NSWPCN Predictor Training

January 19, 2015

1 Preparation

```
library(survival)
## Loading required package: splines
library(glmulti)
## Loading required package: rJava
library(flexsurv)
library(randomForestSRC)
## Loading required package: parallel
##
## randomForestSRC 1.5.5
##
## Type rfsrc.news() to see new features, changes, and bug fixes.
##
library(reshape2)
library(plyr)
library(ggplot2)
library(MASS)
library(boot)
## Attaching package: 'boot'
## The following object is masked from 'package:survival':
##
##
      aml
library(timeROC)
## Loading required package: pec
## Loading required package: mutnorm
## Loading required package: timereg
source("stdca.R")
load("03_NSWPCN_subset.rda")
```

2 Cohort selection and transformation

```
x = data[,c("Patient.Sex", "History.Diagnosis.AgeAt.Cent", "Path.LocationBody", "Path.Size.Cent", "Path
colnames(x) = c("SexM", "AgeCent", "LocBody", "SizeCent", "Ca199", "A2", "A4")
x\$SexM = x\$Sex == "M"
x$Ca199 = x$Ca199 > 100
y = Surv(as.numeric(data$History.Death.Date - data$History.Diagnosis.Date), data$History.DSDeath.Event)
# Note no surgery dates, though for almost all pts there were only a few days difference.
temp = NA
temp = ls()
rm(list = temp[!(temp %in% c("x", "y"))])
sel = !is.na(y[,1]) & !is.na(y[,2]) & !is.na(x$A2) & !is.na(x$A4) & !is.na(x$LocBody)
x = x[sel,]
y = y[sel,]
rm(sel)
# Remove CA-19-9 measurements as they're mostly missing
x = x[,colnames(x) != "Ca199"]
data = as.data.frame(cbind(Time = y[,1], DSD = y[,2], x))
rm(x, y)
data$DSD = data$DSD == 1
```

3 Data splitting

There's going to be an awful lot of model manipulation and black magic going on. Create a holdout validation set for final model comparison and selection.

```
set.seed(20150110)
sel.val = sample.int(nrow(data), floor(nrow(data)/4))
sel.val = 1:nrow(data) %in% sel.val
mean(sel.val)
## [1] 0.25
data.val = data[sel.val,,drop = FALSE]
data = data[!sel.val,,drop = FALSE]
```

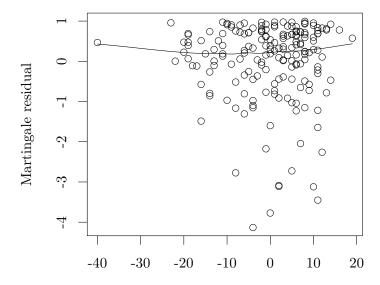
4 EDA

Use the CPH model as a convenient framework for EDA.

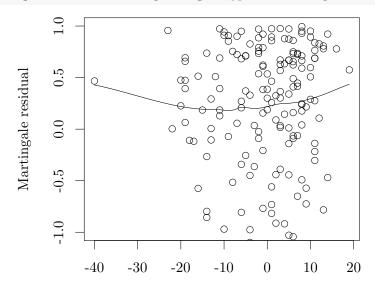
4.1 Functional form

Investigate functional form with martingale residuals.

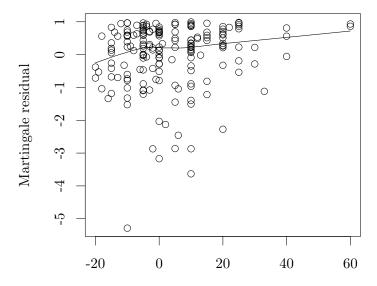
```
fit.cph.NoAge = coxph(Surv(Time, DSD) ~ SexM + LocBody + SizeCent + A2 + A4, data = data)
scatter.smooth(data$AgeCent, resid(fit.cph.NoAge, type = "martingale"), xlab = "", ylab = "Martingale re
```



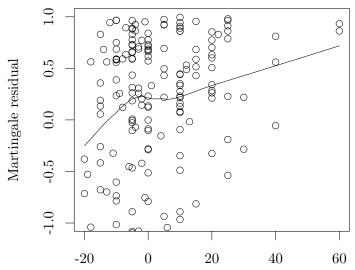
scatter.smooth(data\$AgeCent, resid(fit.cph.NoAge, type = "martingale"), xlab = "", ylab = "Martingale re



fit.cph.NoSize = coxph(Surv(Time, DSD) ~ SexM + AgeCent + LocBody + A2 + A4, data = data)
scatter.smooth(data\$SizeCent, resid(fit.cph.NoSize, type = "martingale"), xlab = "", ylab = "Martingale")



scatter.smooth(data\$SizeCent, resid(fit.cph.NoSize, type = "martingale"), xlab = "", ylab = "Martingale

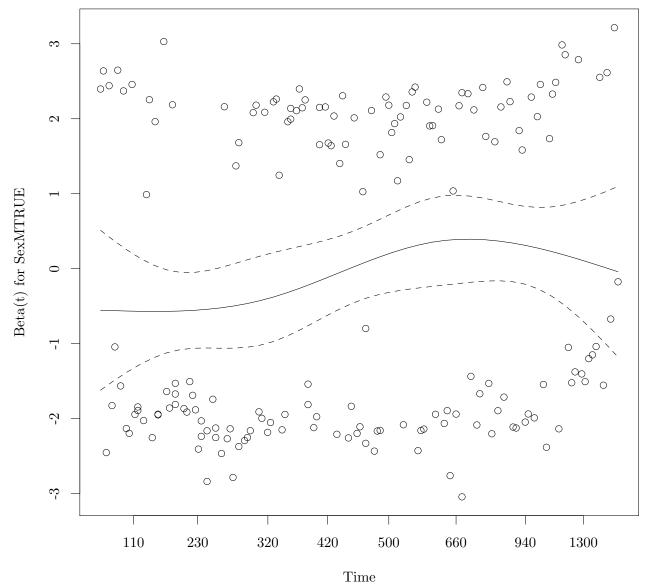


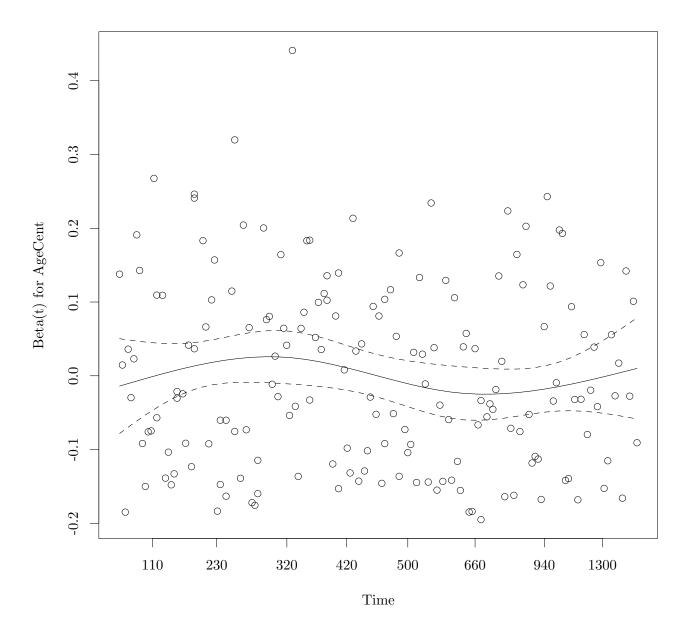
It looks like age has a minor nonlinear component, leading to a quadratic-like U shape. The size relationship appears to have a knee, close to size ==0, around which the relationship is approximately linear.

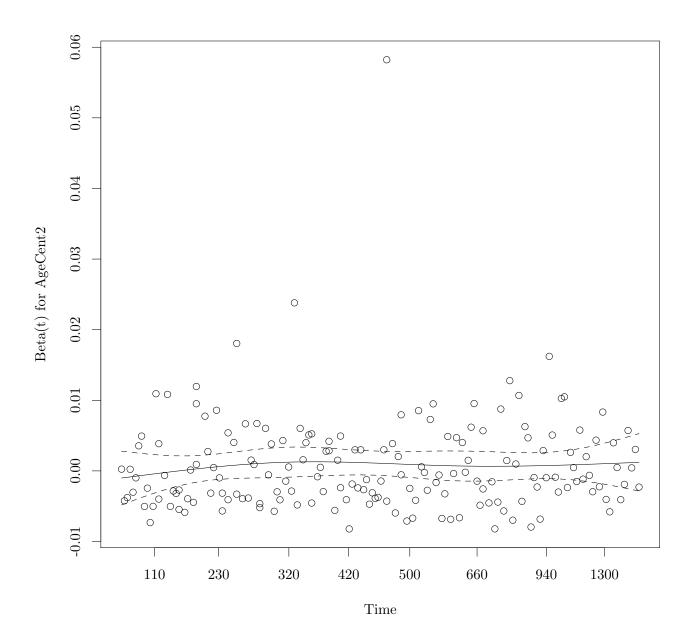
 $\label{eq:model} \mbox{Model age as: } \mbox{$AgeCent+SizeCentI(SizeCent>0)$} \equiv \mbox{$SizeCent+Size$

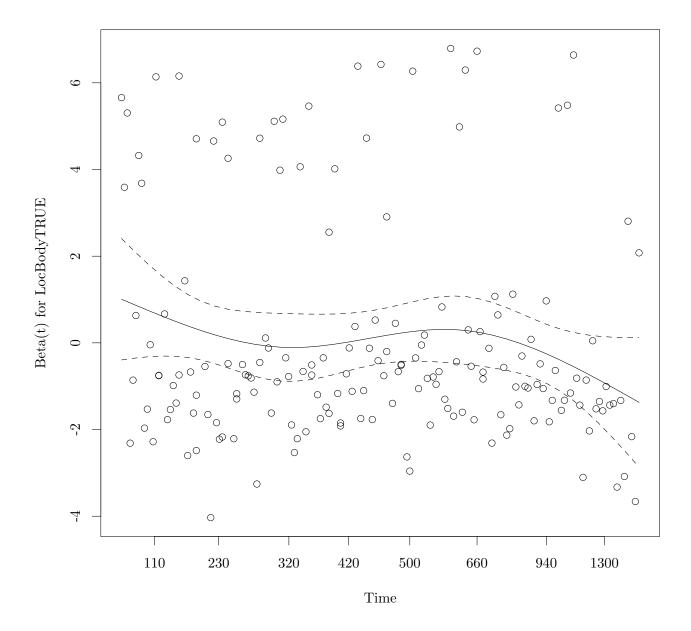
```
data$SizeSmall = data$SizeCent * (data$SizeCent < 0)
data$AgeCent2 = data$AgeCent^2</pre>
```

