

# Non-Parametric Path Based Model for Taxonomy Induction in Knowledge Graphs

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# Knowledge Graphs

- Triples are how data is stored in a knowledge graph
  - Links a subject (head) to and object (tail) via a predicate

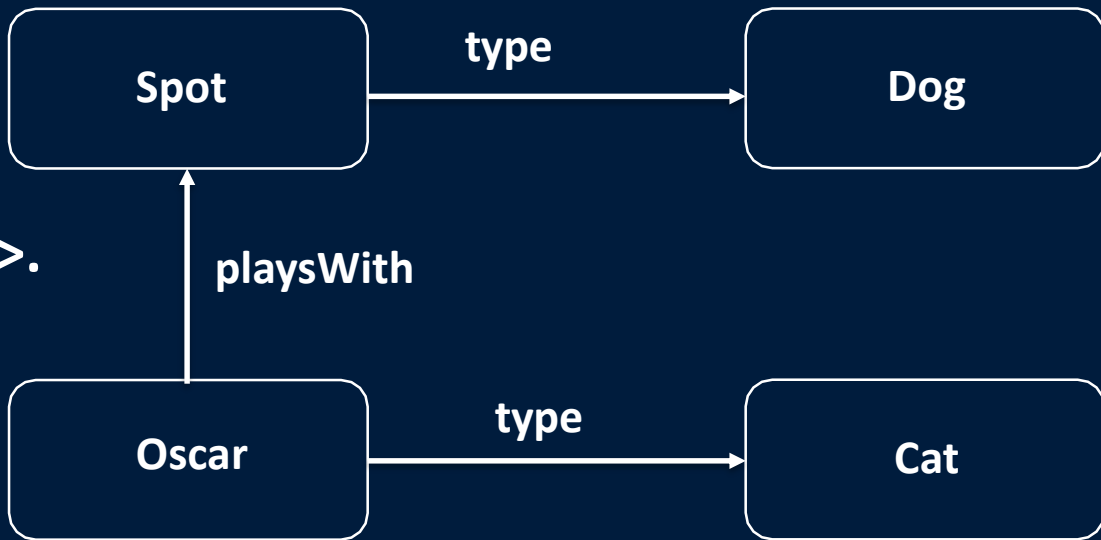
**<Oscar> <type> <Cat>.**



# Knowledge Graphs

- Put triples together and you get a knowledge graph

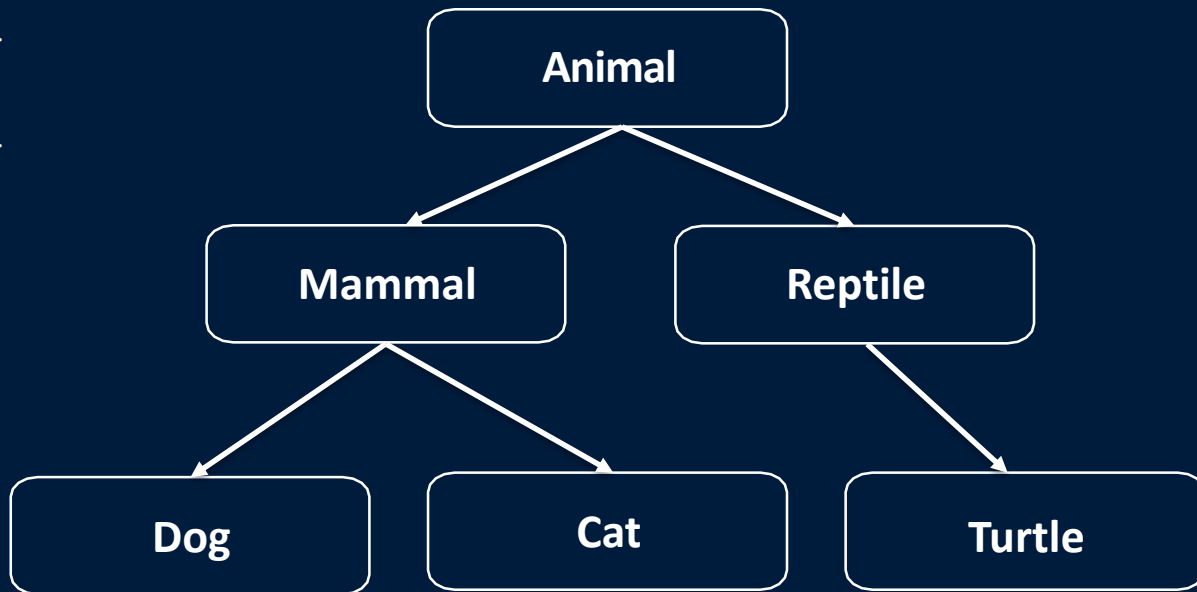
`<Spot> <type> <Dog>.`  
`<Oscar> <playsWith> <Spot>.`  
`<Oscar> <type> <Cat>.`



# Class Taxonomies

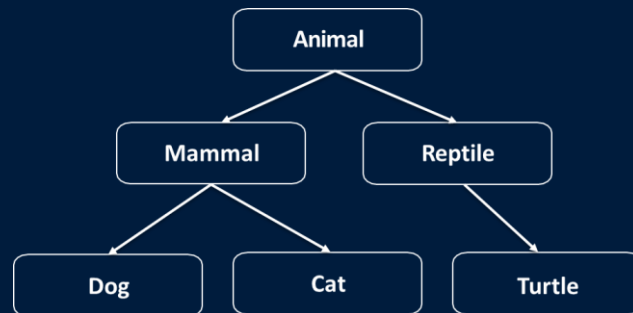
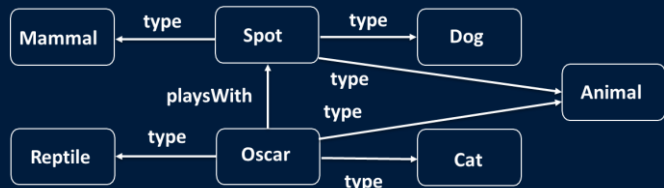
- Class taxonomies define a hierarchy between classes in a knowledge graph

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</owl:Class>
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  <rdfs:subClassOf rdf:resource="#Mammal" />
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  <rdfs:subClassOf rdf:resource="#Reptile" />
</owl:Class>
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  <rdfs:subClassOf rdf:resource="#Animal" />
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</owl:Class>
```



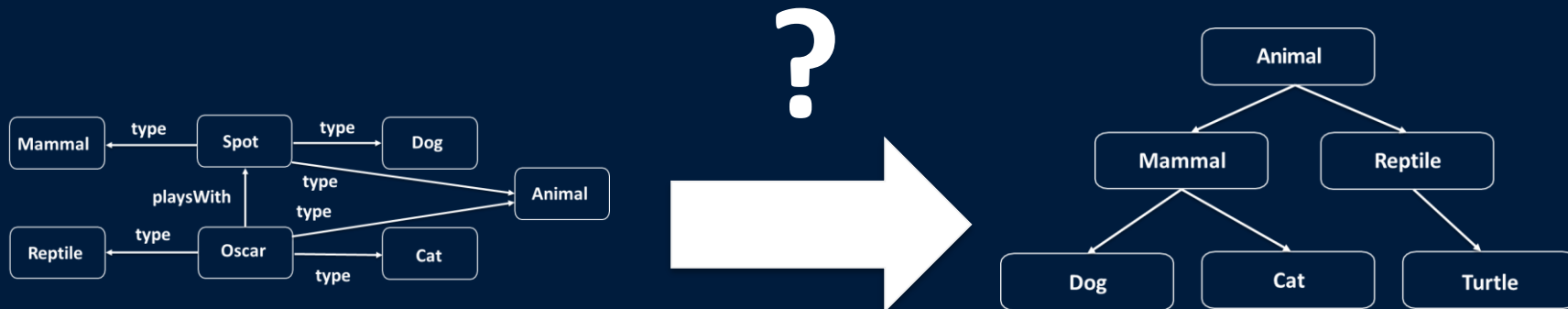
# Problem

- How can we automatically induce a class taxonomy from an otherwise flat knowledge graph?



