

## I. INTRODUCTION

This final project is cumulative of everything taught in the course CSIS 200: Software Tools for Physicists. It tests how much students truly learned in the course by requiring them to pull together all the coding skills taught throughout the semester into one functional code for every problem. Although most of the assigned problems can be worked out by hand analytically, students only receive credit for solving them numerically in Jupyter Notebook. Solving a problem numerically is when data is gathered/produced and tested, and the conclusions of the data tests are the answers. By using the numerical method, students must use everything they have learned from the beginning of the course all the way to the end of the course. This includes everything from variables to loops and functions, and all the way to the `numpy.random.random` function. If a student can successfully use all the tools they have learned in the course to solve the problems given, then they have truly learned the course material.

## II. PROBLEM 1

In the first problem, the odds of it raining on any given day in a month is 20%, and for simplicity, one month is thirty days. The question asked is: what are the odds of it raining only one day out of the month?

### A. Analytic Approach

The probability of it raining on any given day is 20%, or 0.2. This means the probability of it not raining on any given day is 80%, or 0.8. To find the probability of it raining only once in one month, the probability of it raining only once and not raining the other 29 days must be calculated. In probability, “and” means multiply. Also, because the one day of rain could occur on any of the days of the month, the probabilities must be multiplied by 30. So the equation should look like this:

$$P = ((P_{rain}) * (P_{dry})^{29} * 30 * 100\%$$

$$P = \frac{1}{5} * \left(\frac{4}{5}\right)^{29} * 30 * 100\%$$

$$P = 0.928\%$$

The analytical approach results in the conclusion that the probability of it raining only one day of the month is 0.928%.

## B. Numerical Approach

To solve this problem numerically, first a function that takes in a list of thirty random numbers between one and five was defined (where one is a day it rains and 2 through 5 are days it does not rain). A variable was set equal to zero to track the number of days it rained and another variable was set equal to False. Then the function loops over the list of thirty numbers and, using an if statement, if one of the numbers in the list is equal to one, then it adds one to the variable tracking the number of days it rains. After the function loops over the list, outside of the for-loop it looks at whether or not the variable tracking the number of rainy days is equal to one. If it is equal to one, the other variable becomes True. The function returns the variable that will either be True or False.

Next, a Monte Carlo approach is used to test numerically the probability of rain by generating fake data. A variable is set equal to the number of months tested. Note that the higher this number is, the more accurate the answer is, but the longer it takes to compute the answer. Another variable is set to zero to track the number of months it rains only one day. A list from zero to the number of months tested is then looped over, and for every month, a list of thirty numbers between one and five is generated using the `numpy.random.randint` function. Calling the function and using an if statement, if a month has one day of rain only, the variable tracking the number of months increases by one. Dividing this by the total number of months and multiplying by one hundred consistently gives an answer around 0.9%, which close to the analytical answer, but not exactly. The answer is different every time the program is run because it generates different numbers between one and five every time.

## III. PROBLEM 2

Problem 2 states there is a 10% chance that it will rain on any given day in a month and asks the probability that it rains at least eight days in any order in a month.

Like in Problem 1, a function that takes in a list of thirty random numbers between one and five was defined, a variable was set equal to zero to track the rainy days, and another variable was set equal to False. The function loops over a list of thirty random numbers between one and ten (because the probability of rain is now 10%) and every time one of the numbers in the list is one, the variable set equal to zero increases by one. After the function loops over the list, it looks at the variable tracking the rainy days and if it is greater than or equal to eight, the other variable originally set to False becomes True. The function returns this True/False variable.

Then, like in Problem 1, a variable is set to the number of months to test and another is set equal to zero this time to count the number of days it rains a least eight days. Then a list of all the months is looped over and for every

month a list of thirty random numbers between one and ten is generated using the `numpy.random.randint` function. Then using an if statement and calling the function, if a month has greater than or equal to eight days of rain, the variable tracking the number of months with at least eight days of rain increases by one. By dividing this by the total number of months and multiplying by one hundred, and the answer is consistently around 0.8%.