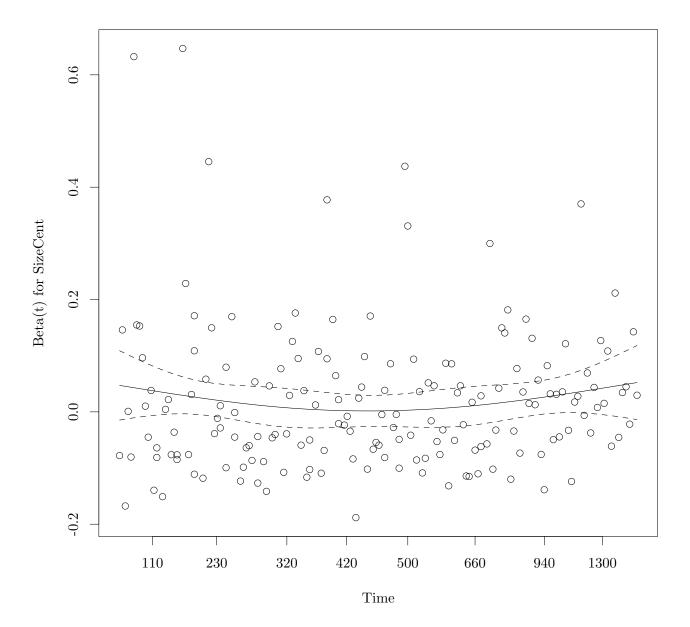
4.2 PH assumption: full model

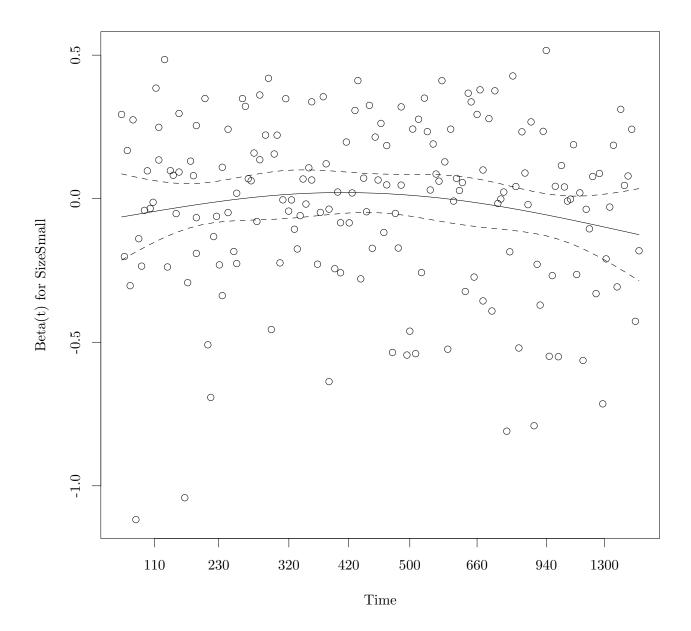


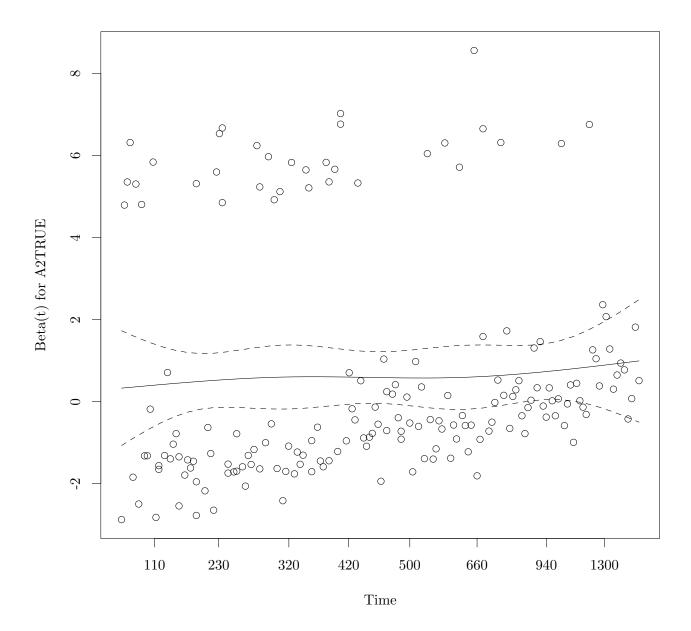


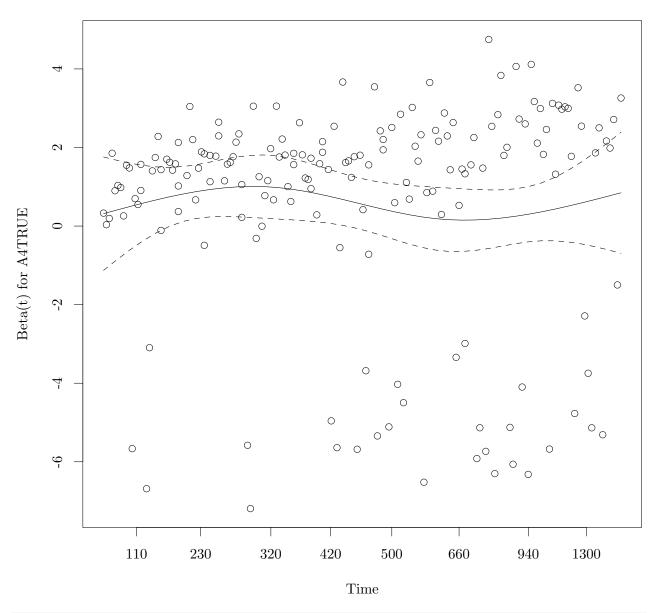












```
temp = function (x, resid = TRUE, se = TRUE, df = 4, nsmo = 40, var, ...) {
    xx <- x$x
    уу <- х$у
    d <- nrow(yy)</pre>
    df \leftarrow max(df)
    nvar <- ncol(yy)</pre>
    pred.x \leftarrow seq(from = min(xx), to = max(xx), length = nsmo)
    temp <- c(pred.x, xx)</pre>
    lmat <- ns(temp, df = df, intercept = TRUE)</pre>
    pmat <- lmat[1:nsmo, ]</pre>
    xmat <- lmat[-(1:nsmo), ]</pre>
    qmat <- qr(xmat)</pre>
    if (qmat$rank < df)</pre>
         stop("Spline fit is singular, try a smaller degrees of freedom")
    if (se) {
         bk <- backsolve(qmat$qr[1:df, 1:df], diag(df))</pre>
         xtx <- bk %*% t(bk)
```

```
seval <- d * ((pmat %*% xtx) * pmat) %*% rep(1, df)
ylab <- paste("Beta(t) for", dimnames(yy)[[2]])</pre>
if (missing(var))
    var <- 1:nvar</pre>
else {
    if (is.character(var))
        var <- match(var, dimnames(yy)[[2]])</pre>
    if (any(is.na(var)) || max(var) > nvar || min(var) <</pre>
        stop("Invalid variable requested")
if (x$transform == "log") {
    xx \leftarrow exp(xx)
    pred.x <- exp(pred.x)</pre>
else if (x$transform != "identity") {
    xtime <- as.numeric(dimnames(yy)[[1]])</pre>
    indx <- !duplicated(xx)</pre>
    apr1 <- approx(xx[indx], xtime[indx], seq(min(xx), max(xx),</pre>
        length = 17)[2 * (1:8)]
    temp <- signif(apr1$y, 2)</pre>
    apr2 <- approx(xtime[indx], xx[indx], temp)</pre>
    xaxisval <- apr2$y</pre>
    xaxislab <- rep("", 8)</pre>
    for (i in 1:8) xaxislab[i] <- format(temp[i])</pre>
for (i in var) {
    y <- yy[, i]
    yhat <- pmat %*% qr.coef(qmat, y)</pre>
    if (resid)
        yr <- range(yhat, y)</pre>
    else yr <- range(yhat)</pre>
    if (se) {
        temp <- 2 * sqrt(x$var[i, i] * seval)</pre>
        yup <- yhat + temp
        ylow <- yhat - temp
        yr <- range(yr, yup, ylow)</pre>
    if (x$transform == "identity")
        plot(range(xx), yr, type = "n", ...)
    else if (x$transform == "log")
        plot(range(xx), yr, type = "n", log = "x", ...)
    else {
        plot(range(xx), yr, type = "n", axes = FALSE, ...)
        axis(1, xaxisval, xaxislab)
        axis(2)
        box()
    if (resid)
        points(xx, y)
    lines(pred.x, yhat)
    if (se) {
```

```
lines(pred.x, yup, lty = 2)
               lines(pred.x, ylow, lty = 2)
temp(cox.zph(fit.cph), var = 1, ylab = "Scaled Schoenfeld residual for patient sex", xlab = "Time")
abline(h = 0, lty = "dotted")
                                                                                                             0
                          0
               00
               00 00
      2
Scaled Schoenfeld residual for patient sex
                       0
      0
                                                                                                              0
                                                     0
      7
                                 0
                                     0
                                                                               0
                                       0
                                  0
      \ddot{\varsigma}
                                                                                 0
```

Looks like there's a violation of CPH with gender. Not unexpected. First check whether there is any evidence of gender interaction.

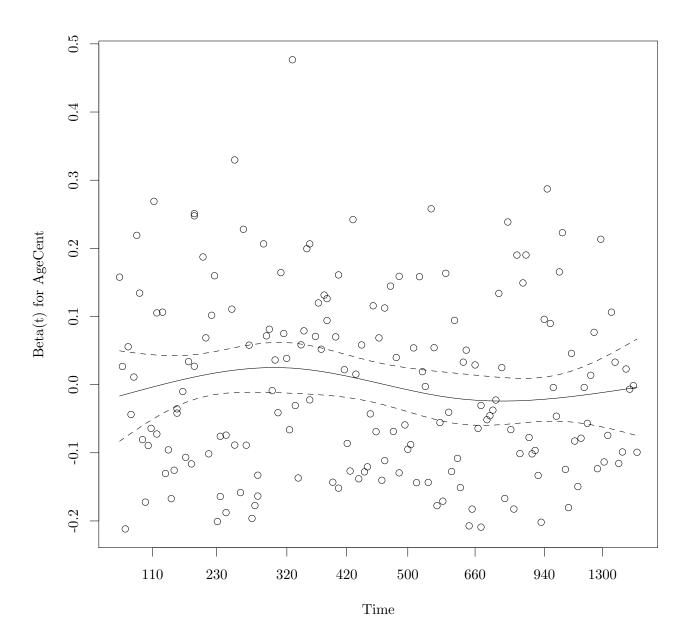
```
anova(coxph(Surv(Time, DSD) ~ SexM*(AgeCent + AgeCent2 + LocBody + SizeCent + SizeSmall + A2 + A4), data
## Analysis of Deviance Table
## Cox model: response is Surv(Time, DSD)
## Terms added sequentially (first to last)
##
```

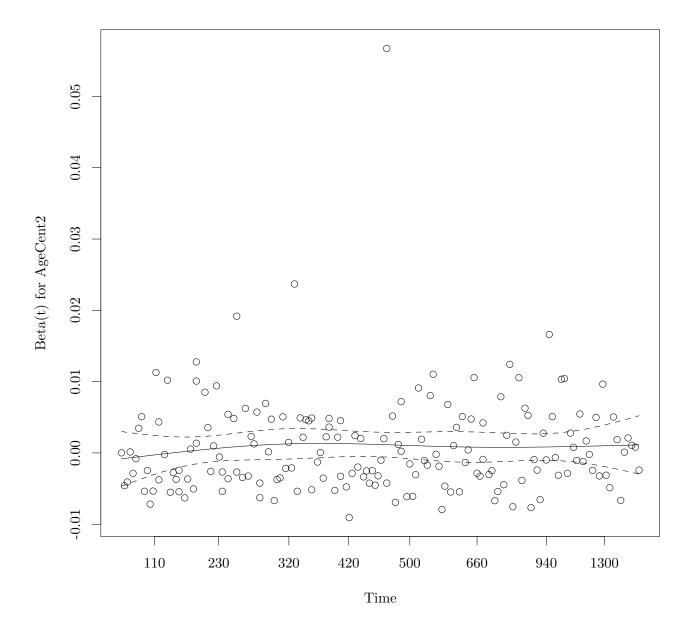
Time

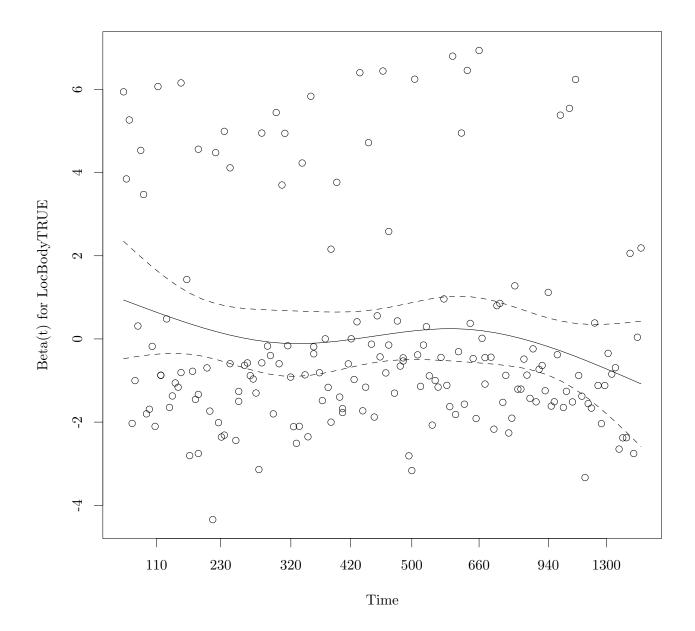
```
loglik Chisq Df Pr(>|Chi|)
                 -748
## NULL
## SexM
                  -748 0.51 1
                                  0.4762
## AgeCent
                  -747 0.19 1
                                  0.6625
## AgeCent2
                  -747 0.81 1
                                  0.3694
## LocBody
                  -746 2.40 1
                                  0.1215
## SizeCent
                  -742 6.82 1
                                  0.0090
## SizeSmall
                  -742 0.00 1
                                  0.9563
## A2
                  -738 9.50 1
                                  0.0021
## A4
                  -734 8.18 1
                                  0.0042
                  -733 0.37 1
## SexM:AgeCent
                                  0.5408
## SexM:AgeCent2
               -733 0.17 1
                                  0.6822
## SexM:LocBody
                -733 0.09 1
                                  0.7654
## SexM:SizeCent
                  -733 0.35 1
                                  0.5568
## SexM:SizeSmall
                  -733 0.06 1
                                  0.8068
## SexM:A2
          -733 0.00 1
                                  0.9588
## SexM:A4
                 -733 0.06 1
                                  0.8000
```

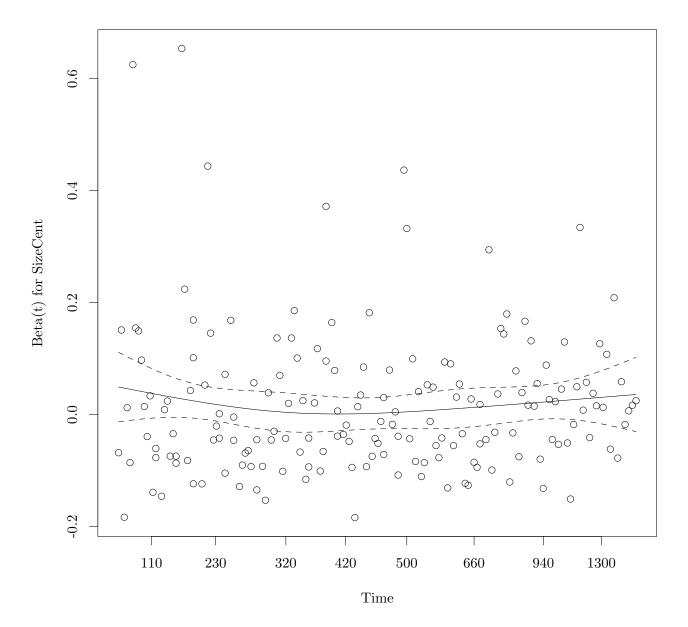
Nope, good. We're not interested in gender effects so just stratify.

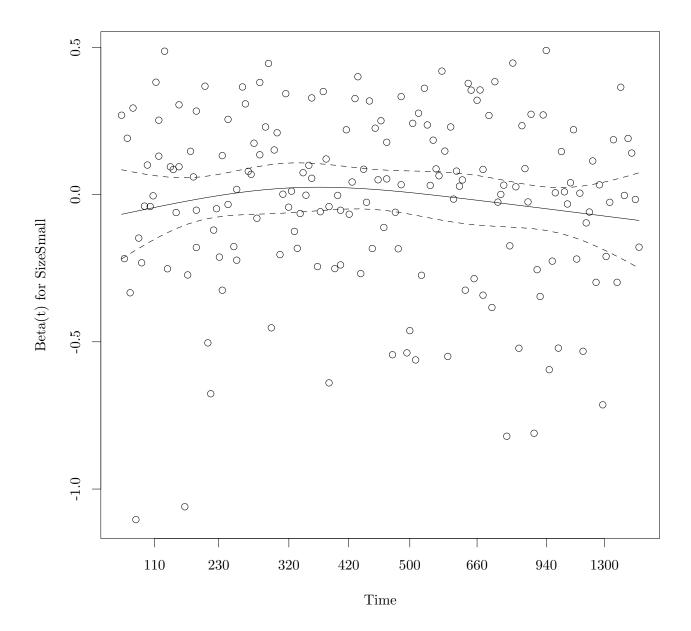
```
fit.cph = coxph(Surv(Time, DSD) ~ strata(SexM) + AgeCent + AgeCent2 + LocBody + SizeCent + SizeSmall + AgeCent2
cox.zph(fit.cph)
##
                   rho chisq
## AgeCent
              -0.07987 1.18163 0.277
## AgeCent2
              0.03673 0.20762 0.649
## LocBodyTRUE -0.10954 1.84364 0.175
## SizeCent
              -0.00689 0.00961 0.922
## SizeSmall -0.04493 0.36247 0.547
## A2TRUE 0.04775 0.40111 0.527
              -0.05491 0.51655 0.472
## A4TRUE
## GLOBAL
                    NA 6.85340 0.444
plot(cox.zph(fit.cph))
```

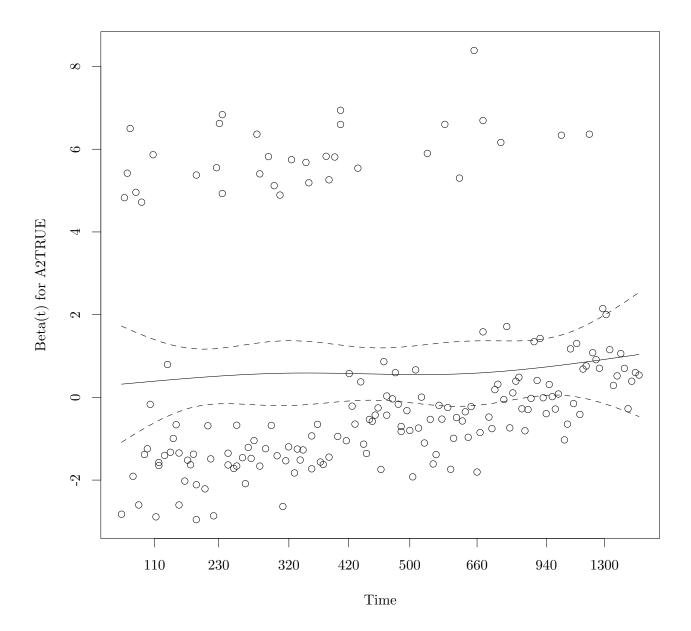


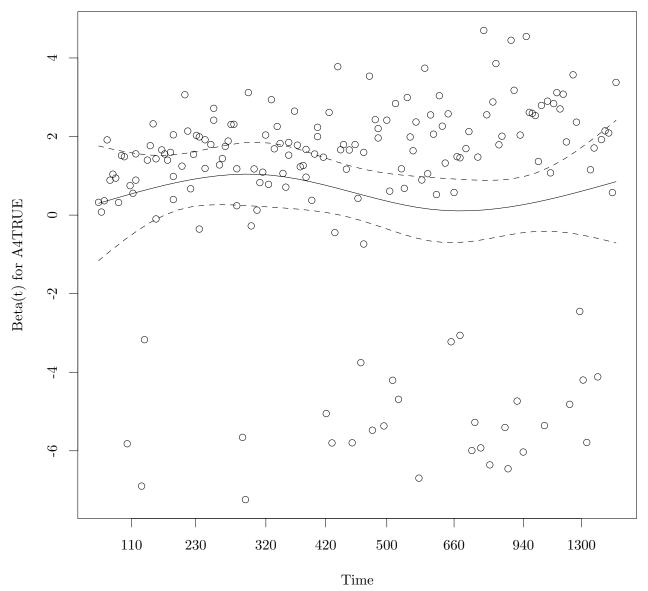






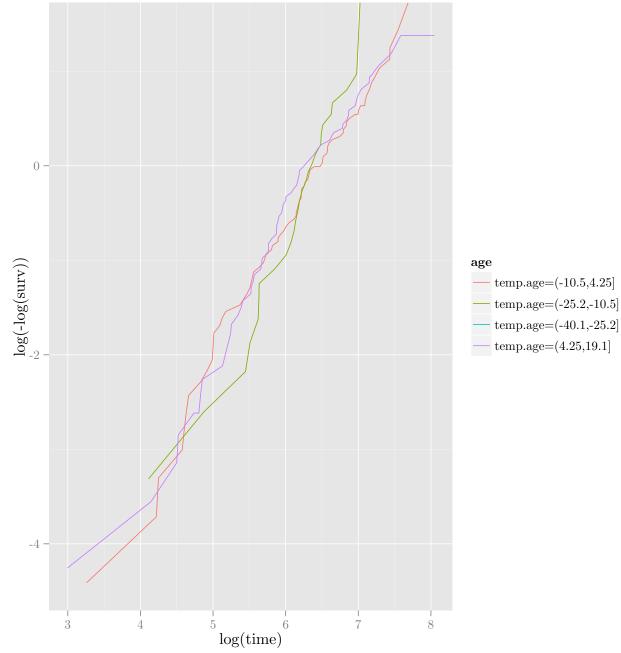






Looks good. Slight snifter with age but I'm not particularly concerned. Split into age groups and do KM plots to verify.

```
temp.age = cut(data$AgeCent, 4)
temp = survfit(Surv(Time, DSD) ~ temp.age, data)
ggplot(data.frame(surv = temp$surv, time = temp$time, age = rep(names(temp$strata), temp$strata)), aes()
```

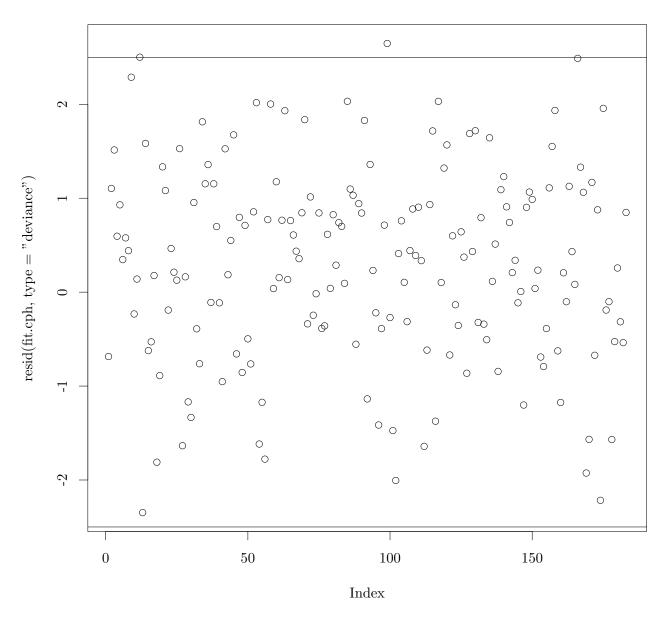


Not perfect but it'll do.

