

永中鍾定柳

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NO 333 65

三級教[177

ex.1

1) all 滿足 $11x + 13y = 1$ 整數 tuple (x, y)

5	a	11	13	b	1
$5b - 5a$		10	11	a	
$6a - 5b$		1	2	$b - a$	2
			2	$12a - 10b$	
			0	$11b - 13a$	

$$\begin{cases} x = b + 13k \\ y = -5 - 11k \end{cases}, k \in \mathbb{Z}^{\#}$$

2) all x 滿足 $11x \equiv 1 \pmod{13}$

$$\Rightarrow 11x - 1 = 13y$$

$$\Rightarrow 11x - 13y = 1$$

$$\Rightarrow \begin{cases} x = b + 13k \\ y = 5 + 11k \end{cases}, k \in \mathbb{Z}$$

$$\Rightarrow x \equiv 6 \pmod{13}^{\#}$$