#### IV. PROBLEM 3

##### A. Part A

This question asks for the probability it will rain at least 10 cm in any given month, given the following conditions.

The odds of it raining depend on if it rained the day before:

- If it is the first day of the month, there is a 10% chance of rain
- If it rained one day before but not two days before, there is a 20% chance of rain
- If it rained both of the two days before, but not the third day before, there is a 25% chance of rain
- If it rained for three or more days before, then there is a 25% chance of rain
- Otherwise there is a 10% chance of rain.

If it does, in fact, rain, then the probabilities of certain amounts of rainfall are:

- 20% 1 cm of rain
- 30% 2 cm of rain
- 30% 3 cm of rain
- 10% 4 cm of rain
- 5% 5 cm of rain.

To solve this problem numerically, first a function was defined to keep track of when it does actually rain. The input to this function will be a list of thirty random numbers between zero and one. In the function, first a variable was set equal to zero (in order to count the days it rains) and another variable was set equal to the length of the input. Then, using a for loop, the function loops over the the list from zero to the variable set equal to the length of the list. This is so that the conditionals in the loop can look at the values of the numbers (i.e. a number between zero and one) that come one, two, or three days, or places, before the day the function is looking at. First the loop looks at the three days before. If three days before is less than or equal to 0.1 and two days before is less than or equal to 0.2 and the day before is less than

or equal to 0.25 (which means it rained all three days before this day), then if the number in the loop is less than or equal to 0.05, one is added to the variable counting the amount of days it rained. Next, if the number in the loops is not satisfied by that condition, the loop looks at the three days before the day that the loop is on. If the second day before is less than or equal to 0.1 and the day before is less than or equal to 0.2 (meaning it rained both days before), but the third day before is greater than 0.1 (meaning it did not rain the third day before, then if the number the loop is looking at is less than or equal to 0.25, it means it rained that day and the variable tracking the amount of days it rained increases by one. Then, if the number does not meet those conditions, the loop looks at the day before and if the value of the day before is less than or equal to 0.1 (meaning it rained the day before), and if two days before the valued is greater than 0.1 (meaning it didn't rain two days before), then if the value of the number in the loop is less than or equal to 0.2, then the function adds one to the variable counting the days it rained. Lastly, if none of those conditions are met, then if the number in the loop is less than or equal to 0.1, it rained that day and the variable tracking the days it rained increases by one. This process is repeated for every number in the loop and the function returns the variable tracking the number of days in the loop.

Next, a function to track how much it rained was defined. The input to this function will be the output of the first function. First, a random list of numbers between zero and one is generated and the length of the list depends on the input of the function. So every day it rained has a random value from zero to one assigned to it. A variable is set to zero to count the centimeters of rainfall for each day it rains. The function loops over the list generated and if it is less than or equal to 0.2, the variable tracking the rainfall, or the tracking variable, increases by one (cm). Else, if the number is greater than 0.2 but less than or equal to 0.5, then the tracking variable increases by two (cm). Else, if the number is greater than 0.5 but less than or equal to 0.8, then the tracking variable increases by three (cm). Else, if the number is greater than 0.8 and less than or equal to 0.9, then the tracking variable increases by four (cm). Lastly, if the number is greater than 0.9 but less than or equal to 1.0, then five (cm) is added to the tracking variable. The loop does this for every variable in the list. The function returns the variable tracking the rainfall.

Finally, many months can be tested. First, a variable is set to a number (the higher the number, the more accurate the answer, but the longer the code takes to run) and another variable is set equal to zero to track the amount of months with at least 10 cm of rain. Then a for loop loops over the same amount of times as the first variable is set to. In the loop, so for every month, a variable is set equal to a list of thirty numbers between zero and one. A second variable is set equal to the output of the first function that tracks if/when it rains with the input of the variable equal to the list of thirty random num-

bers between zero and one. Then, for the output of the second function defined with the input as the second variable (equal to how many days it rained), if it is greater than or equal to ten, the variable tracking the number of months it rained 10 cm increases by one. The number of months it rains at least 10 cm is divided by the total number of months and multiplied by 100%. The answer is consistently around 40%.

