# Lab 1: Python Intro, Flat-Top PAM, PCM

# 1 Introduction

# 1.1 Baseband Signaling

A simple communication scenario is the transmission of a text string over a waveform channel such as a pair of twisted wires or a wireless radio frequency (RF) link. Starting from simple baseband signaling over an ideal noiseless channel and later proceeding to more complicated situations, many important aspects of the theory and practice of communication engineering can be studied in this context. One goal of this lab is to introduce Python as a high-level tool for signal processing and, in particular, for the generation and reception of communication signals. Another goal is to be able to transmit and receive ASCII text strings in Python using flat-top PAM (pulse amplitude modulation) which is a simple baseband signaling technique. An extension of this is to use pulse code modulation (PCM) to also transmit analog message signals.

Communication signals can be broadly divided into **baseband signals** and into **bandpass signals** (or passband signals). One way to define baseband and bandpass signals is as follows.

**Definition:** A communication signal is called a **baseband signal** if the filter of smallest bandwidth (BW) that passes the signal essentially undistorted is a LPF (lowpass filter) with passband  $0 \le f < f_L$ . Conversely, if this filter of smallest BW is a BPF (bandpass filter) with passband  $0 < f_1 < f < f_2$ , then the corresponding signal is called a **bandpass signal**.

#### 1.2 ASCII Code

The ASCII (American Standard Code for Information Interchange) code is a 7-bit code for encoding upper/lower case characters from the English alphabet, as well as numbers, punctuation marks, and control characters. The following table shows all the possible 128 code sequences of the original ASCII code.

7-Bit ASCII (American Standard Code for Information Interchange)								
	000	001	010	011	100	101	110	111
0000	NUL	DLE	SP	0	@	Р	(	р
0001	SOH	DC1	!	1	A	Q	a	q
0010	STX	DC2	11	2	В	R	ъ	r
0011	ETX	DC3	#	3	C	S	С	s
0100	EOT	DC4	\$	4	D	Т	d	t
0101	ENQ	NAK	%	5	E	U	е	u
0110	ACK	SYN	&	6	F	V	f	v
0111	BEL	ETB	,	7	G	W	g	W
1000	BS	CAN	(	8	Н	Х	h	х
1001	HT	EM	)	9	I	Y	i	у
1010	LF	SUB	*	:	J	Z	j	z
1011	VT	ESC	+	;	K	Г	k	{
1100	FF	FS	,	<	L	\	1	I
1101	CR	GS	_	=	М	]	m	}
1110	SO	RS		>	N	^	n	~
1111	SI	US	/	?	0	_	0	DEL

The first two columns consist of non-printable control characters, e.g., CR stands for carriage return and LF stands for line feed. The space character (ASCII code 0100000) is shown as SP in the table. In the teletype days transmissions typically started with a few synchronization characters (SYN), followed by a start of text character (STX). After that the actual message would be sent and at the end terminated with an end of text character (ETX). The main purpose of characters like SYN, STX, and ETX was to synchronize the transmitting and the receiving teletype machines.

The binary codes in the ASCII table above are shown with the MSB (most significant bit) on the left and the LSB (least significant bit) on the right. Because the wordlengths used in computers are typically powers of 2, it is quite common to extend the ASCII code by adding a zero to the left of the MSB to make 8-bit codewords as shown in the following example.

"Test" in Extended (8-bit) ASCII					
Character	Extended ASCII Code				
Т	01010100				
е	01100101				
s	01110011				
t	01110100				

#### 1.3 Parallel to Serial Conversion

Using the extended 8-bit ASCII code, the letter "T", for instance, is encoded in binary as 01010100. To transmit this 8-bit quantity in binary over a communication channel, each bit must be read out and transmitted indivdually, according to a specific scheme that is known to both the transmitter and receiver. The two most common schemes are to either read the bits out from left to right and therefore transmit MSB-first, or to read from right to left and in this case transmit LSB-first. In either case the codeword for the first character is sent first, followed by the codeword of the second character, etc.

The following two tables show the serial data sequence  $d_n$ ,  $n \ge 0$ , for the string "Test" using MSB-first and LSB-first parallel (8-bit) to serial conversion.

MSB-first Bit Sequence for "Test" (Extended 8-bit ASCII) 
$$d_n = 01010100 \ 01100101 \ 01110011 \ 01110100$$
  $\rightarrow$  Index  $n$  increases from left to right  $\rightarrow$  
$$d_0=0, \ d_1=1, \ d_2=0, \ d_3=1, \ d_4=0, \ d_5=1, \ d_6=0, \ d_7=0, \ d_8=0, \ d_9=1, \ d_{10}=1, \dots$$

LSB-first Bit Sequence for "Test" (Extended 8-bit ASCII) 
$$d_n = 00101010 \ 10100110 \ 11001110 \ 00101110$$

$$\rightarrow \text{Index } n \text{ increases from left to right } \rightarrow$$

$$d_0 = 0, d_1 = 0, d_2 = 1, d_3 = 0, d_4 = 1, d_5 = 0, d_6 = 1, d_7 = 0, d_8 = 1, d_9 = 0, d_{10} = 1, \dots$$

The spaces after every 8 bits are shown only for ease of reading. In an actual data transmission all 32 bits would be sent consecutively, without any spaces or pauses.

In practice the LSB-first scheme is the one that is most commonly used for the transmission of ASCII text.

