

Q1a)

		YZ			
WX		00	01	11	10
	00	1	1	1	X
	01	X	0	1	0
	11	0	1	X	0
	10	1	X	0	1

Essential prime implicants: $W'X'$, $X'Z'$

minterms 7 and 13 can be covered in multiple ways:

m7 can be covered using $W'YZ$ or XYZ

m13 can be covered using $WY'Z$ or WXZ

$$F1 = W'X' + X'Z' + W'YZ + WY'Z$$

Q1b)

		YZ			
WX		00	01	11	10
	00	1	1	1	X
	01	X	0	1	0
	11	0	1	X	0
	10	1	X	0	1

(selecting zeros) Essential Prime implicants: $(X'+Z)$, $(W+X'+Y)$

maxterm 11 can be covered in two ways: $(W'+Y'+Z')$ or $(W'+X+Z')$

$$F2 = (X'+Z)(W+X'+Y)(W'+X+Z')$$

$$F1 = \sum m(0,1,2,3,7,8,9,10,13) \neq F2 = \prod M(4,5,6,9,11,12,14) = \sum m(0,1,2,3,7,8,10,13,15)$$

It does not have to be equivalent due to different don't cares being used.

Q2.

	A	B	C	D	X	Y	Z
0	0	0	0	0	1	1	1
1	0	0	0	1	0	0	0
2	0	0	1	0	0	0	0
3	0	0	1	1	1	0	0
4	0	1	0	0	0	1	0
5	0	1	0	1	0	0	0
6	0	1	1	0	1	0	0
7	0	1	1	1	0	0	1
8	1	0	0	0	0	1	0
9	1	0	0	1	1	0	0
10	1	0	1	0	0	0	0
11	1	0	1	1	0	0	0
12	1	1	0	0	1	1	0
13	1	1	0	1	0	0	0
14	1	1	1	0	0	0	1
15	1	1	1	1	1	0	0

X CD

AB 00 01 11 10

00	1	0	1	0
01	0	0	0	1
11	1	0	1	0
10	0	1	0	0

$$\begin{aligned}
 X &= A'B'C'D' + A'B'CD + A'BCD' + ABC'D' + ABCD + AB'C'D \\
 &= A'B'(C \text{ XOR } D)' + BC(A \text{ XOR } D)' + AC'(B \text{ XOR } D)
 \end{aligned}$$

Y CD

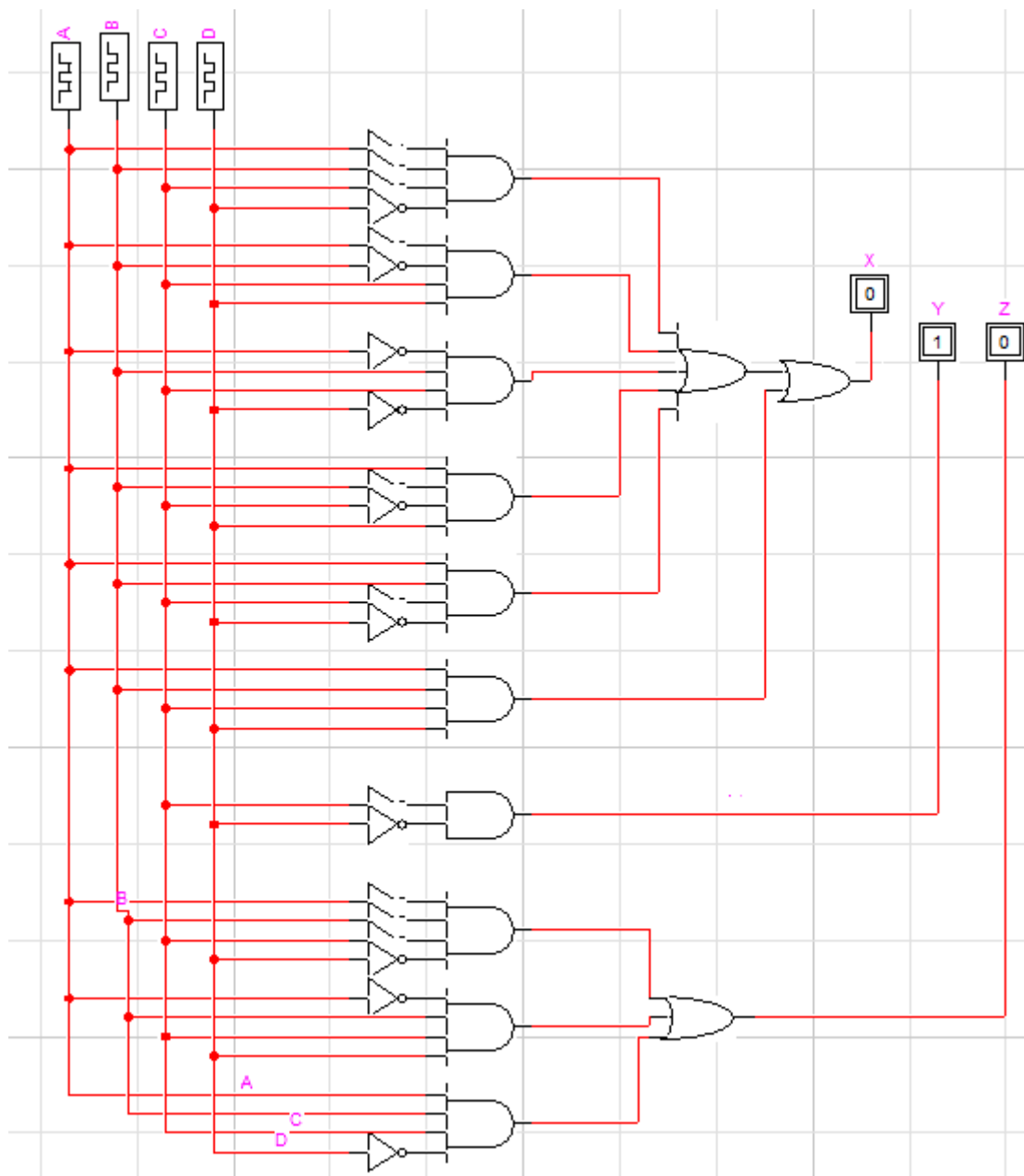
AB	00	01	11	10
00	1	0	0	0
01	1	0	0	0
11	1	0	0	0
10	1	0	0	0

