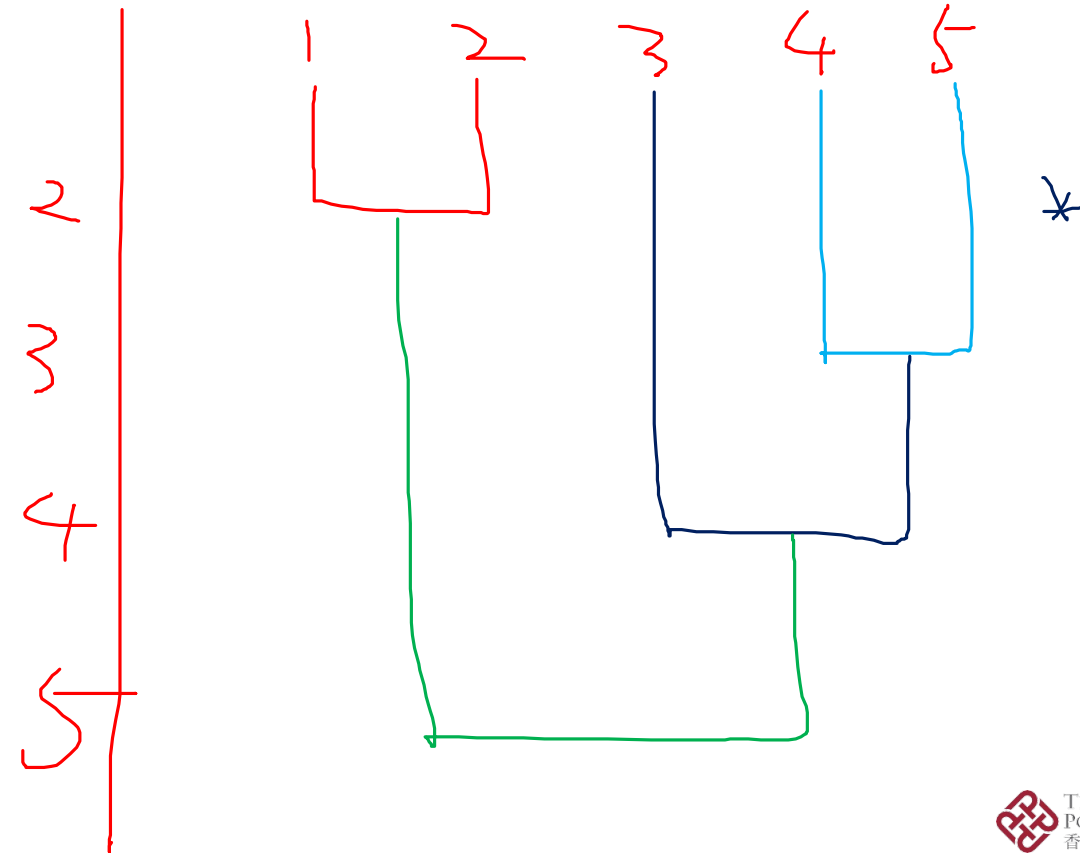
Cluster Outcome

Suppose:

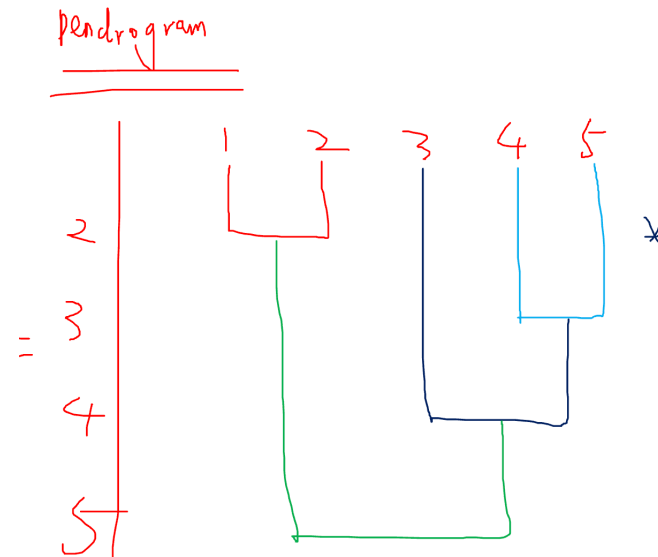
* cutoff = 4.5

⇒ two clusters
 $(1, 2), (3, 4, 5)$

Dendrogram



Object	1	2	3	4	5
1					
2					
3	6	5			
4	10	9	4		
5	9	8	5	3	



Suppose:

* cut off = 3.5

Three clusters: (1, 2), (3), (4, 5)