#### 1.4 Flat-Top PAM

Most physical communication channels, like twisted-pair wire, coaxial cable, free-space radio frequency (RF) transmission, etc, are analog in nature. This implies in particular that

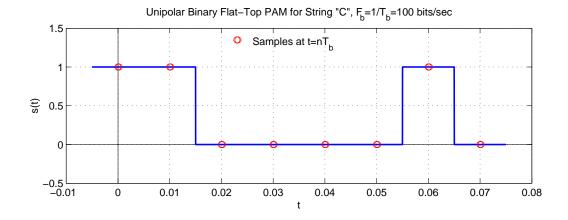
they require a continuous-time (CT) signal or waveform at the input. A discrete-time (DT) sequence, like  $d_n$  in the ASCII examples of the previous section, therefore needs to be converted to a CT signal s(t) before it can be transmitted over a waveform channel. A simple and straightforward rule, informally called "flat-top" PAM (pulse amplitude modulation), to obtain a waveform s(t) from  $d_n$  with bit rate  $F_b = 1/T_b$  is to set

$$s(t) = d_n$$
,  $(n - 1/2) T_b \le t < (n + 1/2) T_b$ .

In blockdiagram form, the function of a flat-top PAM transmitter is represented as shown in the following figure.



The graph below shows the letter "C" (ASCII code 01000011) converted (LSB-first) to a binary flat-top PAM signal s(t).



A DT sequence  $d_n$ ,  $n \ge 0$ , can also be expressed as

$$\{d_n\} = \{d_0 \,\delta_n + d_1 \,\delta_{n-1} + d_2 \,\delta_{n-2} + \ldots\},\,$$

where  $\delta_k = 1$  if k = 0 and  $\delta_k = 0$  otherwise. Each  $d_m \, \delta_{n-m}$  gets converted to a piece, from  $(m-1/2) \, T_b$  to  $(m+1/2) \, T_b$ , of the signal s(t). Thus, another way to describe flat-top PAM mathematically is

$$s(t) = \sum_{n=0}^{\infty} d_n p(t - nT_b) ,$$

where  $d_n$  is a binary sequence with bitrate  $F_b = 1/T_b$ , and p(t) is the rectangular pulse shown in the following figure.

$$p(t) = \begin{cases} 1, & -T_b/2 \le t < T_b/2, \\ 0, & \text{otherwise}. \end{cases}$$

### 1.5 Flat-Top PAM Receiver

In any communication system the task of the receiver is to reproduce the transmitted information as faithfully as possible. For flat-top PAM, the receiver initially simply consists of a sampler that samples the received signal r(t) at times  $t = nT_b$ , so that  $r_n = r(nT_b)$  as shown in the following blockdiagram.

$$r(t) \qquad r_n \qquad t = nT_b$$

In the absence of noise and other channel degradations,  $r(t) \approx s(t)$  and thus  $r_n = \hat{d}_n$ , the estimate of the received sequence  $d_n$ . In fact, setting r(t) = s(t),

$$\hat{d}_n = r_n = s(t)\big|_{t=nT_b} = \left[\sum_{m=0}^{\infty} d_m p(t - mT_b)\right]\Big|_{t=nT_b} = \sum_{m=0}^{\infty} d_m p(nT_b - mT_b).$$

Defining the sampled version of p(t) as

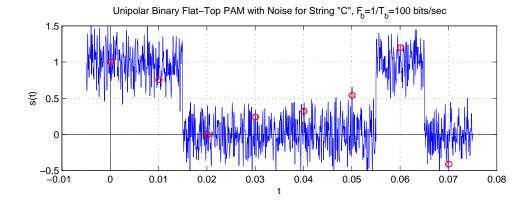
$$p_n = p(nT_b)$$
  $\Longrightarrow$   $\hat{d}_n = \sum_{m=0}^{\infty} d_m p_{n-m} = d_n * p_n$ .

Thus, the DT equivalent of PAM followed by sampling at the receiver is convolution between the input sequence  $d_n$  and the pulse samples  $p_n$ , as shown in the next blockdiagram.

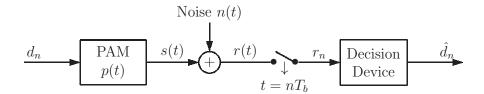
$$\begin{array}{c|c}
d_n & \text{DT Equiv.} \\
h_n = p_n & \\
\end{array}$$

The rectangular pulse p(t) that is used for flat-top PAM satisfies  $p_n = p(nT_b) = \delta_n$  and thus the DT convolution is trivial. But, as you will see later, the same DT equivalent blockdiagram can be used for PAM with more general p(t) and thus more general  $p_n$ .

But suppose now that noise gets added to s(t) during the transmission and the received signal becomes r(t) = s(t) + n(t), where n(t) is noise. An example of how r(t) might look for the letter "C" (8-bit ASCII, LSB-first) is shown in the graph below.



Now just sampling the received signal at the right time and converting it back to ASCII text will not work because  $r_n$  is a real number and not just 0 or 1. Thus, a decision device needs to be introduced after the sampler as shown in the blockdiagram below.



The characteristic of the decision device is shown below. Assuming that the statistics of positive and negative noise levels are similar and that the noise is independent of the transmitted data, the threshold of the decision device is chosen halfway between the "legal" values of 0 and 1.

$$\hat{d}_n = \begin{cases} 0, & r_n < 1/2, \\ 1, & r_n \ge 1/2. \end{cases}$$

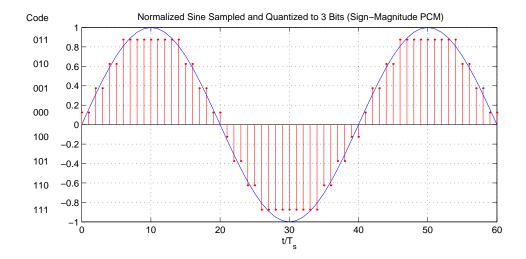
Note that, no matter how the threshold is chosen, errors will occur as the noise gets stronger and the signal-to-noise ratio (SNR) decreases. The structure of an optimum receiver that maximizes the SNR before using the decision device will be derived later on.

