



# Data Structure and Analysis

## Offline Session 1

Il-Chul Moon

Department of Industrial and Systems Engineering

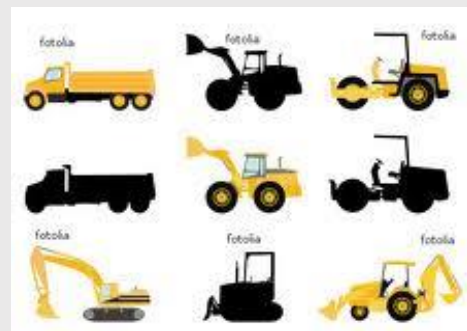
KAIST

icmoon@kaist.ac.kr

- 1300-1415 : Summary lecture on
  - Python basics
  - Object oriented paradigm
  - Linked List, Stack and Queue
  - Recursions and Dynamic Programming
- 1430-1545 : Exercise on AI Blackjack programming

# SUMMARY LECTURE

- [illegible]



## List is another type of sequence variables

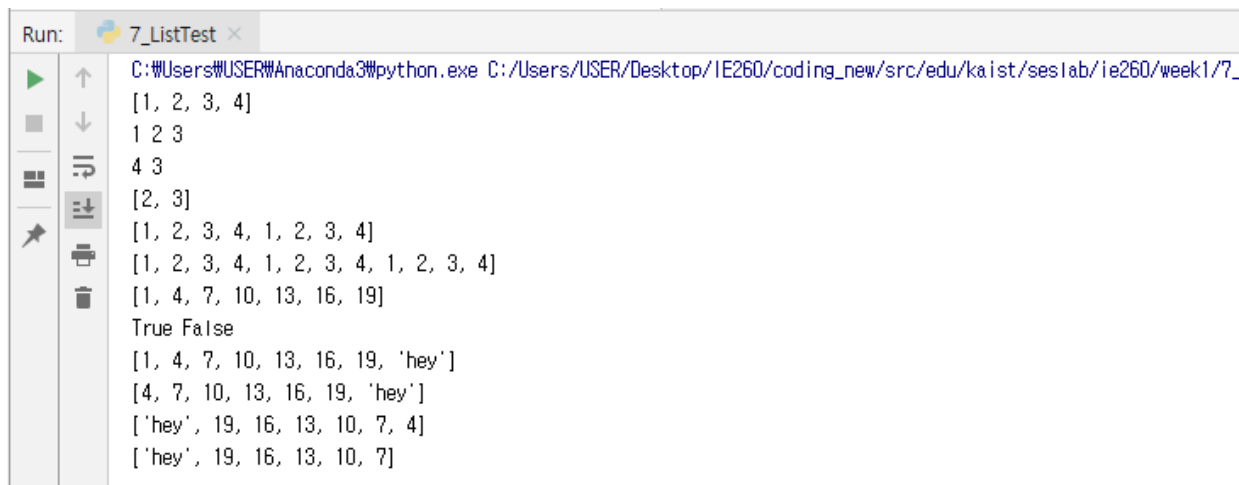
```
lstTest = [1, 2, 3, 4]
print(lstTest)
print(lstTest[0], lstTest[1], lstTest[2])
print(lstTest[-1], lstTest[-2])
print(lstTest[1:3])
print(lstTest+lstTest)
print(lstTest*3)
```

See how the operators work

$\text{range}(x,y,z) == x:y:z$   
You will use this function many, many times

```
lstTest = list(range(1, 20, 3))
print(lstTest)
print(4 in lstTest, 100 in lstTest)
lstTest.append('hey')
print(lstTest)
del lstTest[0]
print(lstTest)
lstTest.reverse()
print(lstTest)
lstTest.remove(4)
print(lstTest)
```

in and not in comes pretty handy



```
Run: 7_ListTest x
C:\Users\USER\Anaconda3\python.exe C:/Users/USER/Desktop/IE260/coding_new/src/edu/kaist/seslab/ie260/week1/7_
[1, 2, 3, 4]
1 2 3
4 3
[2, 3]
[1, 2, 3, 4, 1, 2, 3, 4]
[1, 2, 3, 4, 1, 2, 3, 4, 1, 2, 3, 4]
[1, 4, 7, 10, 13, 16, 19]
True False
[1, 4, 7, 10, 13, 16, 19, 'hey']
[4, 7, 10, 13, 16, 19, 'hey']
['hey', 19, 16, 13, 10, 7, 4]
['hey', 19, 16, 13, 10, 7]
```

- Dictionary is also a collection variable type
  - However, it is not sequential
  - It works by a pair of keys and values
    - A set of (key 1, value 1), (key 2, value 2), (key 3, value 3)...
    - Exact syntax is { key1:value1, key2:value2, key3:value3 ... }

```
dicTest = {1: 'one', 2: 'two', 3: 'three'}  
print(dicTest[1])  
dicTest[4] = 'four'  
print(dicTest)  
dicTest[1] = 'hana'  
print(dicTest)  
print(dicTest.keys())  
print(dicTest.values())  
print(dicTest.items())
```

Run: 9\_DictionaryTest x

```
C:\Users\USER\Anaconda3\python.exe C:/Users/USER/Desktop/IE260/coding_n  
one  
{1: 'one', 2: 'two', 3: 'three', 4: 'four'}  
{1: 'hana', 2: 'two', 3: 'three', 4: 'four'}  
dict_keys([1, 2, 3, 4])  
dict_values(['hana', 'two', 'three', 'four'])  
dict_items([(1, 'hana'), (2, 'two'), (3, 'three'), (4, 'four')])
```

# Assignment and Equivalence

```
x = [1, 2, 3]
y = [100, x, 120]
z = [x, 'a', 'b']
```

```
print('x : ', x)
print('y : ', y)
print('z : ', z)
```

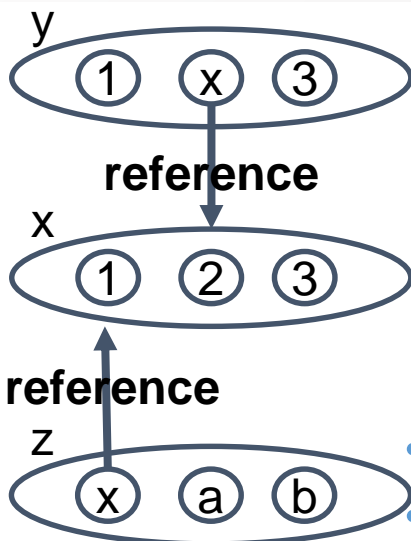
```
x[1] = 1717
```

```
print('x : ', x)
print('y : ', y)
print('z : ', z)
```

```
x[1] = 2
x2 = [1, 2, 3]
if x == x2:
    print("Values are equivalent")
else:
    print("Values are not equivalent")
```

```
if x is x2:
    print("Values are stored at the same place")
else:
    print("Values are not stored at the same place")
```

```
if x[1] is y[1][1]:
    print("Values are stored at the same place")
else:
    print("Values are not stored at the same place")
```



```
Run: 15_AssignmentAndEquivalence x
C:\Users\USER\Anaconda3\python.exe C:/Users/USER/Desktop/IE260/coding_new/src/edu/kaist/seslab
x : [1, 2, 3]
y : [100, [1, 2, 3], 120]
z : [[1, 2, 3], 'a', 'b']

x : [1, 1717, 3]
y : [100, [1, 1717, 3], 120]
z : [[1, 1717, 3], 'a', 'b']
Values are equivalent
Values are not stored at the same place
Values are stored at the same place
```

- One variable's value is changed
- But, you see three changes
- Why this happened?
  - Because of references
  - x has two references from y and z
  - The values of y and z are determined by x, and x is changed
    - See the ripple effects
- **==**
  - Checks the equivalence of two referenced values
- **is**
  - Checks the equivalence of two referenced objects' IDs

# References, Symbol Table, and Object Table

```
import sys

x = [1, 2, 3]
y = [100, x, 120]
z = [x, 'a', 'b']

print(sys.getrefcount(x))
print(sys.getrefcount(y))

print(id(x))
print(id(y[1]))
print(id(y))

print(x is y[1])
print(x is y)
```

Run: 16\_UnderstandingReference x

C:\Users\USER\Anaconda3\python

4

2

2519459127816

2519459127816

2519459127880

True

False

**ID(variable)** returns the referenced object ID

**ID(variable1)==ID(variable2)**  
→ variable1 is variable2

**sys.getrefcount(variable)** returns the number of references of an object ID + 1

Symbol Table

Var.	x	y	z
------	---	---	---

Object Table

ID	3887 2808	...	...	...	...	...	...	...	3887 3048	...
Value	List object name d x	1	2	3	100	120	'a'	'b'	List object name d y	List object name d z





# Class and Instance



instantiation



```
class MyHome:
    colorRoof = 'red'
    stateDoor = 'closed'
    def paintRoof(self,color):
        self.colorRoof = color
    def openDoor(self):
        self.stateDoor = 'open'
    def closeDoor(self):
        self.stateDoor = 'close'
    def printStatus(self):
        print ("Roof color is", self.colorRoof, ", and door is", self.stateDoor)
```

