Differential Equations Student Notebook

Julian Alexander Alvarez

February 2, 2020

Contents

1	Pre	face	3
2	The	Very Beginning	4
	2.1	Requirements	4
	2.2	Types of Differential Equations	4
	2.3	Classification By Order	5
		2.3.1 Type	5
		2.3.2 Order	5
		2.3.3 Linearity	6

Chapter 1

Preface

Welcome to my Differential Equations Student Notebook. I created this "borderline text-book" notebook as a way for me and others to study and/or learn Differential Equations from. You may be asking: "What qualifications do you have to be making this Differential Equations Notebook?" and my response to that is that I am not. I AM NOT QUALIFIED. I am just a student who thought that making a textbook would assist me in learning about DEs. However, I have taken Calculus I, II, III, Discrete Mathematics, Linear Algerbra, and any other foundation-building mathematical class that University of Houston - Clear Lake provides (if that makes you trust me more).

It would be greatly appreciated if you simply took this as a study resource for any current, soon-to-be-current, already-took-this-and-just-forgot student. Therefore, without further ado, lets begin our dive into DIFFERENTIAL EQUATIONS.

Chapter 2

The Very Beginning

2.1 Requirements

As it is in every area of mathematics, there is a certain level of knowledge that is to be expected to be known by students. Requirements for *Differential Equations* is prior experience in Calculus I and II.

Of course, it is **expected that you are a BORDERLINE SAVANT in Calculus**. If you are not absolutely comfortable with Calculus, I reccommend that you REALLY go over it.

2.2 Types of Differential Equations

There are two types of Differential Equations: Ordinary Differential Equations (ODEs) and Partial Differential Equations (PDEs). The two differences between a **ODE** and a **PDE** is that an ODE is (as the name suggests) an equation that contains ordinary differentials. An example of an ODE is as follows:

$$\frac{dy}{dx} = 4y - 2x\tag{2.1}$$

An example of a PDE is as follows:

$$\frac{\partial y}{\partial x} = 17x^2 - 3y * \sin y \tag{2.2}$$

Did you spot the difference? The differentiating factor between example 2.1 and 2.2 is $\frac{dy}{dx}$ and $\frac{\partial y}{\partial x}$. One contains partials while the other does not.

Definition 2.2.1: Differential Equation

An equation that contains the derivatives of one or more unknown functions or variables (f(x), y, etc.), with respect to one or more independent variables is a **DIFFERENTIAL EQUATION**.

2.3 Classification By Order

The ordering of a differential equation is set by these three tenets:

- Type
- Order
- Linearity

2.3.1 Type

The type of DQ is nothing more that it being an ODE or a PDE (as was explained above). Of course there are differences in notation, such as the **Leibniz notation**, **prime notation**, and **dot notation**, with their respective notations being written as such: $\frac{dy}{dx}$, y', and \dot{y}

2.3.2 Order

The **order of a differential equation** is simply the the order of the highest derivative in an equation. An example of a 2nd order differential equation is:

$$\frac{d^2y}{dx^2} + 21(\frac{dy}{dx}) + 2y = 0 (2.3)$$

In equation (2.3) we can tell that it is a 2nd order equation due to the fact that the number 2 appears in $\frac{d^2y}{dx^2}$. As such, it can be said that this equation is a 2nd order equation. Additionally, it can be said that equation (2.3) can be written in the **differential form** (possibly).

Definition 2.3.1: Differential Form

The **differential form** of an equation is an equation that is written as M(x,y)dx + N(x,y)dy = 0. In other words, differential form is when the fraction is turned into not being a fraction.

In addition to there being a differential form of a differential equation, there also exists the **normal form** of a differential equation.

Definition 2.3.2: Normal Form

The **normal form** of a differential equation is an equation that contains the highest-order differential on one side of the equation, such as

$$\frac{d^2y}{dx^2} = f(x, y, y') \tag{2.4}$$

Of course, it is expected that you can aleady manipulate any given equation to normal or differential form. If you are not able to do so, I am sorry.

2.3.3 Linearity

An