# Package 'fabMix'

January 25, 2017

<b>Title</b> Overfitting Bayesian Mixtures of Factor Analyzers with an Unknown Number of Components
Version 1.0
<b>Date</b> 2017-01-25
Author Panagiotis Papastamoulis
Maintainer Panagiotis Papastamoulis <papapast@yahoo.gr></papapast@yahoo.gr>
Description
Model-based clustering of multivariate continuous data with possibly complex covaria
ture. The underlying model is a Bayesian mixture of factor analyzers with a large number
0.4.11.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4

Model-based clustering of multivariate continuous data with possibly complex covariance structure. The underlying model is a Bayesian mixture of factor analyzers with a large number of components (overfitting mixture). Suitable prior assumptions ensure that asymptotically the extra components will have zero posterior weight (empty), therefore, the inference on the number of clusters is based on the ``alive" components. The number of factors is considered fixed, and the optimal one can be estimated using information criteria. Identifiability issues related to label switching are dealt by post-processing the simulated output with the ECR algorithm.

Imports MASS, doParallel, foreach, label.switching, mvtnorm

License GPL-2

Type Package

NeedsCompilation no

## **R** topics documented:

fabMix-package
complete.log.likelihood
compute_A_B_G_D_and_simulate_mu_Lambda
compute_sufficient_statistics
dealWithLabelSwitching_same_sigma
fabMix
getStuffForDIC
log_dirichlet_pdf
myDirichlet
observed.log.likelihood0
overfittingMFA
update all y

2 fabMix-package

fabMi	ix-package	Over Num	,	0	-		xti	ure	2 <b>S</b> (	of	Fa	ct	or	Ai	ıaı	lyz	er	s v	vi	th	an	ı L	Jn.	kn	ou	'n
Index																										15
	update_z_b				•	 •				•		•										•				13
	update_z4																									
	update_SigmaINV	_faster																								12
	update_OmegaIN	V																								1.

#### **Description**

Model-based clustering of multivariate continuous data with possibly complex covariance structure. The underlying model is a Bayesian mixture of factor analyzers with a large number of components (overfitting mixture). Suitable prior assumptions ensure that asymptotically the extra components will have zero posterior weight (empty), therefore, the inference on the number of clusters is based on the "alive" components. The number of factors is considered fixed, and the optimal one can be estimated using information criteria. Identifiability issues related to label switching are dealt by post-processing the simulated output with the ECR algorithm.

#### **Details**

Model-based clustering of multivariate continuous data with possibly complex covariance structure. The underlying model is a Bayesian mixture of factor analyzers with a large number of components (overfitting mixture). Suitable prior assumptions ensure that asymptotically the extra components will have zero posterior weight (empty), therefore, the inference on the number of clusters is based on the "alive" components. The number of factors is considered fixed, and the optimal one can be estimated using information criteria. Identifiability issues related to label switching are dealt by post-processing the simulated output with the ECR algorithm.

#### Author(s)

Panagiotis Papastamoulis

Maintainer: Panagiotis Papastamoulis <papapast@yahoo.gr>

#### References

Fokoue, E. and Titterington, D.M. (2003). Mixtures of Factor Analysers: Bayesian Estimation and Inference by Stochastic Simulation. Machine Learing, 50(1): 73-94.

Papastamoulis P. and Iliopoulos G. (2010). An artificial allocations based solution to the label switching problem in Bayesian analysis of mixtures of distributions. Journal of Computational and Graphical Statistics, 19: 313-331.

van Havre, Z., White, N., Rousseau, J. and Mengersen, K. (2015). Overfitting Bayesian Mixture Models with an Unknown Number of Components. PLOS ONE, 10(7): 1-27.

Papastamoulis, P. (2016). label.switching: An R Package for Dealing with the Label Switching Problem in MCMC Outputs. Journal of Statistical Software, 69(1), 1-24.

Papastamoulis, P. (2017). Overfitting Bayesian mixtures of factor analyzers with an unknown number of components. arXiv:1701.04605 [stat.ME]

#### See Also

```
fabMix, dealWithLabelSwitching_same_sigma, getStuffForDIC
```

## **Examples**

```
runif(1)
```

```
complete.log.likelihood
```

Complete log-likelihood function

## Description

Complete log-likelihood function

## Usage

```
complete.log.likelihood(x_data, w, mu, Lambda, SigmaINV, z)
```

#### Arguments

x_data	Data

w Mixture weightsmu Marginal meansLambda Factor loadings

SigmaINV Precision matrix (inverse covariance)

z Allocation vector of the data to the mixture components

#### Value

complete log-likelihood value

## Author(s)

#### **Description**

This function simulates  $\mu$  and  $\Lambda$ .

