Calculus 1 for Informaticians, Exam 2 Problem Set

Rules

You have to work alone, exchange of solutions are prohibited and easy to detect!

Do not use any kind of human or artificial intelligence, except your own!

You can use symbolic programs like Wolfram Alpha or Symbolab, however in the "problems to elaborate" parts you have to explain your solution as detailed, as it is needed; the more you detail your solution the higher it will be scored.

The exam lasts from Monday 10:00 to 12:00. After that, you should upload your work up to 12:10. **Do not break the rules!**

Make the following table on the top of the page. Fill it with the letter of the correct answer.

Name	Neptun code	1.	2.	3.	4.	5.	6.

Elaborate your detailed solution on at best 6 pages and upload them on the following site in pdf format, not larger than 10 MBs

https://forms.gle/Ws2eKgNpQKvd95u57

under the name

your name.pdf

Don't forget to hit Submit

In the four choice test part, you have to choose the one and only correct answer. Each one of the four choice test problems are scored 0 or 2 points. You don't have to explain your choice.

All the correct and full solutions of the problems to elaborate are scored at best 8 points.

Problem 1

PROBLEM TO ELABORATE – Determine q' and prove that q' is continuous at point a, where g is

$$g(x) = \begin{cases} \sqrt{x} \cdot \sin\left(\frac{1}{x}\right), & \text{if } x > 0\\ 0, & \text{if } x = 0 \end{cases}$$

FOUR CHOICE TEST – Consider the function g above (that is, exactly the g above)

Problem 2

PROBLEM TO ELABORATE – Determine the one-sided limits of the following function at points -1 and 1!

$$h(x) = \frac{x^2 + 1}{x^2 - 1}$$

FOUR CHOICE TEST – Classify the discontinuity of h at point 1.

Problem 3

PROBLEM TO ELABORATE – Compute the indefinite integral $\int (2x+1) \cdot \ln x \, dx$. FOUR CHOICE TEST – The improper integral of $f:(1,\infty)\to \mathbf{R}, x\mapsto \frac{1}{x^3}$

Problem 4

PROBLEM TO ELABORATE – Evaluate the following definite integral: $\int_{0}^{2} (2x+1)e^{-x} dx$ FOUR CHOICE TEST - Determine the location of the global minima of

$$f: \mathbf{R} \to \mathbf{R}; x \mapsto (x+1)e^x$$

Problem 5

PROBLEM TO ELABORATE – Compute the following limit $\lim_{n \to \infty} \left(\frac{n^2 - 1}{n^2 + 2} \right)^{n^2}$. FOUR CHOICE TEST – If $b_n > 0$ and $b_n \to 1$, then

- $\begin{array}{c|c} \hline A & \lim_{n \to \infty} (b_n)^8 = 0. & \hline B & \lim_{n \to \infty} (b_n)^8 = 1. \\ \hline C & b_n^n \text{ is unbounded.} & \hline D & b_n^n \text{ is monotone increasing.} \end{array}$

Problem 6

PROBLEM TO ELABORATE – Compute the following limit: $\lim_{n\to\infty} n \cdot \left(\sqrt{n^2+1} - \sqrt{n^2-1}\right)$ FOUR CHOICE TEST – The sequence $c_n = \left(1 - \frac{1}{4n}\right)^n$