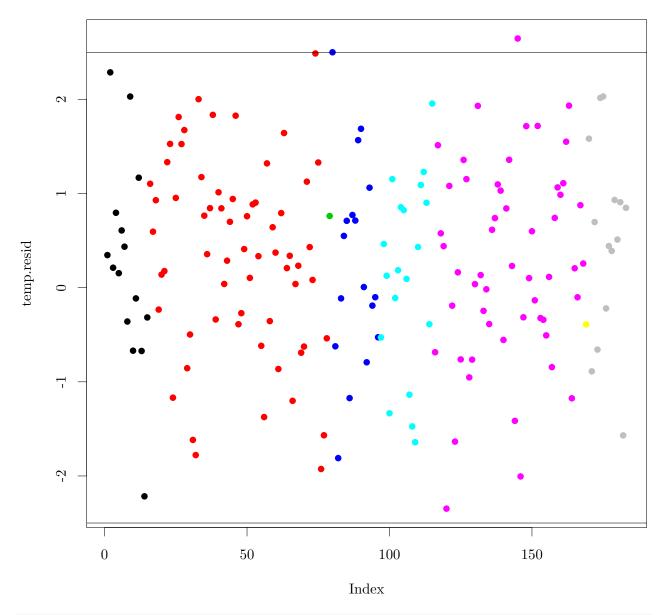
4.3 Outliers: full model

Look at deviance residuals, both marginally and stratified by major subgroups.

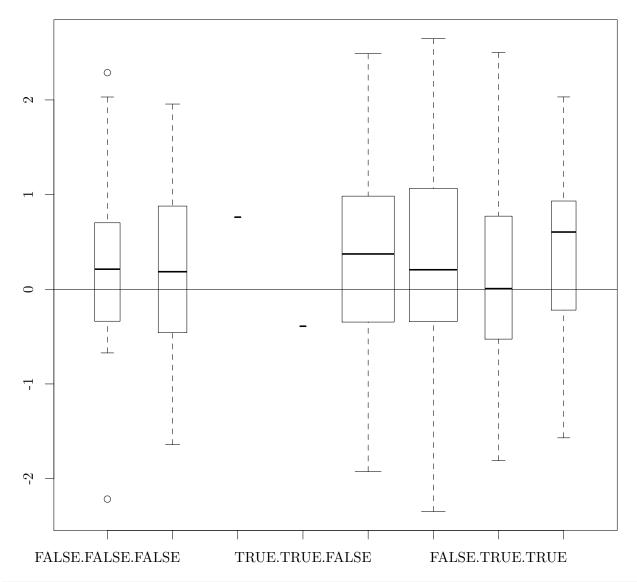
```
plot(resid(fit.cph, type = "deviance"))
abline(h = c(-2.5, 2.5))
```



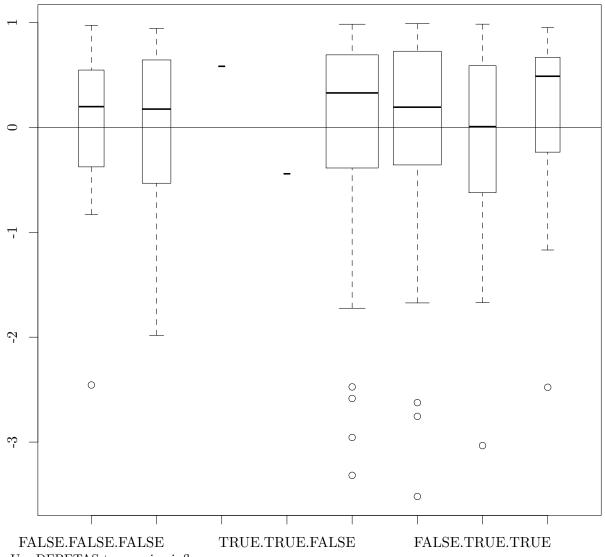
```
temp.ord = order(data$SexM, data$A2, data$A4)
temp.resid = resid(fit.cph, type = "deviance")[temp.ord]
temp.col = (4*data$SexM + 2*data$A2 + data$A4 + 1)[temp.ord]
plot(temp.resid, col = temp.col, pch = 16)
abline(h = c(-2.5, 2.5))
```



boxplot(resid(fit.cph, type = "deviance") ~ data\$SexM + data\$A2 + data\$A4, varwidth = TRUE)
abline(h = 0)

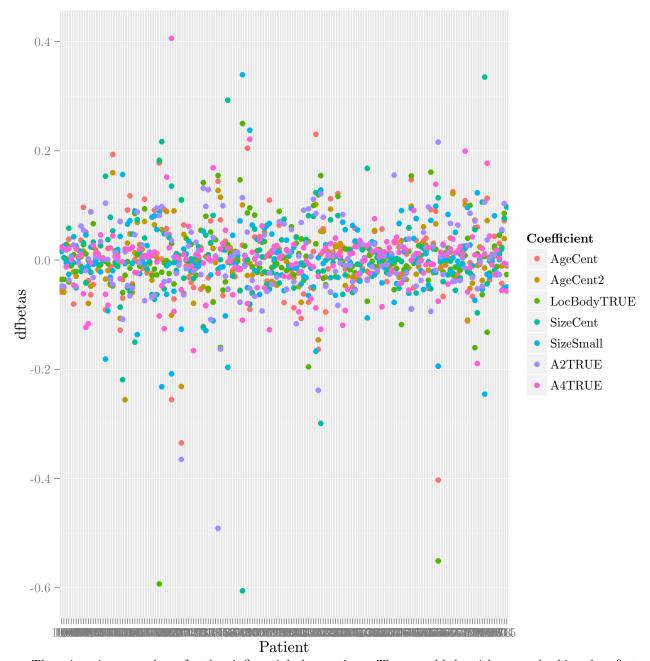


boxplot(resid(fit.cph, type = "martingale") ~ data\$SexM + data\$A2 + data\$A4, varwidth = TRUE)
abline(h = 0)



Use DFBETAS to examine influence.

temp = resid(fit.cph, type = "dfbetas")
colnames(temp) = names(fit.cph\$coefficients)
temp = melt(temp)
colnames(temp) = c("Patient", "Coefficient", "dfbetas")
temp\$Patient = gsub("NSWPCN_", "", temp\$Patient)
ggplot(temp, aes(y = dfbetas, x = Patient, col = Coefficient)) + geom_point()



There is quite a number of rather influential observations. These could do with some checking, but first collapse down the model – there's little point doing dfbeta fucking about based on coefficients that will never get fit in the end anyway.

4.4 EDA: Variable selection

```
nobs.coxph <<- function(obj, ...) sum(obj$y[,2])
# Note: Exhaustive search at level 2 is only feasible for at most 5 variables
#fit.cph.as = glmulti(Surv(Time, DSD) ~ strata(SexM) + AgeCent + AgeCent2 + LocBody + SizeCent + SizeSmall
set.seed(20150110)
fit.cph.as = glmulti(Surv(Time, DSD) ~ strata(SexM) + AgeCent + AgeCent2 + LocBody + SizeCent + SizeSmall
## TASK: Genetic algorithm in the candidate set.</pre>
```

```
## Initialization...
## Algorithm started...
## Warning in fitter(X, Y, strats, offset, init, control, weights = weights, : Loglik converged
before variable 9; beta may be infinite.
## Warning in fitter(X, Y, strats, offset, init, control, weights = weights, : Loglik converged
before variable 12; beta may be infinite.
## Warning in fitter(X, Y, strats, offset, init, control, weights = weights, : Loglik converged
before variable 12; beta may be infinite.
## Warning in fitter(X, Y, strats, offset, init, control, weights = weights, : Loglik converged
before variable 21; beta may be infinite.
## Improvements in best and average IC have bebingo en below the specified goals.
## Algorithm is declared to have converged.
## Completed.
# fit.cph.as
# After 830 generations:
# Best model: Surv(Time, DSD)~1+strata(SexM)+SizeCent+A2+A4
# Crit= 1367.16344569113
# Mean crit= 1401.37248769175
# Improvements in best and average IC have belingo en below the specified goals.
# Algorithm is declared to have converged.
# Completed.
rm(nobs.coxph)
```

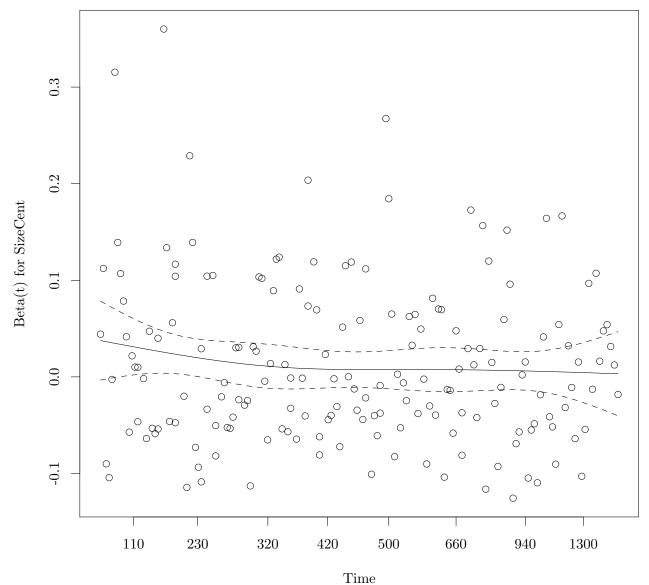
Also run BIC stepwise, because we can.

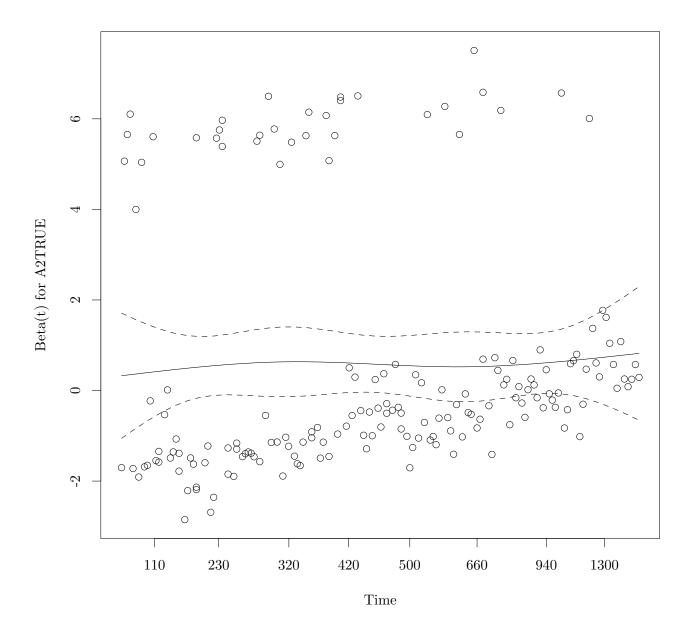
```
stepAIC(fit.cph, k = log(nrow(data)))
## Start: AIC=1269
## Surv(Time, DSD) ~ strata(SexM) + AgeCent + AgeCent2 + LocBody +
      SizeCent + SizeSmall + A2 + A4
##
##
              Df AIC
## - AgeCent
             1 1264
## - LocBody
             1 1264
## - SizeSmall 1 1264
## - AgeCent2 1 1266
## - SizeCent
             1 1267
## <none>
                1269
## - A2
              1 1272
              1 1272
## - A4
## Step: AIC=1264
## Surv(Time, DSD) ~ strata(SexM) + AgeCent2 + LocBody + SizeCent +
      SizeSmall + A2 + A4
##
              Df AIC
##
## - LocBody
              1 1259
## - SizeSmall 1 1259
## - AgeCent2 1 1261
## - SizeCent
             1 1262
## <none>
               1264
## - A2 1 1266
```

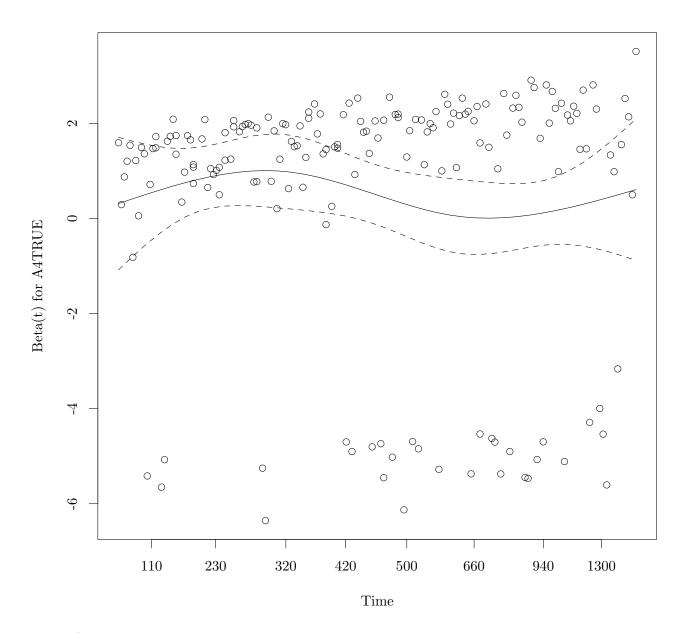
```
## - A4 1 1267
##
## Step: AIC=1259
## Surv(Time, DSD) ~ strata(SexM) + AgeCent2 + SizeCent + SizeSmall +
## A2 + A4
##
##
             Df AIC
## - SizeSmall 1 1254
## - AgeCent2
              1 1256
## - SizeCent 1 1257
## <none>
              1259
## - A2
             1 1261
## - A4
             1 1262
##
## Step: AIC=1254
## Surv(Time, DSD) ~ strata(SexM) + AgeCent2 + SizeCent + A2 + A4
##
           Df AIC
## - AgeCent2 1 1252
## - SizeCent 1 1253
## <none> 1254
## - A2
            1 1257
## - A4
             1 1257
##
## Step: AIC=1252
## Surv(Time, DSD) ~ strata(SexM) + SizeCent + A2 + A4
##
           Df AIC
## - SizeCent 1 1250
## <none>
             1252
## - A4
             1 1253
## - A2
            1 1254
##
## Step: AIC=1250
## Surv(Time, DSD) ~ strata(SexM) + A2 + A4
##
## Df AIC
## <none> 1250
## - A4 1 1254
## - A2 1 1254
## Call:
## coxph(formula = Surv(Time, DSD) ~ strata(SexM) + A2 + A4, data = data)
##
         coef exp(coef) se(coef) z
## A2TRUE 0.630 1.88 0.201 3.14 0.0017
## A4TRUE 0.556
                  1.74 0.203 2.74 0.0061
##
## Likelihood ratio test=19.8 on 2 df, p=4.97e-05 n= 183, number of events= 175
```

Consensus, excellent.