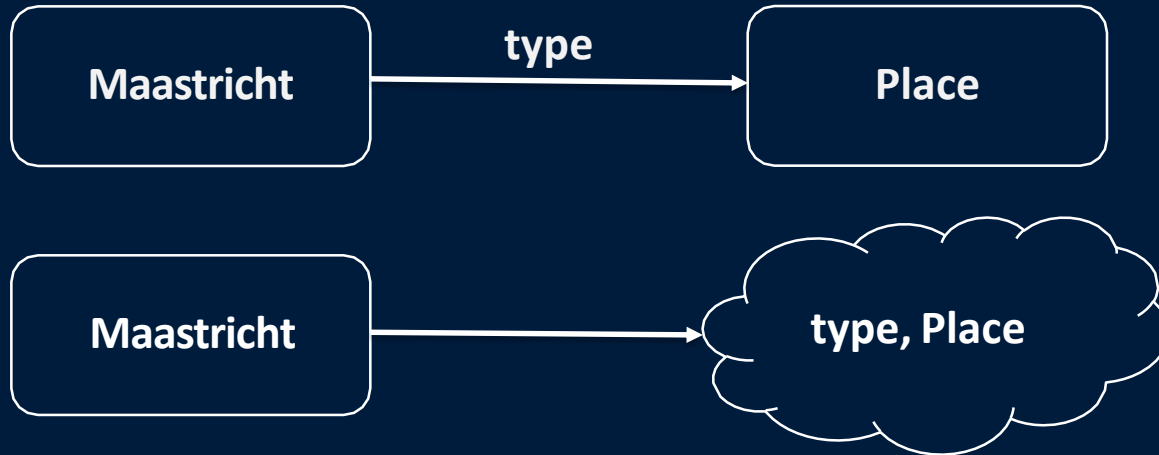
# Problem

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# Restructuring

- Leverage the predicate which relates an entity to its class and restructure a knowledge graph to entities and tags
- Tags are defined as predicate-object pairs

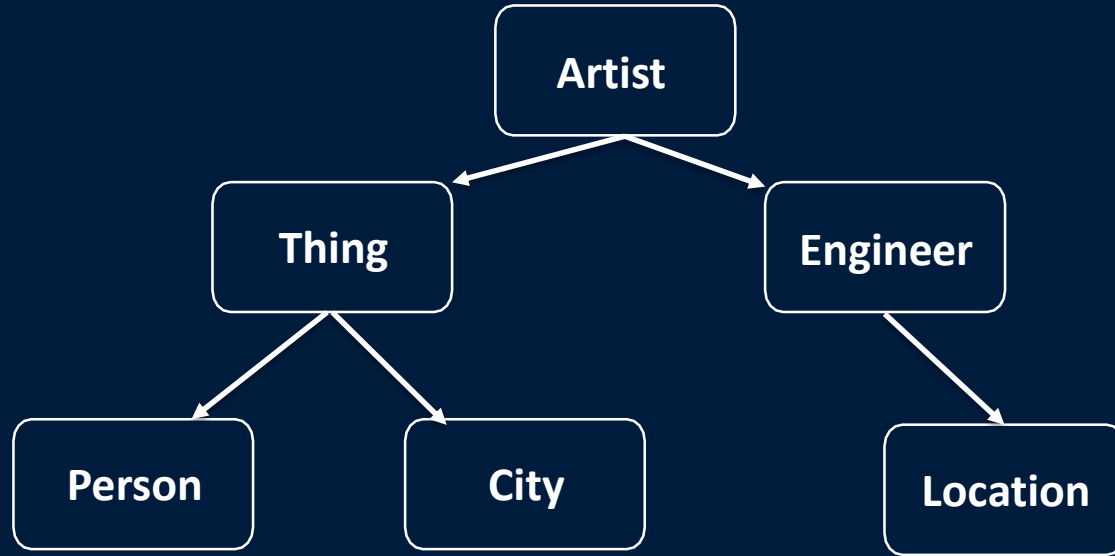


# Proposed Model

- Restructuring the knowledge graph allows us to leverage ideas from topic models such as **Hierarchical Latent Dirichlet Allocation (hLDA)**
- Our proposed model is comprised of **three components**:
  - Subject paths (Nested Chinese Restaurant Process in hLDA)
  - Tag paths (Nested Chinese Restaurant Process in hLDA)
