

# Assignment 4

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## Assignment #4

### Problem 1:

a)  $28 + 91$

28:

$$\begin{aligned} 28 \% 2 &= 14 \text{ r } 0 \\ 14 \% 2 &= 7 \text{ r } 0 \\ 7 \% 2 &= 3 \text{ r } 1 \\ 3 \% 2 &= 1 \text{ r } 1 \\ 1 \% 2 &= 0 \text{ r } 1 \end{aligned}$$

$$28 = 00011100$$

91:

$$\begin{aligned} 91 \% 2 &= 45 \text{ r } 1 \\ 45 \% 2 &= 22 \text{ r } 1 \\ 22 \% 2 &= 11 \text{ r } 0 \\ 11 \% 2 &= 5 \text{ r } 1 \\ 5 \% 2 &= 2 \text{ r } 1 \\ 2 \% 2 &= 1 \text{ r } 0 \\ 1 \% 2 &= 0 \text{ r } 1 \end{aligned}$$

$$91 = 01011011$$

$$01110111 \checkmark$$

$$= 119 \checkmark$$

$$\Rightarrow 00011100 \Rightarrow 28$$

$$\begin{array}{r} + 01011011 \Rightarrow 91 \\ \hline 01110111 \quad 119 \end{array}$$

b)  $102 + 75$

102:

$$\begin{aligned} 102 \% 2 &= 51 \text{ r } 0 \\ 51 \% 2 &= 25 \text{ r } 1 \\ 25 \% 2 &= 12 \text{ r } 1 \\ 12 \% 2 &= 6 \text{ r } 0 \\ 6 \% 2 &= 3 \text{ r } 0 \\ 3 \% 2 &= 1 \text{ r } 1 \\ 1 \% 2 &= 0 \text{ r } 1 \\ \Rightarrow 102 &= 01100110 \end{aligned}$$

-75: First, we will convert  $(+75)$  to binary.

$$\begin{aligned} 75 \% 2 &= 37 \text{ r } 1 \\ 37 \% 2 &= 18 \text{ r } 1 \\ 18 \% 2 &= 9 \text{ r } 0 \\ 9 \% 2 &= 4 \text{ r } 1 \\ 4 \% 2 &= 2 \text{ r } 0 \\ 2 \% 2 &= 1 \text{ r } 0 \\ 1 \% 2 &= 0 \text{ r } 1 \end{aligned}$$

$$01001011 = (+75)$$

$\rightarrow$  Flip and add 1:

$$10110101 = -75 \checkmark$$

$$\begin{array}{r} 0100110 \\ + 10110101 \\ \hline 10011011 \end{array}$$

$$\begin{array}{r} 10011011 \\ \hline \end{array}$$

$\Rightarrow$  overflow

8-bits.

c)  $12 \times -5$

12:

$12 \% 2 = 0$   
 $6 \% 2 = 0$   
 $3 \% 2 = 1$   
 $1 \% 2 = 1$

$\Rightarrow 12 = 00001100$

5:

$5 \% 2 = 2 \text{ r } 1$   
 $2 \% 2 = 1 \text{ r } 0$   
 $1 \% 2 = 0 \text{ r } 1$

$00000101 = 5$

$\Rightarrow -5 \Rightarrow 111101$

$12 \times -5$ : We know the answer is -60. So, first, we will do the operation  $12 \times 5$

$12 = 00001100$

$5 = 00000101$

$00001100$

$00000101$

$00001100$

$00000000$

$0000110000$

$0000000000$

$0000000000$

$0000000000$

$0000000000$

$0000000000$

$0000000000111100 = 60$

So, we get  $011100 = 60 \Rightarrow$  Change this to -60.

$1000011$  add 1.

$\Rightarrow 1000100 = -60$

12

$\frac{12}{-60}$

$\neq$

c)  $10 = 01010$

$240 = 0111000$

$01010 \mid 0111000$

$R = 0$

$01010 \downarrow$   
 $01010 \downarrow$   
 $01010 \downarrow$   
 $000000$

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## Problem 2:

(n=5)

$$A = -12$$

$$B = -10$$

A:

$$12 \div 2 = 6 \text{ r } 0 \rightarrow 01100 = (+12)_{10}$$

$$6 \div 2 = 3 \text{ r } 0$$

$$3 \div 2 = 1 \text{ r } 1$$

$$1 \div 2 = 0 \text{ r } 1$$

Flip  $\Rightarrow 10011$  add 1 to end

$$\Rightarrow 10100 = -12$$

B:

$$10 \div 2 = 5 \text{ r } 0 \rightarrow (+10)_{10} = 01010$$

$$5 \div 2 = 2 \text{ r } 1$$

$$2 \div 2 = 1 \text{ r } 0$$

$$1 \div 2 = 0 \text{ r } 1$$

$\Rightarrow$  Flip  $\Rightarrow 10101$

$$\text{add } 1 \Rightarrow 10110 \Rightarrow (-10)_{10}$$

a)  $A+B = (-12) + (-10)$

$$\Rightarrow 10100$$

$$+ 10110$$

$$\underline{101010}$$

b)  $A-B = (-12) - (-10)$

$$\Rightarrow 010100$$

$$- 10110$$

$$\underline{10000}$$

Need to borrow.

overflow or not?

-4



$$c) -A + B = -(-12) + (-10) \Rightarrow (-10) - (-12)$$

$$\begin{array}{r} 10110 \\ -10100 \\ \hline 00010 \end{array} \quad \checkmark \quad \begin{array}{r} -10 \\ +12 \\ \hline 2 \end{array} \quad \checkmark$$

$$d) -A + B = -(-12) - (-10) = 12 + 10$$

$$\begin{array}{r} 12 = 01100 \\ 10 = 01010 \end{array} \quad \Rightarrow \quad \begin{array}{r} 01100 \\ 01010 \\ \hline 10110 \end{array} \quad \begin{array}{r} 12 \\ +10 \\ \hline 22 \end{array}$$

#### Question 4:

- a) Arithmetic Shift: the bits that are shifted out of their ends are discarded.

Logical Shift: Zeros are shifted in to replace discarded bits

Rotational Shift: the bits are rotated as if the left and right ends of the register were joined.

- b) 1) Arithmetic shift left might cause an overflow.  
2) To Preserve MSB of a binary string.

-2

- c) Using arithmetic shift right for signed #'s.

ex:  $1000 = -8 \Rightarrow \text{shift right}$   
 $\Rightarrow 10100 = -12$   
↑  
must add

We must add a "1" in the MSB to keep the # a signed value (-). This results in a totally different value.