#### 1.6 Pulse Code Modulation

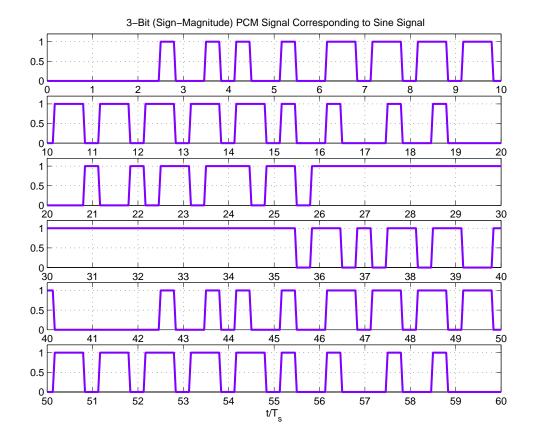
Pulse code modulation (PCM) was invented by Alec Reeves in 1937 to obtain a digital representation of analog message signals m(t). In essence, m(t) is sampled at rate  $F_s$  samples per second and then each sample is quantized to b bits which are in turn transmitted serially, e.g., using flat-top PAM. In telephony  $F_s = 8000$  samples per second and b = 8 are the most commonly used parameters for individual subscriber lines, resulting in a binary signal with

bit rate  $F_b = 64$  kbit/sec. One advantage of using PCM is that several signals can easily be multiplexed in time so that they can share a single communication channel. A T1 carrier, for example, is used in telephony to transmit 24 multiplexed PCM signals with a total rate of 1.544 Mbit/sec (this includes some overhead for synchronization). A second advantage is that repeaters that need to be used to compensate for losses over large distances can (within some limits) restore the signal perfectly because only two signal levels need to be distinguished.

**Example: 3-Bit PCM for a Sinewave.** The figure below shows a normalized sinewave (blue line) and its sampled and quantized version (red stem plot). A 3-bit quantizer with sign-magnitude output was used. The sign-magnitude format (rather than 2's complement) reduces the sensitivity for small amplitude values to sign errors that may occur during transmission.

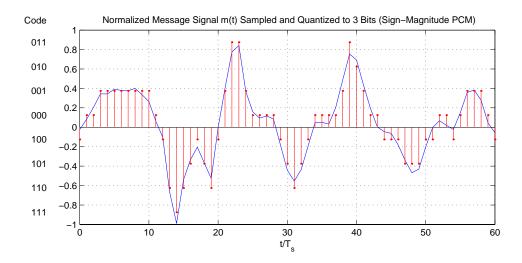


The 6 graphs below show how the quantized samples of the sine signal are transmitted serially using binary flat-top PAM. In this case the parallel to serial conversion is MSB first, i.e., the sign bit is transmitted first and the LSB of the magnitude representation is transmitted last.

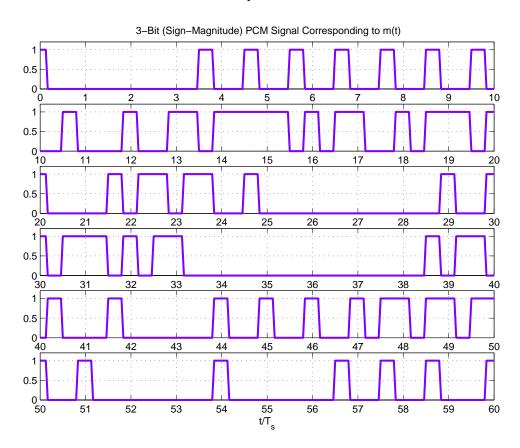


An interesting question is how to synchronize the receiver to the bit rate used at the transmitter when long strings of zeros or ones occur in the data. Several variations of the basic PCM scheme exist to deal with this problem, but their treatment is beyond the scope of this lab description.

**Example: 3-Bit PCM for a Message Signal.** The graph below shows a small segment of a typical (normalized) speech message signal m(t) (blue line) and its digitized version (red stem plot) using 3-bit sign-magnitude format. It is quite visible that the 3-bit quantization is too crude. In fact, since low amplitudes are much more common in speech signals than high amplitudes, practical PCM schemes often use a non-linear quantization scheme.



The conversion of the digitized message signal to a binary PCM signal is shown below. Again, the MSB-first rule was used for the parallel to serial conversion.



The name "pulse code modulation" may seem a bit confusing, since PCM is really mostly a technique for digitizing analog signals and making them into binary data streams. It has to be understood in the context of other techniques that were developed at about the same time, for example pulse width modulation (PWM) and pulse position modulation (PPM).

### 1.7 Python and Jupyter Installation

The easiest way to get started with Python and Jupyter is to download and install Anaconda from https://www.continuum.io/downloads. Anaconda installs Python, the Jupyter Notebook, and commonly used packages for scientific computing, such as numpy, scipy, and matplotlib. There are two different versions of Anaconda, one for Python 2.x and one for Python 3.x. For this course Python 3.x will work fine, but it is also possible to install both, the Python 2.x and the Python 3.x versions, on the same computer.

If you prefer to install Python and Jupyter separately, you can go to https://www.python.org/downloads/ for Python and afterwards to

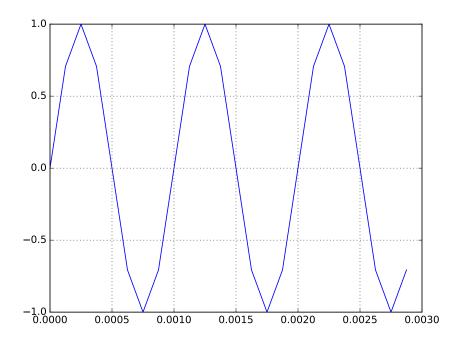
http://jupyter.readthedocs.io/en/latest/install.html (scroll down to "Installing Jupyter with pip"). If you already have Python installed you can directly go to the step of installing Jupyter. To be able to use vectors and matrices efficiently, use signal processing functions such as filtering and fft, and make plots, you will also need numpy, scipy, and matplotlib, see https://www.scipy.org/install.html for instructions to install the SciPy stack.

