

Exercise 2

Introduction to Complex Network Analysis

Melanija Kraljevska

17 October 2021

1

Edge list

Advantages:

Uses less memory for storing the graph. It is easy to iterate over all the edges.

Disadvantages:

It is hard to tell if an edge exists from A to B and to compute the degree of a node. It is usually not suitable for isolated nodes.

Adjacency matrix

Advantages:

We can check if two nodes have an edge in constant time. It is easier to compute the degrees of the nodes.

Disadvantages:

Large memory complexity. It has redundant information for undirected graphs.

2

If all of the 14 friends are also friends with each other, then this is the case of a complete graph - where between every pair of nodes there is an edge.

The number of edges can be calculated with the following formula: $N(N-1)/2$ where N is the number of nodes.

In this case, the number of nodes is $N = 15$ (me and my 14 friends), so the total number of edges is: $15*14 / 2 = 105$.

3

a) Adjacency matrix:

```

0,1,0,0,0,0,0,0,0
1,0,1,1,1,0,0,0,0
0,1,0,0,0,1,0,0,0
0,1,0,0,0,0,0,0,0
0,1,0,0,0,1,1,0,0
0,0,1,0,1,0,0,0,0
0,0,0,0,1,0,0,1,1
0,0,0,0,0,0,1,0,1
0,0,0,0,0,0,1,1,0
0,0,0,0,0,0,1,1,0
0,0,0,0,0,0,0,0,0

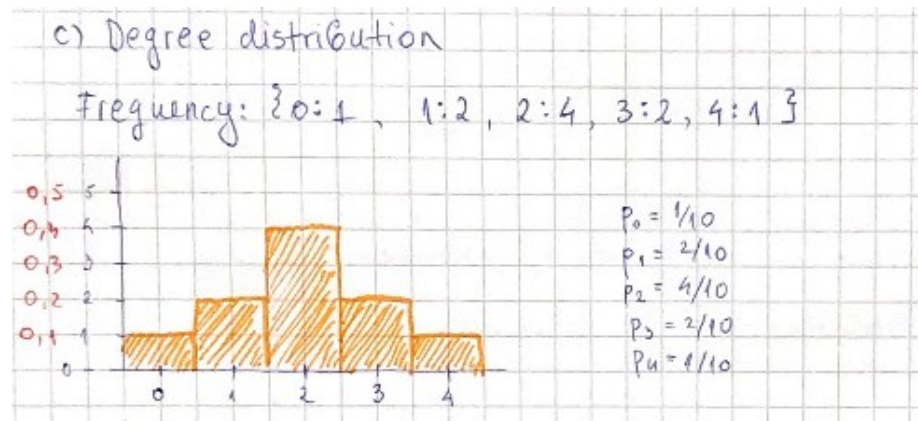
```

b) Edge list:

```

(1, 2)
(2, 3)
(2, 4)
(2, 5)
(3, 6)
(5, 6)
(5, 7)
(7, 8)
(7, 9)
(8, 9)

```



e) Number of $d=3$ paths between 2 and 3: 1

f) The node pair 1 and 6 has 2 $d=3$ paths (there are also more node pairs that satisfy this).

d)

Clustering coefficient

$$C_i = \frac{e_i}{[u_i(u_i-1)/2]}$$

$$C_1 = \frac{0}{[1(1-1)/2]} = 0 \quad C_5 = \frac{0}{[3(3-1)/2]} = 0 \quad C_9 = \frac{1}{[2(2-1)/2]} = 1$$

$$C_2 = \frac{0}{[4(4-1)/2]} = 0 \quad C_6 = \frac{0}{[2(2-1)/2]} = 0 \quad C_{10} = \frac{0}{[0(0-1)/2]} = 0$$

$$C_3 = \frac{0}{[2(2-1)/2]} = 0 \quad C_7 = \frac{1}{[3(3-1)/2]} = 1/3 \quad \langle C \rangle = \frac{1}{10} \left(\frac{1}{3} + 1 + 1 \right) =$$

$$C_4 = \frac{0}{[1(1-1)/2]} = 0 \quad C_8 = \frac{1}{[2(2-1)/2]} = 1 \quad = \frac{1}{10} \cdot \frac{7}{3} = 0,2333$$

Diameter

$d_{1,2} = 1$	$d_{2,3} = 1$	$d_{3,4} = 2$	$d_{4,5} = 2$	$d_{5,6} = 1$	$d_{6,7} = 2$	$d_{7,8} = 1$	$d_{8,9} = 1$
$d_{1,3} = 2$	$d_{2,4} = 1$	$d_{4,5} = 2$	$d_{5,6} = 3$	$d_{6,7} = 1$	$d_{7,8} = 3$	$d_{8,9} = 1$	
$d_{1,4} = 2$	$d_{2,5} = 1$	$d_{3,6} = 1$	$d_{4,7} = 3$	$d_{5,8} = 2$	$d_{6,9} = 3$		
$d_{1,5} = 2$	$d_{2,6} = 2$	$d_{3,7} = 3$	$d_{4,8} = 4$	$d_{5,9} = 2$			
$d_{1,6} = 3$	$d_{2,7} = 2$	$d_{3,8} = 4$	$d_{4,9} = 4$				
$d_{1,7} = 3$	$d_{2,8} = 3$	$d_{3,9} = 4$					
$d_{1,8} = 4$	$d_{2,9} = 3$						
$d_{1,9} = 4$							

diameter = 4

density:

$$D = \frac{2L}{N(N-1)} = \frac{2 \cdot 10}{10(10-1)} = \frac{2}{9} = 0,222$$

The computations by computer are made and presented in Tutorial2.

4

A bipartite network with N_1 and N_2 nodes in the two sets.

a) Maximum number of edges: $N_1 * N_2$.

b) The total number of edges in a nonbipartite graph is: $N(N-1)/2$, which is $(N_1 + N_2)(N_1 + N_2 - 1)/2$. The maximal number of edges in a bipartite graph is: $N_1 * N_2$, so the differences between these two numbers is: $(N_1^2 + N_2^2 - N_1 - N_2)/2$.