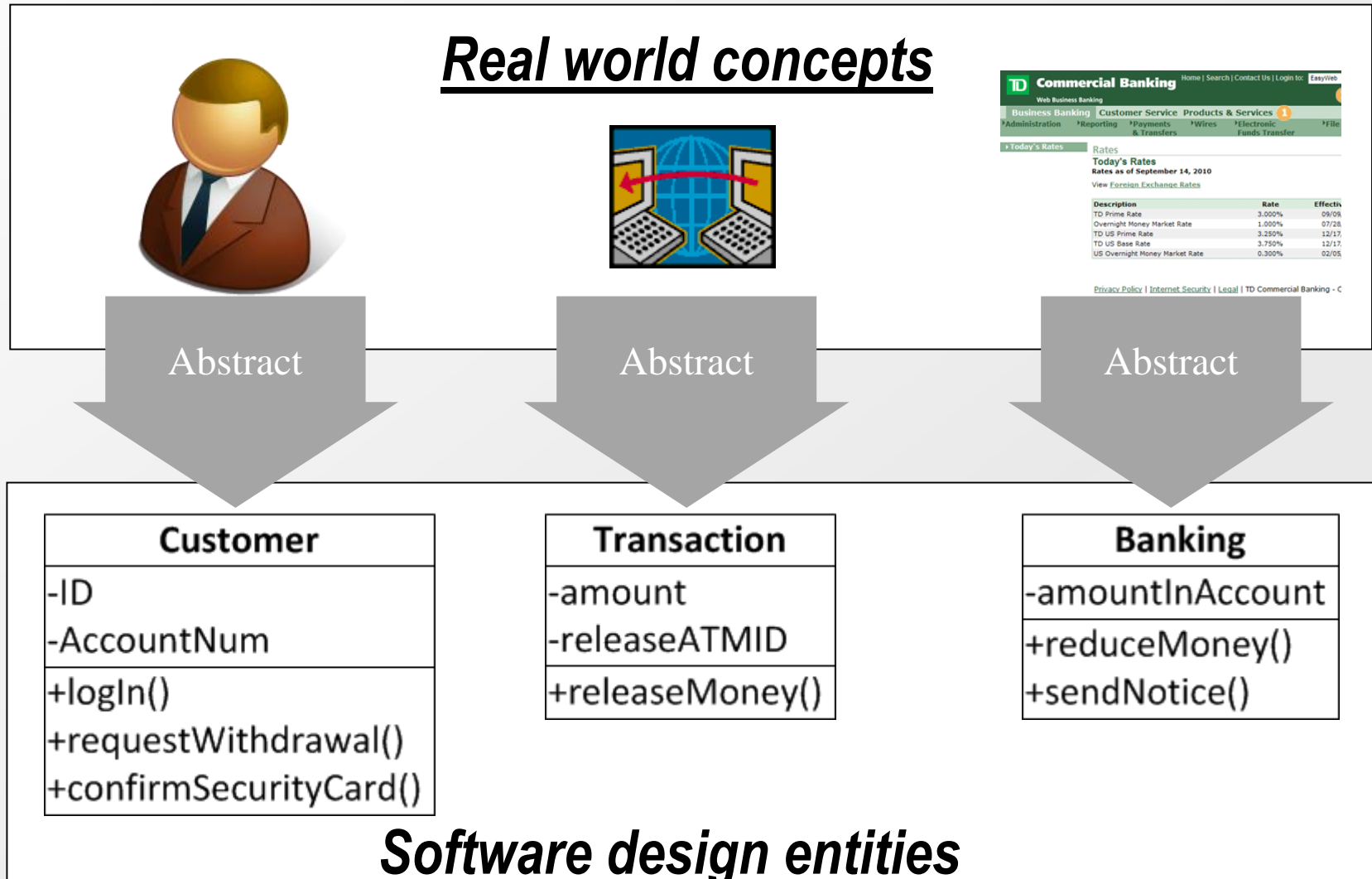
See how to define a class  
→ **class** classname:

```
homeAtDaejeon = MyHome()
homeAtSeoul = MyHome()
homeAtSeoul.openDoor()
homeAtDaejeon.paintRoof('blue')
homeAtDaejeon.printStatus()
homeAtSeoul.printStatus()
```

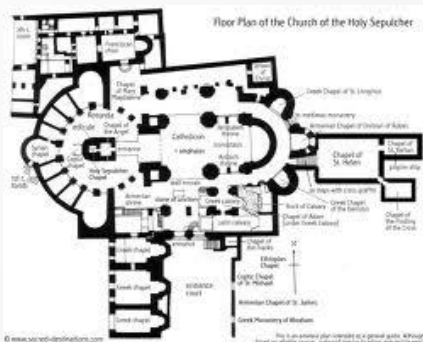
See how to instantiate a class  
→ **var = classname(param)**

Run: 17\_ClassInstanceAndObject x

```
C:\Users\USER\Anaconda3\python.exe C:/User
Roof color is blue , and door is closed
Roof color is red , and door is open
```



# What are Class and Instance?



- Class vs. Instance
- Class
  - Result of design and implementation
  - Conceptualization
  - Corresponds to design abstractions
- Instance
  - Result of execution
  - Realization
  - Corresponds to real world entities



Customer
-ID
-AccountNum
+login()
+requestWithdrawal()
+confirmSecurityCard()



**ID: John**  
**Acct #: 123**



**ID: Park**  
**Acct #: 456**



**ID: Kim**  
**Acct #: 789**



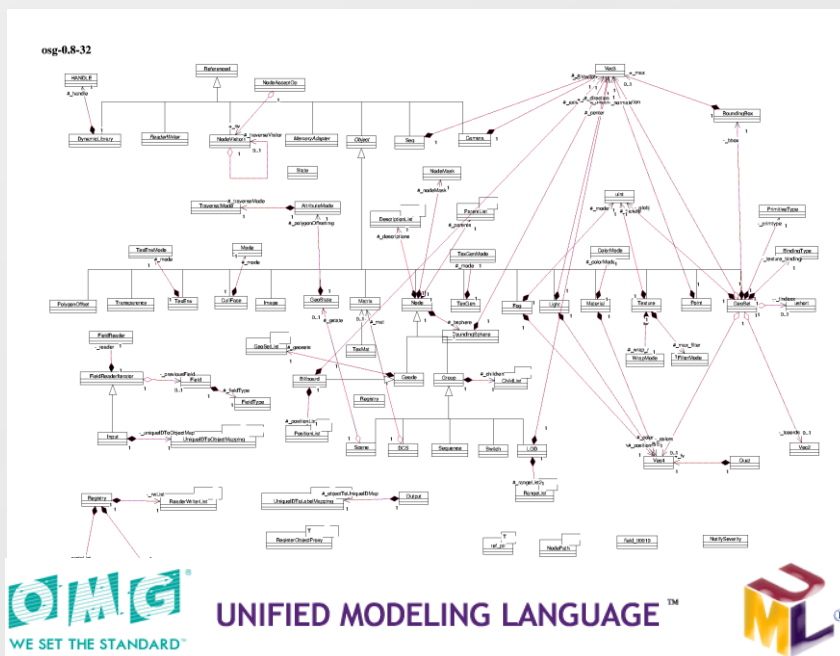
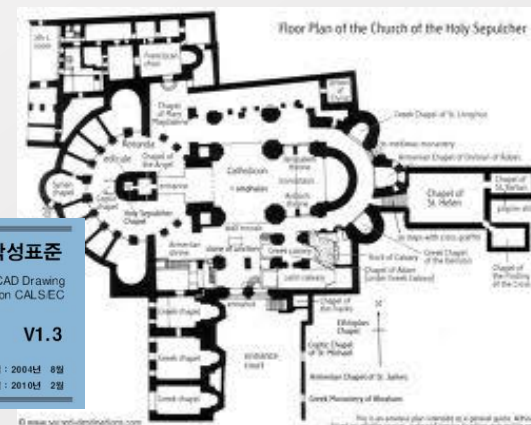
**ID: Koh**  
**Acct #: 035**

- # 건설CALS/EC 전자도면 작성표준

Korea Standard of the CAD Drawing  
in Construction CALS/EC

## V1.3

제정일 : 2004년 8월  
개정일 : 2010년 2월



# UML Notation : Class and Instance

Abstract class

*Person*

Class

Customer

Named instance

Park::Customer

Unnamed instance

:Customer

Instance Name

Class Name

Park::Customer

-ID : String

#AccountNum : Integer

+Name : String = Hey

+login() : void

+requestWithdrawal() : Boolean

+confirmSecurityCard() : Boolean

Member variables

+-#(name):(type)=(default value)

Visibility options

+ → public

# → protected

- → private

Methods

+-#(name)(arguments):(type)



# Encapsulation

- Object = Data + Behavior
  - Data : field, member variable, attribute
  - Behavior : method, member function, operation
- Delegating the implementation responsibility!
  - Bring me a sausage, and I don't care how you made it
- Utilizing the visibility
  - private: seen only within the class
  - protected: seen only within the class and its descendants
  - public: seen everywhere
- Python does not support the visibility options!



## Building Architecture I care overall composition



Room
-location
-size
+openDoor()
+openWindow()



## Interior Designer I care inside implementation



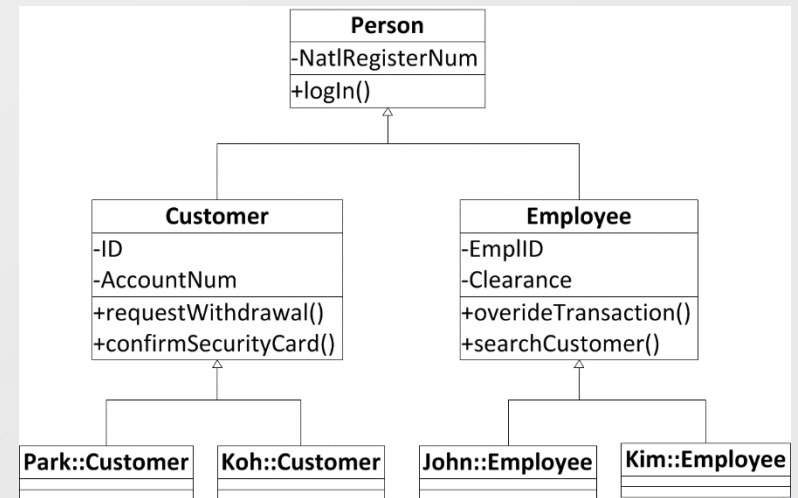
Class Definition

Interface as a specification



# Inheritance

- Inheritance
  - Giving my attributes to my descendants
    - My attributes include
      - Member variables
      - Methods
    - My descendants may have new attributes of their own
    - My descendants may mask the received attributes
    - But, if not specified, sons follow their father
- Superclass
  - My ancestors, specifically my father
  - Generalized from the conceptual view
- Subclass
  - My descendants, specifically my son
  - Specialized from the conceptual view
- How about having a mother?
  - Yes. It is possible in Python



Generalized

Specialized

# Inheritance in Python

```
class Father(object):  
    strHometown = "Jeju"  
    def __init__(self):  
        print("Father is created")  
    def doFatherThing(self):  
        print("Father's action")  
    def doRunning(self):  
        print("Slow")
```

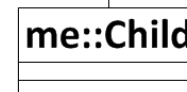
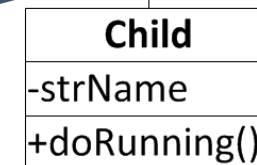
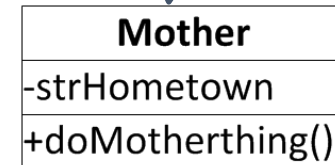
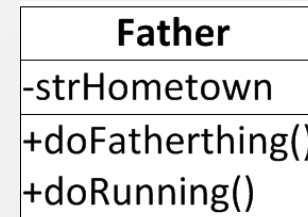
```
class Mother(object):  
    strHometown = "Seoul"  
    def __init__(self, paramHome):  
        self.strHometown = paramHome  
        print("Mother is created")  
    def doMotherThing(self):  
        print("Mother's action")
```

```
class Child(Father, Mother):  
    strName = "Moon"  
    def __init__(self):  
        super(Child, self).__init__()  
        print("Child is created")  
    def doRunning(self):  
        print("Fast")
```

```
me = Child()  
me.doFatherThing()  
me.doMotherThing()  
me.doRunning()  
print(me.strHometown)  
print(me.strName)
```

Run: Inheritance x

```
C:\Users\USER\Anaconda3\python.exe C:/Users/USER/Desktop/  
Father is created  
Child is created  
Father's action  
Mother's action  
Fast  
Jeju  
Moon
```



