

CS 101: Computer Programming and Utilization

12-Functions

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Activity – Calculate GCD

Write a program to calculate the GCD of 2 numbers.

Use Euclid's Observation:

- If d divides m , n , then
 d divides $m - kn$, n , for all integers k .
- Euclid's observation can be repeatedly applied to reduce numbers whose GCD we want to find.

$$\text{GCD}(m, n) = \text{GCD}(m - kn, n)$$

Euclid's observation - example

$\text{GCD}(3977, 943)$

$= \text{GCD}(3034, 943)$

$= \text{GCD}(2091, 943)$

$= \text{GCD}(205, 943)$

$= \text{GCD}(205, 123)$

$= \text{GCD}(82, 123)$

$= \text{GCD}(82, 41)$

$= 41$

We can shorten this process:

$205 = 3977 \% 943$

$123 = 943 \% 205$

$82 = 205 \% 123$

$41 = 123 \% 82$

$0 = 82 \% 41$

Write a program to calculate the GCD of 2 numbers.

GCD program

```
int main() {  
    int Large, Small, Remainder;  
    cin >> Large >> Small;  
    while (true) {  
        Remainder = Large % Small;  
        if (Remainder == 0) break;  
        Large = Small;    //Note this step!  
        Small = Remainder;  
    } cout << "The GCD is: " << Small << endl;  
    return 0;  
}
```

Repeated calculation of GCD

If we have to evaluate GCD for values (x_1, y_1) at one place in our program and assign the result to z_1 , and evaluate GCD for values (x_2, y_2) at another place in our program and assign the results to z_2 .

One way of doing this is to repeat the GCD program code wherever required. → **Why is this a bad idea?**

It would be useful to write the code once and write statements like $z_1 = \text{gcd}(x_1, y_1)$ in the main program.

Functions

A mechanism to write instructions once and reuse them, is provided by most programming languages

- Called a function

A function accepts 'parameters', executes the 'body' (code) on the given parameters and returns the result.

A function can be invoked from within a program as many times as needed.

- Some functions that we have already used – `rand()`, `abs()`

Functions

- Single statement
- Statement block { ... }
- If-then-else
- While, for, break, continue
- Next device for writing modular, reusable code:

functions

- One declaration
- Many uses

Return
type

Formal
parameter

```
int abs(int a) {  
    return a > 0? a : -a;  
}
```

```
int x = -3, y = 5;  
int z = abs(x) - abs(y);  
int b = z*2;
```

“Argument”

A “call site”

Defining functions

return-type name-of-function(

The type of the value that will be returned by the function. gcd: int

parameter1-type parameter1-name,
parameter2-type parameter2-name,

...) {

function-body

}

variables for holding values of arguments.
gcd: Large, Small

Designer of the function decides the type of the corresponding arguments.
gcd: both arguments must be int.

- Definition must appear before use.

GCD function

```
int gcd (int Large, int Small) {  
    int Remainder;  
    while(true) {  
        Remainder = Large %  
        Small;  
        if (Remainder == 0) break;  
        Large = Small;  
        Small = Remainder;  
    }  
    return Small;  
}
```

// GCD must be defined or
declared before main()

```
int main () {  
    int x1, y1, z1, x2, y2, z2;  
    cin >> x1 >> y1;  
    z1 = gcd (x1, y1);  
    cin >> x2 >> y2;  
    z2 = gcd (x2, y2);  
    return 0;  
}
```

Function calls

Within a program, a function is invoked simply by using the function name within any expression, with appropriate parameters:

- Main program reaches the function call and suspends.
- Given parameters are copied to the respective locations in the function block.
- Function code is now executed.
- Result value is returned to the main (calling) program, which resumes from where it had suspended.

Difference between functions and threads?

Execution internals

- What happens when you run

```
main() {  
    int a = 3;  
    fun1(a);  
    cout << a;  
} ?
```
- Just before executing the implementation of fun1, the computer notes down in a special area of RAM what to do after fun1 returns
- fun1 may call fun2 may call fun3...