4.5 PH assumption: reduced model

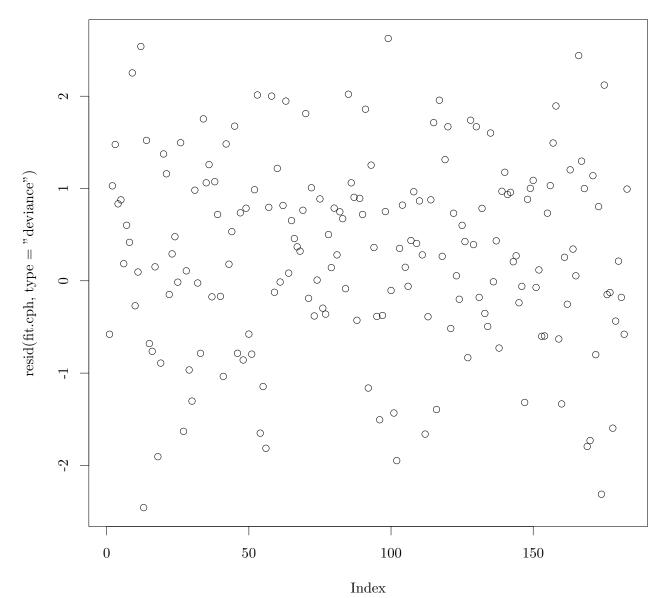






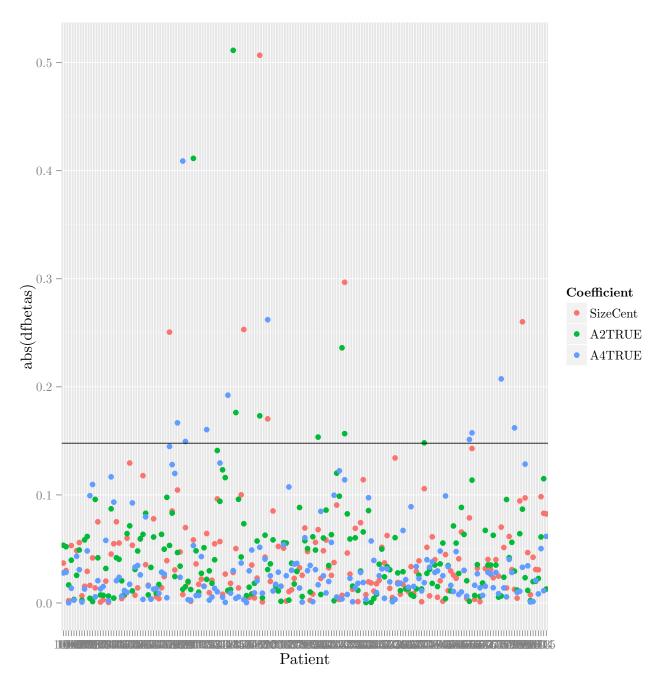
4.6 Outliers: reduced model

```
plot(resid(fit.cph, type = "deviance"))
```



Now generate the restricted fit and examine the DFBETAS on the reduced model.

```
temp = resid(fit.cph, type = "dfbetas")
colnames(temp) = names(fit.cph$coefficients)
temp = melt(temp)
colnames(temp) = c("Patient", "Coefficient", "dfbetas")
temp$Patient = gsub("NSWPCN_", "", temp$Patient)
2/sqrt(nrow(data))  # The classic threshold for concern is 2/sqrt(n).
## [1] 0.1478
ggplot(temp, aes(y = abs(dfbetas), x = Patient, col = Coefficient)) + geom_point() + geom_hline(yintercent)
```



sort(apply(abs(resid(fit.cph, type = "dfbetas")), 1, max), decreasing = TRUE) ## NSWPCN_144 NSWPCN_183 NSWPCN_1212 NSWPCN_1195 NSWPCN_318 NSWPCN_195 ## 0.511340 0.506815 0.411412 0.408937 0.296728 0.262110 ## NSWPCN_799 NSWPCN_154 NSWPCN_1182 NSWPCN_317 NSWPCN_777 NSWPCN_142 ## 0.260153 0.253014 0.250597 0.236114 0.207351 0.192280 NSWPCN_145 NSWPCN_1188 NSWPCN_795 NSWPCN_125 NSWPCN_655 NSWPCN_296 ## ## 0.176188 0.166665 0.162051 0.160416 0.157420 0.153478 ## NSWPCN_654 NSWPCN_1196 NSWPCN_374 NSWPCN_131 NSWPCN_354 NSWPCN_133 ## 0.151246 0.149449 0.148152 0.141058 0.134170 0.129507 NSWPCN_802 NSWPCN_1186 NSWPCN_135 NSWPCN_316 NSWPCN_315 ## NSWPCN_1155 0.129471 ## 0.128471 0.128036 0.123203 0.122328 0.120121 ## NSWPCN_1187 NSWPCN_1167 NSWPCN_1143 NSWPCN_138 NSWPCN_814 NSWPCN_333

```
##
     NSWPCN_1072 NSWPCN_269 NSWPCN_152 NSWPCN_312 NSWPCN_1071 NSWPCN_636
                                                 0.099250
##
     0.109648
                0.107374
                          0.100089
                                      0.099732
                                                           0.099010
##
   NSWPCN_813 NSWPCN_1179 NSWPCN_335 NSWPCN_1453 NSWPCN_1082 NSWPCN_789
##
     0.098347
                0.097750
                         0.097415
                                      0.095938
                                               0.095841
                                                          0.095735
##
   NSWPCN_798 NSWPCN_1145 NSWPCN_1157 NSWPCN_364 NSWPCN_647 NSWPCN_276
##
     0.094433
                0.093340
                           0.092592
                                      0.089047
                                               0.088390
                                                          0.088343
##
   NSWPCN_305 NSWPCN_200 NSWPCN_303 NSWPCN_1168 NSWPCN_322 NSWPCN_815
##
     0.085945
              0.085147
                           0.084780
                                    0.082972
                                               0.082445
                                                          0.082391
  NSWPCN_1172 NSWPCN_1146 NSWPCN_1088 NSWPCN_331 NSWPCN_640 NSWPCN_281
##
     0.077888
              0.075122
                          0.075085
                                      0.074289
                                               0.071269
                                                           0.069418
##
   NSWPCN_326 NSWPCN_664 NSWPCN_360 NSWPCN_1153 NSWPCN_1177 NSWPCN_651
##
##
     0.069060
              0.067170
                         0.067089
                                      0.064155
                                                 0.063501
                                                          0.063455
   NSWPCN_310 NSWPCN_194 NSWPCN_769 NSWPCN_351 NSWPCN_1029 NSWPCN_790
##
              0.062687
                         0.062634
                                      0.062402
                                               0.061529
##
     0.063192
                                                            0.061523
   NSWPCN_284 NSWPCN_377 NSWPCN_304 NSWPCN_1165 NSWPCN_324 NSWPCN_1028
##
              0.061213
                         0.060116
                                    0.059436
                                               0.059216
##
     0.061268
                                                           0.058363
  NSWPCN_1139 NSWPCN_336 NSWPCN_182 NSWPCN_794 NSWPCN_294 NSWPCN_1023
##
##
     0.057912
              0.057377
                         0.057341
                                    0.056127
                                               0.056116
                                                           0.055877
   NSWPCN_257 NSWPCN_445 NSWPCN_1147 NSWPCN_268 NSWPCN_643 NSWPCN_13
##
##
     0.055813
                0.055469 0.055464
                                      0.055426
                                               0.055403
                                                           0.054730
    NSWPCN_10 NSWPCN_1019 NSWPCN_24 NSWPCN_1016 NSWPCN_347 NSWPCN_375
##
##
     0.053392
                0.053156 0.052313
                                      0.052050
                                               0.051517
                                                           0.051489
##
   NSWPCN_781 NSWPCN_1227 NSWPCN_282 NSWPCN_1178 NSWPCN_164 NSWPCN_1022
     0.051333
                0.051115 0.050311
                                      0.049749
                                               0.048995
                                                           0.048464
##
                         NSWPCN_4 NSWPCN_1190 NSWPCN_804 NSWPCN_1219
##
  NSWPCN_1213 NSWPCN_1160
              0.048105 0.048021
##
     0.048263
                                      0.047256
                                               0.046638
                                                          0.042923
##
   NSWPCN_807 NSWPCN_646 NSWPCN_666 NSWPCN_381 NSWPCN_770 NSWPCN_341
##
     0.042281
              0.040889
                         0.040225
                                      0.040068
                                               0.040056
                                                          0.039362
##
   NSWPCN_370 NSWPCN_350 NSWPCN_270 NSWPCN_273
                                               NSWPCN_20 NSWPCN_272
##
     0.038992
              0.037026 0.036778
                                      0.036591
                                               0.036201
                                                          0.035952
   NSWPCN_346 NSWPCN_657 NSWPCN_7 NSWPCN_283 NSWPCN_309 NSWPCN_637
##
##
     0.035888
              0.035464
                         0.035127
                                      0.034719
                                                0.034677
                                                            0.034559
##
   NSWPCN_369 NSWPCN_1158 NSWPCN_376 NSWPCN_1171 NSWPCN_810 NSWPCN_352
##
     0.033701
              0.033208 0.033132
                                      0.032882
                                               0.030954
                                                           0.030734
##
   NSWPCN_811 NSWPCN_126 NSWPCN_161 NSWPCN_384 NSWPCN_638 NSWPCN_358
                         0.029730
                                      0.029667
                                               0.029548
                                                            0.027843
##
     0.030726
              0.029736
   NSWPCN_280 NSWPCN_775 NSWPCN_362 NSWPCN_128 NSWPCN_653 NSWPCN_1150
##
##
     0.025663
              0.024846 0.021612
                                    0.020969
                                               0.020569
                                                          0.020533
##
  NSWPCN_1207 NSWPCN_662 NSWPCN_36 NSWPCN_330 NSWPCN_143 NSWPCN_166
                         0.018340
##
     0.019948
              0.018477
                                      0.018191
                                                0.018187
                                                           0.018185
##
   NSWPCN_345 NSWPCN_1215 NSWPCN_21 NSWPCN_1176 NSWPCN_1018 NSWPCN_656
##
     0.017812
              0.017340
                         0.017265
                                      0.017131
                                                 0.016678
                                                          0.016425
  NSWPCN_1170 NSWPCN_325 NSWPCN_256 NSWPCN_366 NSWPCN_1136 NSWPCN_363
##
##
     0.016398
                0.015592
                           0.015547
                                      0.015304
                                                 0.015192
                                                            0.014593
   NSWPCN_658 NSWPCN_1175 NSWPCN_1091 NSWPCN_373 NSWPCN_1211 NSWPCN_797
##
     0.014004
               0.013425
                           0.013036
                                    0.012972
                                               0.012450
                                                            0.011917
                                   NSWPCN_806 NSWPCN_157 NSWPCN_1027
## NSWPCN_1152 NSWPCN_190 NSWPCN_334
              0.009024
                          0.007702
                                      0.007660
                                               0.006790
                                                            0.006582
##
     0.011502
## NSWPCN_1140 NSWPCN_353 NSWPCN_1020
     0.006373
              0.005084
                           0.003220
##
sum(apply(abs(resid(fit.cph, type = "dfbetas")), 1, max) > 2/sqrt(nrow(data)))
## [1] 21
```

4.7 Summary of EDA

- 1. On the basis of pre-operative assessability and data availability, variables were filtered down to Sex, AgeCent, LocBody, SizeCent, A2, A4.
- 2. Functional forms for the continuous variates AgeCent and SizeCent indicated a possible slight quadratic effect on AgeCent, and a knee on SizeCent. These were modelled by incorporating additional terms.
- 3. Analysis of a full model fit (with additional nonlinear terms included) indicated violation of PH for gender. This was dealt with by stratification. A slight PH violation by age was deemed unimportant.
- 4. Variable selection by BIC (both stepwise and genetic all-subset) settled on a final model of Surv(Time,DSD) $\sim 1 + \text{strata(SexM)} + \text{SizeCent} + \text{A2} + \text{A4}$. This model was refit by coxph.
- 5. PH was verified on the final model. Deviance residuals showed no egregious outliers. dfBetaS indicated a number of influential observations, which require checking.

5 Final fits

```
fit.cph = coxph(Surv(Time, DSD) ~ strata(SexM) + SizeCent + A2 + A4, data = data)
```

```
set.seed(20150111)
fit.rsf = rfsrc(Surv(Time, DSD) ~ SexM + AgeCent + LocBody + SizeCent + A2 + A4, data = data, mtry = 1,
```

```
fit.gg = flexsurvreg(Surv(Time, DSD) ~ SexM + SizeCent + A2 + A4,
        anc = list(
                 sigma = ~ SexM,
                 Q = \sim SexM),
        data = data, dist = "gengamma")
fit.gf = flexsurvreg(Surv(Time, DSD) ~ SexM + SizeCent + A2 + A4,
        anc = list(
                 sigma = ^{\sim} SexM,
                 Q = ^{\sim} SexM,
                 P = ^{\sim} SexM),
        data = data, dist = "genf")
fit.gg$loglik
## [1] -1263
fit.gf$loglik
## [1] -1262
pchisq(2*(fit.gf$loglik - fit.gg$loglik), 2, lower.tail = FALSE)
## [1] 0.3625
AIC(fit.gg)
## [1] 2545
AIC(fit.gf)
```

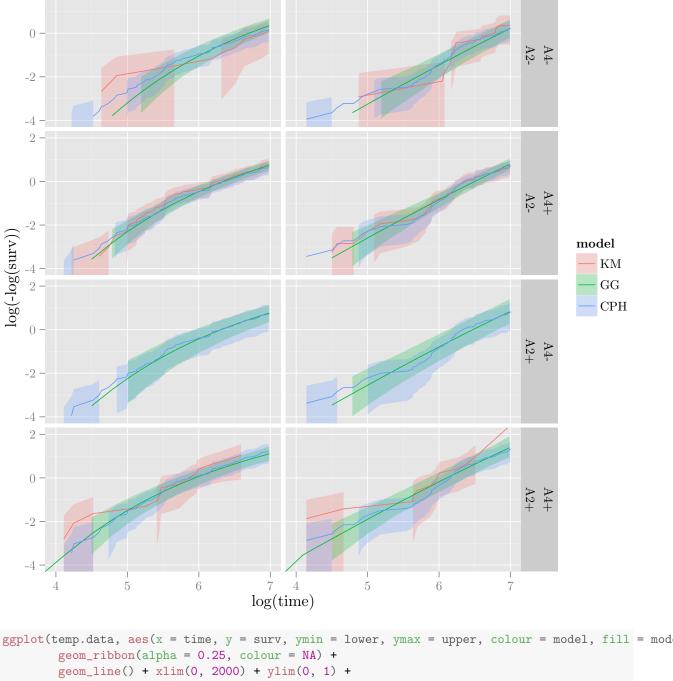
```
## [1] 2547
BIC(fit.gg)
## [1] 2574
BIC(fit.gf)
## [1] 2582
fit.gg
##
## Call:
## flexsurvreg(formula = Surv(Time, DSD) ~ SexM + SizeCent + A2 + A4, anc = list(sigma = ~SexM, Q =
## Estimates:
##
                   data mean est
                                      L95%
                                                U95%
## mu
                       NA
                              6.44681 6.07286
                                                6.82076
                                                           0.19079
                            0.80245 0.69416
                                                0.92763
## sigma
                        NA
                                                          0.05935
                            0.06179 -0.51053
## Q
                        NA
                                                0.63411
                                                           0.29201
                            0.38255 0.03482
## SexMTRUE
                   0.47541
                                                0.73028
                                                           0.17742
## SizeCent
                    3.18579
                             -0.00953 -0.01742 -0.00164 0.00403
## A2TRUE
                    0.18033
                            -0.38859 -0.66061 -0.11657 0.13879
                            -0.36208 -0.63874 -0.08542
## A4TRUE
                   0.80328
                                                          0.14116
## sigma(SexMTRUE) 0.47541
                            -0.25308 -0.49389
                                                -0.01227
                                                           0.12287
## Q(SexMTRUE)
                  0.47541
                            0.78916 0.03792
                                                1.54039
                                                          0.38329
##
                   exp(est) L95% U95%
## mu
                        NA
                                  NA
                                           NA
## sigma
                        NA
                                  NA
                                            NA
                        NA
## Q
                                  NA
                                            NΑ
## SexMTRUE
                   1.46602
                            1.03543
                                       2.07567
## SizeCent
                   0.99052
                            0.98274
                                      0.99837
## A2TRUE
                    0.67801
                             0.51653
                                       0.88997
## A4TRUE
                    0.69623
                             0.52796
                                      0.91812
## sigma(SexMTRUE)
                    0.77640
                             0.61025
                                       0.98781
## Q(SexMTRUE)
                    2.20154
                             1.03865
                                       4.66643
##
## N = 183, Events: 175, Censored: 8
## Total time at risk: 106023
## Log-likelihood = -1263, df = 9
## AIC = 2545
```

6 Fit assessment

Plot fit stratified by sex, separate curves for A2, A4 status, at median (approx.) Size.