  - Tag levels (Stick-breaking Process in hLDA)
- The taxonomy is learned through **simulated annealing**
  - Local search through a space by generating **candidate solutions** and probabilistically accepting them



Tags create a hierarchy defined by their **paths** and **level allocations**

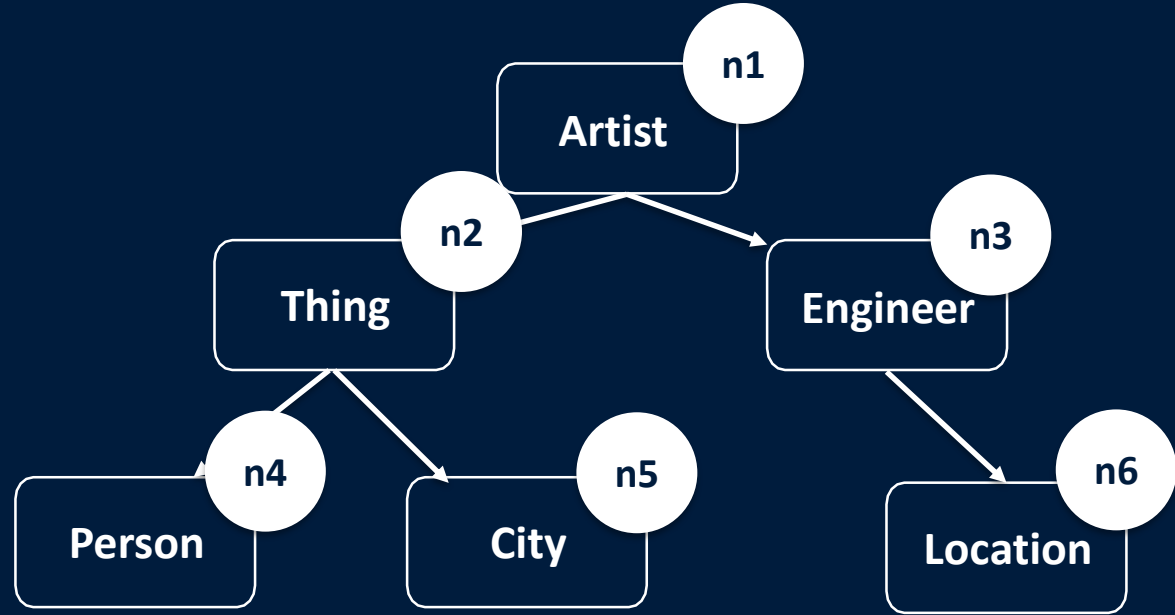


Tags create a hierarchy defined by their paths and level allocations

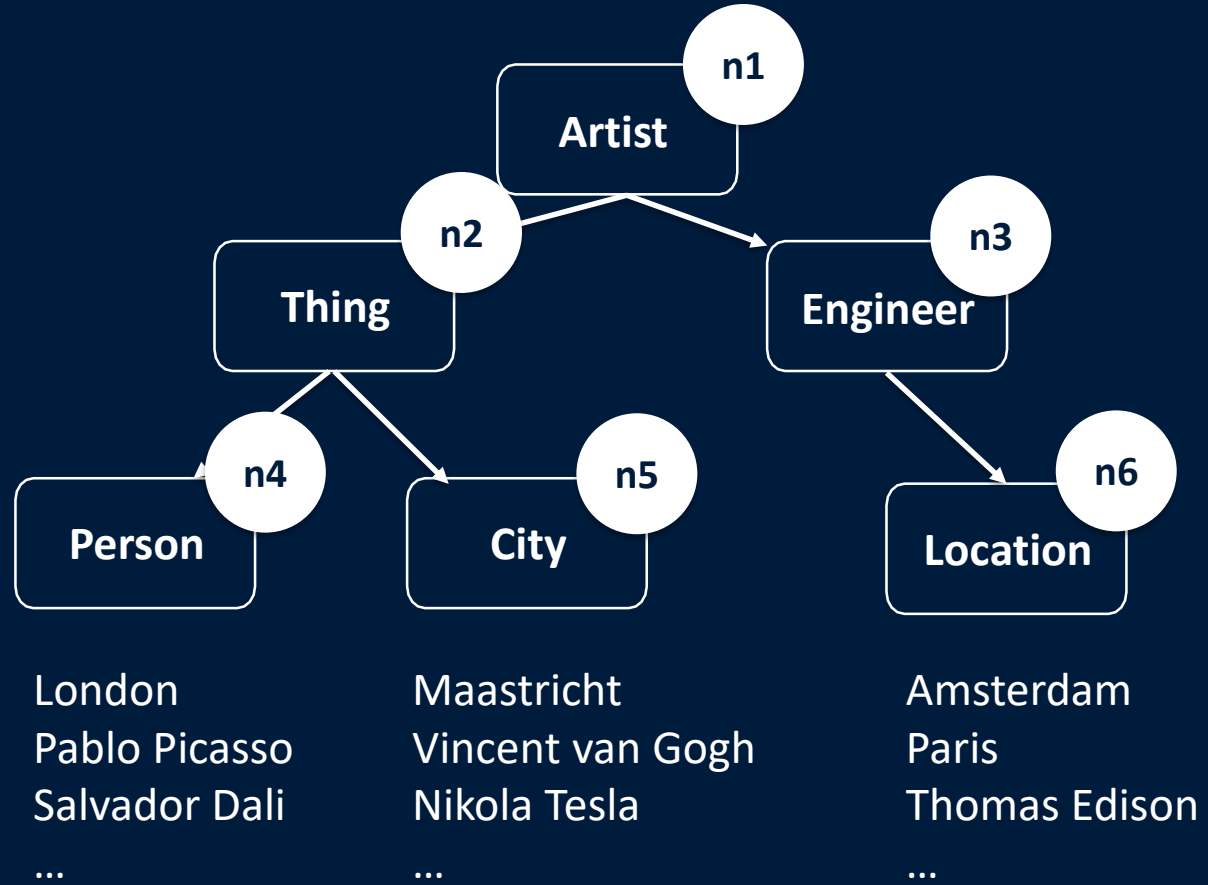
For example, the tag Engineer has:

Path: [n1, n3, n6]

Level: 2



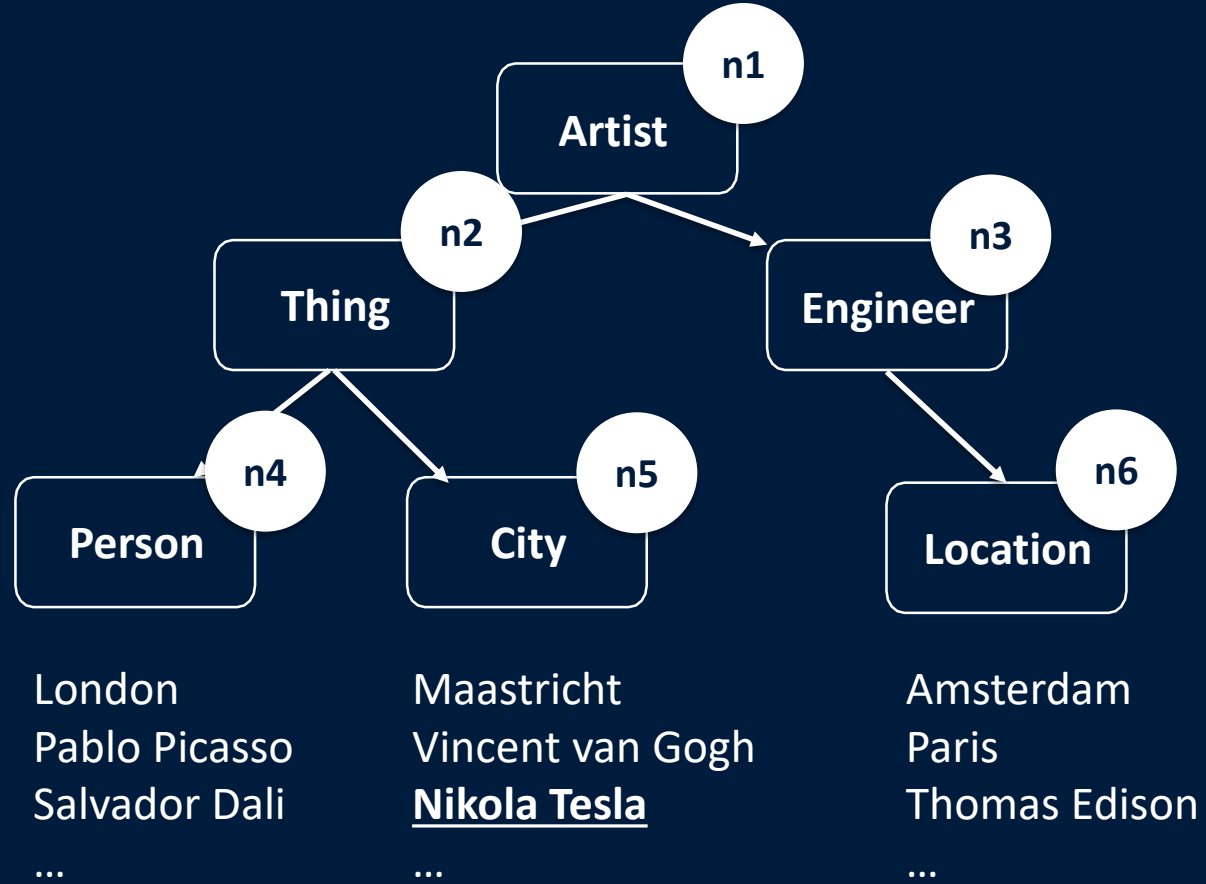
Subjects are allocated  
to paths



Subjects are allocated  
to paths

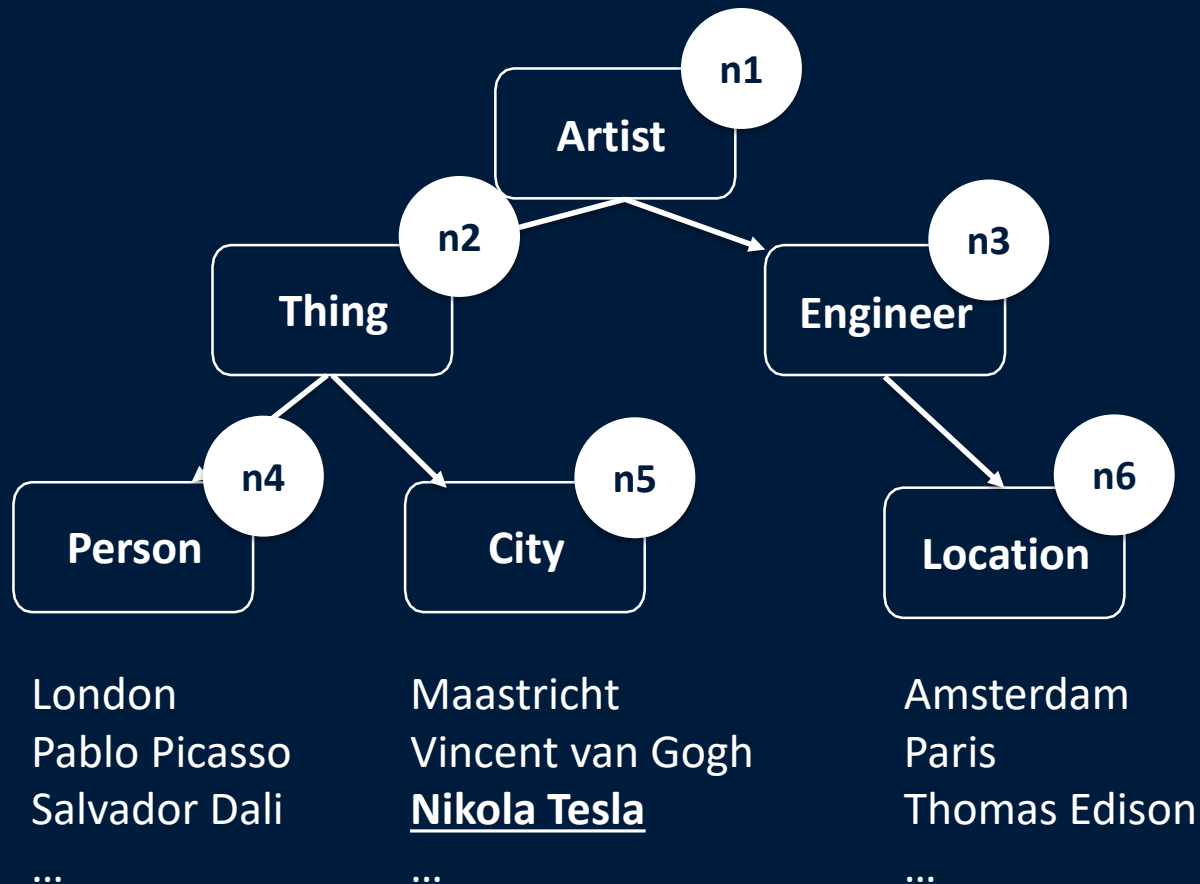