Recall: Program counter (PC)

- How does the CPU know what to do next?
- Assign **ID**s (e.g., 1—8 in the example)
- CPU has a register with the **ID** of the next statement to be executed
- Recall: PC keeps track of statements at the level of assembly instructions, not C++ statements

```
1. cin >> fah;  
2. v2 = fah - 32;  
3. v3 = v2 / 9;  
4. cen = v3 * 5;  
5. if (cen < 5) {  
6.     cout << "cold";  
7. }  
8. kel = cen + 273;
```

A key use of the PC is in implementing function calls

Memory segments

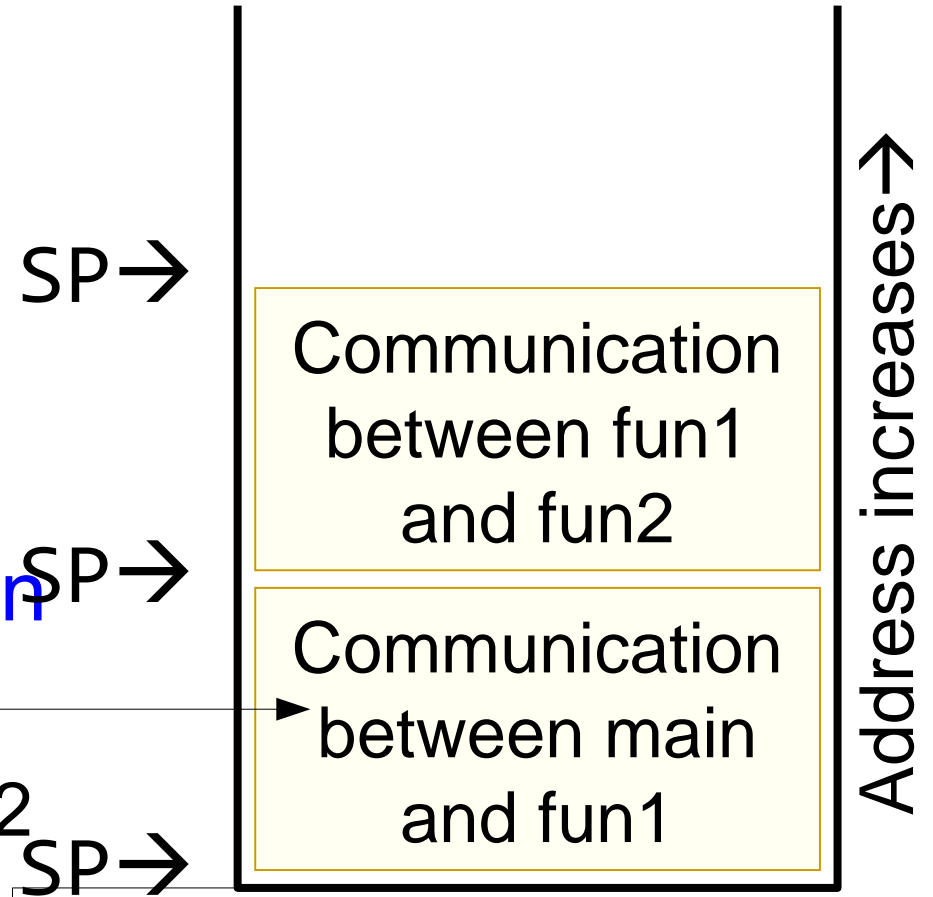
- A process is given three memory segments
- **Code segment**
 - Stores compiled executable code
 - Read-only once loaded
- **Data segment**
 - Storage for variables declared, string, vector<T>, matrix<T>, other data structures
 - Will discuss in more detail later
- **Stack segment:** memory used for
 - Communication between caller and callee
 - Keeping track of pending work

“Segmentation violation”

The stack pointer (SP)

- SP is a special register like PC
- Not directly accessible to the programmer
- Points to the “top” of the stack segment
- Each call has an **Activation Record**
- e.g., main calls fun1 calls fun2

Base of stack segment, say 4000



Variables and Arguments

New variables can be created in called function.

