

Connectivity matrix from a fODF weighted graph: An alternative to probabilistic tractography

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Synopsis

We introduce a computationally efficient fODF-weighted graph structure where shortest-paths through white matter compute the probability of connection while naturally limiting the angle of propagation between steps. Connectivity matrices obtained from this structure maintain many properties of probabilistic streamline count connectomes while avoiding the sampling bias of tractography.

Introduction

Probabilistic tractography¹ typically generates streamlines by taking steps and reselecting orientations based on the angle-of-arrival and the composition of the local fiber-ODF (fODF). These streamlines sample the paths through white matter between regions of interest (ROIs), e.g. cortex parcellation. However, this sampling process is highly inefficient, leaving most paths unvisited and lowering overall connectivity. An alternative approach entails creating a directed-graph where each voxel is a node connected to its neighbors with weights computed from the fODF and to compute shortest-paths between ROIs^{2,3,4,5}. In this work, we improve this idea by building a static graph structure that limits the propagation depending on the orientation of arrival in each voxel. We apply this approach to build a full brain connectome without bias from streamline sampling.

Methods

A standard fODF-weighted graph is computed from the probability of connection between each voxel and its 26 neighbors by projecting the fODF onto a set of directions uniformly spanning a sphere. We project vectors from the center of each neighbor on the sphere and assign each direction to the nearest. We apply a threshold on the fODF proportional to its maximum and normalize the remaining weights for each neighbor based on the previous association (fig.1). We build a directed-graph by creating a node for each voxel within the "tracking" mask (e.g. WM mask) and creating an edge to each neighbor with nonzero probability. The edge weight is chosen as $-\log(\mathbb{P})$ such that a path minimizing the sum of the weights maximizes the products of the probability. We add the ROIs as new nodes and connect them to all spatially relevant voxels. We use Dijkstra's algorithm⁶ to compute the shortest-path between pairs of ROI and build a connectivity matrix. The resulting probabilities represent the probability of a given path starting from a source ROI versus all other possible paths and we can compute the probability for any pair of nodes as long as there is no discontinuity in the graph. A problem with this approach, which limits the comparability with probabilistic tractography, is the lack of consistency in the choice of the orientation with respect to the angle-of-arrival^{4,5}. In tractography, it is common to define a cone around the orientation at each step and only consider the directions inside. To obtain an ideologically similar result while maintaining a static graph structure where Dijkstra's can be used, we introduce a new graph structure with multiple nodes for each voxel; one for each neighbor. As before, we compute the probability of connection between neighbors. However, for each voxel, we clip the probability of all directions outside of a cone centered around \vec{v}_i with half-angle θ where $\{\vec{v}_i\}_{i \in [0,25]}$ are the vectors projected from each neighbors' center, therefore each voxel has 26 different probability distributions toward its neighbors (fig.2). We create a directed-graph with 26 nodes for each voxel, representing all possible angles-of-arrival from the neighborhood, node (x, y, z, i) corresponds to voxel (x, y, z) with vector of arrival \vec{v}_i . All 26 nodes of each voxel have edges to the same 26 neighbors but with different probability distributions (fig.2). Computing the shortest path is performed identically in this oriented-graph but we have guarantees on the maximum "curvature" of the paths and the capacity to mitigate the impact of crossings on the final probabilities. Finally, alongside the path probabilities, we also compute the geometric mean of the steps' probability to obtain a metric insensitive to path length.

Results

We computed fODFs using MRTRIX⁷ on a 1.3mm isotropic ($b = 1000 \frac{s}{mm^2}$) dMRI dataset. We used a surface-based parcellation of 180 ROIs per hemisphere⁸, shifted into the WM, as connectivity targets (fig.3). We computed probabilistic tractography with step-size 0.5 voxel, angle-limit 45° , and interface seeding⁹. We build the oriented-graph using a 20% fODF threshold, and a cone of $\theta = 60^\circ$. The method is implemented¹⁰ using the igraph library¹¹. While not computing exactly the same thing, the connectivity weights show a good correlation with the streamline-counts, while also providing a value for all possible connections (fig.4A). Similarly to tractography, the path probabilities are inversely correlated with the length, since it is the product of step probability (fig.4B). However, looking at the geometric means of the probability, which account for the length, reveals a positive correlation (fig.4C). This may be explained if we consider that the majority of steps for longer paths follow very high probability, (i.e. high anisotropy) "main branches" of the WM. For illustration purposes, we projected the connectivity weights from the left PGi to all other parcels for streamline-count and for graph probability (fig.5). The graph weights are dominated by the distance to the seed area similar to the tractography case but extend many more orders of magnitude and cover the entire cortex including areas with very low connectivity.