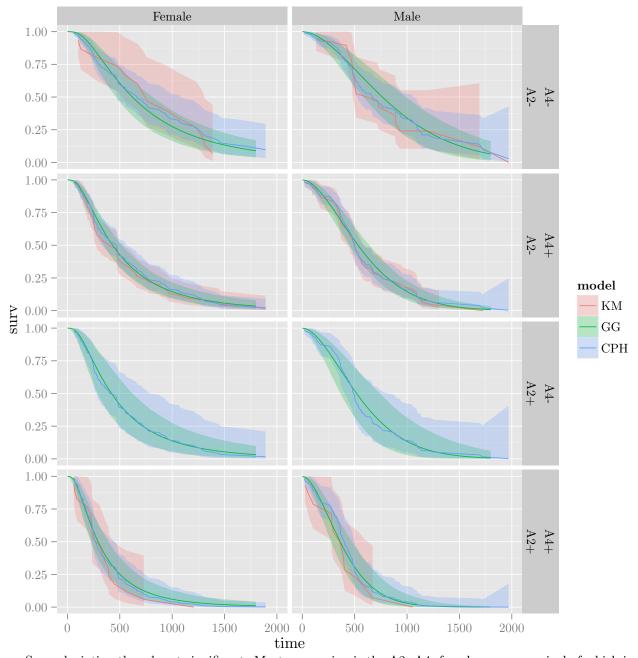
```
temp.grid = expand.grid(A4 = c(FALSE, TRUE), A2 = c(FALSE, TRUE), SexM = c(FALSE, TRUE), SizeCent = 0)
temp.grid$ID = sprintf("SexM=%s, A2=% -5s, A4=% -5s", temp.grid$SexM, temp.grid$A2, temp.grid$A4)
temp.preds = summary(fit.gg, newdata = temp.grid, type = "survival", t = seq(0, 365*5, 30))
temp.preds2 = do.call(rbind, temp.preds)
temp.preds2$group = rep(gsub(".*ID=", "", names(temp.preds)), each = nrow(temp.preds[[1]]))
temp.preds.cox = survfit(fit.cph, newdata = temp.grid)
```

```
temp.survfit = survfit(Surv(Time, DSD) ~ SexM + A2 + A4, data)
temp.data = data.frame(time = temp.survfit$time, surv = temp.survfit$surv, upper = temp.survfit$lower,
temp.data = rbind(temp.data, data.frame(time = temp.preds2$time, surv = temp.preds2$est, upper = temp.preds2$time, surv =
temp.data = rbind(temp.data, data.frame(time = temp.preds.cox$time, surv = temp.preds.cox$surv, upper =
temp.data$Sex = c("Male", "Female")[grepl("SexM=FALSE", temp.data$group)+1]
temp.dataA2 = c(A2-, A2+)[grep1(A2=TRUE, temp.data$group)+1]
temp.data$A4 = c("A4-", "A4+")[grepl("A4=TRUE", temp.data$group)+1]
ggplot(temp.data, aes(x = log(time), y = log(-log(surv)), ymin = log(-log(lower)), ymax = log(-log(upper))
                    geom_ribbon(alpha = 0.25, colour = NA) +
                    geom_line() +
                    xlim(4, 7) + ylim(-4, 2) +
                    facet_grid(A2 ~ A4 ~ Sex)
## Warning: Removed 46 rows containing missing values (geom_path).
## Warning: Removed 39 rows containing missing values (geom_path).
## Warning: Removed 48 rows containing missing values (geom_path).
## Warning: Removed 43 rows containing missing values (geom_path).
## Warning: Removed 39 rows containing missing values (geom_path).
## Warning: Removed 36 rows containing missing values (geom_path).
## Warning: Removed 40 rows containing missing values (geom_path).
## Warning: Removed 37 rows containing missing values (geom_path).
```



Male

Female



Some deviation though not significant. Most concerning is the A2- A4- female group, survival of which is underestimated by the flexsurv model. To approach this in a modelling sense would require interaction terms between Sex and A2, A4. Overfitting seems likely considering the very few data available for the A2+/A4-group. Perhaps just add a single "DoubleNegFemale" term.

```
## Call:
## flexsurvreg(formula = Surv(Time, DSD) ~ SexM + SizeCent + A2 + A4 + I(SexM == FALSE & A2 == FALSI
## Estimates:
##
                                                    data mean est
                                                               6.37090
## mu
                                                         NA
## sigma
                                                          NA
                                                               0.79990
## Q
                                                          NA
                                                             0.09541
## SexMTRUE
                                                     0.47541 0.40816
## SizeCent
                                                     3.18579
                                                             -0.00941
## A2TRUE
                                                     0.18033
                                                              -0.38417
## A4TRUE
                                                     0.80328
                                                             -0.29393
## I(SexM == FALSE & A2 == FALSE & A4 == FALSE)TRUE 0.08197
                                                             0.19993
## sigma(SexMTRUE)
                                                     0.47541
                                                              -0.25570
## Q(SexMTRUE)
                                                     0.47541
                                                               0.76926
##
                                                    L95%
                                                             U95%
## mu
                                                     5.95233 6.78948
## sigma
                                                     0.69156 0.92521
## Q
                                                    -0.46926 0.66007
## SexMTRUE
                                                     0.05768 0.75863
## SizeCent
                                                    -0.01726 -0.00156
## A2TRUE
                                                    -0.65634 -0.11200
## A4TRUE
                                                    -0.62047 0.03260
## I(SexM == FALSE & A2 == FALSE & A4 == FALSE)TRUE -0.35382 0.75369
## sigma(SexMTRUE)
                                                    -0.49656 -0.01485
## Q(SexMTRUE)
                                                     0.02665
                                                             1.51187
##
                                                             exp(est)
## mu
                                                     0.21356
## sigma
                                                     0.05939
                                                                   NΑ
## Q
                                                     0.28810
                                                                   NA
## SexMTRUE
                                                     0.17882 1.50404
## SizeCent
                                                     0.00401 0.99064
                                                     0.13886 0.68102
## A2TRUE
## A4TRUE
                                                     0.16660 0.74533
## I(SexM == FALSE & A2 == FALSE & A4 == FALSE)TRUE 0.28253 1.22132
## sigma(SexMTRUE)
                                                     0.12289
                                                             0.77437
                                                             2.15816
## Q(SexMTRUE)
                                                     0.37889
                                                    L95%
                                                             U95%
##
## mu
                                                         NA
                                                                   NA
## sigma
                                                         NA
                                                                   NA
## Q
                                                          NA
                                                                   NA
                                                     1.05938
## SexMTRUE
                                                             2.13535
## SizeCent
                                                     0.98289
                                                             0.99844
## A2TRUE
                                                              0.89404
                                                     0.51875
## A4TRUE
                                                     0.53769
                                                              1.03313
## I(SexM == FALSE & A2 == FALSE & A4 == FALSE)TRUE 0.70200
                                                              2.12482
## sigma(SexMTRUE)
                                                     0.60862 0.98526
## Q(SexMTRUE)
                                                     1.02701
                                                              4.53518
## N = 183, Events: 175, Censored: 8
## Total time at risk: 106023
## Log-likelihood = -1263, df = 10
## AIC = 2546
```

```
AIC(fit.gg)

## [1] 2545

AIC(fit.gg2)

## [1] 2546

AIC(fit.gg) - AIC(fit.gg2)

## [1] -1.505

# Equivocal on AIC. BIC would favour gg then.

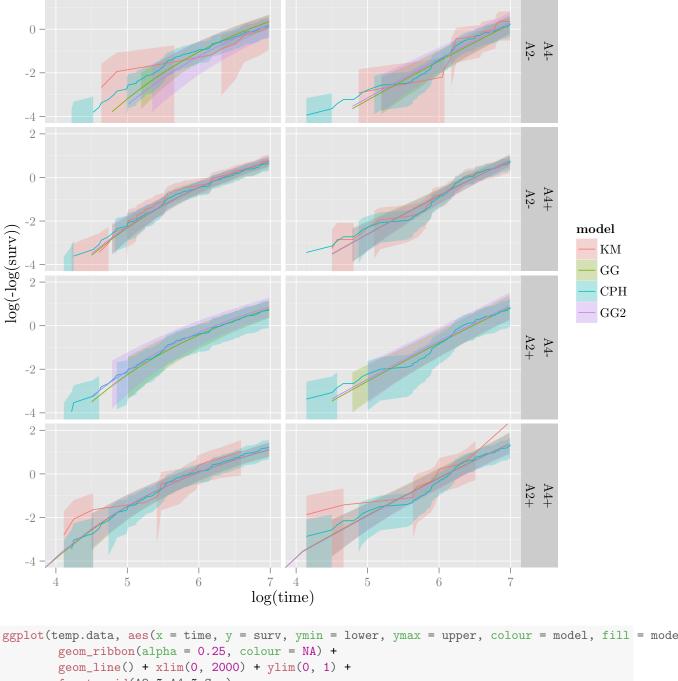
pchisq(-2*(fit.gg$loglik - fit.gg2$loglik), 1, lower.tail = FALSE)

## [1] 0.4815

# Not good evidence on LRT
```

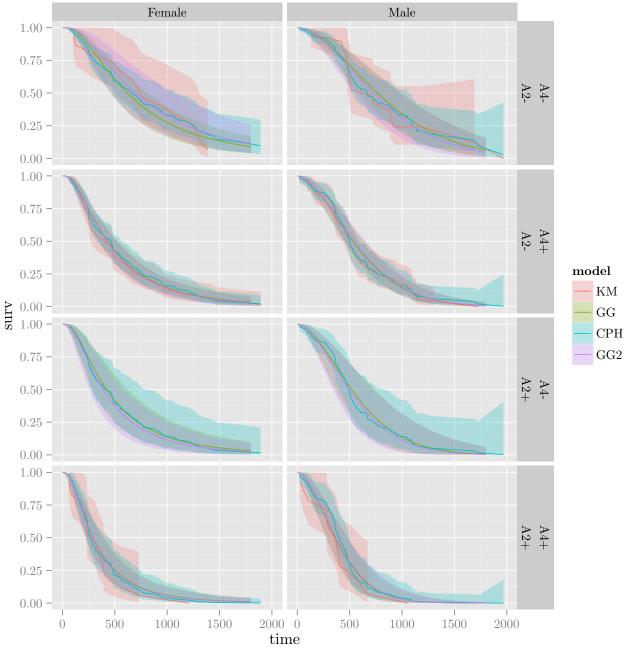
See how it plots relative to the others.

```
temp.preds = summary(fit.gg2, newdata = temp.grid, type = "survival", t = seq(0, 365*5, 30))
temp.preds2 = do.call(rbind, temp.preds)
temp.preds2$group = rep(gsub(".*ID=", "", names(temp.preds)), each = nrow(temp.preds[[1]]))
temp.data = rbind(temp.data, data.frame(time = temp.preds2$time, surv = temp.preds2$est, upper = temp.pr
temp.data$Sex = c("Male", "Female")[grep1("SexM=FALSE", temp.data$group)+1]
temp.dataA2 = c("A2-", "A2+")[grep1("A2=TRUE", temp.data$group)+1]
temp.data$A4 = c("A4-", "A4+")[grepl("A4=TRUE", temp.data$group)+1]
ggplot(temp.data, aes(x = log(time), y = log(-log(surv)), ymin = log(-log(lower)), ymax = log(-log(upper))
        geom_ribbon(alpha = 0.25, colour = NA) +
        geom_line() +
        xlim(4, 7) + ylim(-4, 2) +
        facet_grid(A2 ~ A4 ~ Sex)
## Warning: Removed 71 rows containing missing values (geom_path).
## Warning: Removed 64 rows containing missing values (geom_path).
## Warning: Removed 73 rows containing missing values (geom_path).
## Warning: Removed 68 rows containing missing values (geom_path).
## Warning: Removed 64 rows containing missing values (geom_path).
## Warning: Removed 61 rows containing missing values (geom_path).
## Warning: Removed 65 rows containing missing values (geom_path).
## Warning: Removed 62 rows containing missing values (geom_path).
```



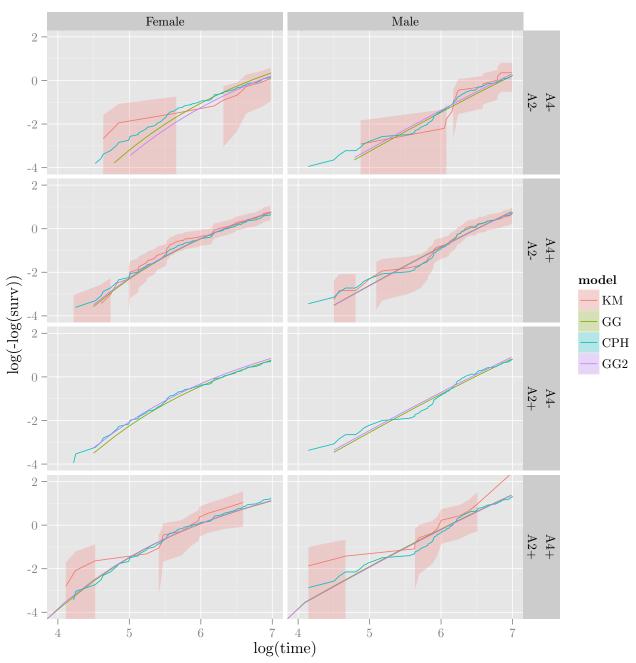
Male

Female

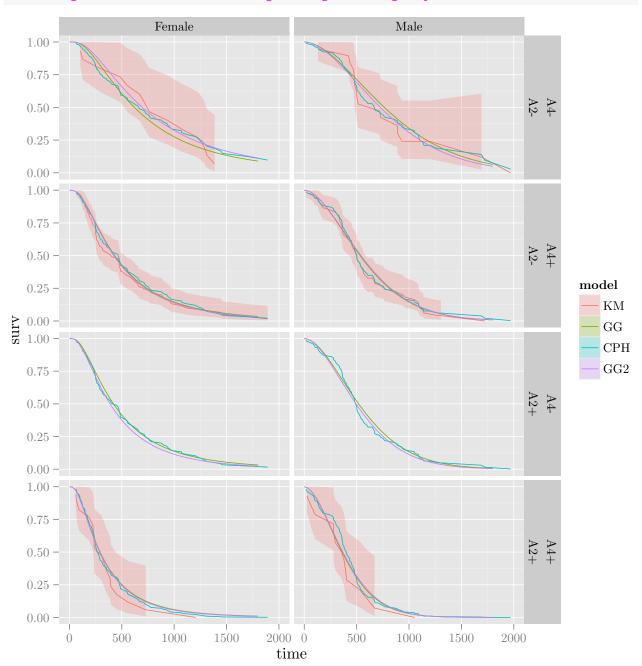


An alternative take, showing errors with the KMs only.