For example, the  
subject Nikola Tesla  
has:

Path: [n1, n2, n5]

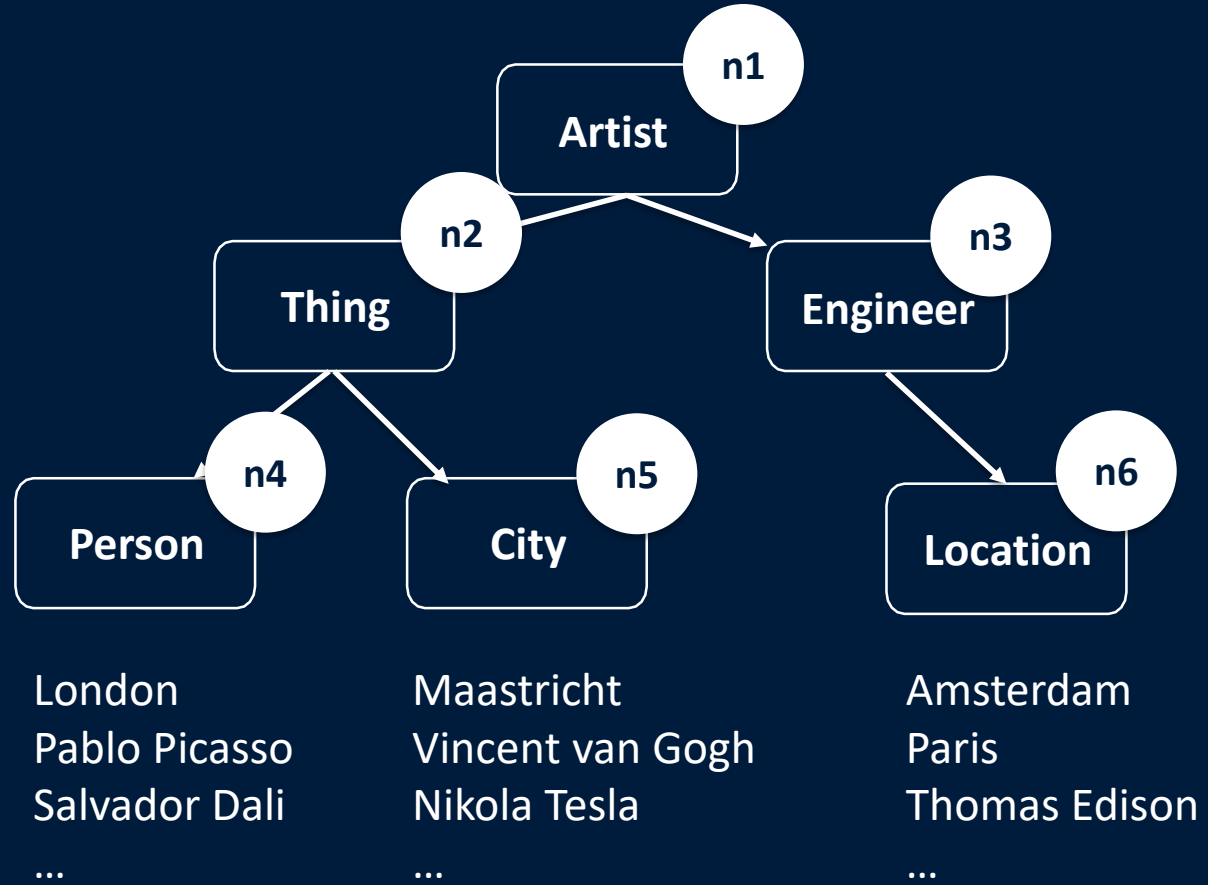


To generate a new candidate tree we must:

1. Update subject paths
2. Update tag paths
3. Update tag levels

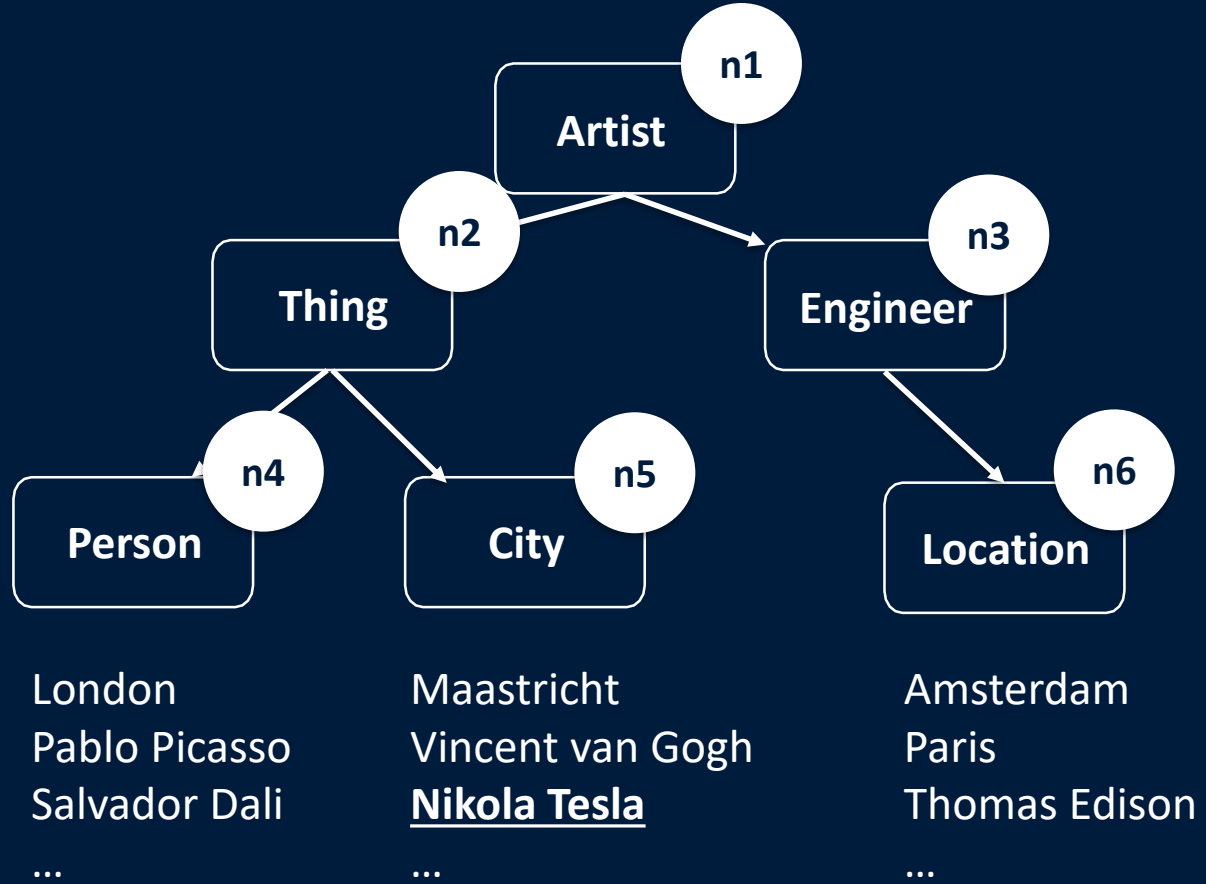


## Updating subject paths



## Updating subject paths

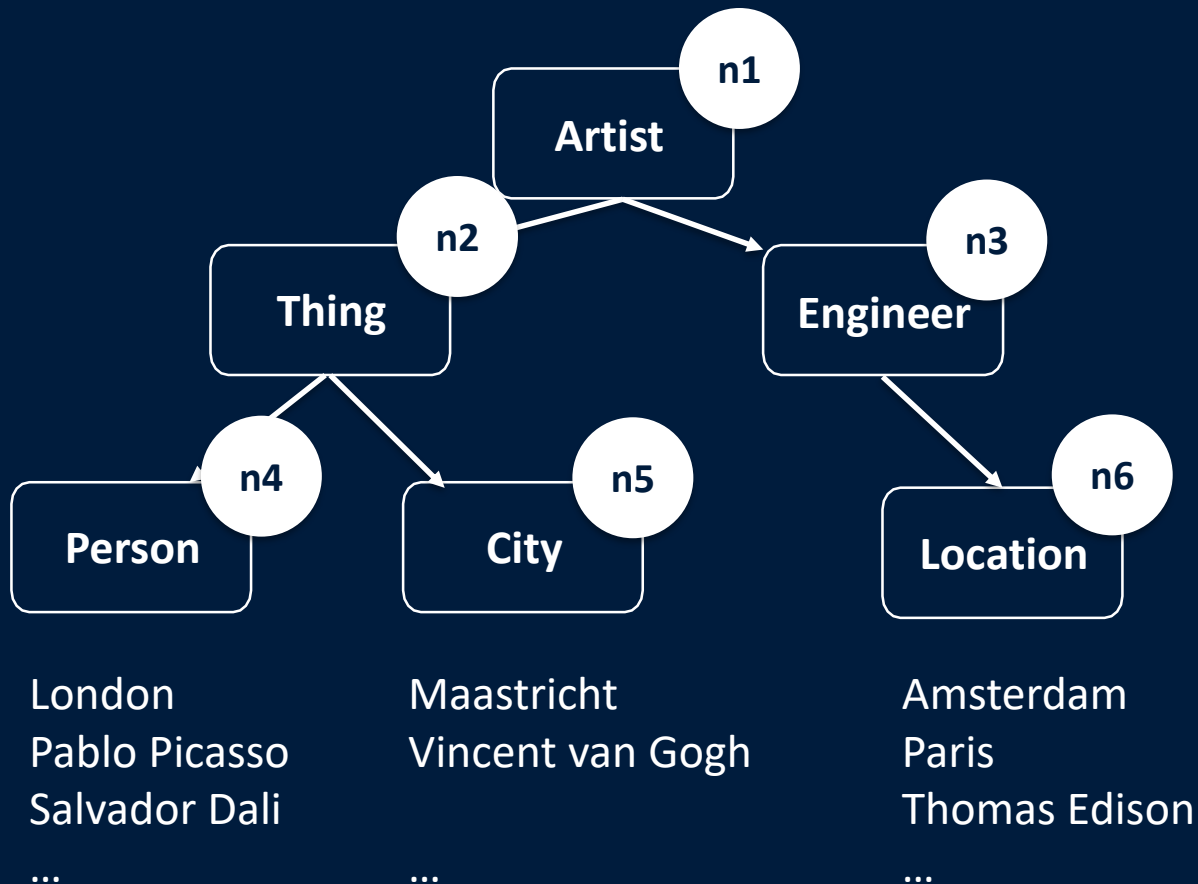
Choose a subject at random. Let's say Nikola Tesla



## Updating subject paths

Choose a subject at random. Let's say Nikola Tesla

Remove Nikola Tesla from the tree



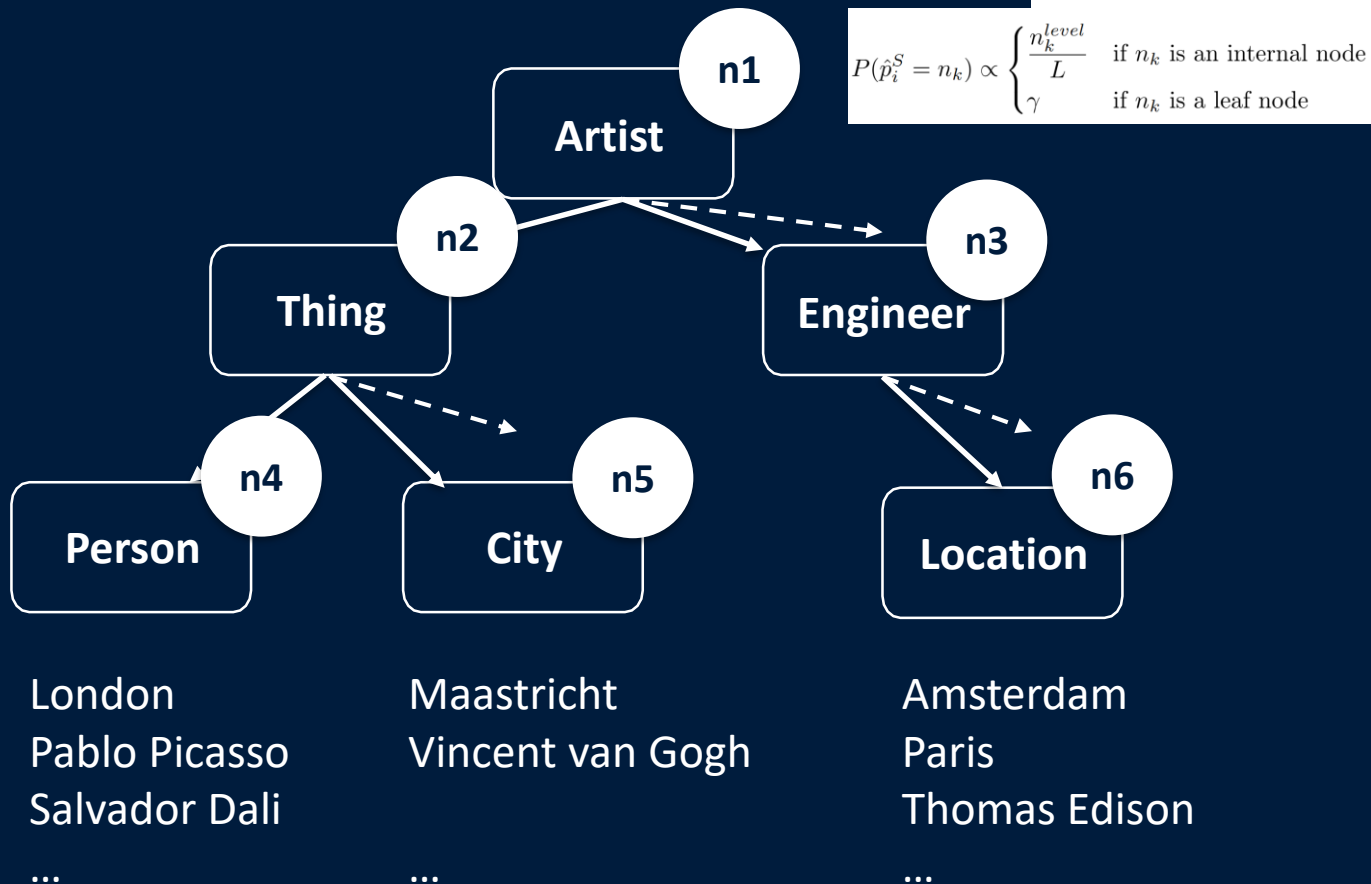


## Updating subject paths

Choose a subject at random. Let's say Nikola Tesla