# 1.8 Python Crash Course

Let's use IPython (interactive Python) to generate 1 second of a sinusoidal waveform with sampling frequency  $F_s$ . We start by importing additional modules and setting parameters:

```
In [1]: from pylab import *
In [2]: Fs = 8000
In [3]: fm = 1000
In [4]: tlen = 1.0
In [5]: tt = arange(0,round(tlen*Fs))/float(Fs) # Time axis
In [6]: xt = sin(2*pi*fm*tt)
                               # Sinewave
In [7]: print(xt[0:12])
[ 0.0000000e+00
                    7.07106781e-01
                                     1.00000000e+00
                                                      7.07106781e-01
   1.22464680e-16 -7.07106781e-01
                                    -1.0000000e+00
                                                     -7.07106781e-01
 -2.44929360e-16
                    7.07106781e-01
                                     1.0000000e+00
                                                      7.07106781e-017
In [8]: plot(tt[0:24],xt[0:24])
Out[8]: [<matplotlib.lines.Line2D at 0x175721f63c8>]
<matplotlib.figure.Figure at 0x17572189ac8>
In [9]: grid()
<matplotlib.figure.Figure at 0x1757223a0b8>
In [10]: show()
```

The resulting graph looks like this:



Now suppose you want to change one of the parameters of the sinusoidal waveform, e.g., the duration tlen. In interactive mode you would have to change tlen and then run all of the subsequent commands again (e.g., using the history command and copying and pasting. A better way is put the Python code for generating a sinusoidal waveform in a separate script file (with extension .py) and then run the script in IPython. Here is the script file sine\_1000.py for producing a sinusoidal waveform:

```
# File: sine_1000.py
# Generates 1.5 sec of 1000 Hz sinusoidal waveform
from pylab import *

# Parameters
Fs = 8000
fm = 1000
tlen = 1.5

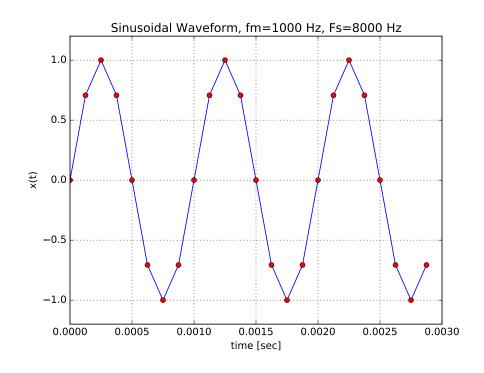
# Generate time axis
tt = arange(0,round(tlen*Fs))/float(Fs)

# Generate sinewave
xt = sin(2*pi*fm*tt)
```

To obtain a graph in IPython we can run the following sequence of commands

```
In [1]: \cd\ d:\courses\4000\ecen4652\s16\abs\lab01\Python
d:\courses\4000\ecen4652\s16\labs\lab01\Python
In [2]: run sine_1000
In [3]: plot(tt[0:24],xt[0:24],'-b',tt[0:24],xt[0:24],'or')
Out[3]:
[<matplotlib.lines.Line2D at 0x21eb25180b8>,
 <matplotlib.lines.Line2D at 0x21eb2518278>]
In [4]: axis([0, 3e-3, -1.2, 1.2])
Out[4]: [0, 0.003, -1.2, 1.2]
In [5]: grid()
In [6]: xlabel('time [sec]')
Out[6]: <matplotlib.text.Text at 0x21eb1b0cb38>
In [7]: ylabel('x(t)')
Out[7]: <matplotlib.text.Text at 0x21eb24cba90>
In [8]: title('Sinusoidal Waveform, fm=1000 Hz, Fs=8000 Hz')
Out[8]: <matplotlib.text.Text at 0x21eb24e4b70>
In [9]: show()
```

This results in the following graph:



Note the labels that have been added to the graph as well as the red dots that show the actual computed values of the sinewave.

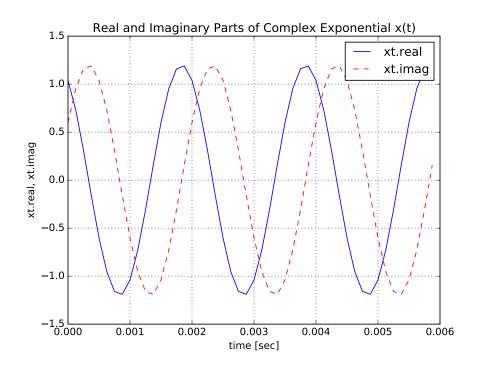
In communications we often work with complex-valued signals. Let's use Euler's relation

$$e^{j\alpha} = \cos \alpha + i \sin \alpha$$
,

to generate a complex exponential waveform in Python that contains both a cosine and a sine waveform.

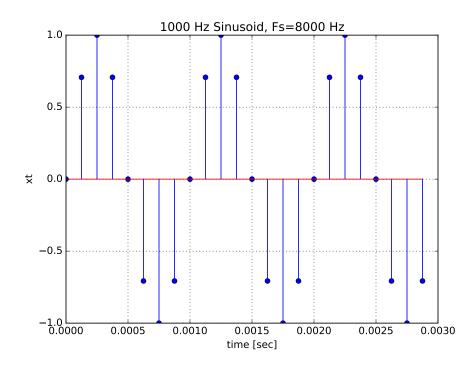
```
In [1]: from pylab import *
In [2]: Fs = 8000  # Sampling rate
In [3]: fm = 500 # Frequency
In [4]: phi = 30  # Angle in degrees
In [5]: A = 1.2  # Amplitude
In [6]: tlen = 1.0 # Duration in sec
In [7]: tt = arange(0,round(tlen*Fs))/float(Fs) # Time axis
In [8]: xt = A*exp(1j*(2*pi*fm*tt+pi/180*phi)) # Complex Exponential
In [9]: plot(tt[0:48],xt[0:48].real,'-b',label='xt.real')
Out[9]: [<matplotlib.lines.Line2D at 0x2556301f898>]
In [10]: plot(tt[0:48],xt[0:48].imag,'--r',label='xt.imag')
Out[10]: [<matplotlib.lines.Line2D at 0x25563026550>]
In [11]: grid()
In [12]: xlabel('time [sec]')
Out[12]: <matplotlib.text.Text at 0x25560981470>
In [13]: ylabel('xt.real, xt.imag')
Out[13]: <matplotlib.text.Text at 0x25562dadfd0>
In [14]: title('Real and Imaginary Parts of Complex Exponential x(t)')
Out[14]: <matplotlib.text.Text at 0x25562dc1b00>
In [15]: legend()
Out[15]: <matplotlib.legend.Legend at 0x255630376d8>
In [16]: show()
```