Multiple Inheritance

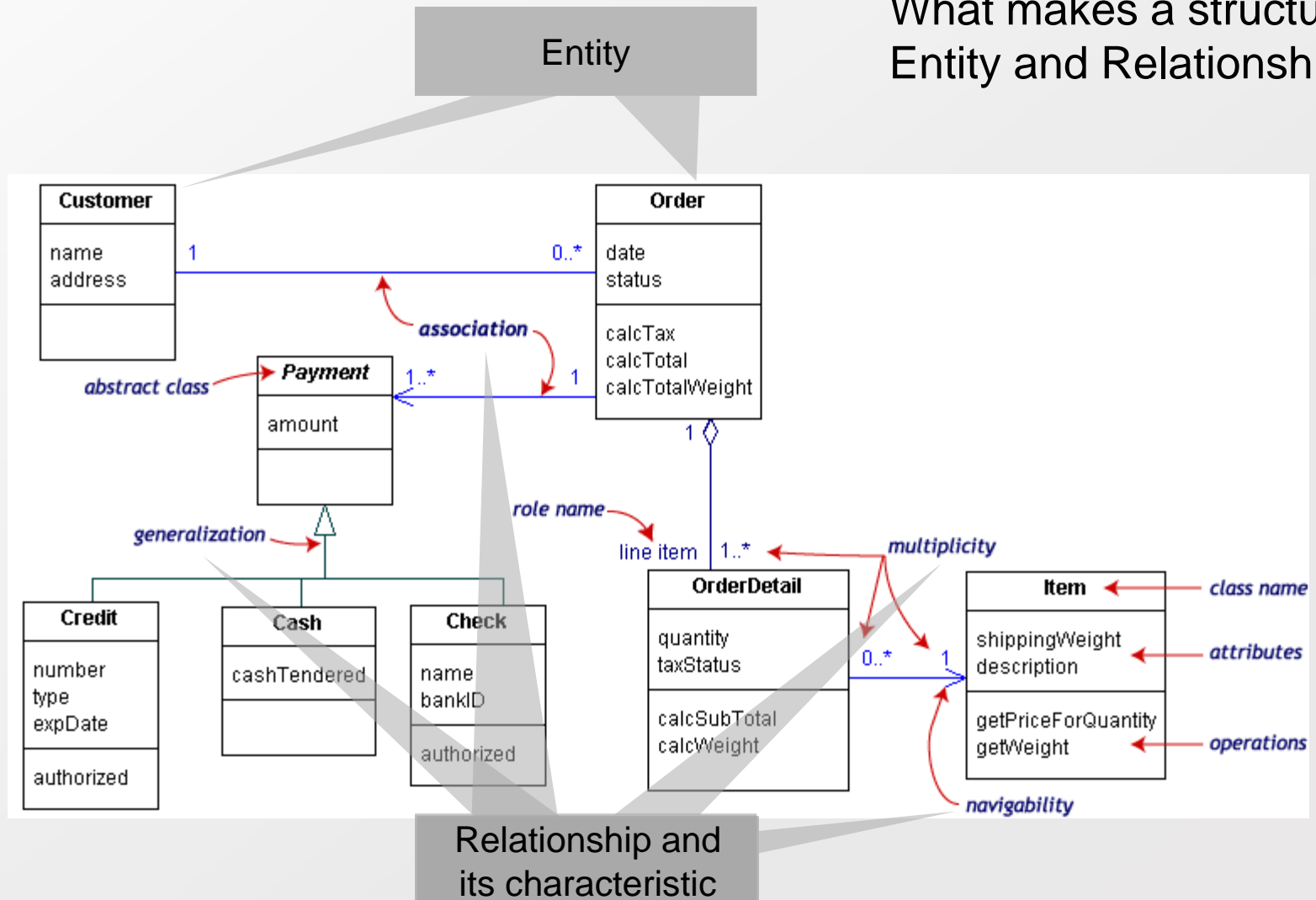
Base Class  
(Super Class)

1. See Child has Father's and Mother's attributes
2. See Child overwrite Father's method by his own



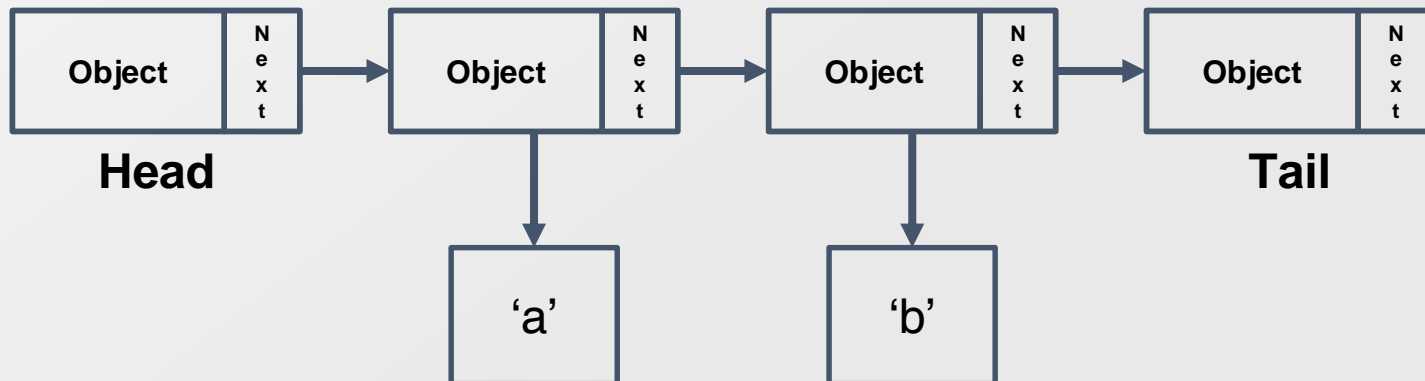
# Structure of Classes in Class Diagram

What makes a structure?  
Entity and Relationship



# Basic Structure: Singly Linked List

- Construct a singly linked list with nodes and references
  - A node consists of
    - A variable to hold a reference to its next node
    - A variable to hold a reference to its value object
  - Special nodes: Head and Tail
    - You can construct the singly linked list without them
    - But, using them makes search, insert and delete more convenient
  - Generally, requires more coding than array



- Member variables
  - Variable to reference the next node
  - Variable to hold a value object
  - (Optional) Variable to check whether it is a head or not
  - (Optional) Variable to check whether it is a tail or not
- Member functions
  - Various set/get methods

```
class Node:
    nodeNext = None
    nodePrev = ''
    objValue = ''
    binHead = False
    binTail = False

    def __init__(self, objValue = '', nodeNext = None, binHead = False, binTail = False):
        self.nodeNext = nodeNext
        self.objValue = objValue
        self.binHead = binHead
        self.binTail = binTail

    def getValue(self):
        return self.objValue

    def setValue(self, objValue):
        self.objValue = objValue

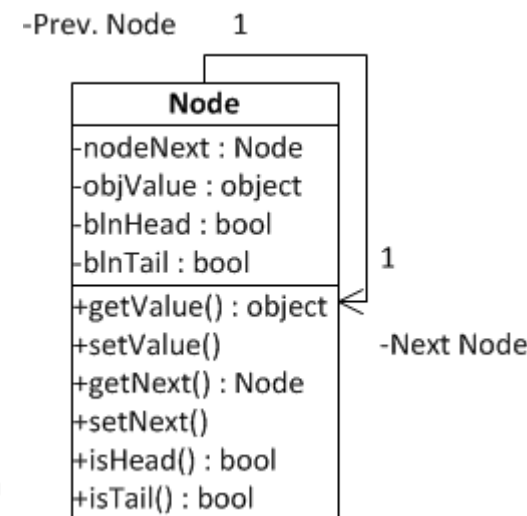
    def getNext(self):
        return self.nodeNext

    def setNext(self, nodeNext):
        self.nodeNext = nodeNext

    def isHead(self):
        return self.binHead

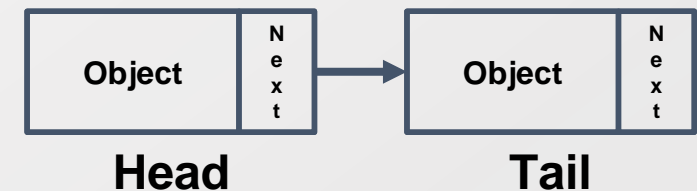
    def isTail(self):
        return self.binTail

node1 = Node(objValue = 'a')
nodeTail = Node(binTail = True)
nodeHead = Node(binHead = True, nodeNext = node1)
```

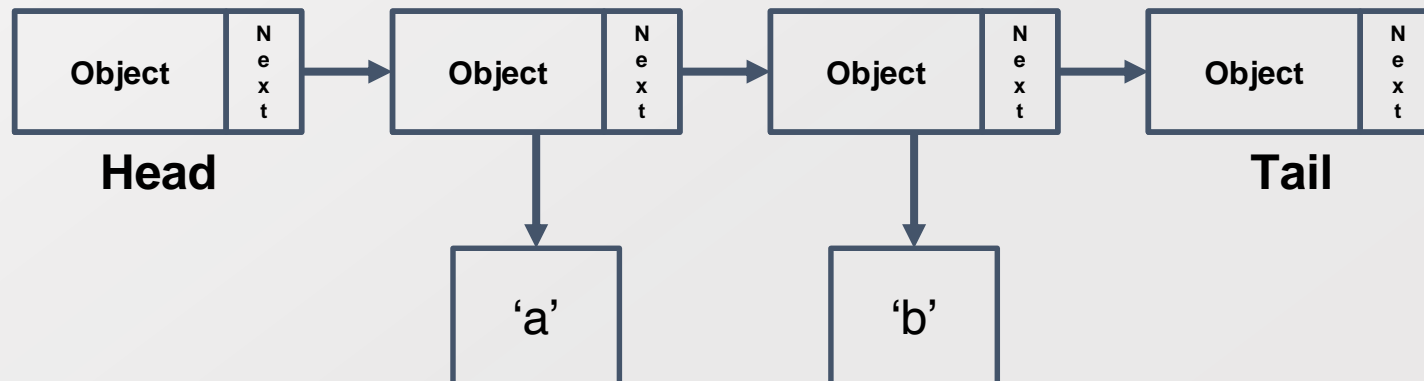


- Specialized node
  - Head : Always at the first of the list
  - Tail : Always at the last of the list
  - These are the two corner stone showing the start and the end of the list
- These are optional nodes.
  - Linked list works okay without these
  - However, having these makes implementation very convenient
  - Any example?

