

$$(a) \{a\} [a] \langle a \rangle |a| \|a\| \quad (1)$$

$$\left(\frac{a}{b}\right) \left\{\frac{a}{b}\right\} \left[\frac{a}{b}\right] \left\langle \frac{a}{b} \right\rangle \left|\frac{a}{b}\right| \left\| \frac{a}{b} \right\| \quad (2)$$

$$\left(\frac{a^2}{b}\right) \left\{\frac{a^2}{b}\right\} \left[\frac{a^2}{b}\right] \left\langle \frac{a^2}{b} \right\rangle \left|\frac{a^2}{b}\right| \left\| \frac{a^2}{b} \right\| \quad (3)$$

$$\left(\frac{a^2}{b^2}\right) \left\{\frac{a^2}{b^2}\right\} \left[\frac{a^2}{b^2}\right] \left\langle \frac{a^2}{b^2} \right\rangle \left|\frac{a^2}{b^2}\right| \left\| \frac{a^2}{b^2} \right\| \quad (4)$$

$$\left(\int \frac{a^2}{b^2}\right) \left\{\int \frac{a^2}{b^2}\right\} \left[\int \frac{a^2}{b^2}\right] \left\langle \int \frac{a^2}{b^2} \right\rangle \left|\int \frac{a^2}{b^2}\right| \left\| \int \frac{a^2}{b^2} \right\| \quad (5)$$

$$\left(\sqrt{\frac{a^2}{b^2}}\right) \left\{\sqrt{\frac{a^2}{b^2}}\right\} \left[\sqrt{\frac{a^2}{b^2}}\right] \left\langle \sqrt{\frac{a^2}{b^2}} \right\rangle \left|\sqrt{\frac{a^2}{b^2}}\right| \left\| \sqrt{\frac{a^2}{b^2}} \right\| \quad (6)$$

$$(1) \{1\} [1] \langle 1 \rangle |1| \|1\| \quad (7)$$

$$(1^2) \{1^2\} [1^2] \langle 1^2 \rangle |1^2| \|1^2\| \quad (8)$$

$$\left(\begin{array}{cc} 1 & 2 \\ 3 & 4 \end{array}\right) \left\{\begin{array}{cc} 1 & 2 \\ 3 & 4 \end{array}\right\} \left[\begin{array}{cc} 1 & 2 \\ 3 & 4 \end{array}\right] \left\langle \begin{array}{cc} 1 & 2 \\ 3 & 4 \end{array} \right\rangle \left|\begin{array}{cc} 1 & 2 \\ 3 & 4 \end{array}\right| \left\| \begin{array}{cc} 1 & 2 \\ 3 & 4 \end{array} \right\| \quad (9)$$

$$\left(\begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{array}\right) \left\{\begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{array}\right\} \left[\begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{array}\right] \left\langle \begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{array} \right\rangle \left|\begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{array}\right| \left\| \begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{array} \right\| \quad (10)$$

$$\left(\begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \\ 7 & 8 \end{array}\right) \left\{\begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \\ 7 & 8 \end{array}\right\} \left[\begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \\ 7 & 8 \end{array}\right] \left\langle \begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \\ 7 & 8 \end{array} \right\rangle \left|\begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \\ 7 & 8 \end{array}\right| \left\| \begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \\ 7 & 8 \end{array} \right\| \quad (11)$$

**Definition 1.** The Galilean group is defined as

$$\text{Gal}(3) = \left\{ \left[ \begin{array}{ccc} 1 & 0 & s \\ \mathbf{v} & R & \mathbf{y} \\ 0 & 0 & 1 \end{array} \right] \mid s \in \mathbb{R}, \mathbf{y}, \mathbf{v} \in \mathbb{R}^3, R \in O(3) \right\}$$

with a natural closed Lie subgroup structure of  $\text{GL}(5; \mathbb{R})$