This produces the following graph:



You may have noticed that the 1000 Hz sinusoidal waveform we generated earlier doesn't look like a "nice" sinusoid because there are only 8 samples per period. A problem that often occurs in digital signal processing is that the sampling rate of a signal needs to be either increased or decreased. To see how this can be done in Python we will use the 1000 Hz sinusoidal signal and increase its sampling frequency from  $F_s = 8000$  Hz to  $3 F_s = F_{s3} = 24000$  Hz. The first step is to insert two zeros in-between any of the existing samples.

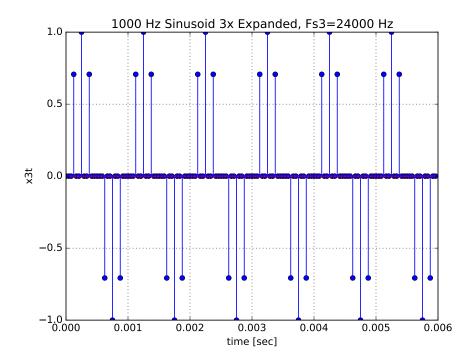
This produces a stem plot of the original sinewave.



To expand the signal xt 3-fold, insert two zeros after each sample by first constructing a 2-dimensional array whose first row is xt and whose remaining two rows are all zeros. Then reshape this array into a 1-dimensional vector, reading it out columns first (order='F' where F stands for Fortran).

```
In [7]: x3at = vstack([xt, zeros(len(xt)), zeros(len(xt))]) # Expand 3x
In [8]: x3t = reshape(x3at,x3at.size,order='F')
                                              # Reshape into vector
In [9]: print(x3t[0:24])
                       # Check readout order
[ 0.00000000e+00 0.0000000e+00 0.0000000e+00
                                                  7.07106781e-01
  0.0000000e+00 0.0000000e+00 1.0000000e+00
                                                  0.0000000e+00
  0.0000000e+00 7.07106781e-01 0.0000000e+00
                                                  0.0000000e+00
  0.00000000e+00 \qquad 0.00000000e+00 \quad -1.00000000e+00 \qquad 0.00000000e+00
  0.00000000e+00 -7.07106781e-01
                                  0.00000000e+00
                                                  0.0000000e+00]
In [10]: Fs3 = 3*Fs
                    # New sampling rate
In [11]: tt3 = arange(0,len(x3t))/float(Fs3)
                                           # New time axis for x3t
In [12]: stem(tt3[0:3*48],x3t[0:3*48]),grid()
Out[12]: (<Container object of 3 artists>, None)
In [13]: xlabel('time [sec]'),ylabel('x3t')
Out [13]:
(<matplotlib.text.Text at 0x276c1531128>,
<matplotlib.text.Text at 0x276c15397f0>)
In [14]: title('1000 Hz Sinusoid 3x Expanded, Fs3=24000 Hz')
Out[14]: <matplotlib.text.Text at 0x276c1694ba8>
In [15]: show()
```

Now the stem plot looks like this:



The next step is to interpolate between the nonzero samples in accordance with the assumption that the original signal is bandlimited to frequencies less than  $F_s/2$ . We will use a truncated sinc pulse for the interpolation, corresponding to a lowpass filter with cutoff frequency  $f_L$ . We will use the following function in the file  $sinc_ipol_py$  to generate the impulse response of the interpolation filter.

```
# File: sinc_ipol.py
# Sinc pulse for Interpolation
from pylab import *

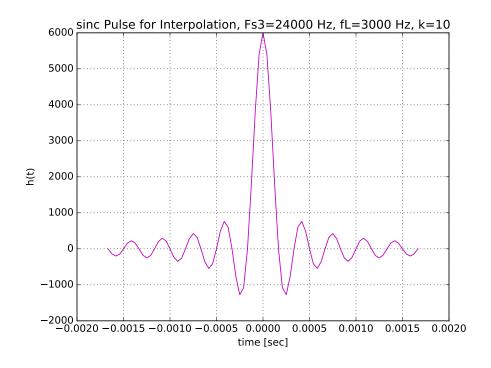
def sinc(Fs, fL, k):
    # Time axis
    ixk = int(round(Fs*k/float(2*fL)))
    tth = arange(-ixk,ixk+1)/float(Fs)

# Sinc pulse
    ht = 2.0*fL*ones(len(tth))
    ixh = where(tth != 0.0)[0]
    ht[ixh] = sin(2*pi*fL*tth[ixh])/(pi*tth[ixh])
    return tth,ht

if __name__ == '__main__':
    sinc()
```

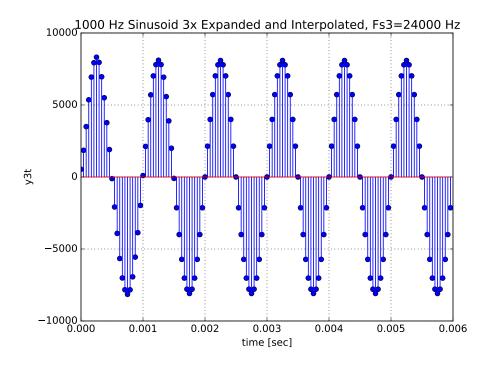
The commands below show how the interpolation filter is generated.

Here is what the sinc pulse looks like:



To obtain the interpolated sinewave it remains to convolve the sinc pulse with the expanded version x3t of the original sinewave.