### **B. Part B**

Before making a histogram of the rainfall, the data from Part A was put into an array by setting a variable equal to an empty array and looping over a list of the number of test months. For every month, a list of 30 random numbers between zero and one was created. This list was put through the function that tracked the number of rainy days, and then the output of that function was the input to the function that tracked how much rain fell. The amount of rainfall was appended to the empty array. This repeated for however many months

were tested. Then the array of the amount of rainfall for each month was plotted into a histogram. See Figure 1 for a sample!

### **C. Part C**

To calculate the average rainfall in any given month, the function `numpy.mean()` was used. The input to this function is the array created in Part B. The average amount of rainfall in a month was consistently around 8.9 cm.

### **D. Part D**

To calculate the uncertainty, the middle 95% of the data was found and the outside edges of the range (the lower 2.5% and the higher 2.5%) were used. There is 95% confidence that the rainfall will be between 0 cm and 22 cm.

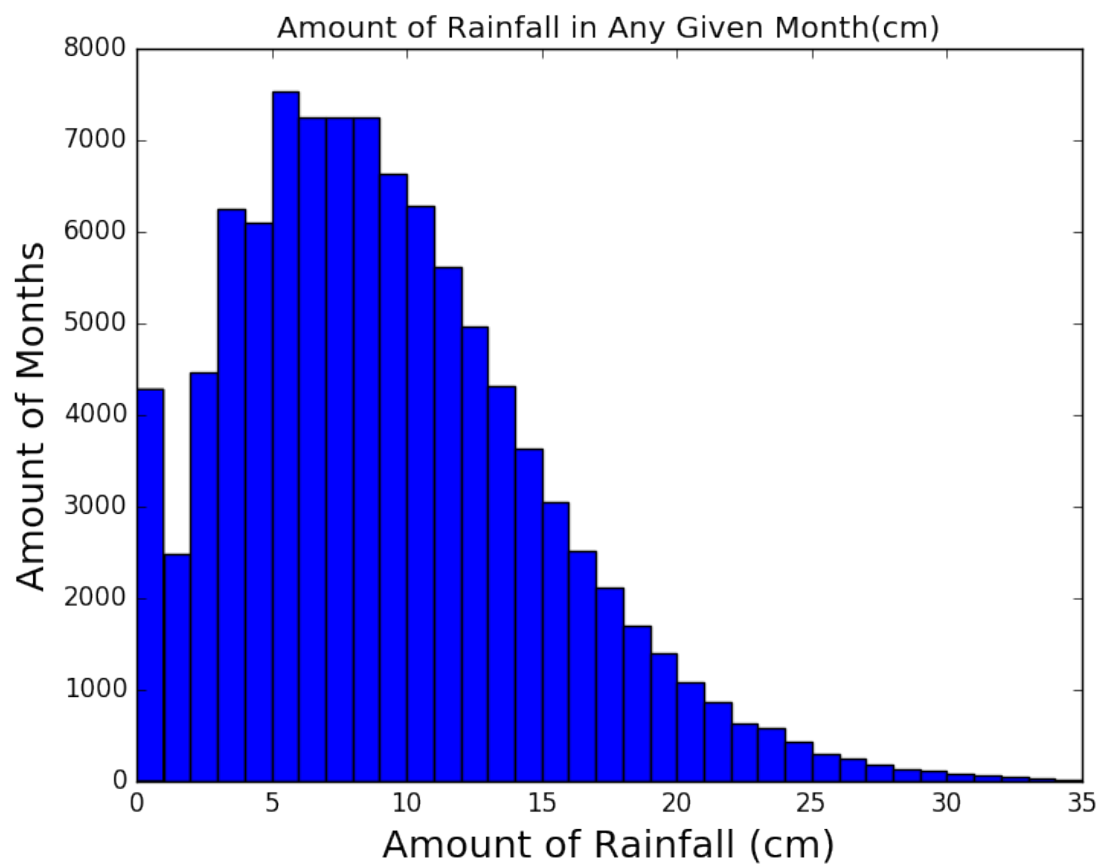


FIG. 1: This is a histogram for a test of 100,000 random months