Remove Nikola Tesla from the tree

Sample new path for Nikola Tesla using the update equations



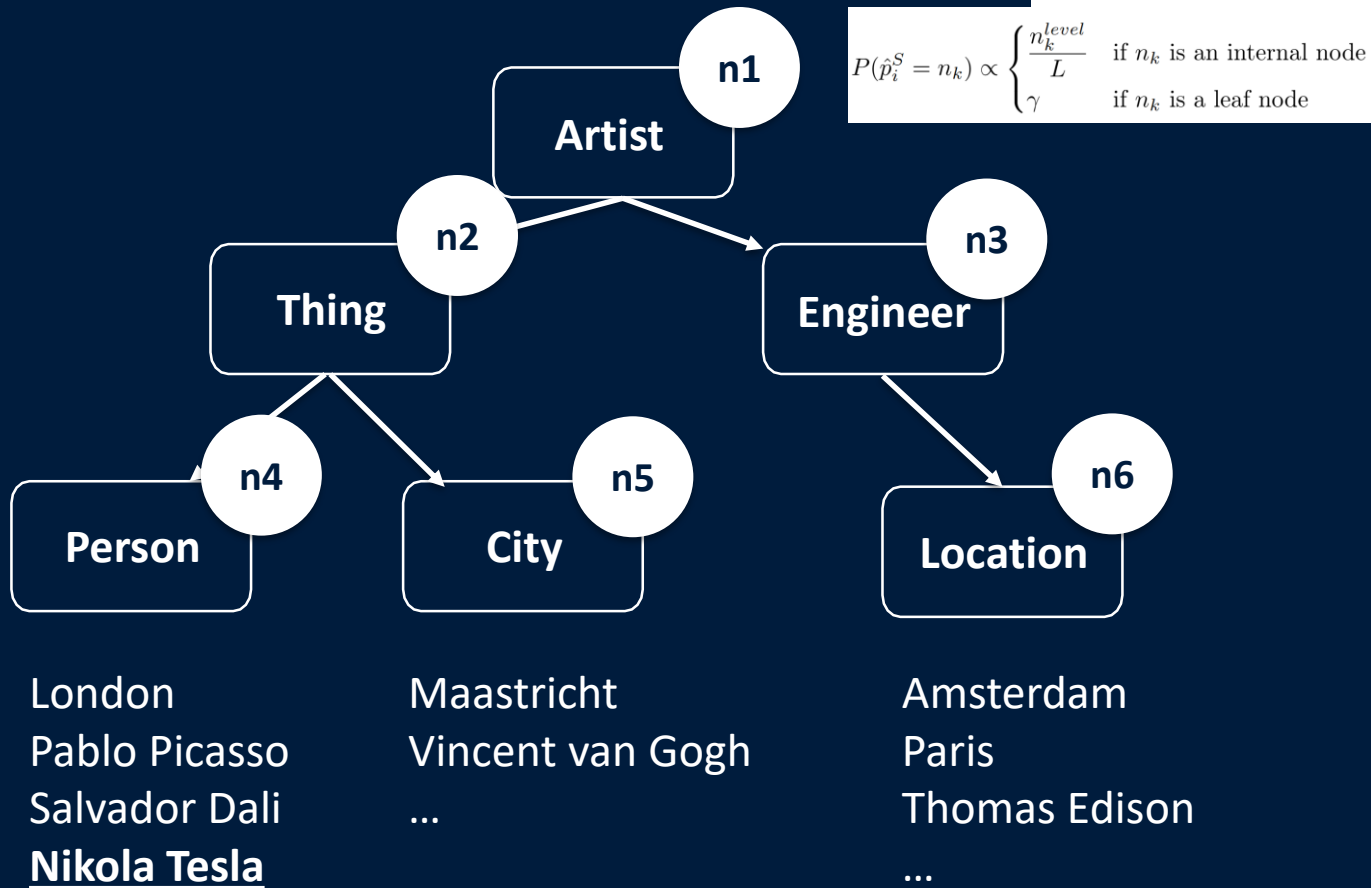
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Choose a subject at random. Let's say Nikola Tesla

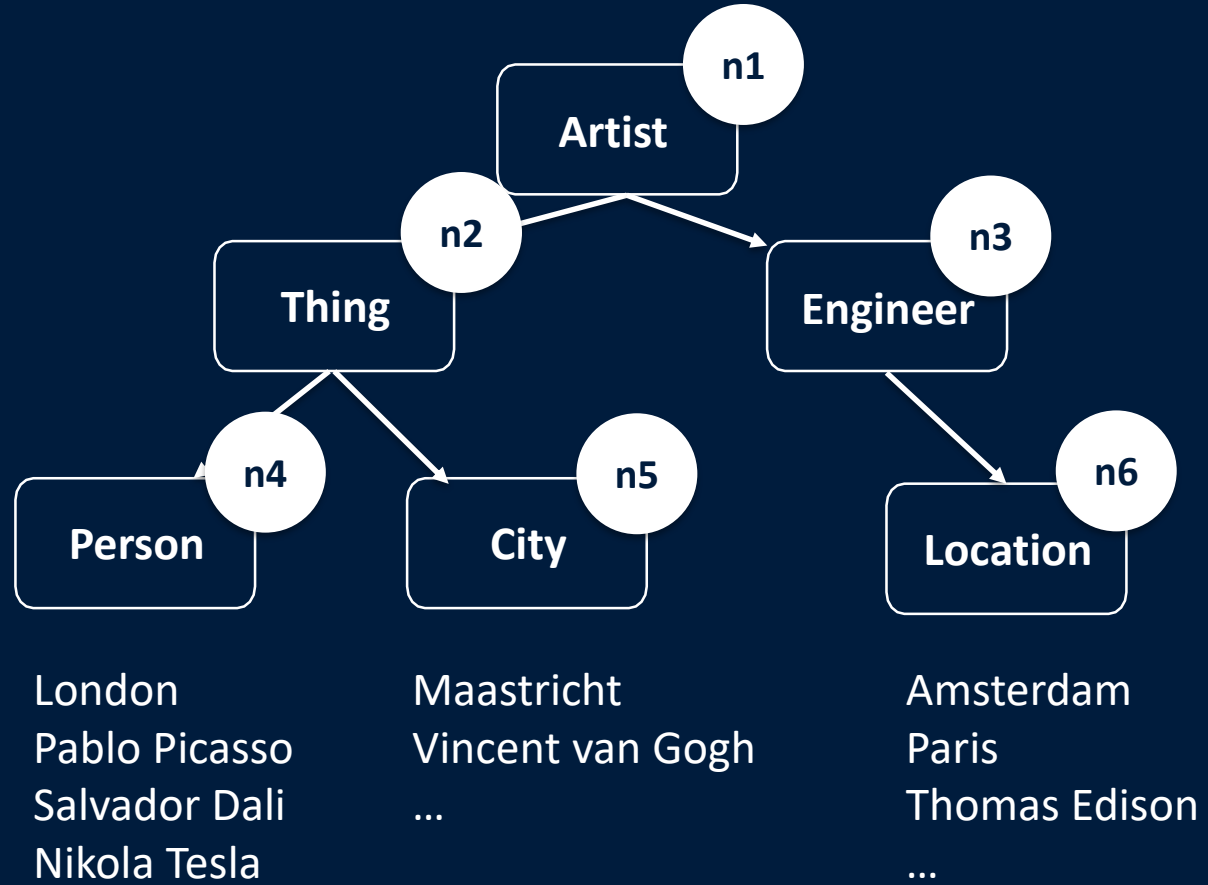
Remove Nikola Tesla from the tree

Sample new path for Nikola Tesla using the update equations

Let's say we sample path [n1, n2, n4]

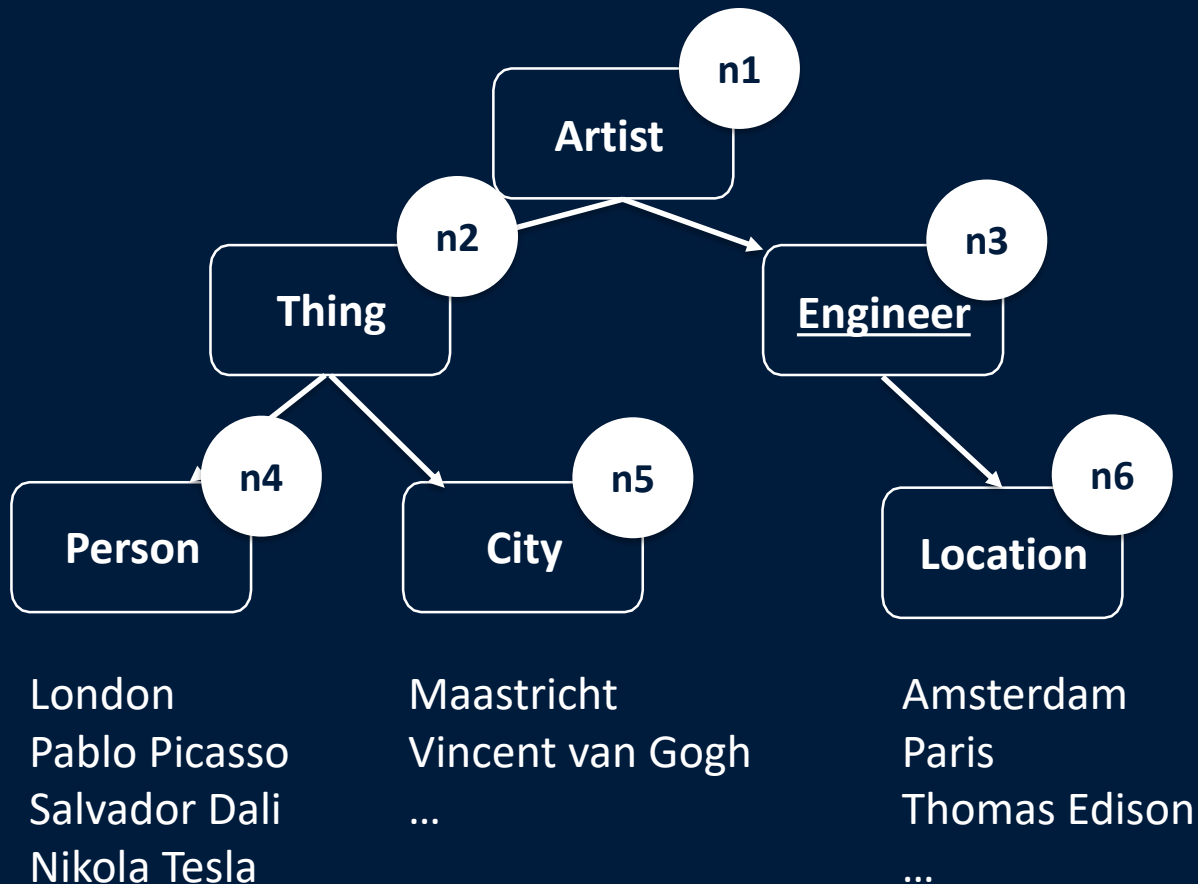


## Updating tag paths



## Updating tag paths

As before choose a tag  
at random. Let's say  
Engineer

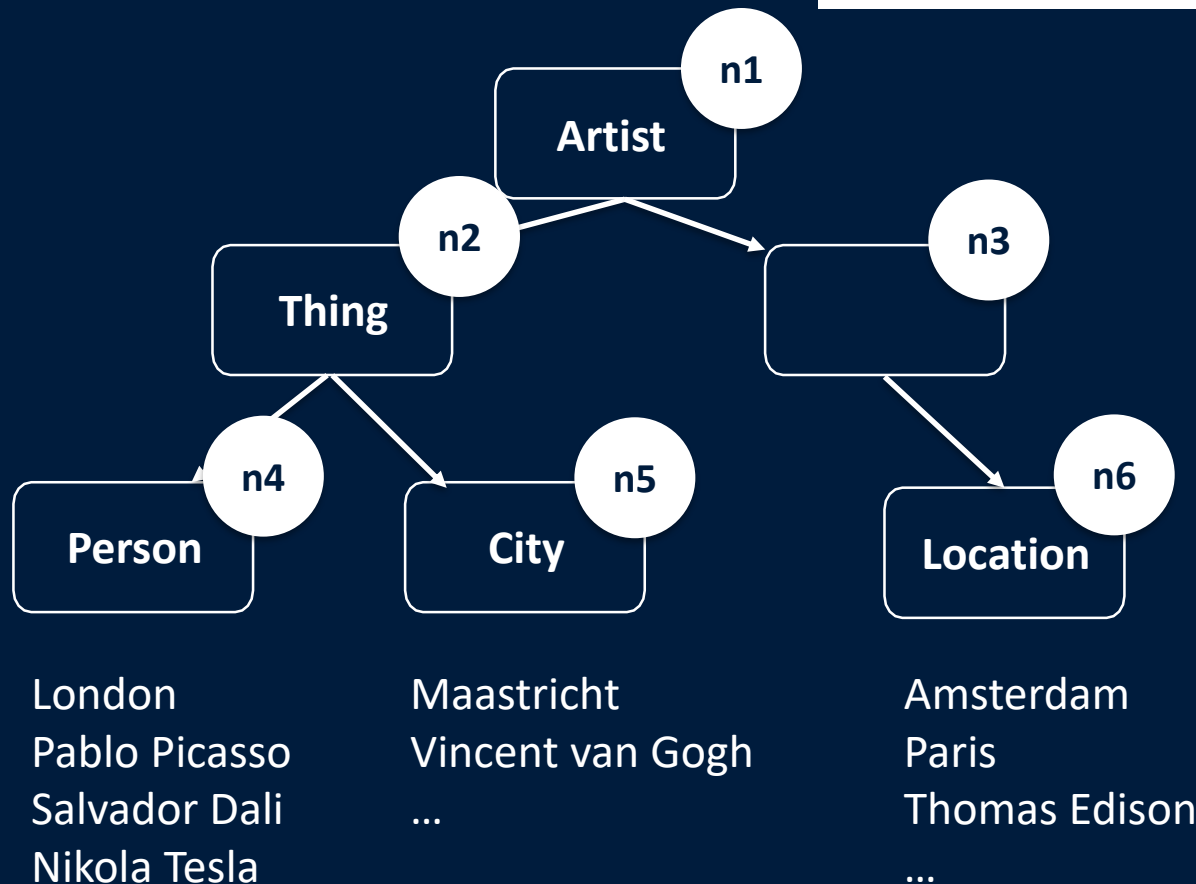


$$\mathbf{p}_j^T \sim \text{Uniform}(\{\mathbf{p}_i^S \in \mathbf{P}_{-j}^S : t_j \in \mathcal{T}_{s_i}\})$$