Here is what the sinc pulse looks like:



## 1.9 CT and DT Signals in Digital Signal Processing

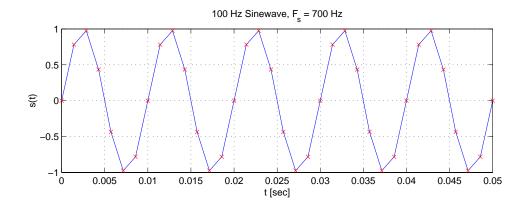
A continuous time (CT) signal or waveform s(t) is a signal whose amplitude is defined for any value of the time variable t. In a digital signal processing (DSP) environment, s(t) has to be represented by a discrete time (DT) signal or sequence  $s_n$  that is related to s(t) by

$$s_n = s(nT_s) = s(n/F_s) ,$$

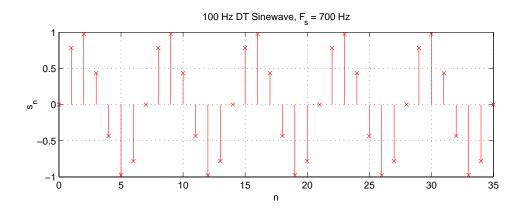
where  $F_s = 1/T_s$  is the sampling rate in Hz. As an example, consider the sinusoid

$$s(t) = \sin 2\pi f_0 t .$$

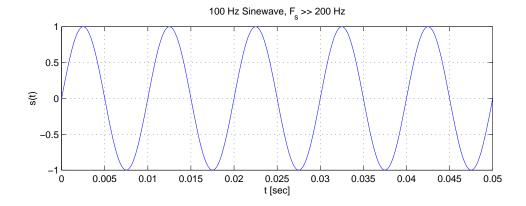
Setting  $f_0 = 100$  Hz and  $F_s = 700$  Hz and plotting  $s_n$  versus  $t = n T_s$  yields the following graph.



Even though the sampling theorem is not violated  $(F_s > 2f_0)$ , the plot (with straight lines between samples) is clearly not a very good approximation to s(t). In such a case it is actually better to just simply plot the DT signal  $s_n$  versus n in the form of a stem plot as shown in the next figure.



However, if  $F_s$  is chosen much larger than  $2f_0$ , then a plot of  $s_n$  versus  $t = n T_s$  is a very close approximation to plotting s(t) versus t, as can be easily seen in the graph below (which uses  $F_s = 5000$  Hz and does not explicitly show the sampling points).



In general, a signal vector  $\mathbf{s}$  in a DSP environment with bandlimitation to  $f_B$  Hz will be considered a DT signal  $s_n$  if the sampling rate  $F_s$  (in Hz) is not much higher than the Nyquist rate  $2f_B$ , and it will be considered (a good approximation to) a CT signal s(t) if  $F_s \gg 2f_B$ .

# 2 Lab Experiments

E1. Signals in Python. Assume that s(t) is a bandlimited CT signal that is to be represented in Python by a DT sequence  $s_n$  with sampling rate  $F_s = 1/T_s$ . According to the sampling theorem,  $F_s$  must be at least twice the highest frequency in s(t), but how should  $F_s$  be chosen so that a plot of  $s_n$  looks like s(t)? The goal of this experiment is to gain some intuitive experience for this question and at the same time practice some Python programming.

(a) Make a script file called sine100.py, using the following (numpy) Python commands:

This creates a discrete time axis tt of duration tlen with time instants spaced 1/Fs seconds apart. The last statement generates the signal st which is a 100 Hz sine, sampled with rate Fs. Plot st versus tt for Fs equal to 200, 400, 800, 1600, 3200, etc. What is the smallest Fs that yields a "nice" and representative graph of a 100 Hz CT sinusoid? Look at the sample graphs shown in the introduction.

(b) After generating the sine in st, use the command

```
rt = sign(st) # Sine -> rectangular
```

to generate a rectangular signal rt with frequency 100 Hz and sampling rate Fs. Note that sign stands for the signum function which is defined as

$$\operatorname{sgn}(x) = \begin{cases} +1, & x > 0, \\ 0, & x = 0, \\ -1, & x < 0. \end{cases}$$

Plot rt versus tt for Fs equal to 200, 400, 800, 1600, 3200, etc. What is the smallest Fs that yields a "nice" and representative graph of a 100 Hz rectangular CT signal?

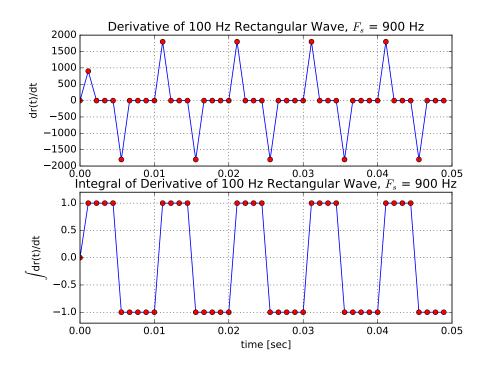
(c) DT approximations to CT signals in Python can be differentiated and integrated, which is often useful for the generation and anlysis of communication signals. Again, the goodness of the approximation of a CT signal by its sampled counterpart depends on the choice of the sampling frequency Fs. The following table shows the (numpy) Python commands for the DT approximations to differentiation and integration of a CT signal x(t).