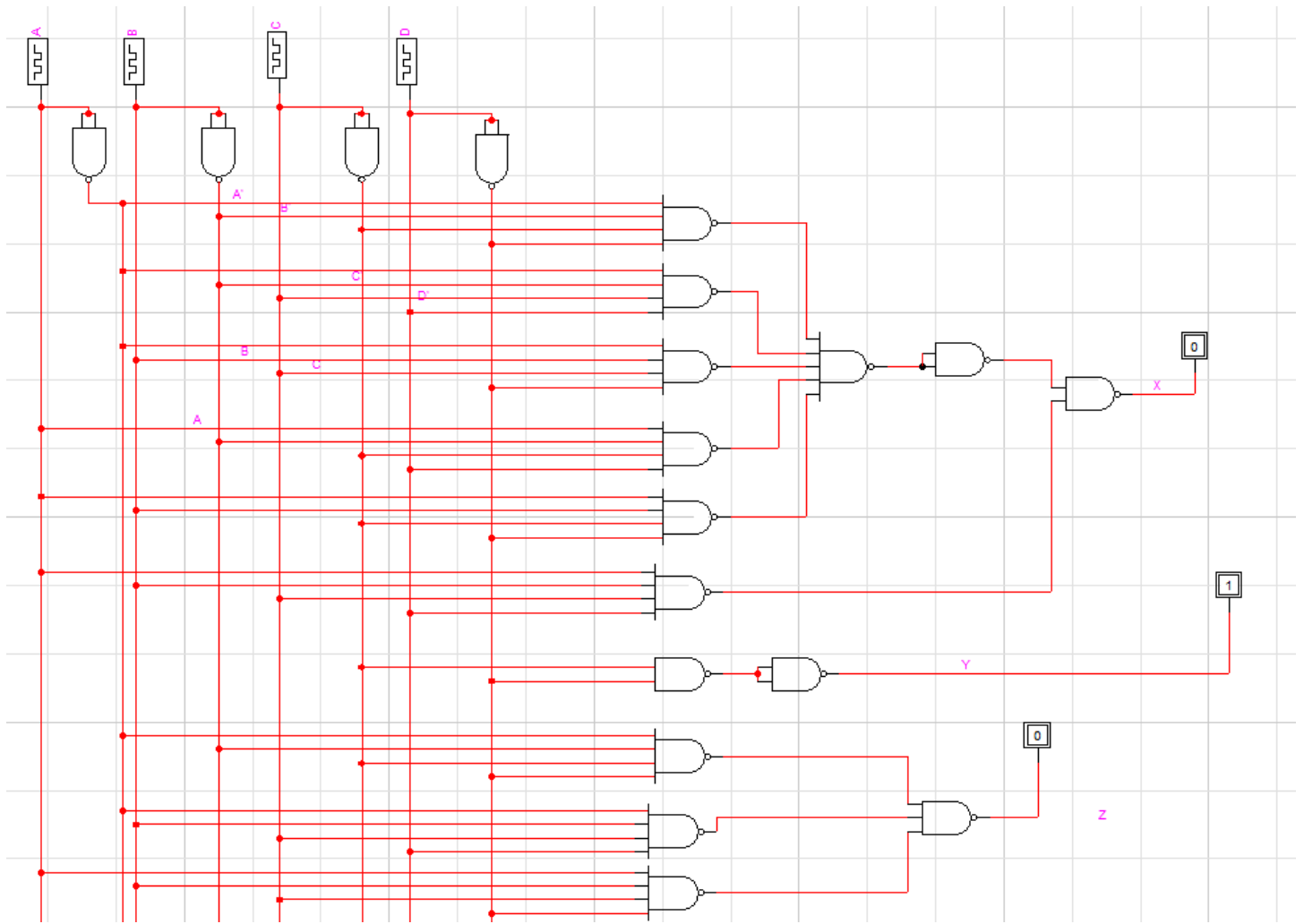
$$Y = C'D'$$

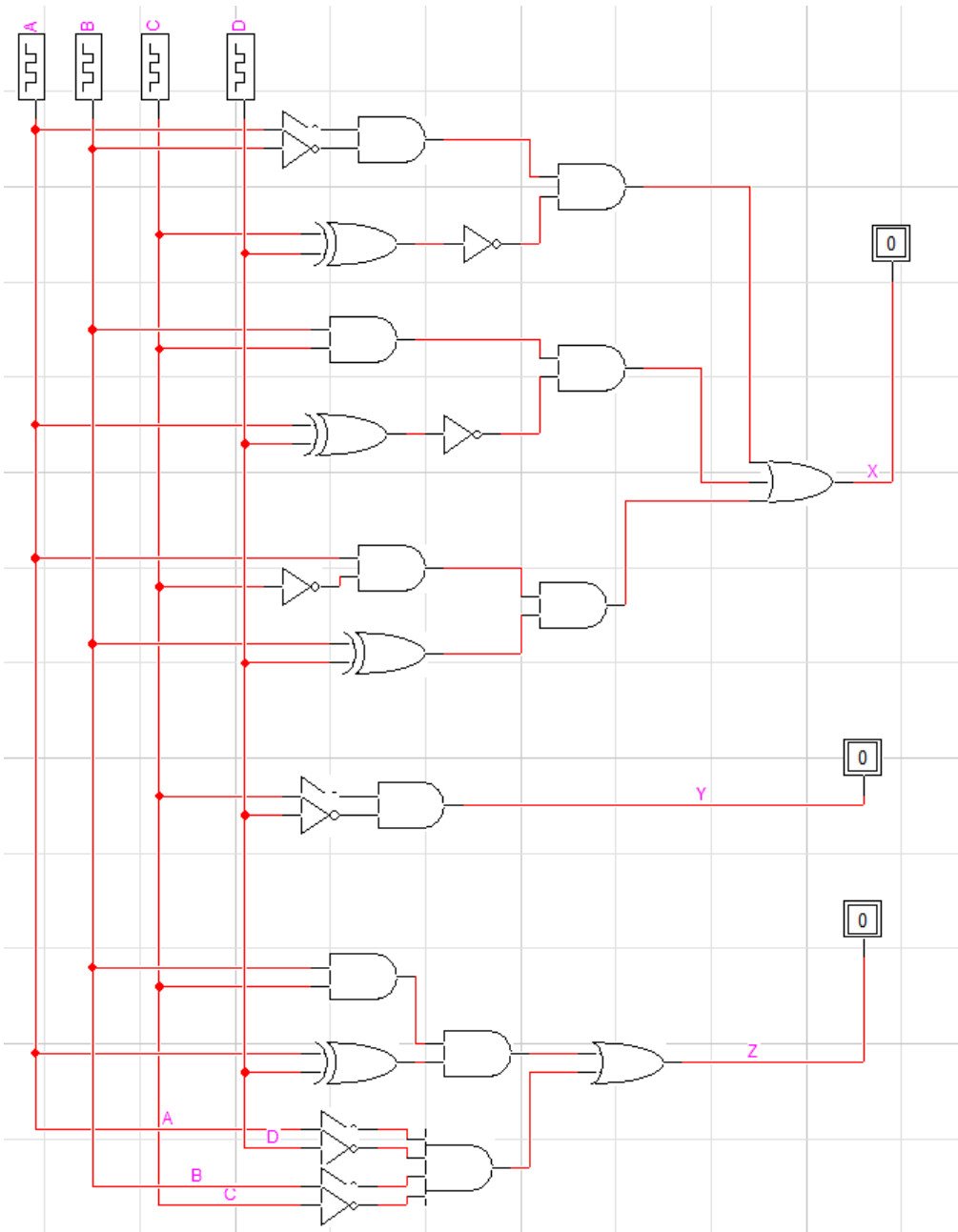
Z CD

AB	00	01	11	10
00	1	0	0	0
01	0	0	1	0
11	0	0	0	1
10	0	0	0	0

$$\begin{aligned} Z &= A'B'C'D' + A'BCD + ABCD' \\ &= BC(A \text{ XOR } D) + A'B'C'D' \end{aligned}$$







Q3

X	Y	Cin	Cout	S
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1

1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

When $X=0$

Let $Y=A$, $Cin=B$

$Cout = AB$ -----AND gate

When $X=1$

Let $Y=A$, $Cin=B$

$Cout = A+B$ -----OR gate

When $X=0, Y=1$ (Or $X=1, Y=0$)

Let $Cin = A$

$S = A'$ -----NOT gate

So a full adder can be a universal Device