Set of variables in `main()` is completely disjoint from the set in called function, `gcd`.

- Both may contain same name, e.g. `Large`.
`main()` will reference the variables in its scope (activation), and `gcd` in its activation.
- Change in `Large` in `gcd` will not affect `Large` in `main`.

Arguments to calls can be expressions, which are first evaluated before called function executes.

Functions can be called while executing functions.

Passing parameters to functions

- Default is “pass by value”

```
void fun(int x) {
```

```
X = 5; } // void: does not return anything.
```

```
main() {
```

```
    int a = 3;
```

```
    fun(a);
```

```
    cout << a << endl;
```

```
}
```

- Value 3 copied from a to x
- x is locally modified
- Modification has no effect outside fun
- Even if the name 'x' in fun is changed to 'a'

Modifying variables outside function

- Use “pass by reference” instead

```
void fun(int& x) {
```

```
X = 5; } // void: does not return anything.
```

```
main() {  
    int a = 3;  
    fun(a);  
    cout << a;  
}
```

- No value copy
- x becomes an “alias” for a
- Modifying x amounts to modifying a
- Efficient, especially if large data structures are to be passed across functions

Arrays are passed by reference

```
void readarray (double*m, int n) {  
    for(int i=0; i<n; i++) cin >> m[i];  
}  
  
int main() { double marks[100];  
    readarray(marks,100);  
}
```

Array name is copied, so when corresponding parameter is used to access elements, elements of original array are accessed, and they can get modified.

For ordinary variables, value is copied, so corresponding parameter change does not affect the variable.

Function declarations

- If you declare first, then definitions can come later in any order.
- Useful if you like the main program to come first in the file. Sometimes easier to follow the logic.

`int gcd(int m, int n); // → Declaration; no body –`

`int lcm(int m, int n);`

`int main () { cout << lcm(24,36);}`

`int lcm(int m, int n){ ... } // → Definition; with body`

`int gcd(int m, int n){ ... }`

says what is the type of gcd:
The full definition will come later
possibly in another file.

Note the reuse of m and n!

A function to compute LCM, using GCD

```
int lcm(int m, int n) { return m*n/gcd(m,n); }
```

```
// must come after gcd definition
```

```
// but before main(), or wherever it is used.
```

```
void printlcm(int m, int n) {
```

```
    cout << lcm(m,n); return;
```

```
} // void: does not return anything.
```

```
int main () {int m, n; cin >> m >> n;
```

```
    printlcm(m,n); return 0;}
```

What is the execution sequence now?

Execution sequence

- `main()` executes. Suspends when call to `printlcm()` is encountered. AR of `main()` is put on the stack. Values of `m`, `n` from AR of `main` are copied into the parameters of `printlcm(m, n)`.
- `printlcm()` executes. Suspends when call to `lcm()` encountered. AR of `printlcm()` put on stack. Values copied for call.
- `lcm()` executes. Suspends when call to `gcd()` encountered. AR of `lcm()` put on stack. Values copied.
- `gcd()` executes and completes. Result is copied from AR of `gcd()` to AR of `lcm()`. AR of `gcd()` deleted. AR of `lcm()` taken from stack. Control returns to `lcm()`.
- `lcm()` resumes and completes. Control returns to `printlcm()`, which completes and control returns to `main()`.

