

* Punto 6

$$x^2(a_0, a_1) = \sum_{i=1}^n (y_i - (a_0 + a_1 x_i))^2$$

$$= y_i^2 - 2y_i(a_0 + a_1 x_i) + (a_0 + a_1 x_i)^2$$

$$= y_i^2 - 2y_i a_0 + 2y_i a_1 x_i + a_0^2 + 2a_0 a_1 x_i + a_1^2 x_i^2$$

$$x^2(a_0, a_1) = \sum y_i^2 - 2a_0 \sum y_i - 2a_1 \sum y_i x_i + \dots + a_1^2 \sum x_i^2$$

$$\frac{\partial x^2}{\partial a_0} = -2 \sum y_i - a_1 \sum x_i = \bar{y}_1 - a_1 \bar{x}_1$$

$$= \sum y_i - a_1 \sum x_i = \bar{y}_1 - a_1 \bar{x}_1$$

$$\frac{\partial x^2}{\partial a_1} = -2 \sum y_i x_i + 2a_0 \sum x_i + 2a_1 \sum x_i^2 = 0$$

$$= -\sum y_i x_i + (\sum y_i \sum x_i - a_1 \sum x_i \sum x_i) + a_1 \sum x_i^2 = 0$$

minimizar

$$x^2(a_0, a_1, a_2) = \sum_{i=1}^n (y_i - (a_0 + a_1 x_i + a_2 x_i^2))^2$$

$$\begin{aligned} \frac{\partial x^2}{\partial a_0} &= -2 \sum y_i + 2N a_0 + 2a_1 \sum x_i + 2a_2 \sum x_i^2 = 0 \\ \sum_{i=1}^n [a_0 + a_1 x_i + a_2 x_i^2] \cdot \frac{y_i}{N} &= \bar{y}_1 \end{aligned}$$

$$\begin{aligned} \frac{\partial x^2}{\partial a_1} &= -2 \sum y_i x_i + 2a_1 \sum x_i^2 + 2a_2 \sum x_i^3 = 0 \\ \sum_{i=1}^n [a_0 x_i + a_1 x_i^2 + a_2 x_i^3] &= \frac{\sum y_i x_i}{N} = \bar{x}_1 \bar{y}_1 \end{aligned}$$

$$\begin{aligned} \frac{\partial x^2}{\partial a_2} &= -2 \sum y_i x_i^2 + 2a_1 \sum x_i^3 + 2a_2 \sum x_i^4 = 0 \\ \sum_{i=1}^n [a_0 x_i^2 + a_1 x_i^3 + a_2 x_i^4] &= \frac{\sum x_i^2 y_i}{N} = \bar{x}_1^2 \bar{y}_1 \end{aligned}$$