## Empty Linked List

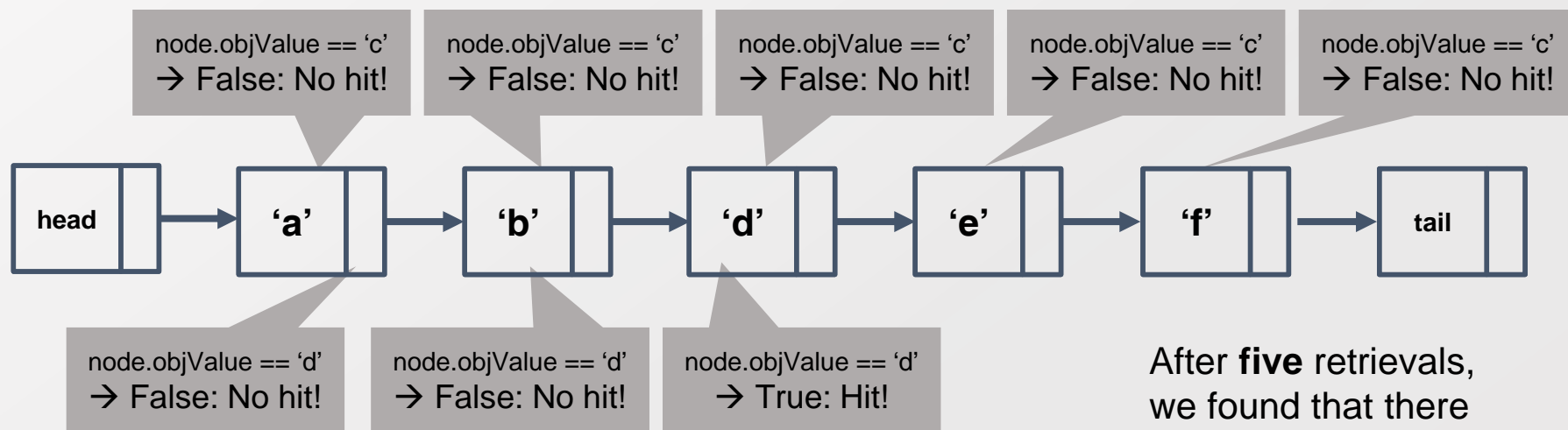


## Linked List with Two Nodes



# Search Procedure in Singly Linked List

- Again, let's find 'd' and 'c' from the list
- Just like an array, navigating from the first to the last until hit is the only way
- No difference in the search pattern, though you cannot use index any further!
  - Your list implementation may include the index function, but it is not required in the linked list

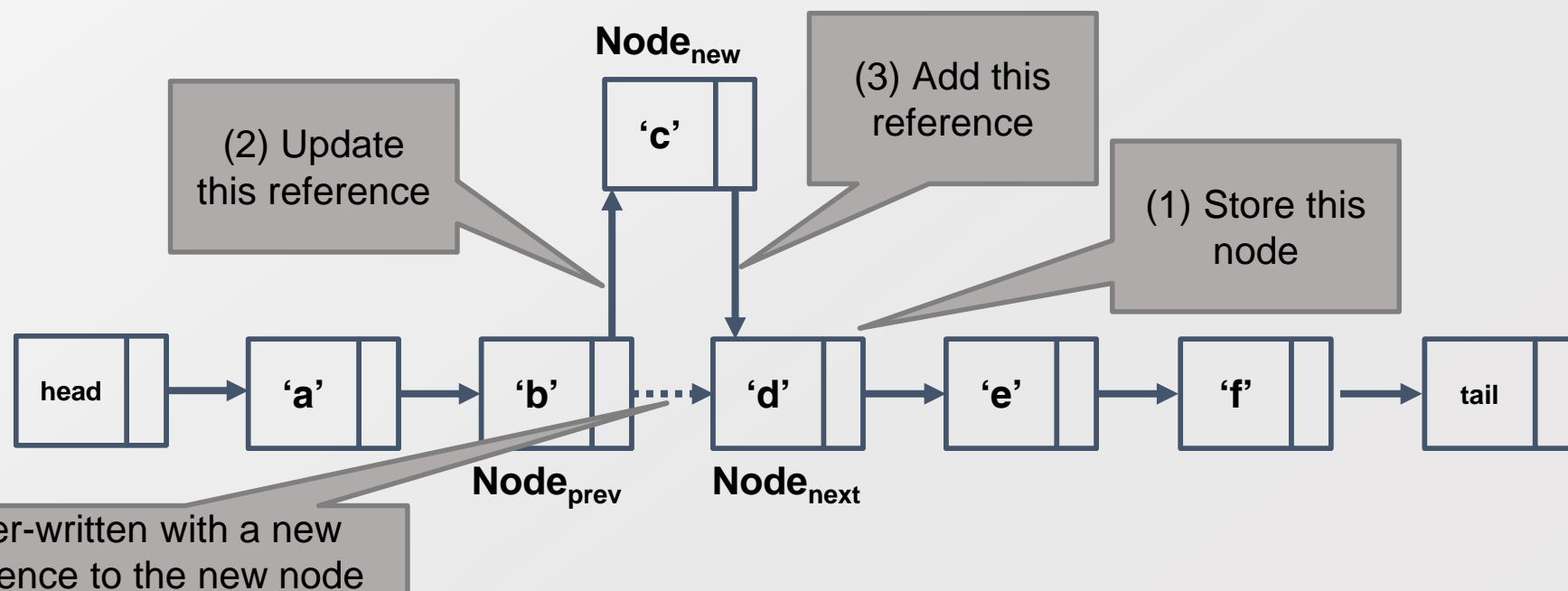


After **three** retrievals,  
we found the hit!  
(maximum N retrievals)

After **five** retrievals,  
we found that there  
will be no hit!  
(always N retrievals)

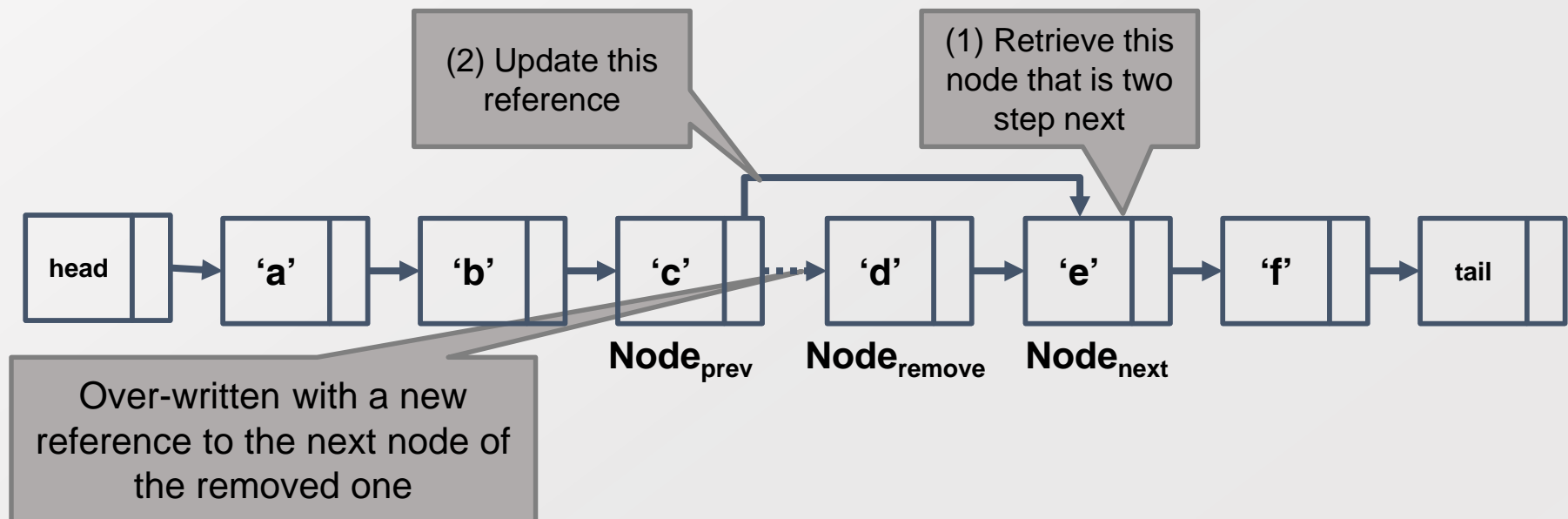
# Insert Procedure in Singly Linked List

- This is the moment that you see the power of a linked list
- Last time, you need N retrievals to insert a value in the array list
- This time, you need only three operations
  - With an assumption that you have a reference to the node,  $\text{Node}_{\text{prev}}$  that you want to put your new node next
  - First, you store a Node, or a  $\text{Node}_{\text{next}}$ , pointed by a reference from  $\text{Node}_{\text{prev}}$ 's `nodeNext` member variable
  - Second, you change a reference from  $\text{Node}_{\text{prev}}$ 's `nodeNext` to  $\text{Node}_{\text{new}}$
  - Third, you change a reference from  $\text{Node}_{\text{new}}$ 's `nodeNext` to  $\text{Node}_{\text{next}}$



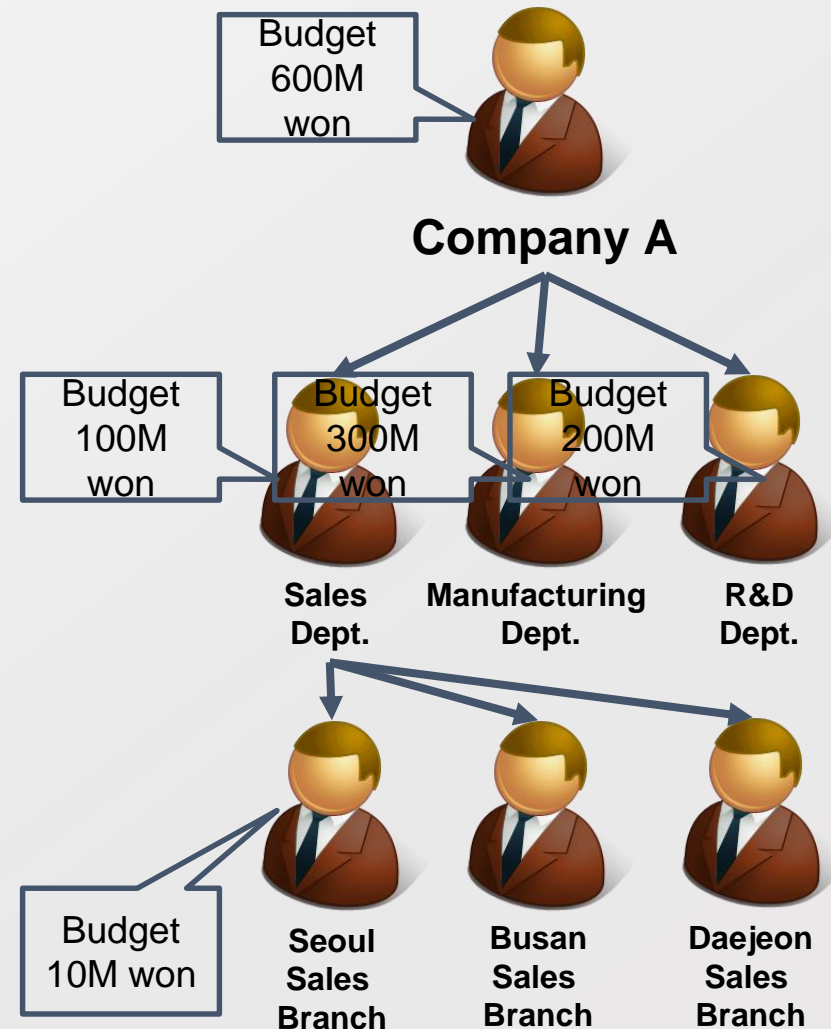
# Delete Procedure in Singly Linked List

