

$$(a) \{a\} [a] \langle a \rangle |a| \|a\| \quad (1)$$

$$\left(\frac{a}{b}\right) \left\{ \frac{a}{b} \right\} \left[ \frac{a}{b} \right] \left\langle \frac{a}{b} \right\rangle \left| \frac{a}{b} \right| \left\| \frac{a}{b} \right\| \quad (2)$$

$$\left(\frac{a^2}{b}\right) \left\{ \frac{a^2}{b} \right\} \left[ \frac{a^2}{b} \right] \left\langle \frac{a^2}{b} \right\rangle \left| \frac{a^2}{b} \right| \left\| \frac{a^2}{b} \right\| \quad (3)$$

$$\left(\frac{a^2}{b^2}\right) \left\{ \frac{a^2}{b^2} \right\} \left[ \frac{a^2}{b^2} \right] \left\langle \frac{a^2}{b^2} \right\rangle \left| \frac{a^2}{b^2} \right| \left\| \frac{a^2}{b^2} \right\| \quad (4)$$

$$\left( \int \frac{a^2}{b^2} \right) \left\{ \int \frac{a^2}{b^2} \right\} \left[ \int \frac{a^2}{b^2} \right] \left\langle \int \frac{a^2}{b^2} \right\rangle \left| \int \frac{a^2}{b^2} \right| \left\| \int \frac{a^2}{b^2} \right\| \quad (5)$$

$$\left( \sqrt{\frac{a^2}{b^2}} \right) \left\{ \sqrt{\frac{a^2}{b^2}} \right\} \left[ \sqrt{\frac{a^2}{b^2}} \right] \left\langle \sqrt{\frac{a^2}{b^2}} \right\rangle \left| \sqrt{\frac{a^2}{b^2}} \right| \left\| \sqrt{\frac{a^2}{b^2}} \right\| \quad (6)$$

$$(\ 1 \ ) \{ \ 1 \ } [ \ 1 \ ] \langle \ 1 \ \rangle | \ 1 \ | \ \| \ 1 \ \| \quad (7)$$

$$(\ 1^2 \ ) \{ \ 1^2 \ } [ \ 1^2 \ ] \langle \ 1^2 \ \rangle | \ 1^2 \ | \ \| \ 1^2 \ \| \quad (8)$$

$$\left( \begin{array}{cc} 1 & 2 \\ 3 & 4 \end{array} \right) \left\{ \begin{array}{cc} 1 & 2 \\ 3 & 4 \end{array} \right\} \left[ \begin{array}{cc} 1 & 2 \\ 3 & 4 \end{array} \right] \left\langle \begin{array}{cc} 1 & 2 \\ 3 & 4 \end{array} \right\rangle \left| \begin{array}{cc} 1 & 2 \\ 3 & 4 \end{array} \right| \left\| \begin{array}{cc} 1 & 2 \\ 3 & 4 \end{array} \right\| \quad (9)$$

$$\left( \begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{array} \right) \left\{ \begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{array} \right\} \left[ \begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{array} \right] \left\langle \begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{array} \right\rangle \left| \begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{array} \right| \left\| \begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{array} \right\| \quad (10)$$

$$\left( \begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \\ 7 & 8 \end{array} \right) \left\{ \begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \\ 7 & 8 \end{array} \right\} \left[ \begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \\ 7 & 8 \end{array} \right] \left\langle \begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \\ 7 & 8 \end{array} \right\rangle \left| \begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \\ 7 & 8 \end{array} \right| \left\| \begin{array}{cc} 1 & 2 \\ 3 & 4 \\ 5 & 6 \\ 7 & 8 \end{array} \right\| \quad (11)$$

**Definition 1.** The Galilean group is defined as

$$\text{Gal}(3) = \left\{ \left[ \begin{array}{ccc} 1 & 0 & s \\ \mathbf{v} & R & \mathbf{y} \\ 0 & 0 & 1 \end{array} \right] \mid s \in \mathbb{R}, \mathbf{y}, \mathbf{v} \in \mathbb{R}^3, R \in O(3) \right\}$$

with a natural closed Lie subgroup structure of  $\text{GL}(5; \mathbb{R})$