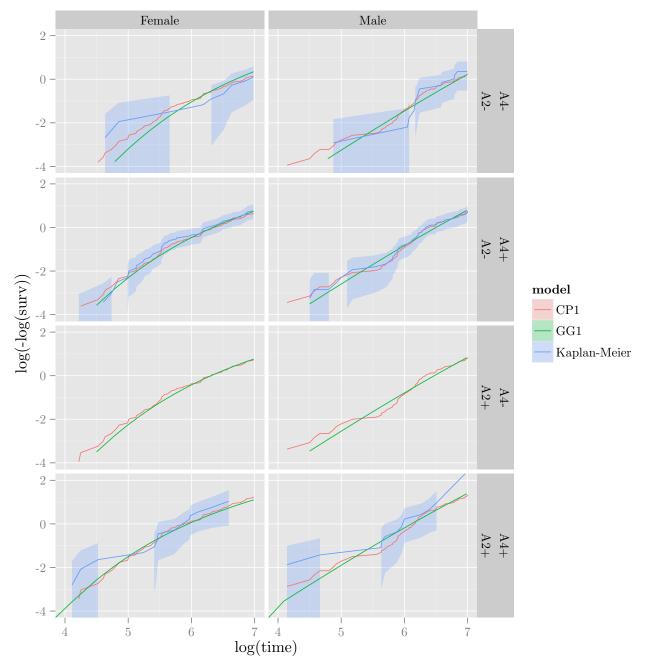
```
## Warning: Removed 64 rows containing missing values (geom_path).
## Warning: Removed 61 rows containing missing values (geom_path).
## Warning: Removed 65 rows containing missing values (geom_path).
## Warning: Removed 62 rows containing missing values (geom_path).
```

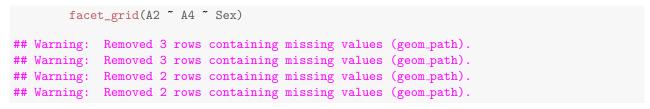


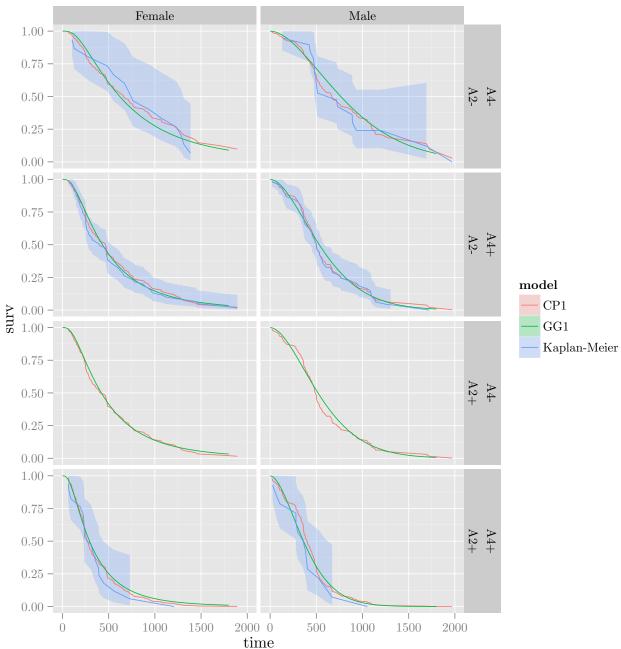
```
## Warning: Removed 2 rows containing missing values (geom_path).
## Warning: Removed 2 rows containing missing values (geom_path).
```



```
## Warning:
             Removed 46 rows containing missing values (geom_path).
## Warning:
             Removed 39 rows containing missing values (geom_path).
## Warning:
             Removed 48 rows containing missing values (geom_path).
## Warning:
             Removed 43 rows containing missing values (geom_path).
             Removed 39 rows containing missing values (geom_path).
## Warning:
## Warning:
             Removed 36 rows containing missing values (geom_path).
## Warning:
             Removed 40 rows containing missing values (geom_path).
## Warning:
             Removed 37 rows containing missing values (geom_path).
```







7 Model selection

It looks like that's as far as we can go with tweaking the fits. Time to put the different models against each other on the holdout data, and choose a winner.

DIY IBS, wooo.

```
calcIBS = function(surv, pred, pred_times, max_time)
        stopifnot(nrow(surv) == nrow(pred) && length(pred_times) == ncol(pred))
        n = nrow(surv)
       marg_survfit = survfit(surv ~ 1)
        marg_censfit = survfit(Surv(surv[,1], !surv[,2]) ~ 1)
        marg_surv_func = approxfun(marg_survfit$time, marg_survfit$surv, method = "constant", yleft = 1
        marg_cens_func = approxfun(marg_censfit$time, marg_censfit$surv, method = "constant", yleft = 1
        pred_funcs = apply(pred, 1, function(pat_preds) approxfun(pred_times, pat_preds, yleft = 1, yrig
        indiv_patient_bsc = function(pat_i, tstars)
                observed_time = surv[pat_i, 1]
                observed_event = surv[pat_i, 2]
                pred_func = pred_funcs[[pat_i]]
                category = 1*(observed_time <= tstars & observed_event) + 2*(observed_time > tstars) + 3
                bsc = rep(NA, length(tstars))
                bsc[category == 1] = pred_func(tstars[category == 1])^2 / marg_cens_func(observed_time)
                bsc[category == 2] = (1 - pred_func(tstars[category == 2]))^2 / marg_cens_func(tstars[category == 2]))
                bsc[category == 3] = 0
                bsc
        bsc_func = function(tstars) { rowMeans(sapply(1:n, function(pat_i) indiv_patient_bsc(pat_i, tstate))
        weight_func = function(tstars) { (1 - marg_surv_func(tstars)) / (1 - marg_surv_func(max_time)) }
        # Be slack and do trapezoidal int. with a fine grid. It should be possible
        # to calulate the int. exactly but I cbfed.
        int_grid = seq(0, max_time, length.out = 1e3)
        bsc_vals = bsc_func(int_grid)
        weight_vals = weight_func(int_grid)
        int_vals = bsc_vals * weight_vals
        ibsc = (2*sum(int_vals) - int_vals[1] - int_vals[length(int_vals)]) * (diff(range(int_grid))) /
        return(list(bsc = bsc_vals, weights = weight_vals, eval_times = int_grid, ibsc = ibsc))
```

Calculate survival probability predictions for each of the models, on the validation data.

```
ibs_times = sort(unique(data.val$Time))
ibs_preds_gg = as.matrix(t(sapply(summary(fit.gg, newdata = data.val, type = "survival", t = ibs_times)
ibs_preds_gg2 = as.matrix(t(sapply(summary(fit.gg2, newdata = data.val, type = "survival", t = ibs_times)
temp_cox_preds = survfit(fit.cph, newdata = data.val)
ibs_preds_cph = simplify2array(tapply(1:length(temp_cox_preds$time), rep(names(temp_cox_preds$strata), re
```

```
temp_km0 = survfit(Surv(Time, DSD) ~ 1, data)
ibs_preds_km0 = t(matrix(rep(approx(temp_km0$time, temp_km0$surv, xout = ibs_times, method = "constant"
ibs_preds_all = list(gg = ibs_preds_gg, gg2 = ibs_preds_gg2, cph = ibs_preds_cph, rsf = ibs_preds_rsf, l
val.prob.times = seq(0, max(data.val$Time), 1)
temp.coefs = coef(fit.gg)
val.linpred.gg = sapply(1:length(temp.coefs), function(coef_i) {
    if (names(temp.coefs)[coef_i] %in% colnames(data.val)) {
        temp.coefs[coef_i] * data.val[,names(temp.coefs)[coef_i]]
    } else if (gsub("TRUE$", "", names(temp.coefs)[coef_i]) %in% colnames(data.val)) {
        temp.coefs[coef_i] * data.val[,gsub("TRUE$", "", names(temp.coefs)[coef_i])]
    } else
        rep(0, nrow(data.val))
    } })
                                          # Negate to bring into concordance with the direction of Co.
val.linpred.gg = -rowSums(val.linpred.gg)
temp = summary(fit.gg, newdata = data.val, ci = FALSE)
val.prob.gg = sapply(temp, function(x) approx(x[,1], x[,2], xout = val.prob.times, yleft = 1, yright = 0
colnames(val.prob.gg) = rownames(data.val)
temp.coefs = coef(fit.gg2)
val.linpred.gg2 = sapply(1:length(temp.coefs), function(coef_i) {
    if (names(temp.coefs)[coef_i] %in% colnames(data.val)) {
        temp.coefs[coef_i] * data.val[,names(temp.coefs)[coef_i]]
    } else if (gsub("TRUE$", "", names(temp.coefs)[coef_i]) %in% colnames(data.val)) {
        temp.coefs[coef_i] * data.val[,gsub("TRUE$", "", names(temp.coefs)[coef_i])]
    } else ·
       rep(0, nrow(data.val))
    } })
val.linpred.gg2 = -rowSums(val.linpred.gg2) # Negate to bring into concordance with the direction of
temp = summary(fit.gg2, newdata = data.val, ci = FALSE)
val.prob.gg2 = sapply(temp, function(x) approx(x[,1], x[,2], xout = val.prob.times, yleft = 1, yright =
colnames(val.prob.gg2) = rownames(data.val)
val.linpred.cph = predict(fit.cph, newdata = data.val)
temp = survfit(fit.cph, newdata = data.val)
val.prob.cph = simplify2array(tapply(1:length(temp$surv), rep(names(temp$strata), temp$strata), function
temp = predict(fit.rsf, newdata = data.val)
# val.linpred.rsf = temp£predicted
# Median survival time:
val.linpred.rsf = apply(temp$survival, 1, function(s1) {
    sfunc = approxfun(temp$time.interest, s1, yleft = 1, yright = 0, rule = 2)
   med = uniroot(function(x) sfunc(x) - 0.5, lower = min(temp$time.interest), upper = max(temp$time.interest)
   med
})
val.linpred.rsf = -val.linpred.rsf
val.prob.rsf = apply(temp$survival, 1, function(s1) approx(temp$time.interest, s1, xout = val.prob.times
colnames(val.prob.rsf) = rownames(data.val)
summary(coxph(Surv(Time, DSD) ~ val.linpred.gg, data.val))
## Call:
```

```
## coxph(formula = Surv(Time, DSD) ~ val.linpred.gg, data = data.val)
##
##
   n= 61, number of events= 60
##
                 coef exp(coef) se(coef) z Pr(>|z|)
## val.linpred.gg 1.320 3.744 0.431 3.06 0.0022
##
##
                exp(coef) exp(-coef) lower .95 upper .95
## val.linpred.gg 3.74 0.267 1.61 8.71
## Concordance= 0.659 (se = 0.044)
## Rsquare= 0.144 (max possible= 0.998)
## Likelihood ratio test= 9.48 on 1 df, p=0.00208
## Wald test = 9.39 on 1 df, p=0.00219
## Score (logrank) test = 9.54 on 1 df, p=0.00201
summary(coxph(Surv(Time, DSD) ~ val.linpred.gg2, data.val))
## Call:
## coxph(formula = Surv(Time, DSD) ~ val.linpred.gg2, data = data.val)
## n= 61, number of events= 60
##
                 coef exp(coef) se(coef) z Pr(>|z|)
## val.linpred.gg2 1.32 3.75 0.45 2.94 0.0033
##
                 exp(coef) exp(-coef) lower .95 upper .95
## val.linpred.gg2 3.75
                              0.267 1.55 9.04
## Concordance= 0.642 (se = 0.044)
## Rsquare= 0.133 (max possible= 0.998)
## Likelihood ratio test= 8.7 on 1 df, p=0.00319
              = 8.63 on 1 df,
                                      p=0.00331
## Wald test
## Score (logrank) test = 8.76 on 1 df, p=0.00307
summary(coxph(Surv(Time, DSD) ~ val.linpred.cph, data.val))
## Call:
## coxph(formula = Surv(Time, DSD) ~ val.linpred.cph, data = data.val)
## n= 61, number of events= 60
##
                  coef exp(coef) se(coef) z Pr(>|z|)
## val.linpred.cph 1.192 3.295 0.338 3.53 0.00042
##
                 exp(coef) exp(-coef) lower .95 upper .95
##
## val.linpred.cph 3.29 0.304
##
## Concordance= 0.649 (se = 0.044)
## Rsquare= 0.177 (max possible= 0.998)
## Likelihood ratio test= 11.8 on 1 df, p=0.000578
## Wald test = 12.4 on 1 df, p=0.000421
## Score (logrank) test = 12.7 on 1 df, p=0.000367
summary(coxph(Surv(Time, DSD) ~ val.linpred.rsf, data.val))
```

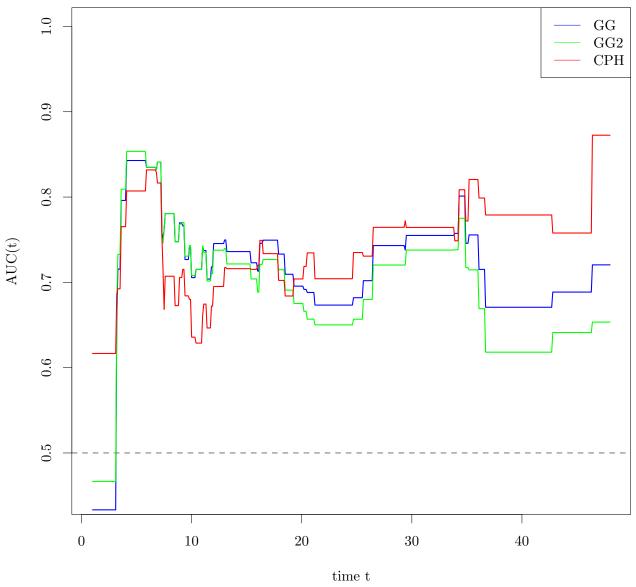
```
## Call:
## coxph(formula = Surv(Time, DSD) ~ val.linpred.rsf, data = data.val)
##
    n= 61, number of events= 60
##
                     coef exp(coef) se(coef) z Pr(>|z|)
##
##
##
                  exp(coef) exp(-coef) lower .95 upper .95
                                             1
## val.linpred.rsf
                      1.01
                                0.993
                                                    1.01
## Concordance= 0.679 (se = 0.044)
## Rsquare= 0.178 (max possible= 0.998 )
## Likelihood ratio test= 12 on 1 df, p=0.000538
                      = 11.9 on 1 df, p=0.000551
## Wald test
## Score (logrank) test = 12.1 on 1 df, p=0.000494
anova(coxph(Surv(Time, DSD) ~ offset(val.linpred.gg) + val.linpred.gg, data.val))
## Analysis of Deviance Table
## Cox model: response is Surv(Time, DSD)
## Terms added sequentially (first to last)
##
##
                 loglik Chisq Df Pr(>|Chi|)
## NULL
                   -184
## val.linpred.gg -184 0.55 1
                                      0.46
anova(coxph(Surv(Time, DSD) ~ offset(val.linpred.gg2) + val.linpred.gg2, data.val))
## Analysis of Deviance Table
## Cox model: response is Surv(Time, DSD)
## Terms added sequentially (first to last)
##
##
                  loglik Chisq Df Pr(>|Chi|)
## NULL
                    -185
## val.linpred.gg2
                  -184 0.51 1
                                       0.48
anova(coxph(Surv(Time, DSD) ~ offset(val.linpred.cph) + val.linpred.cph, data.val))
## Analysis of Deviance Table
## Cox model: response is Surv(Time, DSD)
## Terms added sequentially (first to last)
##
##
                  loglik Chisq Df Pr(>|Chi|)
## NULL
                    -183
## val.linpred.cph -183 0.32 1
                                       0.57
anova(coxph(Surv(Time, DSD) ~ offset(val.linpred.rsf) + val.linpred.rsf, data.val))
## Warning in fitter(X, Y, strats, offset, init, control, weights = weights, : Ran out of
iterations and did not converge
## Error in fitter(X, Y, strats, offset, init, control, weights = weights, : NA/NaN/Inf in
foreign function call (arg 6)
summary(coxph(Surv(Time, DSD) ~ offset(val.linpred.gg) + SexM + AgeCent + LocBody + SizeCent + A2 + A4,
```

```
## Call:
## coxph(formula = Surv(Time, DSD) ~ offset(val.linpred.gg) + SexM +
      AgeCent + LocBody + SizeCent + A2 + A4, data = data.val)
##
   n= 61, number of events= 60
##
##
                 coef exp(coef) se(coef)
                                         z Pr(>|z|)
## SexMTRUE
              0.40127 1.49372 0.27817 1.44
                                                0.149
## AgeCent
             -0.02260 0.97766 0.01371 -1.65
                                                0.099
## LocBodyTRUE 0.81060 2.24925 0.40567 2.00
                                                0.046
## SizeCent -0.00261 0.99740 0.00895 -0.29
                                                0.771
## A2TRUE
             0.69591 2.00553 0.50613 1.37
                                                0.169
## A4TRUE
             0.26205 1.29960 0.29377 0.89
                                               0.372
##
##
             exp(coef) exp(-coef) lower .95 upper .95
                1.494
                         0.669
                                    0.866
## SexMTRUE
                                           2.58
                 0.978
                           1.023
                                    0.952
## AgeCent
                                              1.00
## LocBodyTRUE
                 2.249
                            0.445
                                    1.016
                                               4.98
                                  0.980
## SizeCent
                 0.997
                           1.003
                                               1.02
## A2TRUE
                 2.006
                           0.499
                                  0.744
                                               5.41
## A4TRUE
                1.300
                           0.769
                                  0.731
                                               2.31
##
## Concordance= 0.687 (se = 0.044)
## Rsquare= 0.152 (max possible= 0.998)
## Likelihood ratio test= 10.1 on 6 df, p=0.122
                                      p=0.0972
## Wald test
                  = 10.7 on 6 df,
## Score (logrank) test = 11.2 on 6 df, p=0.0815
summary(coxph(Surv(Time, DSD) ~ offset(val.linpred.gg2) + SexM + AgeCent + LocBody + SizeCent + A2 + A4
## Call:
## coxph(formula = Surv(Time, DSD) ~ offset(val.linpred.gg2) + SexM +
      AgeCent + LocBody + SizeCent + A2 + A4, data = data.val)
##
##
   n= 61, number of events= 60
##
                  coef exp(coef) se(coef)
                                          z Pr(>|z|)
              0.42688 1.53246 0.27817 1.53
## SexMTRUE
                                                0.125
             -0.02260 0.97766 0.01371 -1.65
## AgeCent
                                                0.099
## LocBodyTRUE 0.81060 2.24925 0.40567 2.00
                                                0.046
## SizeCent -0.00249 0.99751 0.00895 -0.28
                                                0.781
## A2TRUE
              0.70033 2.01442 0.50613 1.38
                                                0.166
              0.33020 1.39125 0.29377 1.12
## A4TRUE
                                                0.261
##
##
              exp(coef) exp(-coef) lower .95 upper .95
## SexMTRUE
                 1.532
                           0.653
                                  0.888
                                              2.64
                                               1.00
## AgeCent
                 0.978
                           1.023
                                    0.952
## LocBodyTRUE
                 2.249
                           0.445
                                    1.016
                                               4.98
## SizeCent
                 0.998
                           1.002
                                   0.980
                                               1.02
                                  0.747
## A2TRUE
                 2.014
                            0.496
                                               5.43
## A4TRUE
                1.391
                            0.719
                                   0.782
                                               2.47
## Concordance= 0.687 (se = 0.044)
## Rsquare= 0.162 (max possible= 0.998 )
```

```
## Likelihood ratio test= 10.8 on 6 df,
                                         p=0.0943
## Wald test = 11.4 on 6 df,
                                         p=0.0767
## Score (logrank) test = 11.9 on 6 df,
                                         p=0.0638
summary(coxph(Surv(Time, DSD) ~ offset(val.linpred.cph) + SexM + AgeCent + LocBody + SizeCent + A2 + A4
## Call:
## coxph(formula = Surv(Time, DSD) ~ offset(val.linpred.cph) + SexM +
      AgeCent + LocBody + SizeCent + A2 + A4, data = data.val)
##
##
##
   n= 61, number of events= 60
##
##
                  coef exp(coef) se(coef)
                                            z Pr(>|z|)
## SexMTRUE
              -0.03303 0.96751 0.27817 -0.12
                                                 0.905
             -0.02260 0.97766 0.01371 -1.65
## AgeCent
                                                  0.099
## LocBodyTRUE 0.81060 2.24925 0.40567 2.00
                                                 0.046
             -0.00544 0.99457 0.00895 -0.61
## SizeCent
                                                 0.543
## A2TRUE
              0.51021 1.66563 0.50613 1.01
                                                 0.313
## A4TRUE
              0.12325 1.13117 0.29377 0.42
                                                  0.675
##
              exp(coef) exp(-coef) lower .95 upper .95
##
## SexMTRUE
                  0.968
                            1.034
                                     0.561
                                                1.67
## AgeCent
                  0.978
                            1.023
                                      0.952
                                                1.00
## LocBodyTRUE
                  2.249
                            0.445
                                     1.016
                                                 4.98
                                                 1.01
## SizeCent
                  0.995
                            1.005
                                      0.977
## A2TRUE
                  1.666
                            0.600
                                    0.618
                                                 4.49
## A4TRUE
                 1.131
                            0.884
                                     0.636
                                                 2.01
## Concordance= 0.687 (se = 0.044)
## Rsquare= 0.115 (max possible= 0.998)
## Likelihood ratio test= 7.48 on 6 df,
                                         p=0.279
                      = 8.05 on 6 df,
## Wald test
                                         p=0.234
## Score (logrank) test = 8.41 on 6 df,
                                       p=0.209
summary(coxph(Surv(Time, DSD) ~ offset(val.linpred.rsf) + SexM + AgeCent + LocBody + SizeCent + A2 + A4
## Warning in fitter(X, Y, strats, offset, init, control, weights = weights, : Ran out of
iterations and did not converge
## Error in fitter(X, Y, strats, offset, init, control, weights = weights, : NA/NaN/Inf in
foreign function call (arg 6)
```

