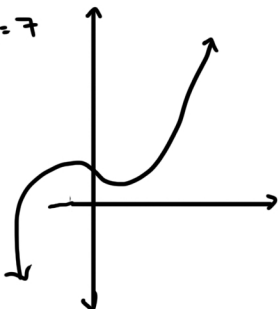


Questions from 2.1 (2.2 extension due to professor absence)

Type 4. prob. 3:

$$\lim_{x \rightarrow 1} S(x) = 7$$

Substitution



$$\lim_{x \rightarrow 1} g(x) = 4$$

$$\lim_{x \rightarrow 1} (5S(x) + g(x))$$

$$\lim_{x \rightarrow 1} 5S(x) + \lim_{x \rightarrow 1} g(x)$$

$$5(\lim_{x \rightarrow 1} f(x)) + 4$$

$$-35 + 4$$

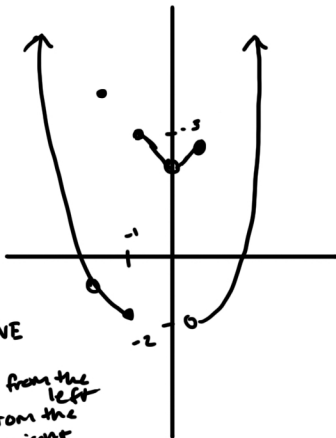
$$\boxed{-31}$$

$$S(x) = -7$$

$$g(x) = 4$$

Section 5 type 2:

In order for a limit to exist, it must approach both sides.



$$\lim_{x \rightarrow -1^-} S(x) = \text{DNE}$$

Negative \rightarrow from the left
Positive \rightarrow from the right

From the right \nwarrow
 $\lim_{x \rightarrow 0^+} S(x) = 2$

\nearrow From the left
 $\lim_{x \rightarrow 0^-} S(x) = 2$

Math Channel: 3 blue 1 brown

(factor and simplify)

$$\frac{3p^2 + 15p + 18}{9p^2 - 27p - 90}$$

$$9p^2 - 27p - 90 \text{ (divisible by 9)}$$

$$9(p^2 - 3p - 10)$$

$$\left| \begin{array}{c|c} p & -5 \\ \hline p & 2 \end{array} \right| \begin{array}{c} -5p \\ 2p \end{array} \left. \vphantom{\begin{array}{c|c} p & -5 \\ \hline p & 2 \end{array}} \right\} -3p$$

$$(p-5)(p+2)$$

$$\frac{3(p+2)(p+3)}{9(p-5)(p+2)}$$

$$\frac{p+3}{3(p-5)}$$

$$3p^2 + 15p + 18 \text{ (divisible by 3)}$$

$$3(p^2 + 5p + 6)$$

$$\left. \begin{array}{cc} p^2 & 2p \\ p & 3p \end{array} \right\} 5p$$

$$3(p+2)(p+3)$$

$$\lim_{x \rightarrow 7} \frac{x^2 - 4x - 21}{x - 7}$$

$$\frac{(7)^2 - 4(7) - 21}{(7) - 7} \quad \left(\begin{array}{c} \text{can't divide} \\ \text{by 0} \end{array} \right)$$

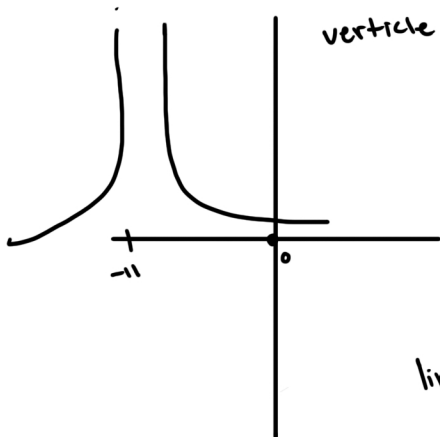
$$\frac{(x-7)(x+3)}{x-7}$$

$$\lim_{x \rightarrow 7} (x+3) = (7)+3 = 10$$

Type 4, problem 5

$$\lim_{x \rightarrow -11} S(x)$$

$$S(x) = \begin{cases} \frac{4x}{x+11} & \text{if } x < 0 \\ \frac{4x}{x-11} & \text{if } x > 0 \end{cases}$$



vertical asymptote = -11

$$\lim_{x \rightarrow -11} \frac{\frac{4x}{x}}{\frac{x+11}{x}} = \lim_{x \rightarrow -11} \frac{4}{1 + \frac{11}{x}} = \frac{4}{0}$$

if divide by 0,
= ∞