- This is the another moment that you see the power of a linked list
- Last time, you need N retrievals to delete a value in the array list
- This time, you need only three operations
  - With an assumption that you have a reference to the node,  $\text{Node}_{\text{prev}}$  that you want to remove the node next
  - First, you retrieve  $\text{Node}_{\text{next}}$  that is two steps next from  $\text{Node}_{\text{prev}}$
  - Second, you change a reference from  $\text{Node}_{\text{prev}}$ 's `nodeNext` to  $\text{Node}_{\text{next}}$
- The node will be removed because there is no reference to  $\text{Node}_{\text{remove}}$



- Calculating a budget of a company?
  - Departments consist of the company
  - Departments within departments
- Can't avoid the below structures
  - class Department
    - dept = [sales, manu, randd]
    - def **calculateBudget**(self)
      - Sum = 0
      - For itr in range(0, numDepartments)
        - Sum = sum + dept[itr].**calculateBudget**()
      - Return sum

**Russian Doll:**  
Dolls within dolls





- Factorial

- $Factorial(n) = \begin{cases} 1 & \text{if } n = 0 \\ n \times (n - 1) \times \dots \times 2 \times 1 & \text{if } n > 0 \end{cases}$

- Repeating problems?

- $Factorial(n) = \begin{cases} 1 & \text{if } n = 0 \\ n \times Factorial(n - 1) & \text{if } n > 0 \end{cases}$

- Great Common Divisor

- $GCD(32, 24) = 8$

- Euclid's algorithm

- $GCD(A, B) = GCD(B, A \bmod B)$

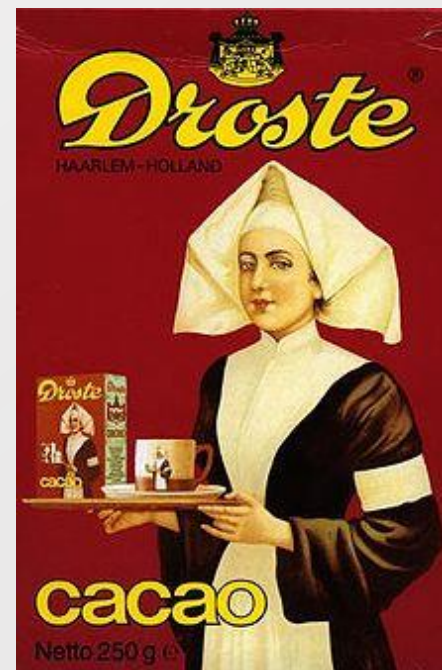
- $GCD(A, 0) = A$

- Commonality

- Repeating function calls

- Reducing parameters

- Just like the mathematical induction



**Self-Similar**

- A programming method to handle the repeating items in a self-similar way
  - Often in a form of
    - Calling a function within the function
      - `def functionA(target)`
        - ....
        - `functionA(target')`
        - ....
        - `if (escapeCondition)`
          - `Return A;`

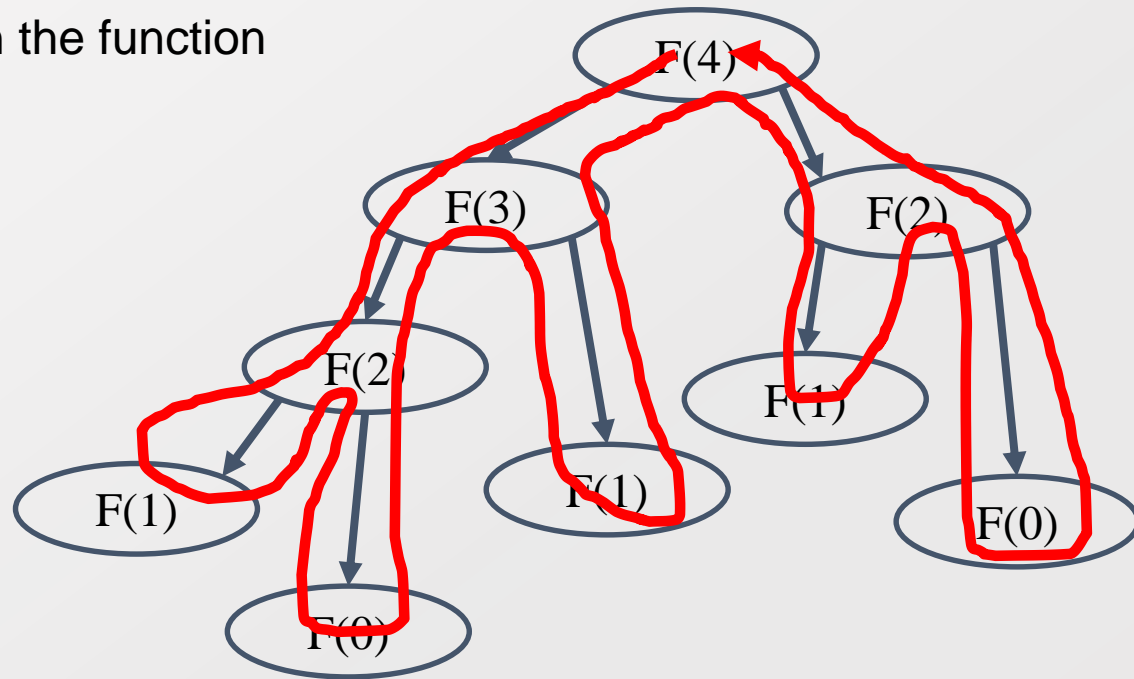
```
def Fibonacci(n):
    if n == 0:
        return 0
    if n == 1:
        return 1
    intRet = Fibonacci(n-1) + Fibonacci(n-2)
    return intRet

for itr in range(0, 10):
    print(Fibonacci(itr), end=" ")
```

Run: FibonacciSequence x

C:\Users\USER\Anaconda3\python.exe C:/Us  
0 1 1 2 3 5 8 13 21 34

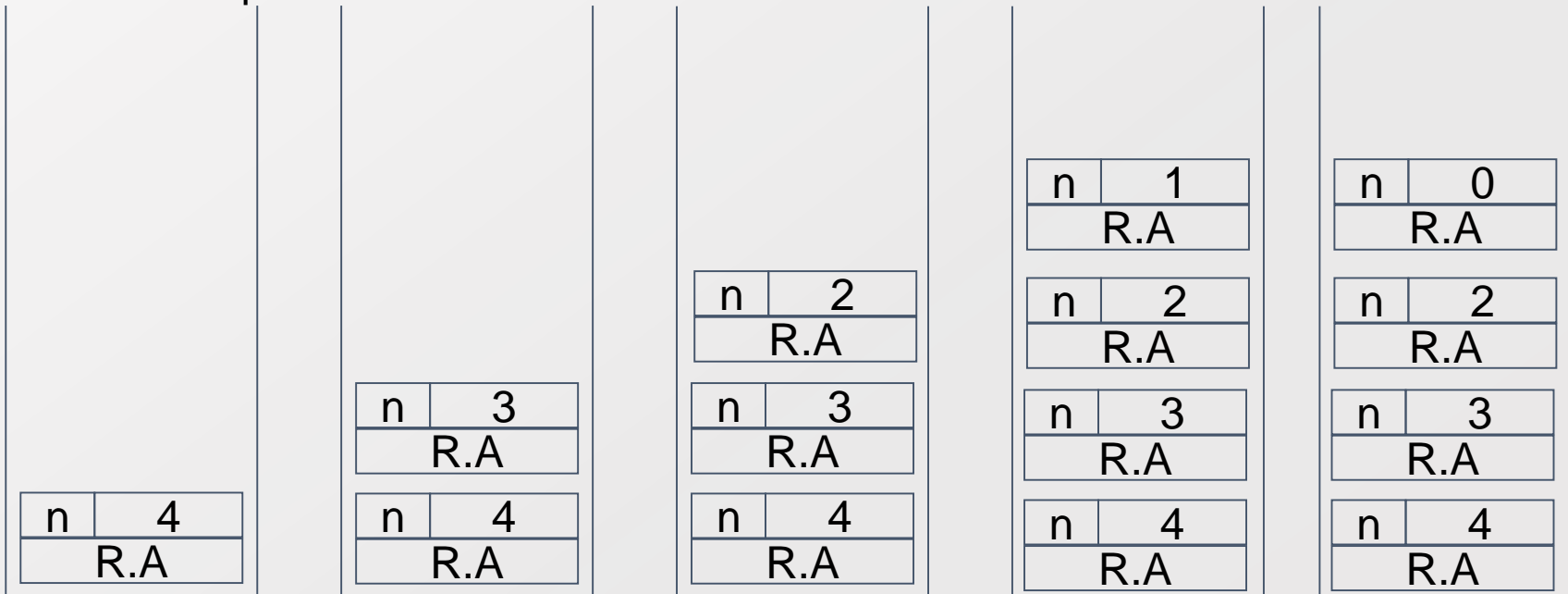
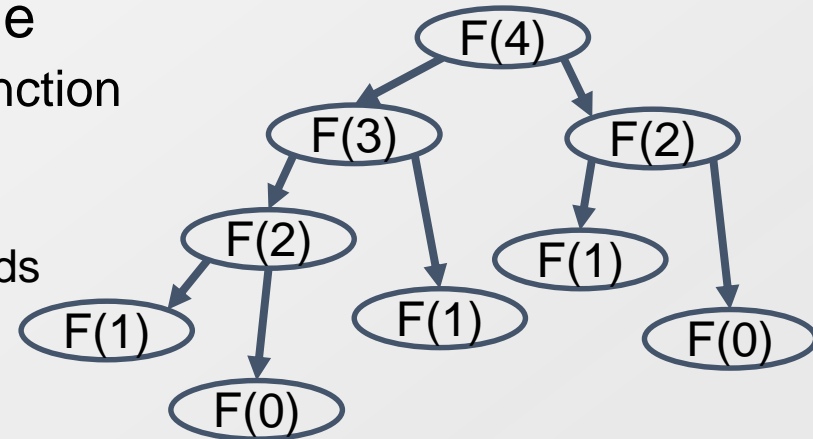
## Program Execution Flow