TD-ROC AUC

```
temp.times = seq(0.1, 48, 0.1)
temp.gg = timeROC(data.val$Time/365.25*12, data.val$DSD, val.linpred.gg, cause = 1, times = temp.times,
temp.gg2 = timeROC(data.val$Time/365.25*12, data.val$DSD, val.linpred.gg2, cause = 1, times = temp.times
temp.cph = timeROC(data.val$Time/365.25*12, data.val$DSD, val.linpred.cph, cause = 1, times = temp.times
plotAUCcurve(temp.gg, conf.int = FALSE, add = FALSE, col = "blue")
plotAUCcurve(temp.gg2, conf.int = FALSE, add = TRUE, col = "green")
plotAUCcurve(temp.cph, conf.int = FALSE, add = TRUE, col = "red")
legend("topright", legend = c("GG", "GG2", "CPH"), col = c("blue", "green", "red"), lty = "solid")
```

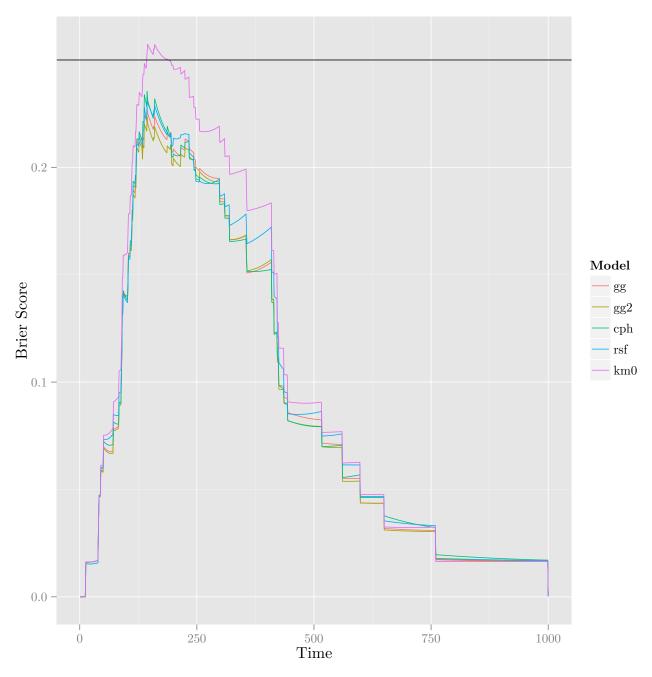


Decision curve analysis.

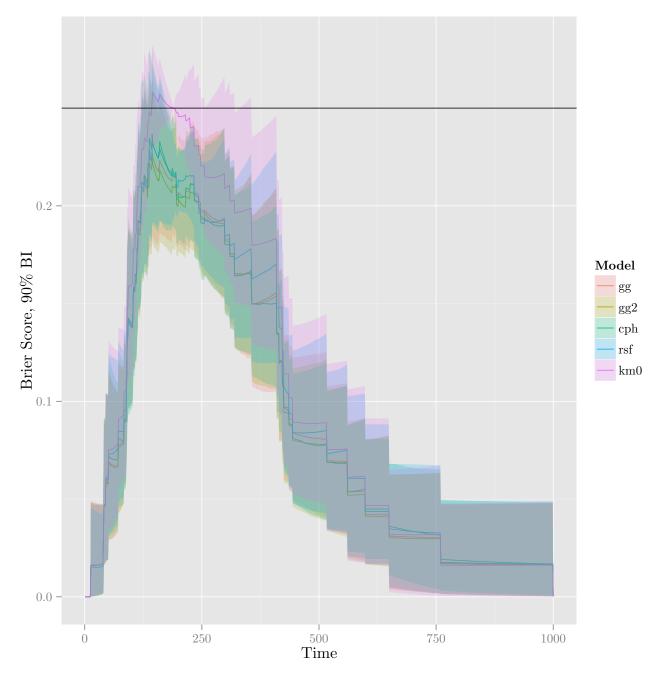
Evaluate IBS point estimates. BS paths over time on bootstrap samples of the holdout set.

```
set.seed(20150111)
ibs_eval_times = calcIBS(Surv(data.val$Time, data.val$DSD), ibs_preds_gg, ibs_times, max(data.val$Time)
# bsc_boot2 = lapply(ibs_preds_all, function(preds) boot(data.val, statistic = function(d, i) calcIBS(Set)
# bsc_boot2ci = lapply(bsc_boot2, function(single_boot) t(sapply(1:length(ibs_eval_times), function(times))
# temp = try(boot.ci(single_boot, index = time_index, type = "bca")fbca, silent = TRUE)
# if(class(temp) == "try-error" || is.null(temp)) { temp = rep(NA, 5) }
# temp })))
bsc_boots = laply(1:500, function(i) {
        if (i %% 50 == 0)
                               { message(i) }
        boot_samp = sample.int(nrow(data.val), replace = TRUE)
        gg = calcIBS(Surv(data.val$Time, data.val$DSD)[boot_samp,], ibs_preds_gg[boot_samp,], ibs_times
        gg2 = calcIBS(Surv(data.val$Time, data.val$DSD)[boot_samp,], ibs_preds_gg2[boot_samp,], ibs_time
        cph = calcIBS(Surv(data.val$Time, data.val$DSD)[boot_samp,], ibs_preds_cph[boot_samp,], ibs_time
        rsf = calcIBS(Surv(data.val$Time, data.val$DSD)[boot_samp,], ibs_preds_rsf[boot_samp,], ibs_time
        km0 = calcIBS(Surv(data.val$Time, data.val$DSD)[boot_samp,], ibs_preds_km0[boot_samp,], ibs_time
        rbind(gg, gg2, cph, rsf, km0)
})
## 50
## 100
## 150
## 200
## 250
## 300
## 350
## 400
## 450
## 500
```

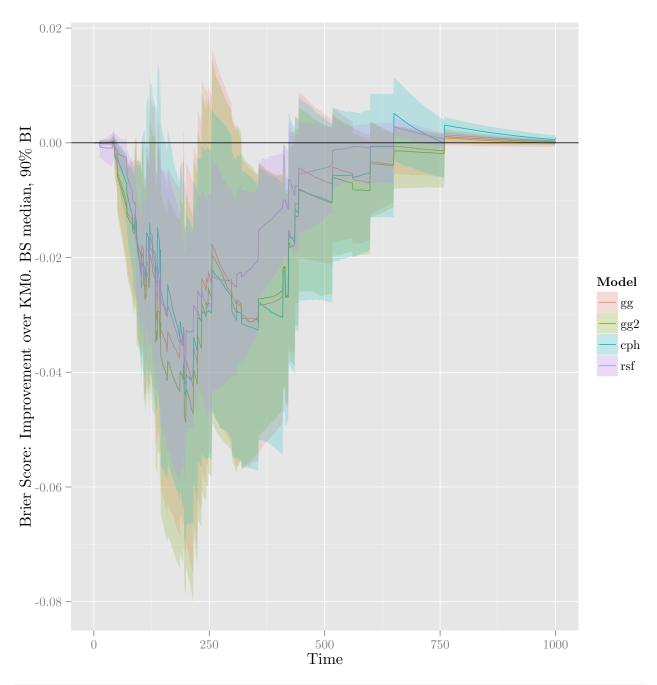
```
temp = sapply(list(gg = ibs_preds_gg, gg2 = ibs_preds_gg2, cph = ibs_preds_cph, rsf = ibs_preds_rsf, km(
temp = melt(temp)
colnames(temp) = c("Time", "Model", "BS")
ggplot(temp, aes(x = Time, y = BS, colour = Model)) + geom_line() + ylab("Brier Score") + geom_hline(ying)
```



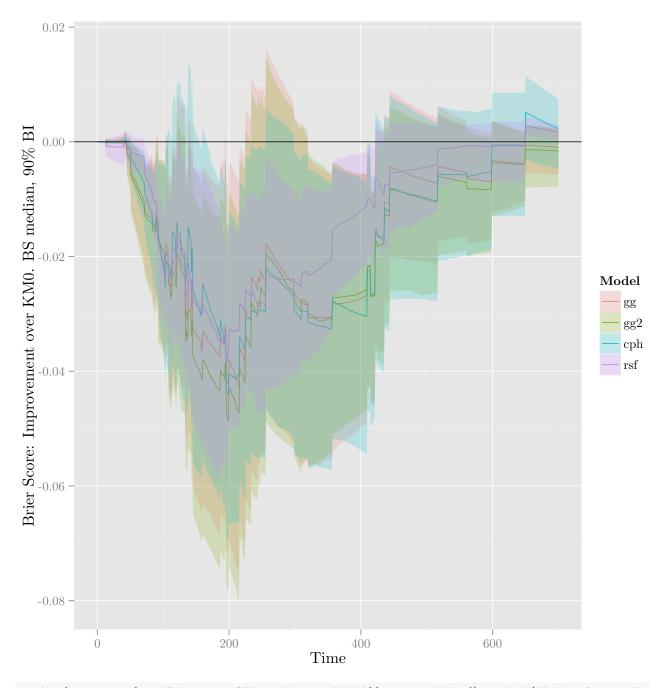
```
temp = melt(aaply(bsc_boots, 2:3, quantile, probs = c(0.05, 0.5, 0.95)))
colnames(temp) = c("Model", "Time", "Quantile", "Value")
temp$Quantile = paste("Q", gsub("%", "", temp$Quantile), sep = "")
temp = dcast(temp, Model + Time ~ Quantile, value.var = "Value")
ggplot(temp, aes(x = Time, y = Q50, ymin = Q5, ymax = Q95, colour = Model, fill = Model)) + geom_line()
```



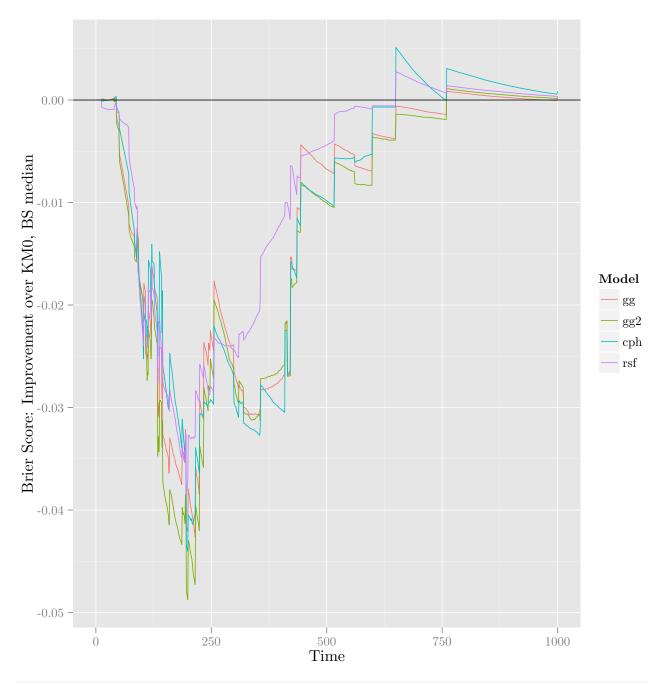
```
bsc_boots_diff = aaply(bsc_boots, 2, function(x) x - bsc_boots[,5,])[1:4,,]
temp = melt(aaply(bsc_boots_diff, c(1,3), quantile, probs = c(0.05, 0.5, 0.95)))
colnames(temp) = c("Model", "Time", "Quantile", "Value")
temp$Quantile = paste("Q", gsub("%", "", temp$Quantile), sep = "")
temp = dcast(temp, Model + Time ~ Quantile, value.var = "Value")
ggplot(temp, aes(x = Time, y = Q50, ymin = Q5, ymax = Q95, colour = Model, fill = Model)) + geom_line()
```



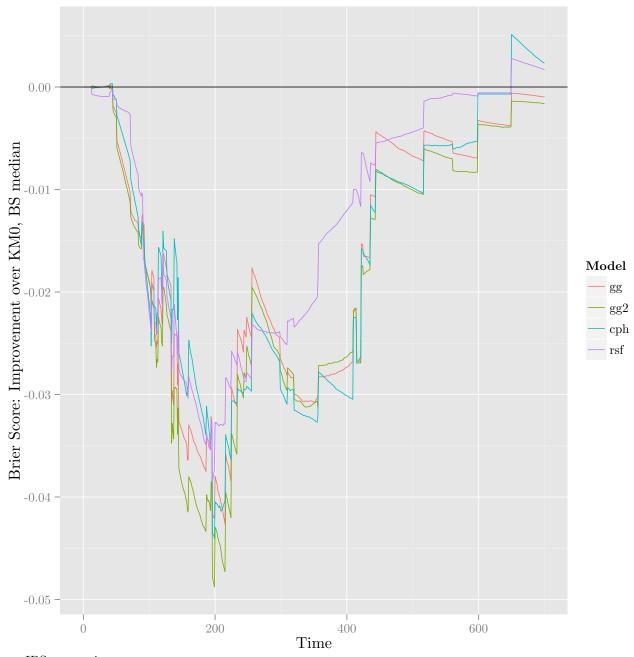
ggplot(temp, aes(x = Time, y = Q50, ymin = Q5, ymax = Q95, colour = Model, fill = Model)) + geom_line()
Warning: Removed 1200 rows containing missing values (geom_path).



ggplot(temp, aes(x = Time, y = Q50, colour = Model)) + geom_line() + ylab("Brier Score: Improvement over



ggplot(temp, aes(x = Time, y = Q50, colour = Model)) + geom_line() + ylab("Brier Score: Improvement over
Warning: Removed 1200 rows containing missing values (geom_path).



