Leeune Z.

$$X_0, X_1, X_2, \dots$$

$$X_0 \sim \mathcal{V} \qquad X_{in} | X_i \sim \mathcal{P}(X_i, \cdot)$$

$$\mathbb{P}(X_0 = i_0, X_1 = i_1, X_2 = i_2) = \mathcal{V}_{i_0} \mathcal{P}_{i_0 i_1} \mathcal{P}_{i_1 i_2}$$

$$\mathbb{P}(X_0 = i_0, X_2 = i_2) = \mathcal{V}_{i_0} \mathcal{Z}_{i_0 i_0} \mathcal{P}_{i_0 i_1} \mathcal{P}_{i_1 i_2}$$

$$\mathcal{V} = \begin{bmatrix} v_0, v_1, & --- & v_2 \end{bmatrix}$$

$$v^{(2)} := \mathbb{P}(X_2 = 1) \qquad v^{(2)} = v \cdot \mathbb{P}^2.$$

$$v^{(2)} := v \cdot \mathbb{P}^3 \qquad v^{(2)} = v \cdot \mathbb{P}^m.$$

Def. 
$$P_{ij}^{(n)} = \mathbb{P}\left(X_n = j \mid X_0 = i'\right)$$
  $\forall i,j \in S$   
 $\left(X_0, X_n, X_{2n}, \dots, X_{mn}, \dots\right)$ 

Recumue and transiène.

Def. M(i) := total number of three for MC to visit i  $= \underbrace{\sum_{t=1}^{60} 1!}_{t=1} X_t = i i$   $f_{ij} := P(N_i j) > |X_0 = i| = P_i(M_i j) > 1$  (Visit j at least once from i)  $f_{ii} : \text{ prob of resumsy to } i \text{ cofter leaving } i.$ 

Paux Pr(Mi) 7k) = (fi)k

$$P(Mi) \ge k = P(Mi) \ge k \mid Mi \ge k + Mi) \ge k + Mi$$

$$P(Mi) \ge k + Mi) \ge k + Mi$$

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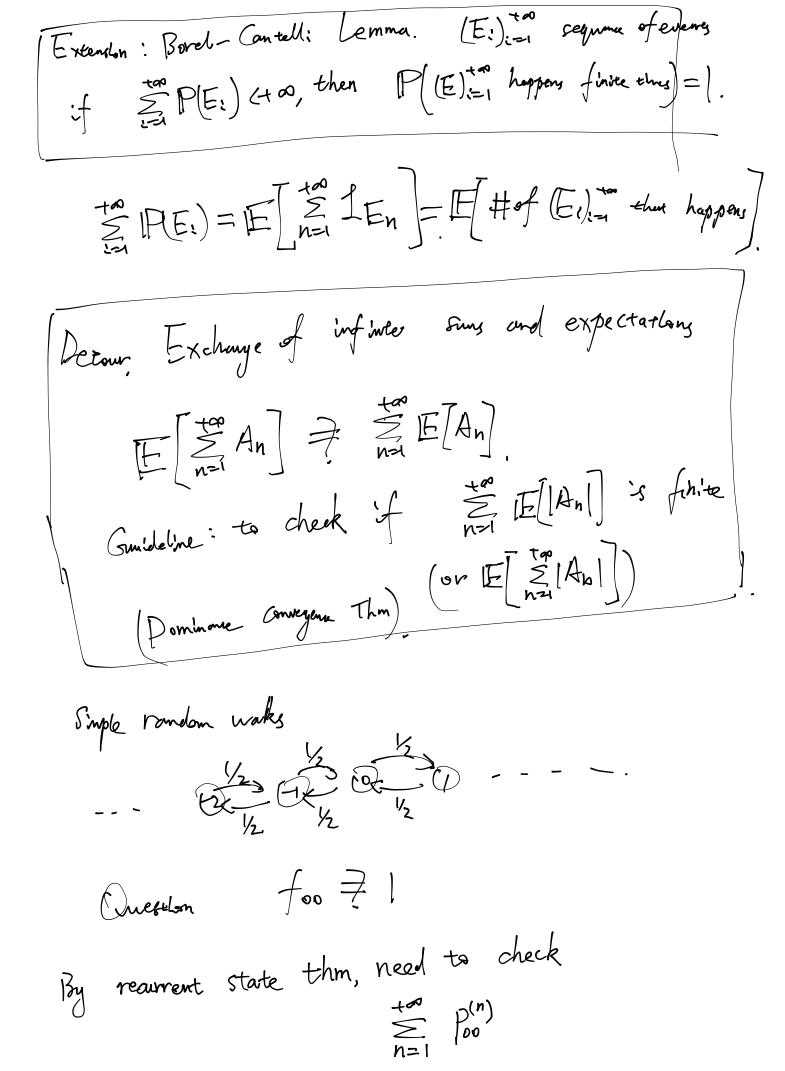
$$P(Mi) \ge k + Mi) \ge k + Mi$$

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$$P(Mi) \ge k + Mi$$

Proof. 
$$P(Ni) \ge k = P(Ti) + \infty$$
  $P(Ni) \ge k = P(Ni) \ge k$ 

Core May:  $E[Nii] = \sum_{k=1}^{10} P(Ni) \ge k = \int_{-1}^{11} \frac{f_{ij}}{f_{ij}} = \int_{-1}^{10} \frac{f_{ij}}{f$ 



For odd  $n: \frac{2^n}{60} = 0$ For even  $n: \begin{cases} n \\ \infty \end{cases} = 2^{-n} \cdot \begin{pmatrix} n \\ \frac{n}{2} \end{pmatrix}$  $=2^{-\eta}\cdot\frac{n!}{(n!)!(n!)!}$ Stirting's approximation Jan. (e) < n! ¿e!an(e)  $\frac{p(n)}{90} > 2^{n} \cdot \frac{\sqrt{2\pi n \cdot (e)^{n}}}{e^{2} \cdot \sqrt{\pi n \cdot (2e)^{n}}} \cdot \sqrt{\pi n \cdot (2e)^{n}}$  $\frac{\sqrt{2}}{\sqrt{2}}$   $\frac{1}{\sqrt{2}}$ Similarly.  $P_{00}^{(n)} \leq \frac{e \cdot \sqrt{2}}{\sqrt{1}} \cdot \frac{1}{\sqrt{n}}$ My wound segment . 2n parks 1/2 Sounumde

Company fig 5. 2/3

2/5 > 4

2/3  $\frac{3}{5} > 4$ 2/3  $\frac{3}{5} > 4$   $\frac{3}{5} >$ 

$$f_{12}=f_{13}=f_{14}=f_{32}=f_{31}=f_{42}=f_{41}=0$$

$$f_{34}=f_{43}=|:$$
Ifor about  $f_{21}$ ?

$$f - explanslom. \qquad f_{ij} = P_{ij} + \sum_{k \in S} P_{ik} f_{kj}.$$

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$$f_{21} = \beta_{21} + \beta_{22} \cdot f_{21} + \beta_{23} \cdot f_{31}$$

$$\int_{1/4}^{1/4} f_{31} = 0$$

$$1/4$$

$$f_{21} = \frac{1}{4} + \frac{1}{4} + \frac{1}{21} + \frac{1}{21} = \frac{1}{3}$$