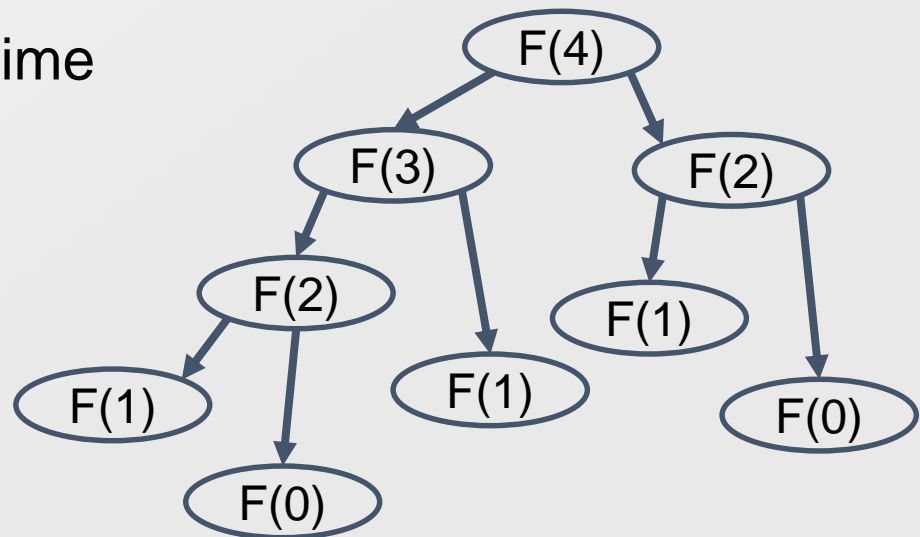
$Fibonacci(n)$

$$= \begin{cases} 0 & n = 0 \\ 1 & n = 1 \\ Fibonacci(n-1) + Fibonacci(n-2) & n \geq 2 \end{cases}$$

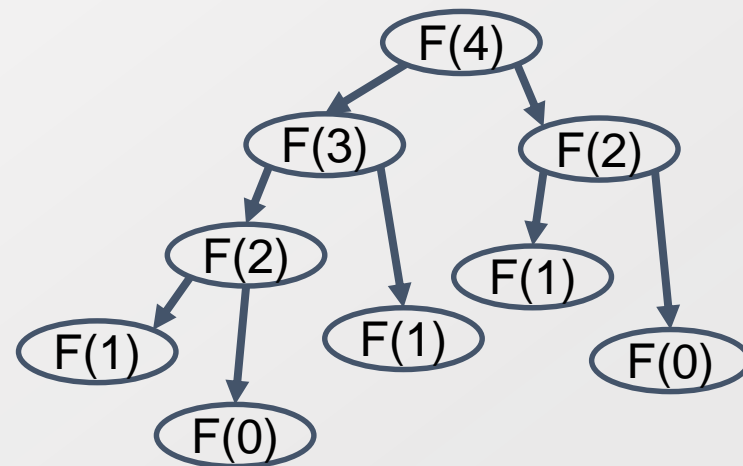
- Recursion of functions
  - Increase the items in the stackframe
    - Stackframe is a stack storing your function call history
      - Push: When a function is invoked
      - Pop: When a function hits return or ends
      - What to store?
        - Local variables and function call parameters



- Problems in recursions
  - Excessive function calls
    - Calling functions again and again
    - Even though the function is executed before with the same parameters
- For instance, Fibonacci(4)
  - Has two repeated calls of F(0)
  - Has three repeated calls of F(1)
  - Has two repeated calls of F(2)
- These are unnecessarily taking time and space
- How to solve this problem?



- Dynamic programming:
  - A general algorithm design technique for solving problems defined by or formulated as **recurrences with overlapping sub-instances**
  - In this context, Programming == Planning
- Main storyline
  - Setting up a recurrence
    - Relating a solution of a larger instance to solutions of some smaller instances
    - Solve small instances once
    - Record solutions in a table
    - Extract a solution of a larger instance from the table

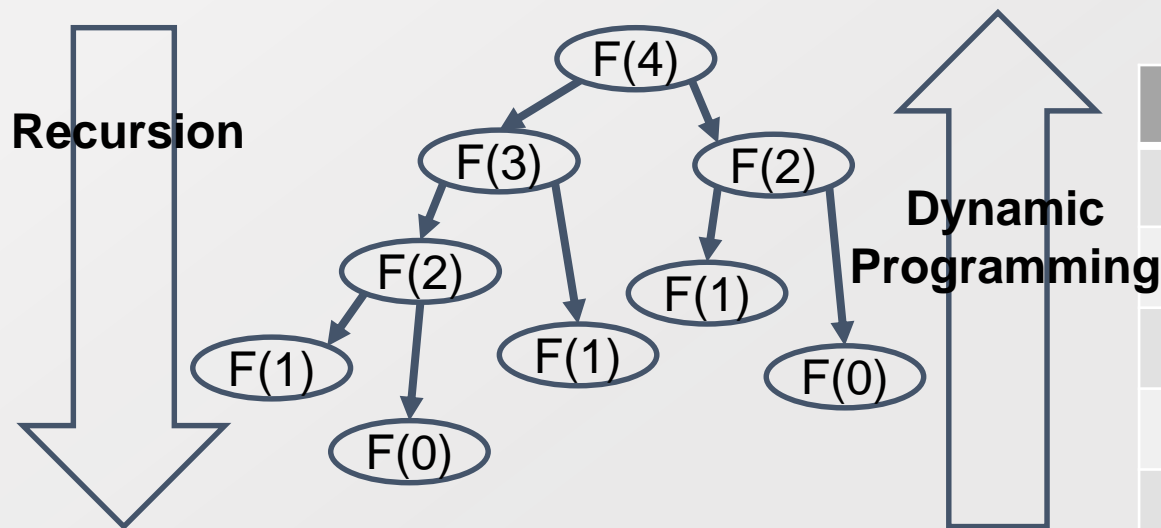


Instance	Solution
F(0)	0
F(1)	1
F(2)	1
F(3)	2
F(4)	?

- Key technique of dynamic programming
  - Simply put
    - Storing the results of previous function calls to reuse the results again in the future
  - More philosophical sense
    - Bottom-up approach for problem-solving
      - Recursion: Top-down of divide and conquer
      - Dynamic programming: Bottom-up of storing and building

## Stackframe

n	2
R.A	
n	3
R.A	
n	4
R.A	



## Memoization

Instance	Solution
F(0)	0
F(1)	1
F(2)	1
F(3)	2
F(4)	3

```
def FibonacciDP(n):  
    dicFibonacci = {}  
    dicFibonacci[0] = 0  
    dicFibonacci[1] = 1  
    for itr in range(2, n + 1):  
        dicFibonacci[itr] = dicFibonacci[itr-1] + dicFibonacci[itr-2]  
    return dicFibonacci[n]  
  
for itr in range(0, 10):  
    print(FibonacciDP(itr), end=" ")
```

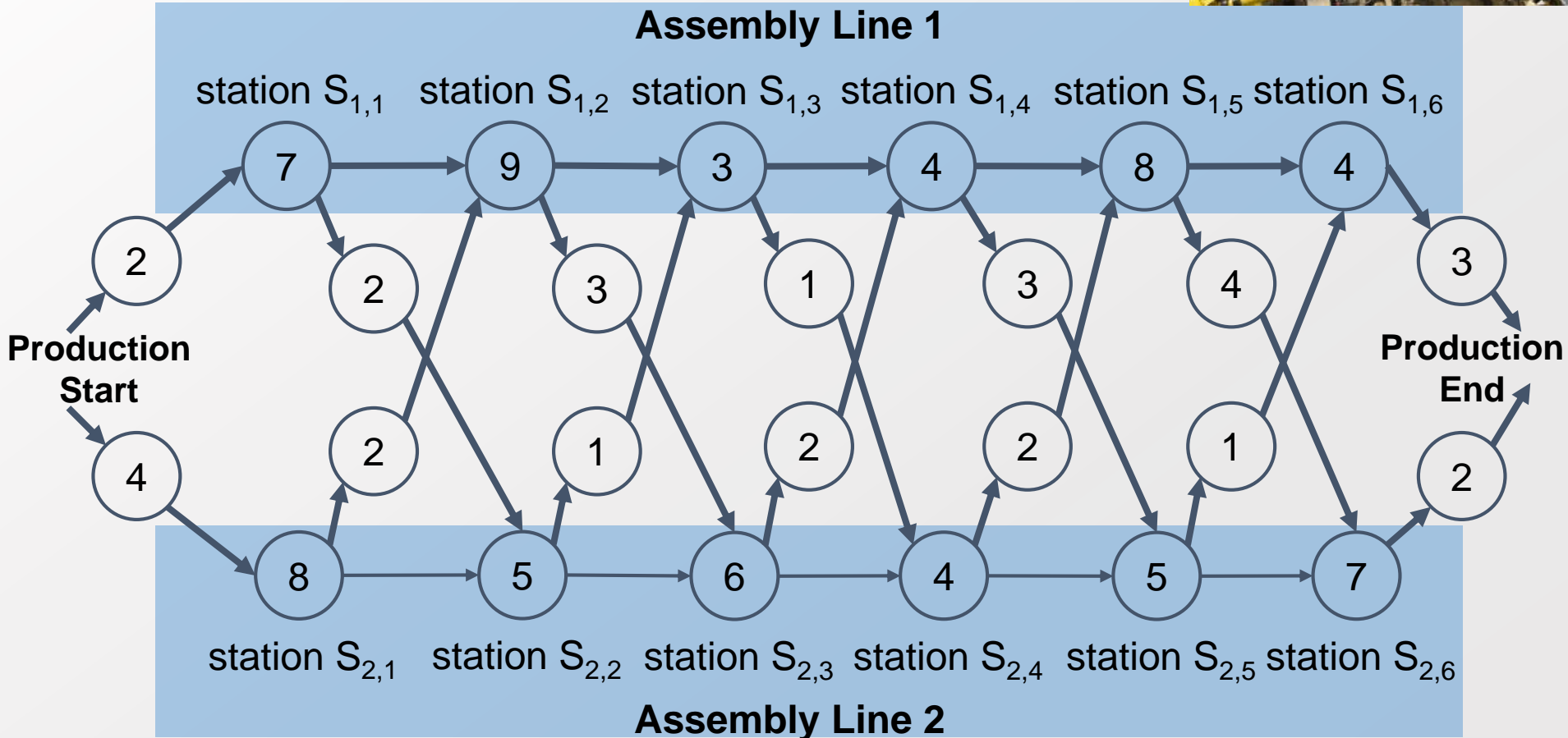
**} Setting up a memoization table**

**} Building up a bigger solutions**

**} Execution Part**

- Use a dictionary collection variable type for memoization
  - Memoization
    - Storing a fibonacci number for a particular index
- Now,
  - We have a new space requirement, the dictionary or the table, of  $O(N)$
  - We have reduced execution time from  $O(2^n)$  to  $O(N)$