Derivative and Integral of Signals						
	CT Signal $x(t)$	DT Signal x				
Derivative	$\frac{dx(t)}{dt}$	<pre>diff(hstack((0,x)))*Fs</pre>				
Integral	$\int dx(t)dt$	cumsum(x)/float(Fs)				

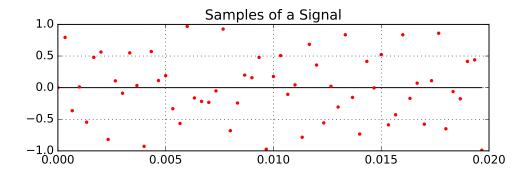
Note that since the sampling rate is Fs, "dt" is equal to Ts=1/Fs. Generate a rectangular 100 Hz signal in rt as in part (b) and then use the following commands to generate the "derivative" rdt of rt and the "integral" rdit of rdt which should be rt again.

```
rdt = diff(hstack((0,rt)))*Fs  # Derivative of rt
rdit = cumsum(rdt)/float(Fs)  # Integral of rdt
```

Make plots of rdt and rdit with Fs at the lower end of the useful range first so that you can see what diff and cumsum are doing. Then increase Fs until you obtain a plot that is a "nice" and representative approximation to differentiation and integration of CT signals. The following graphs show an example when Fs=900 Hz.



(d) The graph below shows the samples of a signal called sig01. This signal is available in sig01.wav. Use the wavread function in the Appendix to read the .wav file.



Make a plot of the "CT version" of sig01, assuming that sig01 is a baseband signal. Explain your approach and specify the parameters that you used.

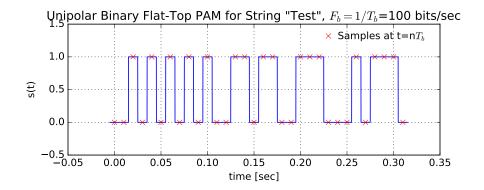
E2. Flat-Top PAM. (a) The goal of the first part of this experiment is to write a Python script file, e.g., called ftpam01.py, that accepts a text string as input and produces a flat-top PAM signal st as output. Here is an outline of ftpam01.py:

```
# File: ftpam01.py
# Script file that accepts an ASCII text string as input and
# produces a corresponding binary unipolar flat-top PAM signal
# s(t) with bit rate Fb and sampling rate Fs.
# The ASCII text string uses 8-bit encoding and LSB-first
# conversion to a bitstream dn. At every index value
# n=0,1,2,\ldots, dn is either 0 or 1. To convert dn to a
# flat-top PAM CT signal approximation s(t), the formula
   s(t) = dn, (n-1/2)*Tb \le t \le (n+1/2)*Tb,
# is used.
from pylab import *
import ascfun as af
Fs = 44100
                  # Sampling rate for s(t)
Fb = 100
                  # Bit rate for dn sequence
txt = 'Test'
                  # Input text string
                  # Number of bits
bits = 8
dn = # >> Convert txt to bitstream dn here <<
                  # Total number of bits
N = len(dn)
Tb = 1/float(Fb)
                            # Time per bit
                            # Left index for time axis
ixL = round(-0.5*Fs*Tb)
ixR = round((N-0.5)*Fs*Tb) # Right index for time axis
tt = arange(ixL,ixR)/float(Fs) # Time axis for s(t)
st = # >> Generate flat-top PAM signal s(t) here <<
```

Hints: The following Python module can be used to convert a text string in txt to ASCII using bits bits per character and then to a serial bitstream in dn (and vice versa).

```
# File: ascfun.py
# Functions for conversion between ASCII and bits
from pylab import *
def asc2bin(txt, bits=8):
    ASCII text to serial binary conversion
    >>>> dn = asc2bin(txt, bits) <<<<
                      input text string
    where txt
           abs(bits) bits per char, default=8
           bits > 0 LSB first parallel to serial
           bits < 0
                      MSB first parallel to serial
                      binary output sequence
           dn
    txtnum = array([ord(c) for c in txt])
                                            # int array
    if bits > 0:
                      # Neg powers of 2, increasing exp
          p2 = np.power(2.0, arange(0, -bits, -1))
    else:
                      # Neg powers of 2, decreasing exp
          p2 = np.power(2.0,1+arange(bits,0))
    B = array(mod(array(floor(outer(txtnum,p2)),int),2),int8)
                      # Rows of B are bits of chars
    dn = reshape(B,B.size)
                      # Serial binary output
    return dn
def bin2asc(dn, bits=8, flg=1):
    Serial binary to ASCII text conversion
    >>>> txt = bin2asc(dn, bits, flg) <<<<
    where dn
                      binary input sequence
           abs(bits) bits per char, default=8
           bits > 0 LSB first parallel to serial
           bits < 0
                      MSB first parallel to serial
           flg != 0
                      limit range to [0...127]
                      output text string
           txt
    11 11 11
    # >>Function to be completed in part (b) <<
```

To generate st from dn you might consider using the differentiation/integration technique from E1(c) by differentiating dn, placing the resulting impulses spaced apart by Tb at  $t = -T_b/2, T_b/2, 3T_b/2, 5T_b/2, \ldots$  in st and then integrating over st to obtain a rectangular flat-top PAM signal. The graph below shows st for the text string Test.



When you have completed the code in ftpam01 and you have verified that it works correctly, generate a known test signal, e.g., with txt='MyTest' and save the resulting signal st in a wav file using the commands (see the wavfun module in the Appendix)

```
import wavfun as wf
wf.wavwrite(0.999*st/float(max(abs(st))),Fs,'MyTest.wav') # Write wav-file
```

so that you can use it in the second part of the experiment. Note that the amplitude A of signals in wav-files is restricted to A < 1 and for this reason 0.999\*st/float(max(abs(st))) is written with the wavwrite command rather than just st.