## Updating tag paths

As before choose a tag at random. Let's say Engineer

Sample new path for Engineer using update equation



$$\mathbf{p}_j^T \sim \text{Uniform}(\{\mathbf{p}_i^S \in \mathbf{P}_{-j}^S : t_j \in \mathcal{T}_{s_i}\})$$

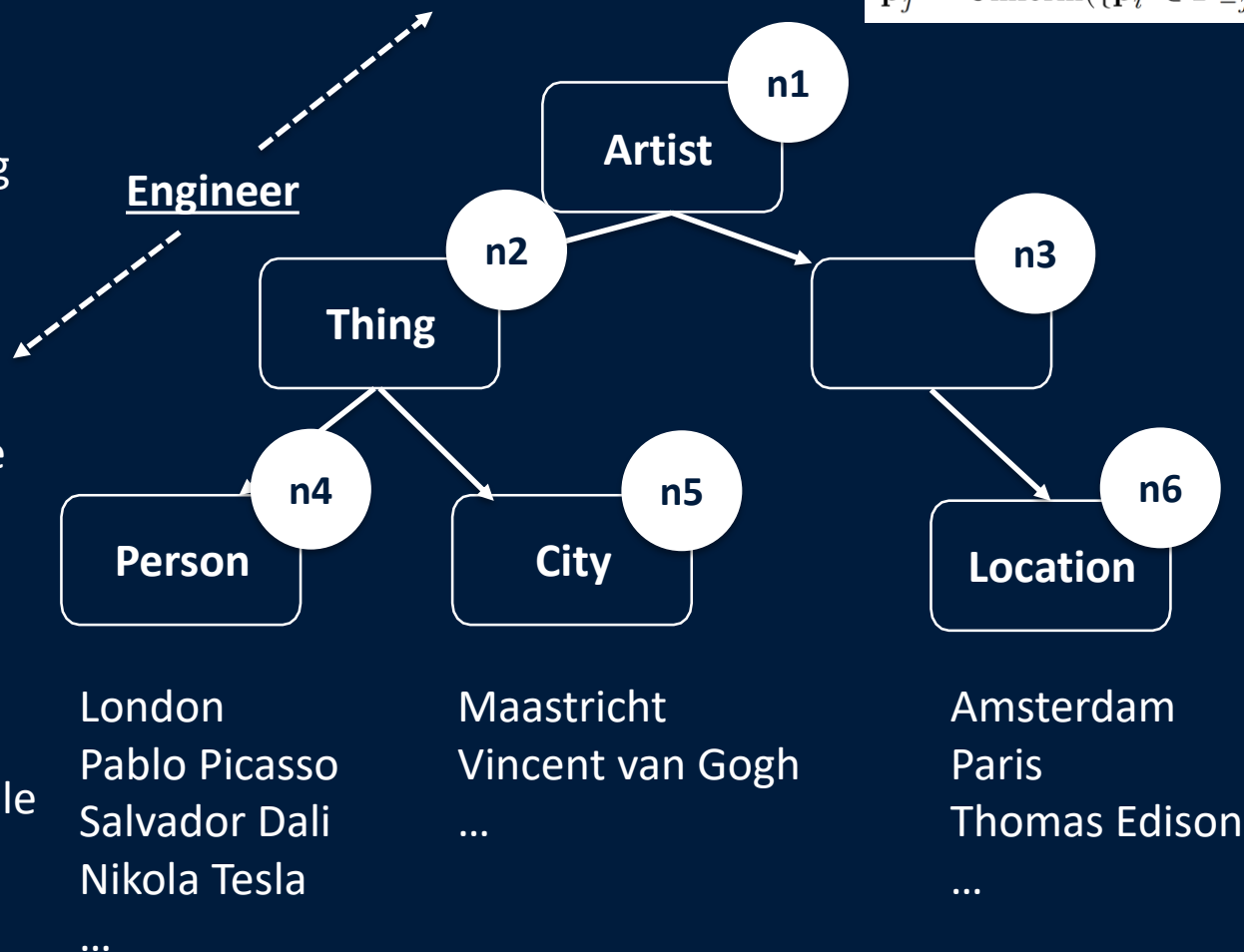
## Updating tag paths

As before choose a tag at random. Let's say Engineer

Sample new path for Engineer using update equation

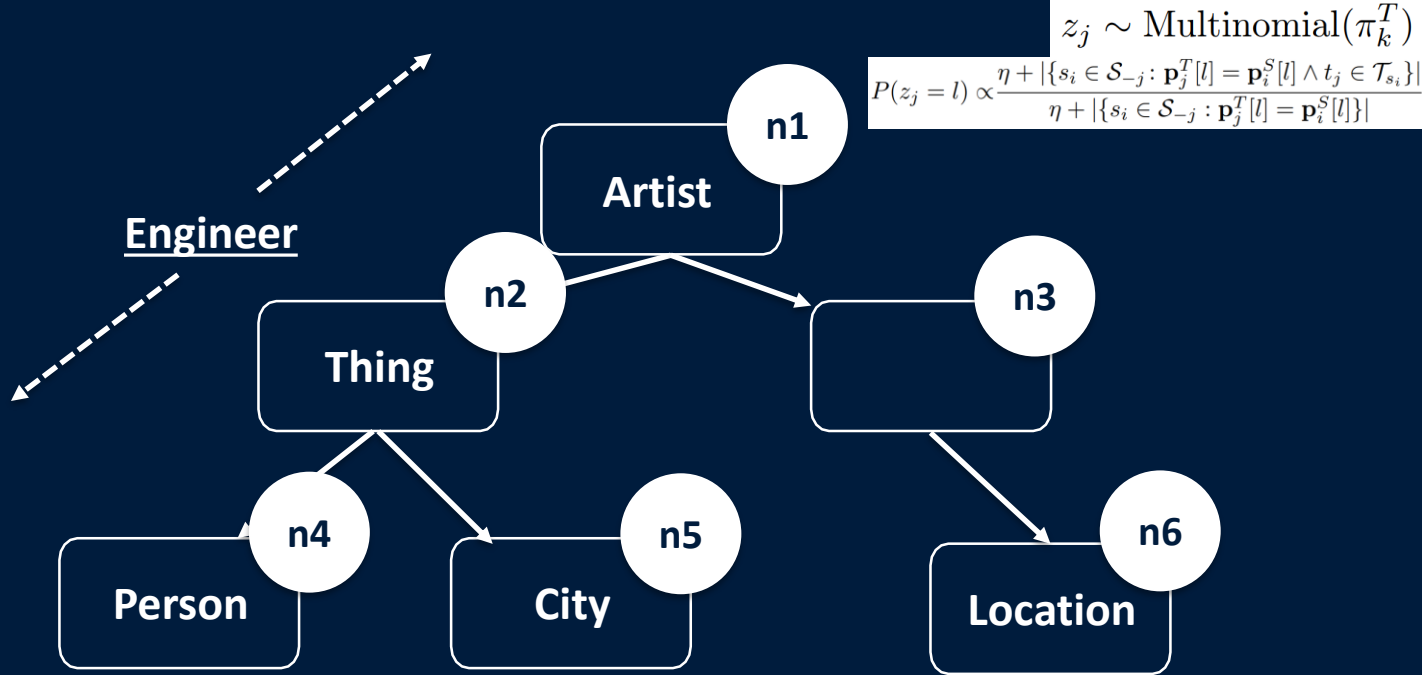
Let's say we sample path: [n1, n2, n4]

We now have to sample a tag level



Updating tag levels

Sample a level for Engineer using the update equations



London  
