



FOL Evaluator

The FOL Evaluator is a semantic calculator which will evaluate a well-formed formula of first-order logic on a user-specified model. In its output, the program provides a description of the entire evaluation process used to determine the formula's truth value. For a list of the symbols the program recognizes and some examples of well-formed formulas involving those symbols, see below. Click the "Sample Model" button for an example of the syntax to use when you specify your own model.

Enter a Model:

Domain	1,2,3
P	1,2
Q	(1,1),(3,1),(3,2),(2,3)

+

Loaded Model

Domain: [1,2,3]
 Q: [(1,1),(3,1),(3,2),(2,3)]
 P: [1,2]

Enter a Formula:

(AzPzvAyEx(Qxy&Py)) is false on this model

Evaluation History:

```

(AzPzvAyEx(Qxy&Py)) is false on {}
  AzPz is false on {}
    Pz is true on {"z":1}
    Pz is true on {"z":2}
    Pz is false on {"z":3}
  AyEx(Qxy&Py) is false on {}
    Ex(Qxy&Py) is true on {"y":1}
      (Qxy&Py) is true on {"y":1,"x":1}
        Qxy is true on {"y":1,"x":1}
        Py is true on {"y":1,"x":1}
      (Qxy&Py) is false on {"y":1,"x":2}
        Qxy is false on {"y":1,"x":2}
        Py is true on {"y":1,"x":2}
      (Qxy&Py) is true on {"y":1,"x":3}
        Qxy is true on {"y":1,"x":3}
        Py is true on {"y":1,"x":3}
    Ex(Qxy&Py) is true on {"y":2}
      (Qxy&Py) is false on {"y":2,"x":1}
        Qxy is false on {"y":2,"x":1}
        Py is true on {"y":2,"x":1}
      (Qxy&Py) is false on {"y":2,"x":2}
        Qxy is false on {"y":2,"x":2}
        Py is true on {"y":2,"x":2}
      (Qxy&Py) is true on {"y":2,"x":3}
        Qxy is true on {"y":2,"x":3}
        Py is true on {"y":2,"x":3}
    Ex(Qxy&Py) is false on {"y":3}
      (Qxy&Py) is false on {"y":3,"x":1}
        Qxy is false on {"y":3,"x":1}
        Py is false on {"y":3,"x":1}
  
```

```
(Qxy&Py) is false on {"y":3,"x":2}
  Qxy is true on {"y":3,"x":2}
  Py is false on {"y":3,"x":2}
(Qxy&Py) is false on {"y":3,"x":3}
  Qxy is false on {"y":3,"x":3}
  Py is false on {"y":3,"x":3}
```

Here is a list of the symbols the program recognizes (note that since the letter 'v' is used for disjunction, it cannot be used as a variable or individual constant):

Logical Symbols

Negation	~
Conjunction	&
Disjunction	∨
Conditional	>
Biconditional	<>
Existential Quantifier	∃
Universal Quantifier	∀
Identity Relation	=
Absurdity/Falsum	#

Non-Logical Symbols

Individual Constants	a, b, c ... z (except v)
Variables	a, b, c ... z (except v)
Propositional Constants	A, B, C, ... Z
1- and 2-Place Predicates	A, B, C, ... Z

Here are some examples of well-formed formulas the program will accept:

```
Fa > ~Raa
ExRxa
ExAy(Rxy <> Ryx)
Ax(Fx > EyRxy) & EzRaz
AxExy=x
AxAy(x=y > (Fx > Fy))
Ex(P > Fx) > (P > ExFx)
```

If you load the "sample model" above, these formulas will all successfully evaluate in that model. In general, in order for a formula to be evaluable in a model, the model needs to assign an extension to every non-logical constant the formula contains.

Notice that only binary connectives introduce parentheses, whereas quantifiers don't, so e.g. 'ExRxa' and 'Ex(Rxa & Fx)' are well-formed but 'Ex(Rxa)' is not. In the above examples, I've left off the outermost parentheses on formulas that have a binary connective as their main connective (which the program allows). In general, the formal grammar that the program implements for complex wffs is:

$$\varphi := \sim\varphi \mid (\varphi \ \& \ \varphi) \mid (\varphi \ \vee \ \varphi) \mid (\varphi \ > \ \varphi) \mid (\varphi \ <> \ \varphi) \mid \exists v\varphi \mid \forall v\varphi \mid$$

One final point: if you load a model that assigns an empty extension to a predicate, the program has no way of anticipating whether you intend to use that predicate as a 1-place predicate or a 2-place predicate. Internally it therefore adds two versions of the predicate to the model, a 1-place version and a 2-place version, each with an empty extension. (Extensions for sentences and individual constants can't be empty, and neither can domains.)