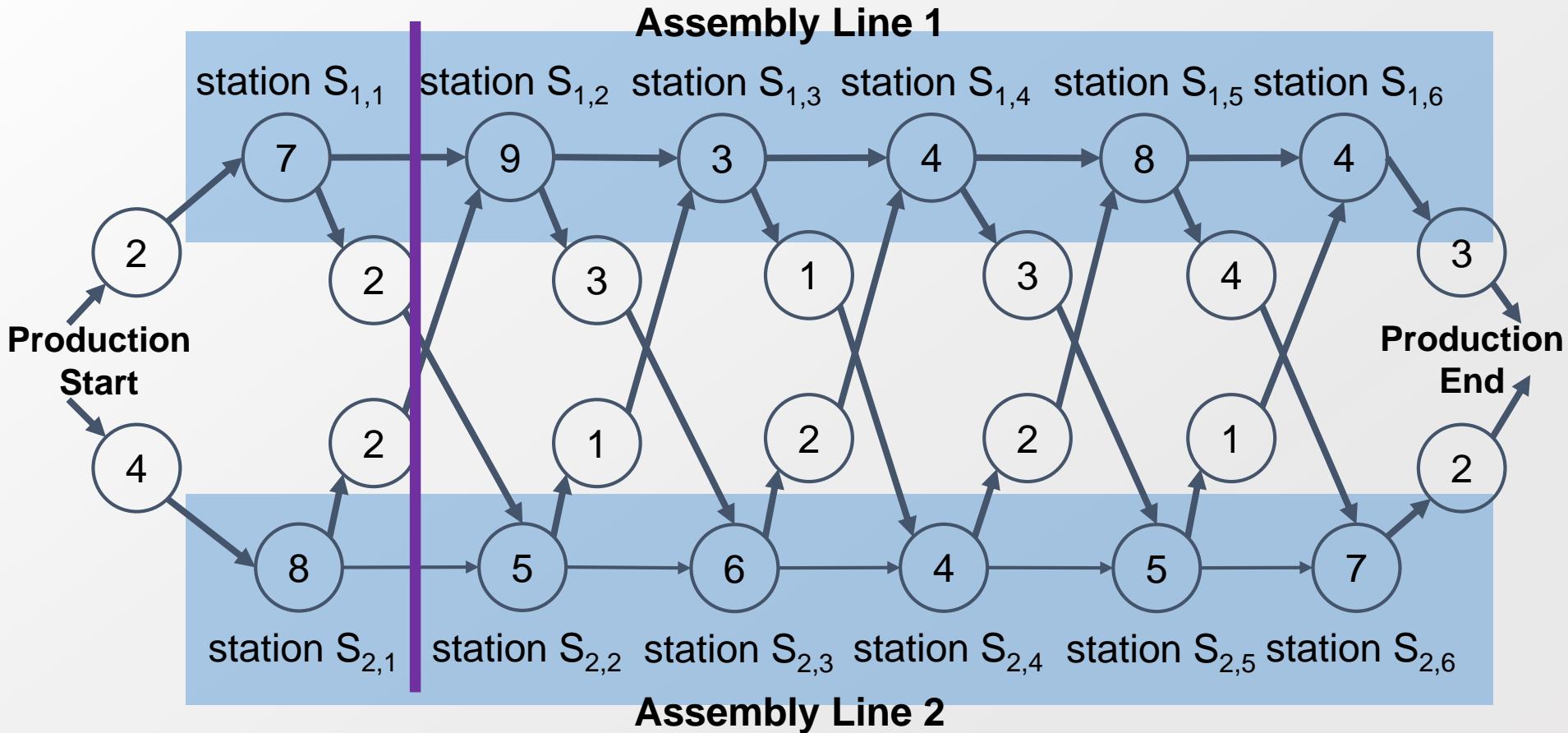
# Assembly Line Scheduling



**Goal:** Computing the fastest production route



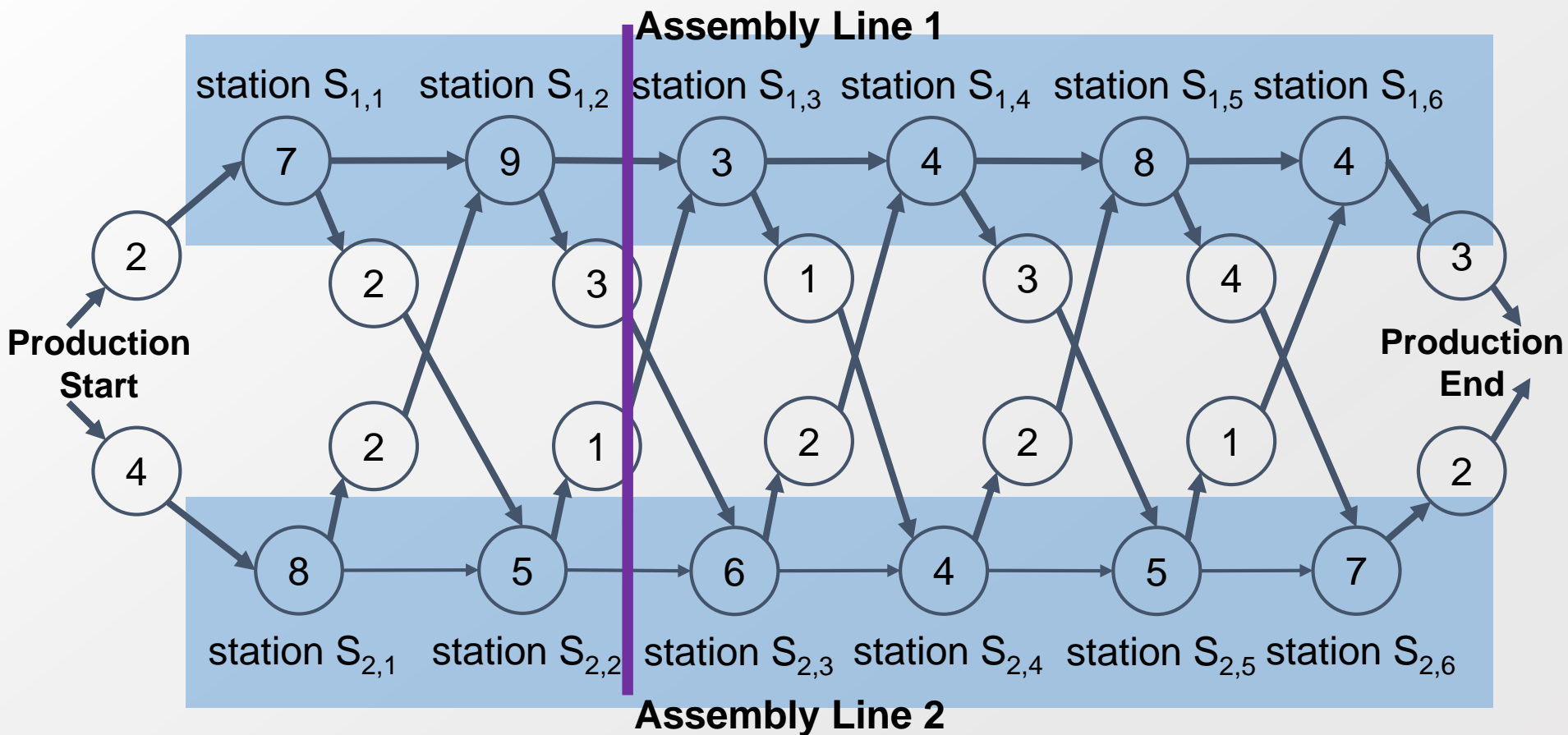
# Process of Assembly Line Scheduling



Time	1	2	3	4	5	6
L1	9					
L2	12					

Trace	1	2	3	4	5	6
L1	S					
L2	S					

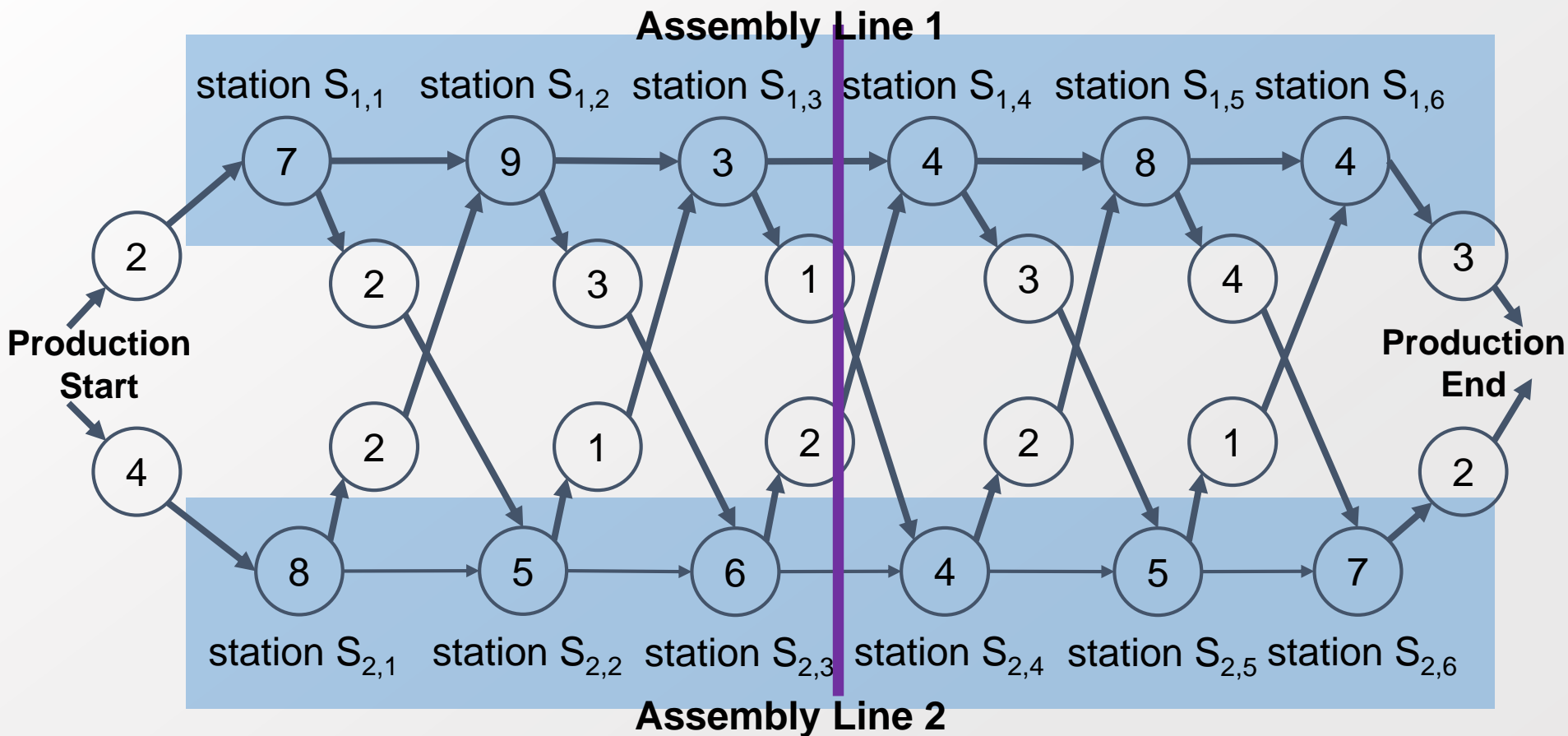
# Process of Assembly Line Scheduling



Time	1	2	3	4	5	6
L1	9	18				
L2	12	16				

Trace	1	2	3	4	5	6
L1	S	1				
L2	S	1				

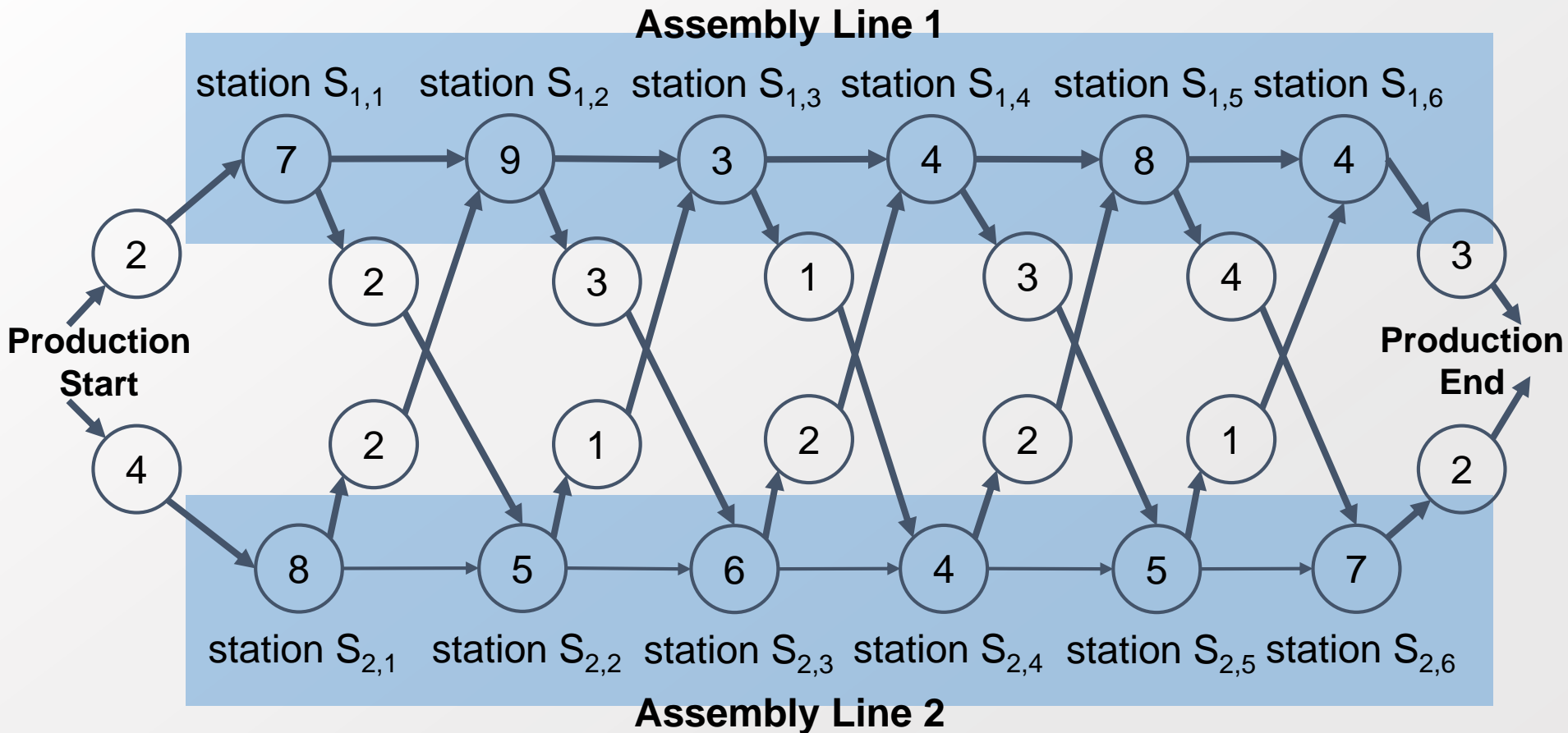
# Process of Assembly Line Scheduling



Time	1	2	3	4	5	6
L1	9	18	20			
L2	12	16	22			

Trace	1	2	3	4	5	6
L1	S	1	2			
L2	S	1	2			

# Process of Assembly Line Scheduling



Time	1	2	3	4	5	6
L1	9	18	20	24	32	35
L2	12	16	22	25	30	37

Trace	1	2	3	4	5	6
L1	S	1	2	1	1	2
L2	S	1	2	1	2	2

# EXERCISE

- Building an AI playing Blackjack game
  - Customized game rule
    - Two players only : AI and player
    - Start with no cards
    - Cards with values : J=11, Q=12, K=13, A=1
    - Can see five cards in advance for each round
    - Each round has two decisions
      - First, Player : Hit or Pass : Hit means receiving a card
      - Second, AI : Hit or Pass : Hit means receiving a card
  - Winner
    - First reach 21 for the card sum
      - Beyond 21 == Lose
    - Both pass for a single round
      - Higher score wins
      - Same score means tie

- **After running 'Blackjack.py'**
- C:\Users\win\Anaconda3\python.exe "D:/SESLab-Teaching/Blackjack.py"
- -----
- Round : 0
- ['7-Spade', '7-Diamond', 'K-Spade', '8-Spade', '10-Clover']
- AI Current Score : 0
- AI's Hand : []
- Player Current Score : 0
- Player's Hand : []
- Player Cards to Play : 7-Spade
- (H)it or (P)ass ??? Type!
- H
- AI Observed Cards : ['7-Diamond', 'K-Spade', '8-Spade', '10-Clover']
- INSIDE AI : AI Expected Total Score : 21
- INSIDE AI : AI Selected Cards : ['K-Spade', '8-Spade']
- AI Cards to Play : 7-Diamond
- AI Pass
- AI Current Score : 0
- Player Current Score : 7
- -----
- Round : 1
- ['7-Diamond', 'K-Spade', '8-Spade', '10-Clover', 'Q-Spade']
- AI Current Score : 0
- AI's Hand : []
- Player Current Score : 7
- Player's Hand : ['7-Spade']
- Player Cards to Play : 7-Diamond
- (H)it or (P)ass ??? Type!
- H
- AI Observed Cards : ['K-Spade', '8-Spade', '10-Clover', 'Q-Spade']
- INSIDE AI : AI Expected Total Score : 21
- INSIDE AI : AI Selected Cards : ['K-Spade', '8-Spade']
- AI Cards to Play : K-Spade
- AI Hit
- AI Current Score : 13
- Player Current Score : 14
- -----
- Round : 2
- ['8-Spade', '10-Clover', 'Q-Spade', 'A-Diamond', '6-Heart']
- AI Current Score : 13
- AI's Hand : ['K-Spade']
- Player Current Score : 14
- Player's Hand : ['7-Spade', '7-Diamond']
- Player Cards to Play : 8-Spade
- (H)it or (P)ass ??? Type!
- P
- AI Observed Cards : ['8-Spade', '10-Clover', 'Q-Spade', 'A-Diamond', '6-Heart']
- INSIDE AI : AI Expected Total Score : 21
- INSIDE AI : AI Selected Cards : ['K-Spade', '8-Spade']
- AI Cards to Play : 8-Spade
- AI Hit
- AI Current Score : 21
- Player Current Score : 14
- AI Win!
- Process finished with exit code 0

Round : 0

['7-Spade', '7-Diamond', 'K-Spade', '8-Spade', '10-Clover'] **Player can observe these cards**