Pablo Picasso  
Salvador Dali  
Nikola Tesla

Maastricht  
Vincent van Gogh  
...

Amsterdam  
Paris  
Thomas Edison  
...

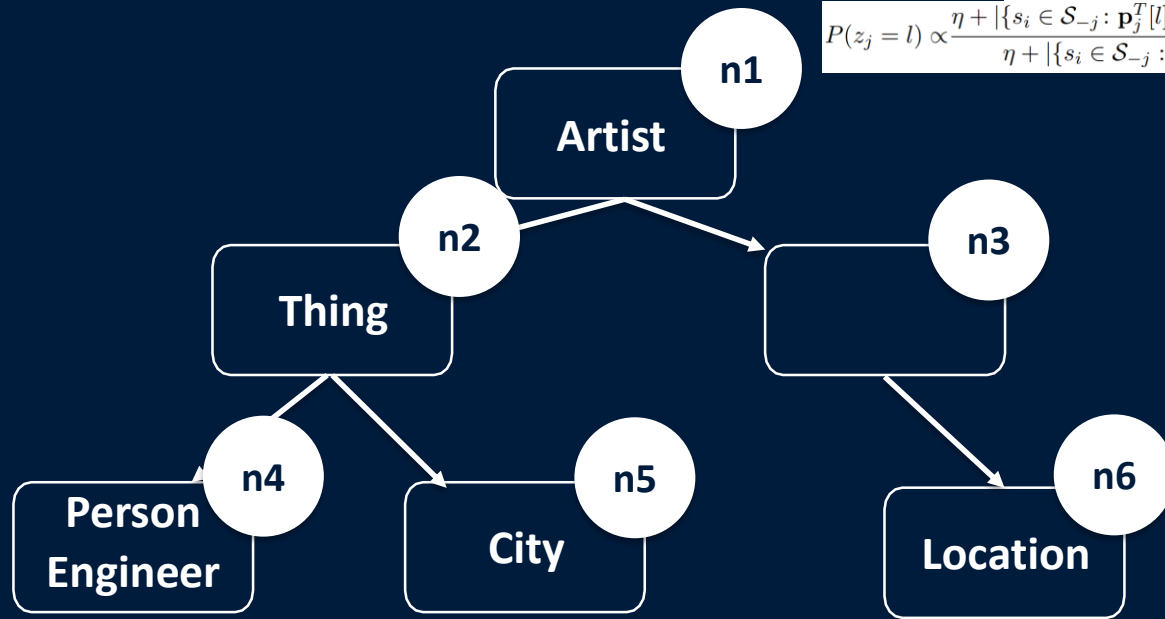
$$z_j \sim \text{Multinomial}(\pi_k^T)$$

$$P(z_j = l) \propto \frac{\eta + |\{s_i \in \mathcal{S}_{-j} : \mathbf{p}_j^T[l] = \mathbf{p}_i^S[l] \wedge t_j \in \mathcal{T}_{s_i}\}|}{\eta + |\{s_i \in \mathcal{S}_{-j} : \mathbf{p}_j^T[l] = \mathbf{p}_i^S[l]\}|}$$

Updating tag levels

Sample a level for **Engineer** using the update equations

Let's say we sample level 3



London  
Pablo Picasso  
Salvador Dali  
Nikola Tesla

Maastricht  
Vincent van Gogh  
...

Amsterdam  
Paris  
Thomas Edison  
...