(b) The goal of this part of the experiment is to take a received flat-top PAM signal rt of the kind generated in (a) and to convert it back to a text string. It is assumed that the received signal rt is available in the form of a wav file. Here is the starting point for a flat-top PAM receiver script file called ftpam\_rcvr01:

```
# File: ftpam_rcvr01.py
# Script file that accepts a binary unipolar flat-top PAM
# signal r(t) with bitrate Fb and sampling rate Fs as
# input and decodes it into a received text string.
# The PAM signal r(t) is received from a wav-file with
# sampling rate Fs. First r(t) is sampled at the right
# DT sequence sampling times, spaced Tb = 1/Fb apart. The
# result is then quantized to binary (0 or 1) to form the
# estimated received sequence dnhat which is subsequently
# converted to 8-bit ASCII text.
from pylab import *
import ascfun as af
import wavfun as wf
rt, Fs = wf.wavread('MyTest.wav')
Fb = 100
                              # Data bit rate
Tb = 1/float(Fb)
                              # Time per bit
bits = 8
                              # Number of bits/char
N = floor(len(rt)/float(Fs)/Tb) # Number of received bits
dnhat = # >> Sample and quantize the received PAM signal here <<
txthat = # >>Convert bitstream dnhat to received text string<<
print(txthat)
                              # Print result
```

**Note:** Because s(t) is obtained from  $d_n$  with bit rate  $F_b = 1/T_b$  by setting

$$s(t) = d_n$$
,  $(n - 1/2) T_b \le t < (n + 1/2) T_b$ ,

the first sample of the received signal in the wav file is at time  $t = -T_b/2$  and not at time t = 0. Also, the signal in a 16-bit wav file may be scaled because the amplitude A has to satisfy A < 1.

Test your receiver with the MyTest.wav file that you generated in (a). When you have verified that your receiver works properly, use it to receive the signal in ftpam\_sig01.wav and convert it back to a text string. The bit rate that was used for this signal is  $F_b = 100$ .

- (c) Use your ftpam\_rcvr01 receiver to receive the signals in ftpam\_sig02.wav and in ftpam\_sig03.wav and convert them back to text strings. The bit rate of the second signal in ftpam\_sig02.wav is unknown and you have to determine it from the signal itself. How difficult is it to find the bit rate and how crucial is it to have exactly the right value? The signal in ftpam\_sig03.wav uses a bit rate of  $F_b = 100$  and noise has been added to it. To record it as a wav file it had to be scaled to have a maximum amplitude less than 1 (including noise), so it is crucial that you use the right threshold at the receiver.
- E3. Pulse Code Modulation. (Experiment for ECEN 5002, optional for ECEN 4652) (a) Complete the following Python module with the mt2pcm and pcm2mt functions as described below:

```
# File: pcmfun.py
# Functions for conversion between m(t) and PCM representation
from pylab import *
def mt2pcm(mt, bits=8):
    Message signal m(t) to binary PCM conversion
    >>>> dn = mt2pcm(mt, bits) <<<<
                  normalized (A=1) "analog" message signal
    where
           \mathtt{mt}
           bits
                  number of bits used per sample
                  binary output sequence in sign-magnitude
           dn
                  form, MSB (sign) first
    # >>Your code goes here<<
def pcm2mt(dn, bits=8):
    Binary PCM to message signal m(t) conversion
    >>>> mt = pcm2mt(dn, bits) <<<<
                  binary output sequence in sign-magnitude
    where
           dn
                  form, MSB (sign) first
           bits
                  number of bits used per sample
                  normalized (A=1) "analog" message signal
    11 11 11
    # >>Your code goes here <<
```

The function mt2pcm is used to convert the (unquantized) samples of a message signal mt to a PCM bit string dn with bits bit quantization per sample. The function pcm2mt is used to convert the bit string dn back to "analog" samples. Test the two functions by using a sine signal for m(t) in mt2pcm, then feeding the resulting dn into pcm2mt and finally plotting this result together with the original m(t) in the same graph. Use a frequency of  $\approx 100$  Hz and a sampling rate in the range  $4000 \dots 8000$  Hz for the sine signal. Try 3-bit and 8-bit quantization.

(b) The signals in the files pcm\_sig01.wav and pcm\_sig02.wav are PCM signals with a bitrate of 64 kbit/sec, using 8-bit quantization, sign-magnitude format and MSB-first transmission. Flat-top PAM was used to convert the bit squences dn to a CT signal with amplitude zero for dn=0 and positive amplitude for dn=1. The first signal is noiseless and the second signal has noise added to it. Note that the noisy signal had to be scaled to have an amplitude less than 1. Demodulate the two signals and convert them back to "analog" message signals. Write the m(t) signals to a wav-file, listen to them in a sound player and describe their content. Use the PCM test signals in pcm\_test01.wav and pcm\_test02.wav to test your PCM receiver. The first test signal is a 3-bit (sign-magnitude, MSB first) PCM signal with bit rate  $F_b = 24000$  and the second test signal is a 8-bit (sign-magnitude, MSB first) PCM signal. The message signal m(t) is in both cases a sine with frequency f = 233.3 Hz.

# 3 Appendix

Python module wavfun for reading and writing n-channel 16-bit wav-files. Note that the amplitude A of signals recorded in wav-files is limited to A < 1 (A = 1 will create overflow and wrap around to A = -1).

```
# File: wavfun.py
# Functions for reading and writing wav files in Python
from pylab import *
import struct
import wave
def wavread(fname):
    fh = wave.open(fname, 'rb')
    (nchannels, sampwidth, framerate, nframes, comptype,
                compname) = fh.getparams()
    if sampwidth == 2:
        frames = fh.readframes(nframes * nchannels)
        dn = struct.unpack_from('%dh' % nframes*nchannels, frames)
        if nchannels > 1:
          out = array([dn[i::nchannels] for i in range(nchannels)])/float(2**15)
          out = array(dn)/float(2**15)
        print('not a 16 bit wav-file')
        out = [0]
    fh.close()
    return out, framerate
def wavwrite(data, framerate, fname):
    fh = wave.open(fname, 'wb')
    if len(data.shape) == 1:
          m = data.size
          n = 1;
    else:
        m, n = data.shape
        if m < n:
                                       # make column vectors
              data = data.transpose()
              m, n = data.shape
    dn = reshape(data,data.size) # interleave channels
    dn = around(dn*2**15).astype(dtype='int16')
    fh.setparams((n, 2, framerate, data.size, 'NONE', 'not compressed'))
    frames = struct.pack('h'*data.size, *dn)
    fh.writeframesraw(frames)
    fh.close()
```