AI Current Score : 0 **Current score of AI**

AI's Hand : [] **AI has these cards**

Player Current Score : 0 **Current score of player**

Player's Hand : [] **Player has these cards**

Player Cards to Play : 7-Spade **Player has to make a decision whether or not to get this card**

(H)it or (P)ass ??? Type! **Make decision of player's action**



Round : 0

['7-Spade', '7-Diamond', 'K-Spade', '8-Spade', '10-Clover'] **Player can observe these cards**

AI Current Score : 0 **Current score of AI**

AI's Hand : [] **AI has these cards**

Player Current Score : 0 **Current score of player**

Player's Hand : [] **Player has these cards**

Player Cards to Play : 7-Spade **Player has to make a decision whether or not to get this card**

(H)it or (P)ass ??? Type! **Make decision of player's action**

H

Round : 0

['7-Spade', '7-Diamond', 'K-Spade', '8-Spade', '10-Clover'] **Player can observe these cards**

AI Current Score : 0 **Current score of AI**

AI's Hand : [] **AI has these cards**

Player Current Score : 0 **Current score of player**

Player's Hand : [] **Player has these cards**

Player Cards to Play : 7-Spade **Player has to make a decision whether or not to get this card**

(H)it or (P)ass ??? Type! **Make decision of player's action**

H

AI Observed Cards : ['7-Diamond', 'K-Spade', '8-Spade', '10-Clover'] **AI can observe these cards**

INSIDE AI : AI Expected Total Score : 21 **Expected score based on the strategy of AI**

INSIDE AI : AI Selected Cards : ['K-Spade', '8-Spade'] **Selected cards based on the strategy of AI**

AI Cards to Play : 7-Diamond **If AI hits, then AI will get this card**

AI Pass

AI Current Score : 0  
**Current score of end of round**

Player Current Score : 7

- Core problem
  - How to find the best combination to reach 21 with the current observations and the current hand
  - This is a customized problem of Knapsack problem
    - English Wikipedia provides a good description
- Key variable
  - `self.tblSelect`
    - `[index = self.scoreAI]`
    - selected cards from the observed cards + current hand(`self.lstAIHand`)
  - `self.tblRemaining`
    - `[index = self.scoreAI]`
    - cards for selection (initially at the method beginning : `self.observedCards`), each element is a list
  - `self.tblBestSelect`
    - the selection set closest to 21

# Memoization Table for Blackjack

Index =Score	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
tblSelect	-							7	8		10			K		7, 8		7, 10	8, 10
tblRemaining	7, K, 8, 10							K, 8, 10	7, K, 10		7, K, 8			7, 8, 10		K, 10		K, 8,	7, K

- Structure the memorization table

- See the score is used as an index
- Make the remaining and the selected card lists

- Retrace from 21 score

- The first selection will be the closest to 21

**AI Current Score : 0**

**AI's Hand : []**

**Player Current Score : 0**

**Player's Hand : []**

**Player Cards to Play : 7-Spade**

**(H)it or (P)ass ??? Type!**

**H**

**AI Observed Cards : ['7-Diamond', 'K-Spade', '8-Spade', '10-Clover']**

**INSIDE AI : AI Expected Total Score : 21**

**INSIDE AI : AI Selected Cards : ['K-Spade', '8-Spade']**