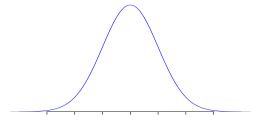
## Worksheet: The Central Limit Theorem for Sample Means

## The Central Limit Theorem for Sample Means

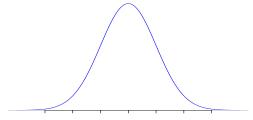
When we collect a sufficiently large sample of n independent observations from a population with mean  $\mu$  and standard deviation  $\sigma$ , the sampling distribution of  $\overline{x}$  will be nearly normal with

Mean = 
$$\mu$$
 and Standard Error (SE) =  $\frac{\sigma}{\sqrt{n}}$ .

- 1. The actual weight of a certain candy bar, whose advertised weight is 2 ounces, varies according to a normal distribution with mean  $\mu = 2$  ounces and standard deviation  $\sigma = 0.04$  ounces.
  - (a) Label the tick marks on the bell curve below so that it represents the distribution of weights of this type of candy bar.



- (b) What is the probability that an individual candy bar will weigh between 1.98 and 2.02 oz? Sketch the probability of interest as an area in the density curve above, convert the question to z-scores, and use a table or R to find your answer.
- (c) Suppose you plan to gather a simple random sample of 9 candy bars and calculate the sample mean weight,  $\bar{x}$ . What does the Central Limit Theorem say about the sampling distribution for  $\bar{x}$ ? Label the tick marks on the bell curve below to represent the sampling distribution of  $\bar{x}$  in this problem.



(d) Shade in the region on the bell curve above that corresponds to the probability that the sample mean weight of these nine candy bars will fall between 1.98 and 2.02 ounces. Determine this probability by converting to z-scores and using R.

