

DATE 2024

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NO. 三校教150

三校教作109

永中鍾定棚

ex. 4 若 $4x^2 - 2x - 3 = 0$ 两解为 p, q , $p > q$, 求 $p^2 - q^2$

$$\Rightarrow x = \frac{2 \pm \sqrt{4 + 48}}{8} = \frac{1}{4} \pm \frac{1}{4}\sqrt{13}$$

$$\Rightarrow p = \frac{1+\sqrt{13}}{4}, q = \frac{1-\sqrt{13}}{4}$$

$$\Rightarrow p^2 - q^2 = \left(\frac{1}{4}\right)^2 + 2 \cdot \frac{1}{4} \cdot \frac{1}{4} \sqrt{13} + \left(\frac{1}{4} \sqrt{13}\right)^2 + \left(\frac{1}{4}\right)^2 - 2 \cdot \frac{1}{4} \cdot \frac{1}{4} \sqrt{13} + \left(\frac{1}{4} \sqrt{13}\right)^2$$

$$= \frac{1 + 13 + 1 + 13}{16} = \frac{28}{16} = \frac{7}{4}$$