Separate compilation units

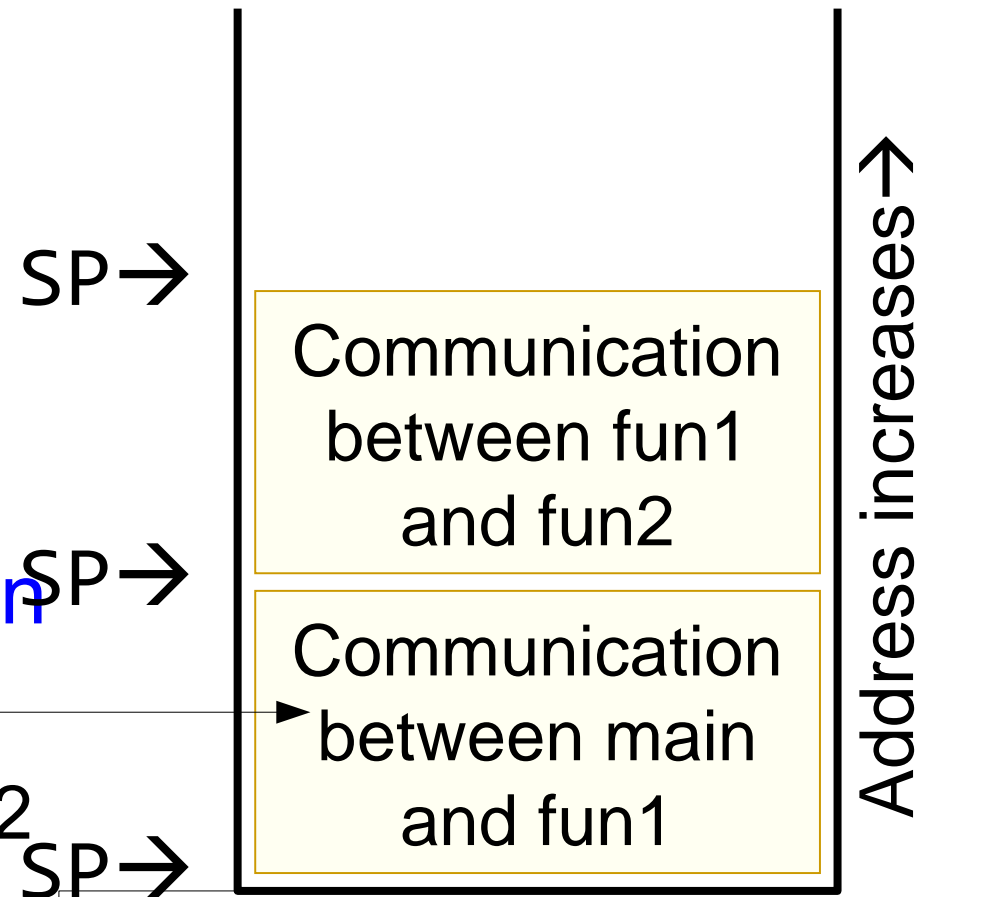
- Thus far, we have placed all our code in one C++ source file.
- Can't share functions from many projects.
- Change one line, compile everything again.
- Solution: The **-c** and **-o** flags to g++
 - Example: Suppose we write the gcd function definition in gcd.cpp and the main program in main.cpp
 - g++ main.cpp gcd.cpp → will produce a.out
 - g++ -c gcd.cpp → will produce gcd.o file
 - g++ -o gcd.o main.o → will produce a.out

Extra Notes (Optional Reading)

Function call internals

- SP is a special register like PC
- Not directly accessible to the programmer
- Points to the “top” of the stack segment
- Each call has an **Activation Record**
- e.g., main calls fun1 calls fun2

