

$$S \rightarrow I \rightarrow R$$

S - susceptible individuals

I - individuals suffering from a disease and spreading the infection

R – recovered

Let's make this assumption:

1. the increase in the group of individuals sought is proportional to the number of individuals released and the number of susceptible individuals - rIS
2. the increase in healed individuals is directly proportional to the number online patients - aI , where $a > 0$.
3. the incubation period is so short that it can be neglected - the individual susceptible who got infected get sick immediately.
4. the population is thoroughly mixed - each type of individual has the same place and an individual of a different type.

With these assumptions, let's formulate the equations (Kermack-McKendrick (1972)):

$$\begin{aligned}\dot{S} &= -rSI \\ \dot{I} &= rSI - aI \\ \dot{R} &= aI\end{aligned}$$

Note that this model has a built-in assumption of constant-count:

$$\dot{S} + \dot{I} + \dot{R} = 0$$

Meaningful baseline data for the epidemiological model are:

$$S(0) = S_0 > 0, I(0) = I_0 > 0, R(0) = 0$$

The critical parameter $\rho = a / r$ is called the relative coefficient recovery and is the inverse of the contact ratio $\sigma = r / a$. Associated with it is the so-called base reproduction rate for a given infection:

$$R_B = \frac{rS_0}{a}$$

It describes the number of individuals newly infected by one currently infected. If $R_B > 1$, the disease spreads. One of the ways the reduction of the R_B is the reduction of the S_0 or the number of susceptible individuals. The baseline reproductive rate is a key controlled parameter e.g. by vaccination.

We have to fit this:

$$\frac{dR}{dt} = aI = a(N - R - S) = a(N - R - S_0 e^{-R/\rho})$$

dR/dt are recovered + deaths per day

We have everything except a and ρ . We can get this by fitting our data. Then we get R_B and we can compare R_B for different periods of time (for different restrictions).