IBS comparisons.

```
## 50
## 100
## 150
## 250
## 350
## 400
## 450
## 450
## 500

colnames(ibsc_boots) = c("gg", "gg2", "cph", "rsf", "km0")
```

```
calcIBS(Surv(data.val$Time, data.val$DSD), ibs_preds_gg, ibs_times, max(data.val$Time))$ibs
## [1] 147.4

calcIBS(Surv(data.val$Time, data.val$DSD), ibs_preds_gg2, ibs_times, max(data.val$Time))$ibs
## [1] 145.6

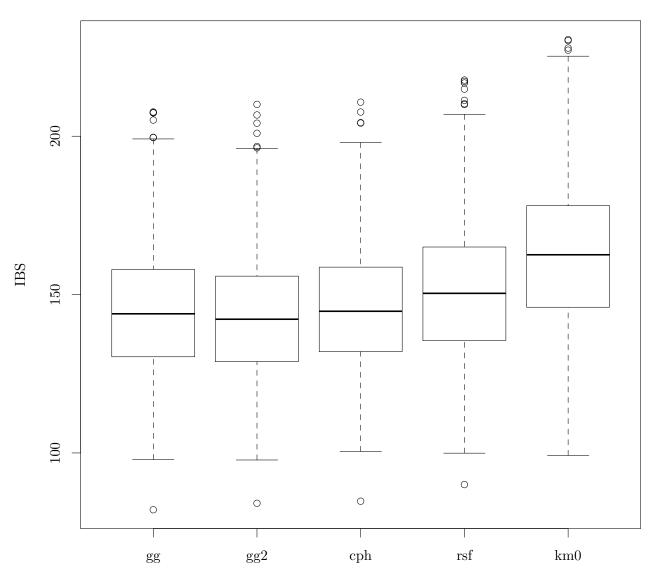
calcIBS(Surv(data.val$Time, data.val$DSD), ibs_preds_cph, ibs_times, max(data.val$Time))$ibs
## [1] 148.6

calcIBS(Surv(data.val$Time, data.val$DSD), ibs_preds_rsf, ibs_times, max(data.val$Time))$ibs
## [1] 153.3

calcIBS(Surv(data.val$Time, data.val$DSD), ibs_preds_km0, ibs_times, max(data.val$Time))$ibs
## [1] 165.4

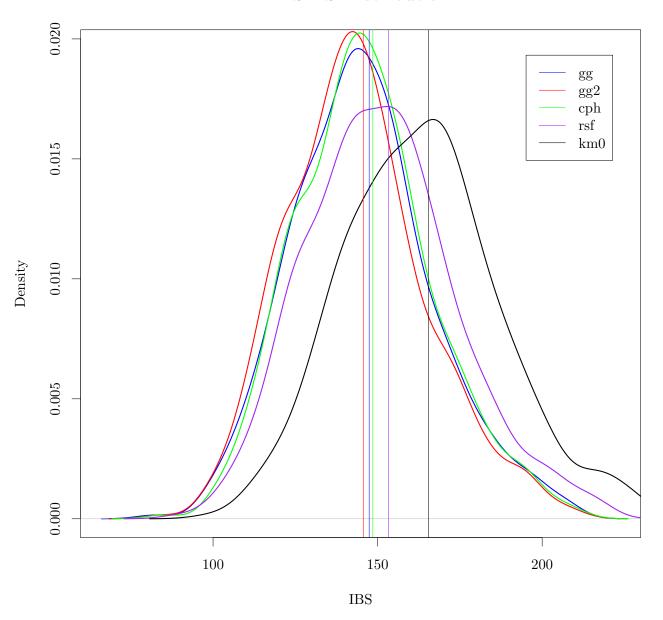
boxplot(ibsc_boots, main = "IBS BS Distribution", ylab = "IBS")
```

IBS BS Distribution



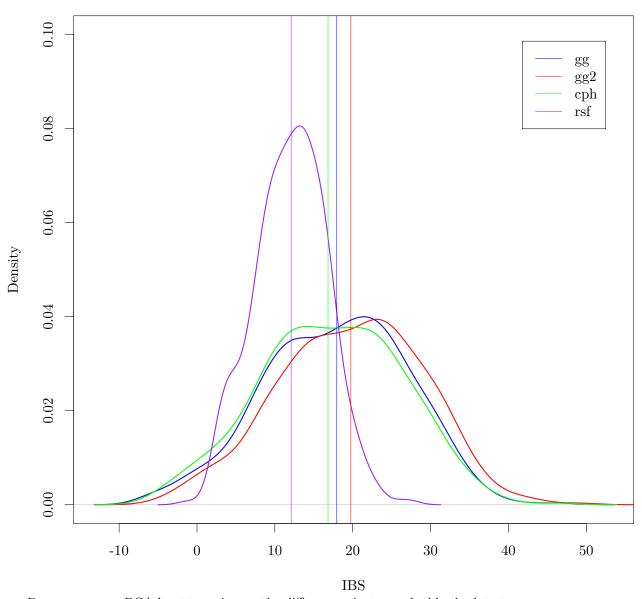
```
plot(density(ibsc_boots[,1]), col = "blue", lwd = 2, main = "IBS BS Distribution", xlab = "IBS")
lines(density(ibsc_boots[,2]), col = "red", lwd = 2)
lines(density(ibsc_boots[,3]), col = "green", lwd = 2)
lines(density(ibsc_boots[,4]), col = "purple", lwd = 2)
lines(density(ibsc_boots[,5]), col = "black", lwd = 2)
abline(v = calcIBS(Surv(data.val$Time, data.val$DSD), ibs_preds_gg, ibs_times, max(data.val$Time))$ibs,
abline(v = calcIBS(Surv(data.val$Time, data.val$DSD), ibs_preds_gg2, ibs_times, max(data.val$Time))$ibs
abline(v = calcIBS(Surv(data.val$Time, data.val$DSD), ibs_preds_cph, ibs_times, max(data.val$Time))$ibs
abline(v = calcIBS(Surv(data.val$Time, data.val$DSD), ibs_preds_rsf, ibs_times, max(data.val$Time))$ibs
abline(v = calcIBS(Surv(data.val$Time, data.val$DSD), ibs_preds_rsf, ibs_times, max(data.val$Time))$ibs
abline(v = calcIBS(Surv(data.val$Time, data.val$DSD), ibs_preds_km0, ibs_times, max(data.val$Time))$ibs
legend("topright", legend = c("gg", "gg2", "cph", "rsf", "km0"), col = c("blue", "red", "green", "purple", "pur
```

IBS BS Distribution



```
plot(density(ibsc_boots[,5] - ibsc_boots[,1]), col = "blue", lwd = 2, main = "IBS\\_KMO - IBS\\_x BS Disc_lines(density(ibsc_boots[,5] - ibsc_boots[,2]), col = "red", lwd = 2)
lines(density(ibsc_boots[,5] - ibsc_boots[,3]), col = "green", lwd = 2)
lines(density(ibsc_boots[,5] - ibsc_boots[,4]), col = "purple", lwd = 2)
abline(v = (calcIBS(Surv(data.val$Time, data.val$DSD), ibs_preds_kmO, ibs_times, max(data.val$Time))$ibs_abline(v = (calcIBS(Surv(data.val$Time, data.val$Time))$ibs_abline(v = (calcIBS(Surv(data.val$Time, data.val$Time)), ibs_times, max(data.val$Time))$ibs_abline(v = (calcIBS(Surv(data.val$Time, data.val$Time)), ibs_times, max(data.val$Time, data.val$Time, data.val$Time, data.val$Time, data.val$Time, data.val$Time, data.val$Time, data.val$Time, data.val$Ti
```

IBS_KM0 - IBS_x BS Distribution



Do some proper BCA bootstrapping on the differences, just as a double-check test.

```
##
## ORDINARY NONPARAMETRIC BOOTSTRAP
##
##
## Call:
## boot(data = data.val, statistic = function(d, i) {
##
       gg = calcIBS(Surv(d$Time, d$DSD)[i, ], ibs_preds_gg[i, ],
##
           ibs_times, max(d$Time[i]))$ibs
##
       gg2 = calcIBS(Surv(d$Time, d$DSD)[i, ], ibs_preds_gg2[i,
##
           ], ibs_times, max(d$Time[i]))$ibs
       cph = calcIBS(Surv(d$Time, d$DSD)[i, ], ibs_preds_cph[i,
##
          ], ibs_times, max(d$Time[i]))$ibs
##
##
       rsf = calcIBS(Surv(d$Time, d$DSD)[i, ], ibs_preds_rsf[i,
           ], ibs_times, max(d$Time[i]))$ibs
##
       km0 = calcIBS(Surv(d$Time, d$DSD)[i, ], ibs_preds_km0[i,
##
##
          ], ibs_times, max(d$Time[i]))$ibs
##
       c(gg - km0, gg2 - km0, cph - km0, rsf - km0, gg - rsf, gg2 -
##
           rsf, cph - rsf, gg - cph, gg2 - cph, gg - gg2)
## \}, R = 500)
##
##
## Bootstrap Statistics :
##
        original
                   bias
                           std. error
## t1*
        -17.960 0.16202
                                9.092
## t2*
         -19.764 0.08589
                                9.303
## t3*
         -16.830 -0.34992
                                9.293
        -12.092 0.06313
## t4*
                                4.847
## t5*
         -5.868 0.09888
                                4.847
         -7.672 0.02275
## t6*
                                5.138
## t7*
          -4.738 -0.41305
                                5.075
## t8*
         -1.129 0.51193
                                2.188
          -2.934 0.43580
## t9*
                                1.239
## t10*
          1.805 0.07613
                                2.012
ibsc_boots2_ci
##
           level orderi1 orderi2
                                     lci
## gg-km0
            0.95
                 12.62
                           488.6 -36.586 0.04987
## gg2-km0 0.95
                  13.26
                           489.1 -38.095 -0.93649
## cph-km0
            0.95
                   15.77
                           490.9 -35.135
                                         1.22396
## rsf-km0 0.95
                  15.92
                           491.0 -21.344 -1.94556
## gg-rsf
            0.95
                   16.84
                           491.8 -13.848 4.78985
                           489.1 -17.593 2.48774
## gg2-rsf 0.95
                   13.27
## cph-rsf
           0.95
                   16.67
                           491.4 -14.727 4.96039
## gg-cph
            0.95
                    6.57
                           477.5 -5.556 3.09545
## gg2-cph 0.95
                    1.63
                           442.8 -5.680 -1.02330
                           489.4 -2.239 5.99125
            0.95
                   13.43
## gg-gg2
```

All models perform equivalently on the validation set. Select the simplest: gg. Final model fitting:

```
data.all = rbind(data[colnames(data.val)], data.val)
head(data.all)
## Time DSD SexM AgeCent LocBody SizeCent A2 A4
```

```
## NSWPCN_4 937 TRUE TRUE -16 FALSE -1 FALSE TRUE
## NSWPCN_7 247 TRUE FALSE
                                -1 FALSE
                                                  -2 FALSE TRUE
## NSWPCN_10 177 TRUE TRUE
                                 -9 FALSE
                                                  10 FALSE TRUE
## NSWPCN_13 247 TRUE FALSE
                                -19
                                      TRUE
                                                  20 FALSE TRUE
## NSWPCN_20 256 TRUE FALSE
                                 -8 FALSE
                                                  O FALSE TRUE
## NSWPCN_21 763 TRUE FALSE
                                 -1 FALSE
                                                  -2 FALSE FALSE
fit.final.gg = flexsurvreg(Surv(Time, DSD) ~ SexM + SizeCent + A2 + A4,
        anc = list(
                sigma = ~ SexM,
                Q = ^{\sim} SexM),
        data = data.all, dist = "gengamma")
fit.final.gg2 = flexsurvreg(Surv(Time, DSD) ~ SexM + SizeCent + A2 + A4 + I(SexM == FALSE & A2 == FALSE
    anc = list(
        sigma = ~ SexM,
        Q = ^{\sim} SexM),
    data = data.all, dist = "gengamma")
fit.final.cph = coxph(Surv(Time, DSD) ~ strata(SexM) + SizeCent + A2 + A4, data = data.all, x = TRUE, y
set.seed(20150111)
fit.final.rsf = rfsrc(Surv(Time, DSD) ~ SexM + AgeCent + LocBody + SizeCent + A2 + A4, data = data.all,
fit.final.km0 = survfit(Surv(Time, DSD) ~ 1, data.all)
saveRDS(list(gg = fit.final.gg, km0 = fit.final.km0, gg2 = fit.final.gg2, cph = fit.final.cph, rsf = fit
```

8 Session information

```
sessionInfo()
## R version 3.1.1 (2014-07-10)
## Platform: x86_64-unknown-linux-gnu (64-bit)
##
## locale:
## [1] LC_CTYPE=en_US.UTF-8
                                   LC_NUMERIC=C
## [3] LC_TIME=en_US.UTF-8
                                    LC_COLLATE=en_US.UTF-8
## [5] LC_MONETARY=en_US.UTF-8
                                   LC_MESSAGES=en_US.UTF-8
## [7] LC_PAPER=en_US.UTF-8
                                   LC_NAME=en_US.UTF-8
                                   LC_TELEPHONE=en_US.UTF-8
## [9] LC_ADDRESS=en_US.UTF-8
## [11] LC_MEASUREMENT=en_US.UTF-8
                                  LC_IDENTIFICATION=en_US.UTF-8
##
## attached base packages:
## [1] parallel splines methods stats
                                           graphics grDevices utils
## [8] datasets base
##
## other attached packages:
## [1] timeROC_0.2
                            timereg_1.8.6
                                                  mvtnorm_1.0-1
## [4] pec_2.4.4
                            boot_1.3-13
                                                  MASS_7.3-35
## [7] ggplot2_1.0.0
                           plyr_1.8.1
                                                  reshape2_1.4
## [10] randomForestSRC_1.5.5 flexsurv_0.5
                                                  glmulti_1.0.7
## [13] rJava_0.9-6
                                                  tikzDevice_0.7.0
                            survival_2.37-7
## [16] filehash_2.2-2
                            knitr_1.8
## loaded via a namespace (and not attached):
## [1] codetools_0.2-9 colorspace_1.2-4 deSolve_1.11 digest_0.6.4
```

#:	# [5]	evaluate_0.5.5	foreach_1.4.2	formatR_1.0	grid_3.1.1
#:	# [9]	gtable_0.1.2	highr_0.4	iterators_1.0.7	labeling_0.3
#:	# [13]	lava_1.3	muhaz_1.2.6	munsell_0.4.2	prodlim_1.5.1
#:	# [17]	proto_0.3-10	Rcpp_0.11.3	scales_0.2.4	stringr_0.6.2
#:	# [21]	tools_3.1.1			