

Proving theorems in Lean

Matej Penciak

Northeastern University

February 18, 2022

Slides available at:

<https://github.com/mpenciak/Lean-Seminar-Sp2022>

Plan for today, and glimpses at the future

- ▶ A review of the tactics from the Natural Number Game

Comments, imports, and namespaces

```
-- single line
/-
    comment
-/

import lean.module

namespace name_space

open other_name_space

end name_space
```

Definitions, lemmas, theorems, and their proofs

```
def definition_name (assumptions : their_types)
  : type_of_output := sorry

lemma lemma_name {implicit : assumptions}
  : lemma_type :=
begin
  sorry
end

theorem theorem_name (
  same : stuff
)
:
usually_Prop
:=
by sorry
```

sections, variables, examples, constants, #check

```
section section_name  
variables (var1 : type)  
end
```

```
example (no : name) : any_type : =  
begin  
  sorry  
end
```

```
constants (G : Type) (a : G) (b : G)  
variable [group G]  
#check a * b
```

Attributes, lemma names, calc mode, term proofs, ...

```
variables (a b c : nat)

@[simp, to_additive]
lemma mul_right_eq_self : a * b = a  $\leftrightarrow$  b = 1 :=
calc a * b = a  $\leftrightarrow$  a * b = a * 1 : by rw mul_one
...            $\leftrightarrow$  b = 1           : mul_left_cancel_iff
```

Structures, classes, inductive data types, instances

```
structure structure_name :=  
  (constructor1 : constructor_type)  
  (constructor2 : constructor_type)  
  (constructor3 : constructor_type)  
  
class class_name (any : hypotheses)  
  extends other_class :=  
    (constructor1 : constructor_type)  
  
inductive inductive_name : its_type  
| cons1 : type1  
| cons1 : type2  
  
instance : class_name := sorry
```

Lots of other stuff!

```
universes univ1 univ2

variables (typeDependingOnAUniv : Type univ1)

noncomputable theory

section

local attribute [simp] add_assoc

end
```


Available resources

Lots of resources with links in the demo3.lean file!