Base of stack segment, say 4000



Design of the callee

High-level function
implementation

```
int abs(int a) {  
    return a > 0? a : -a;  
}
```

in Value of a on entry

out Space to write return value

todo Code address to jump to on return

Activation Record

Compiled low-
level code

abs=2000

a=**stack.top.in**

2001

if a > 0 go to 2003

2002

a = -a

2003

stack.top.out = a

2004

go to **stack.top.todo**

Design of the caller

main=1000

x=-3

1001

y=5

1002

push activation record on stack

1003

stack.top.in = x, stack.top.todo=**1005**

1004

go to abs = **2000**

1005

R1 = stack.top.out

1006

pop activation record from stack

1007

push activation record on stack

1008

stack.top.in = y, stack.top.todo=**1010**

1009

go to abs = **2000**

1010

R2 = stack.top.out

1011

pop activation record from stack

1012

z = R1 - R2

1013

b = z * 2

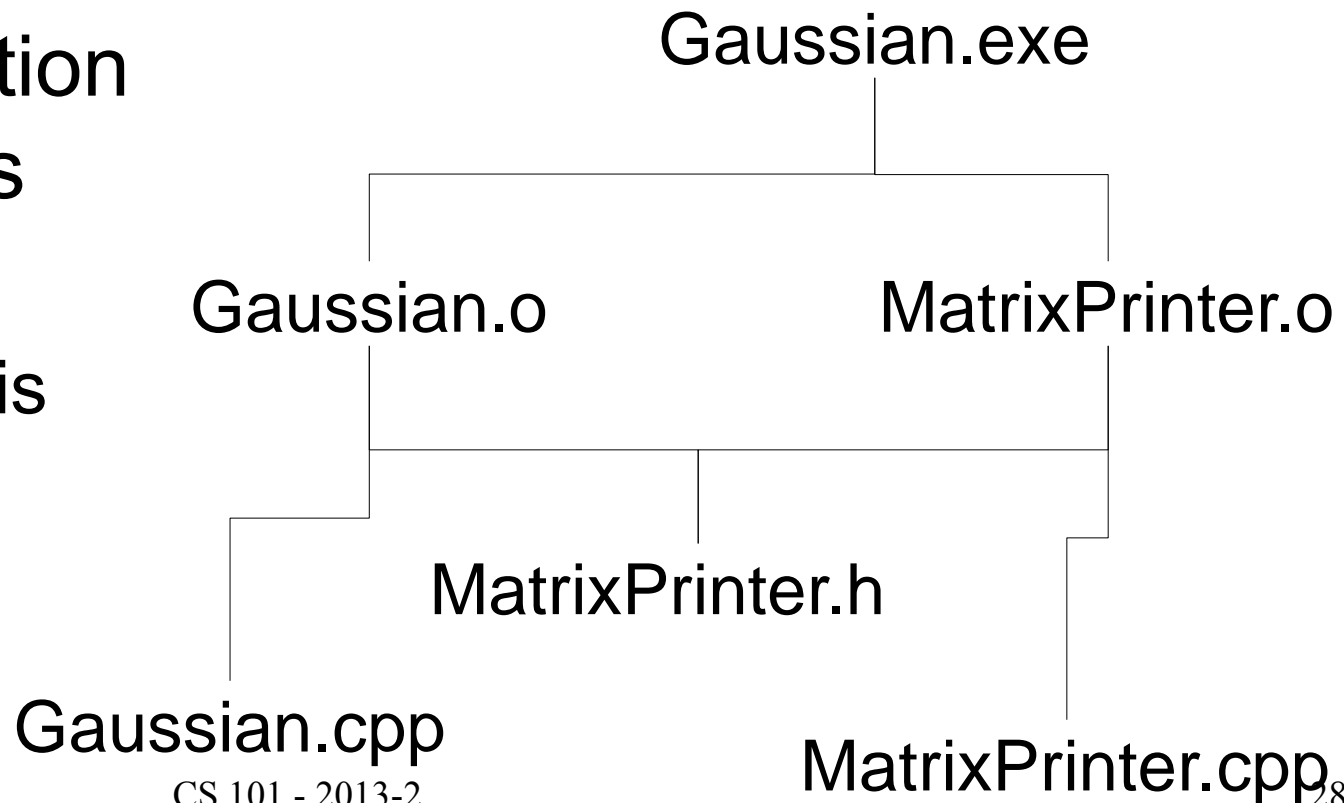
```
main() {  
    int x = -3, y = 5;  
    int z = abs(x) - abs(y);  
    int b = z*2;  
}
```