$$z_j \sim \text{Multinomial}(\pi_k^T)$$

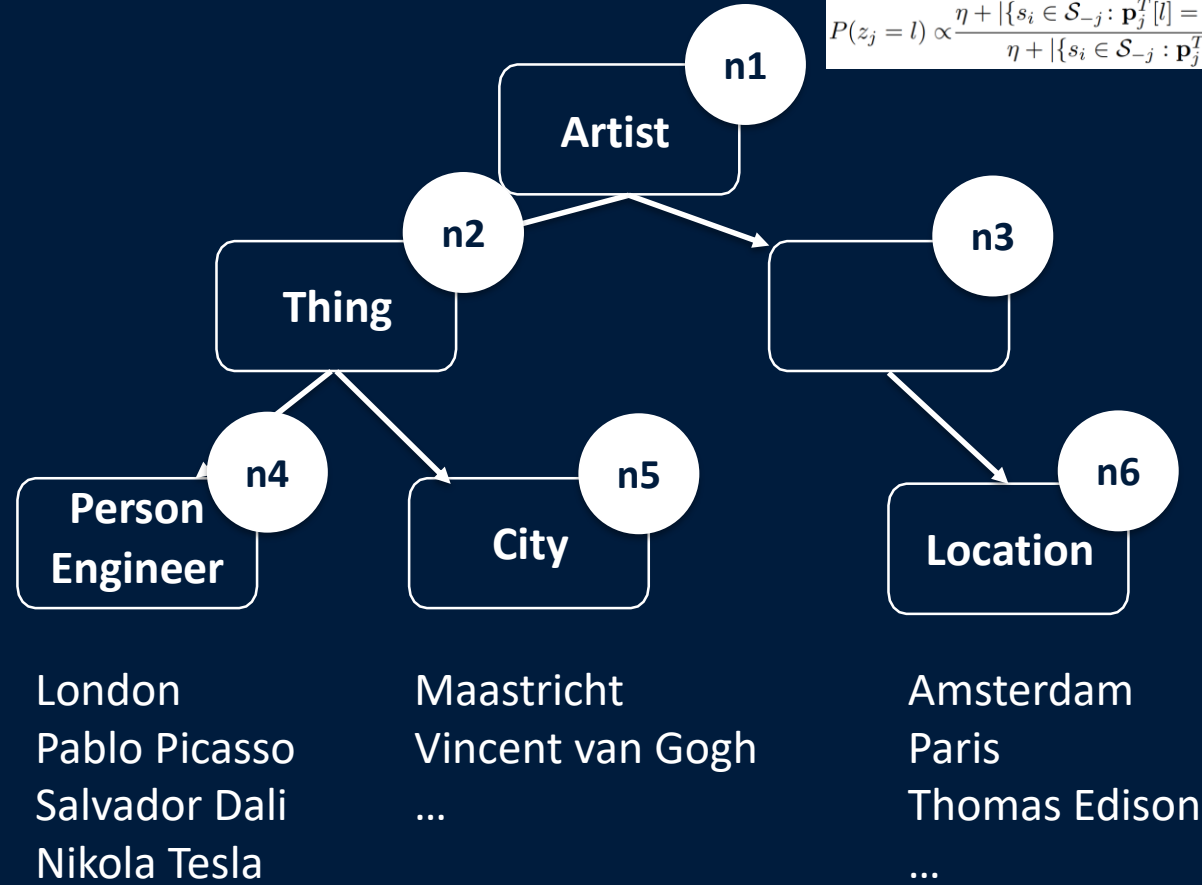
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Updating tag levels

Sample a level for **Engineer** using the update equations

Let's say we sample level 3

We have now generated a local neighbor, i.e. a **candiade solution**



# Simulated Annealing

- Candidate solutions are evaluated according to an objective function

$$J = \sum_{s_i \in \mathcal{S}} \sum_{n_k \in \mathbf{p}_i^{\mathcal{S}}} \sum_{t_j \in \mathcal{T}_{n_k}} \begin{cases} \frac{1}{|\mathcal{T}_{n_k}|} & \text{if } t_j \in \mathcal{T}_{s_i} \\ 0 & \text{otherwise} \end{cases} \\ - \sum_{s_i \in \mathcal{T}} \sum_{n_k \in \mathbf{p}_i^{\mathcal{S}}} \begin{cases} |\mathcal{T}_{n_k}| + \alpha & \text{if } \mathcal{T}_{n_k} \cap \mathcal{T}_{s_i} = \emptyset \\ 0 & \text{otherwise} \end{cases} \\ - \sum_{s_i \in \mathcal{T}} \sum_{n_l \in \mathbf{p}_i^{\mathcal{S}}} \begin{cases} |\mathcal{T}_{n_k}|(L - n_k^{level}) + \alpha & \text{if } |\mathcal{T}_{n_k}| > 1 \\ 0 & \text{otherwise} \end{cases}$$

... and accepted according to an annealing schedule

$$\mathbb{P}(x = x') = \exp\left(-\frac{J_x - J_{x'}}{\theta_{iter}}\right)$$

$$\theta_{iter} = \theta_0 * \frac{\theta_{final}}{\theta_0} \frac{iter}{iter_{max}}$$

# Evaluation Setup

- Run our algorithm on three real-world datasets:
  - Carnivora
  - DBpedia
  - WordNet
- Calculate F1-scores obtained using induced subsumption axioms and gold standard axioms for each dataset
- Compare F1-scores with baselines implemented from the literature

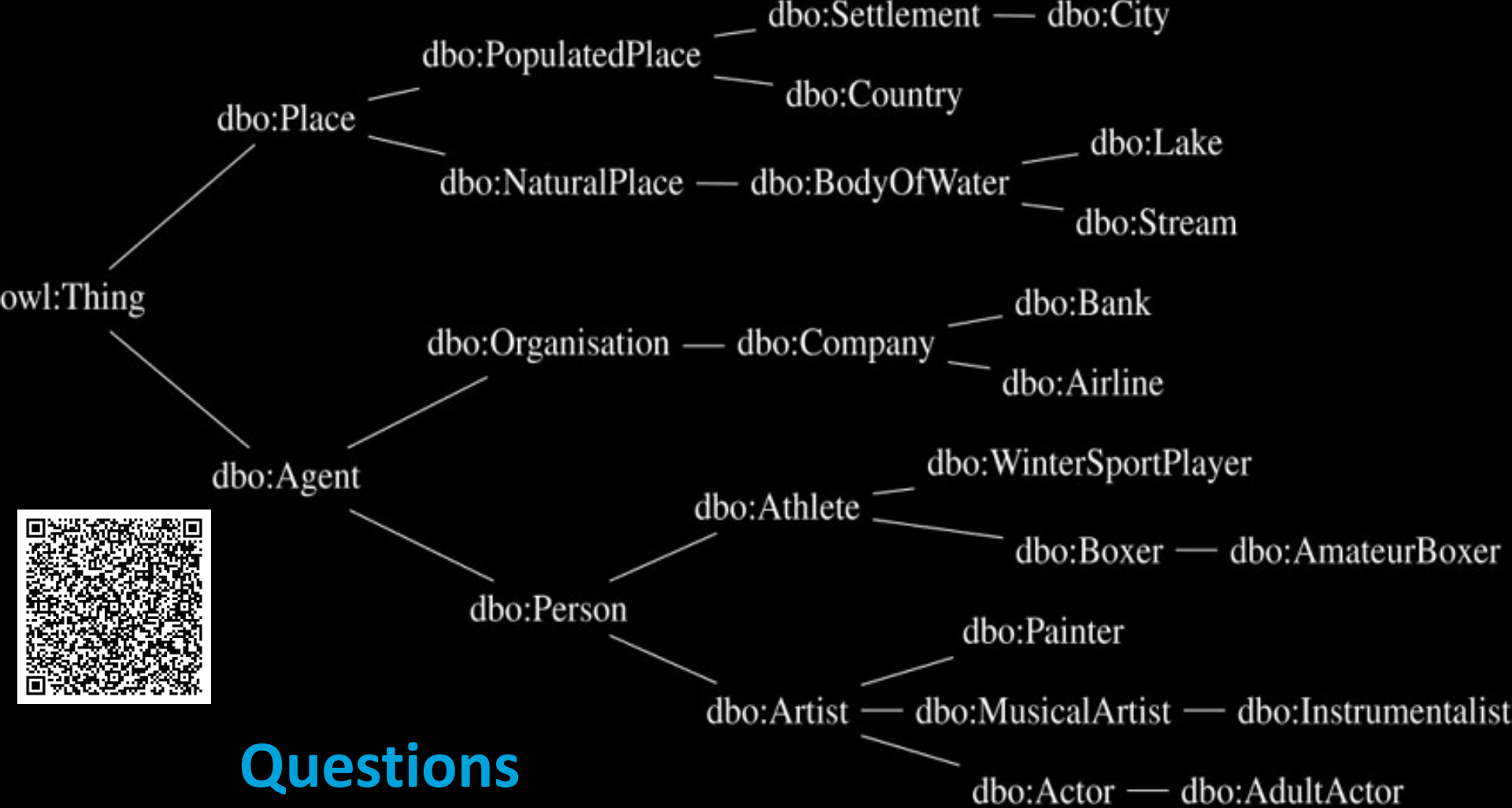
# Results

- Results are comparable or better than state-of-the-art approaches

Model	Carnivora	Dbpedia	WordNet
Heymann and Garcia-Molina	0.9765	0.8673	0.5447
Schmitz	0.9831	0.8502	<u>0.6988</u>
Wang et al. (2012)	0.8571	0.6481	0.4462
Wang et al. (2018)	0.6908	0.5318	0.4286
Pietrasik and Reformat	0.9731	0.8788	0.6171
<b>Our Model</b>	<u><b>0.9866</b></u>	<u><b>0.8981</b></u>	0.5508

# Conclusions and Future Work

- Path based models from topic modelling can be used for class taxonomy induction in knowledge graphs
- Biggest drawback of our model is that it is slow
  - Our model does not scale well to large datasets
- Future work will focus on improving the scalability of the model
  - Improve sampling distributions in update steps
  - Look into alternative optimization schemes



Questions