Conclusion

Probabilistic tractography samples the space of fODF "weighted" paths through the WM to approximate the probability of connection. A more systematic approach is to build a graph that has comparable properties to the steps of tractography and compute geodesics through it. We showed a modification to the naive graph that can account for an important property of tractography. The constructed orientated-graph can produce shortest-paths connectome as an alternative to streamline-count which doesn't exhibit undersampling robustness problems.

Acknowledgements

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Figures

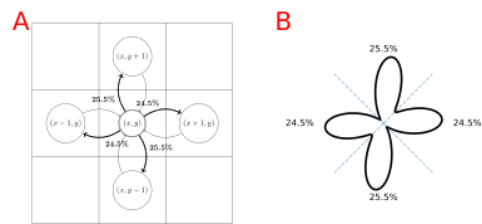


Figure 1: (A) Sketch representation of the naive graph in 2D with 4 neighbors. **(B)** Computing probability of each neighbor from the fODF. The renormalized density in each blue sector is attributed to the corresponding neighbor. Voxel (x,y) has directed edges to all its neighbors that have a nonzero probability. For the 3D case, a vector from the center of voxel (x,y,z) to each of its 26 neighbors is projected on the sphere and each discrete point on the sphere is attributed to the nearest.

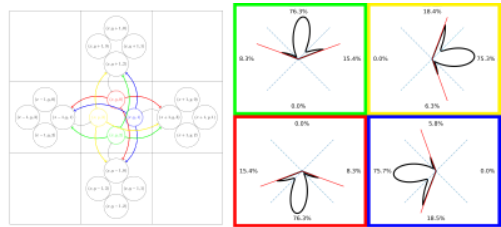


Figure 2: Sketch representation of the oriented-graph in 2D with 4 neighbors. Each voxel has a node for each neighbor, encoding different angle-of-arrival. The fODF at voxel (x,y) is clipped outside of a cone centered around the direction-of-arrival (*i.e.* which neighbor). The colors show the neighborhood probabilities re-weighted for the different orientations and the corresponding connections in the graph. All nodes of voxel (x,y) only connect to up to one node of each neighbor, depending on its relative position in space.

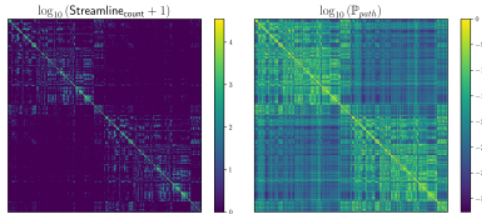


Figure 3: Connectivity matrices computed for 180 parcels per hemisphere⁸ on a 1.3mm isotropic dataset. **(left)** Streamline-count for probabilistic tractography seeded from the WM interface (~2M fibers). **(right)** Probability of shortest-path between each ROIs computed with oriented-graph. We note that the matrix is not symmetrical since the graph is directed, the rows correspond to the connectivity from sources to all targets. The matrices exhibit similar patterns, however, streamline-count fails to sample many connections, especially across hemispheres (off-diagonal block).

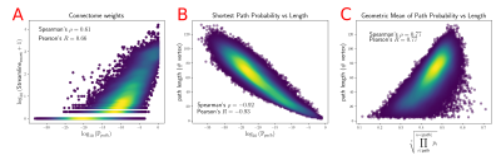


Figure 4: (A) Correlation between streamline-count and path probabilities. We see a large discrepancy in the "bottom lines" which correspond to undersampled or unvisited WM pathways (with only 0, 1, 2, ... streamlines). (B) Correlation between path probability and path length (number of nodes, not Euclidean). (C) Correlation between the geometric mean of the probability of each step and path length. The average probability of each step is higher in long connections, presumably because a higher portion of their total path follows high probability "WM main branches".

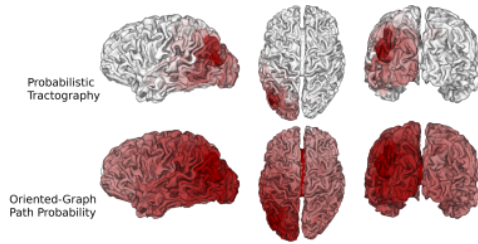


Figure 5: Connectivity weights for the Left PGi to all regions projected on WM surface. We show $\log_{10}(\text{Streamline}_{\text{count}} + 1)$ for probabilistic tractography and $\log_{10}(\mathbb{P}(\text{path}))$ for oriented-graph. Both metrics are influenced by distance from the seed region. However, tractography can't estimate the connection probabilities for the full cortex because of streamline sampling bias.