Saving register values

- Suspend caller, execute callee, resume caller
- CPU has a fixed, small set of registers
- Callee must restore registers to values in caller just before callee was invoked
- Also allocate space in activation record to save registers before call
- After call, copy values back to registers before resuming caller
- Overheads of function calls

Compiling multiple files using “make”

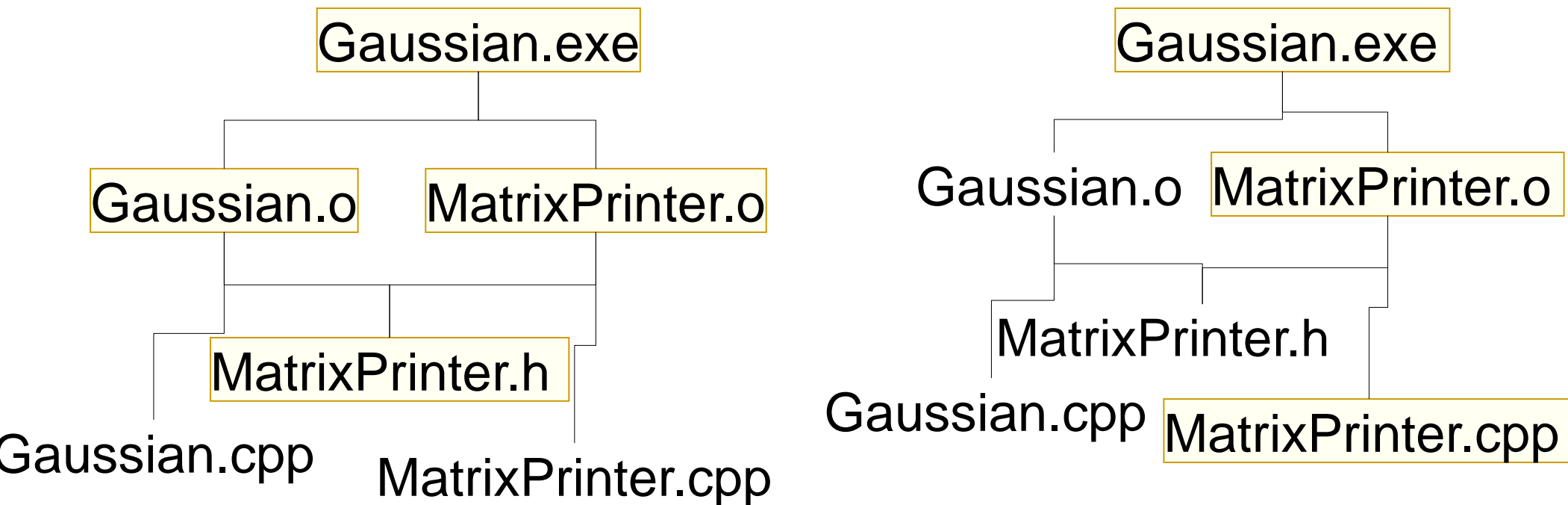
- When we change one file in a large project, which files need to be compiled again?
- (File) system provides no consistency check between x.cpp and x.o and a.out
- A *makefile* gives a formal specification of dependencies
- Example:
 - MatrixPrinter.h is used with both cpp files



Makefile

- The make program looks for a file called Makefile or makefile
- A makefile consists of **rules** and **actions**
- A rule has the form
target: dependencyList
- An action is a program to run, with command-line arguments
- If any file on the dependency list is newer than the target, (re) run the action
 - Check out the “Build” button in Geany

Make schedules “wavefront” of updates



If `MatrixPrinter.h` is updated, then the dependent files – `Gaussian.o`, `MatrixPrinter.o` and `a.out` are also re-created.
If `MatrixPrinter.cpp` is updated, then only `MatrixPrinter.o` and `a.out` are re-created.