#### Usage

```
compute_A_B_G_D_and_simulate_mu_Lambda(SigmaINV,
suff_statistics, OmegaINV, K, priorConst1, T_INV, v_r)
```

#### **Arguments**

SigmaINV Precision matrix  $\Sigma^{-1}$ 

suff\_statistics

Sufficient statistics

OmegaINV Prior parameter:  $\Omega^{-1}$ 

K Number of overfitting mixture components

priorConst1 Prior constant:  $T^{-1}\xi$ T\_INV Prior parameter:  $T^{-1}\xi$ 

v\_r This vector is used to set to zero the upper right  $(q-1) \times (q-1)$  diagonal block

of factor loadings for identifiability purposes.

#### Value

A list containing  $A, B, \Gamma, \Delta$  and a draw from the conditional distributions of  $\mu$  and  $\Lambda$ .

#### Author(s)

Panagiotis Papastamoulis

```
{\tt compute\_sufficient\_statistics}
```

Compute sufficient statistics

#### **Description**

Compute sufficient statistics given y and z.

#### Usage

```
compute_sufficient_statistics(y, z, K, x_data)
```

#### **Arguments**

У	Matrix of factors
Z	Allocation vector

K Number of components

x\_data Data

#### Value

A list with six entries of sufficient statistics.

#### Author(s)

Panagiotis Papastamoulis

dealWithLabelSwitching\_same\_sigma

Apply label switching algorithms for the  $\Sigma$  model

#### **Description**

This functions is a wrapper for the label. switching package and applies the ECR and ECR. ITERATIVE. 1 algorithms. The model should have the same variance of error terms per cluster.

## Usage

```
dealWithLabelSwitching_same_sigma(x_data, outputFolder, q, burn,
z.true, compute_regularized_expression, Km)
```

#### **Arguments**

x\_data Data

outputFolder Name of the folder where the fabMix function has saved its output

q Number of factors

burn Discard observations as burn-in period (optional).

z.true An (optional) vector of cluster assignments which is considered as the groun-

truth clustering of the data. Useful for direct comparisons against the real pa-

rameter values in simulated data.

compute\_regularized\_expression

Logical. Should regularized expression be computed?

Km Number of components in the overfitted mixture model.

#### Value

The following files are produced in the output folder:

6 fabMix

#### Author(s)

Panagiotis Papastamoulis

#### References

Papastamoulis, P. (2016). label.switching: An R Package for Dealing with the Label Switching Problem in MCMC Outputs. Journal of Statistical Software, 69(1), 1-24.

fabMix Main function of the package

## Description

This function runs parallel chains under a prior tempering scheme of the Dirichlet prior distribution of mixture weights.

#### Usage

```
fabMix(dirPriorAlphas, rawData, outDir, Kmax, mCycles, burnCycles,
g, h, alpha_sigma, beta_sigma, q, normalize, thinning, zStart, nIterPerCycle)
```

#### **Arguments**

${\tt dirPriorAlphas}$	The prior Dirichlet parameters for each chain.
rawData	The observed data as an $n \times p$ matrix. Clustering is performed on the rows of the matrix.
outDir	Name of the output folder.
Kmax	Number of components in the overfitted mixture. Default: 20.
mCycles	Number of MCMC cycles. Each cycle consists of nIterPerCycle MCMC iterations. At the end of each cycle a swap of the state of two randomly chosen adjacent chains is attempted.
burnCycles	Number of cycles that will be discarded as burn-in period.
g	Prior parameter $g$ . Default value: $g = 2$ .
h	Prior parameter $h$ . Default value: $h = 1$ .
alpha_sigma	Prior parameter $\alpha$ . Default value: $\alpha = 2$ .
beta_sigma	Prior parameter $\beta$ . Default value: $\beta = 1$ .
q	Number of factors $q$ , where $1 \leq q \leq L$ . An error is thrown if the Ledermann bound $(L)$ is exceeded.
normalize	Should the observed data be normalized? Default value: TRUE.
thinning	Optional integer denoting the thinning of the keeped MCMC cycles.
zStart	Optional starting value for the allocation vector.
nIterPerCycle	Number of iteration per MCMC cycle. Default value: 10.

getStuffForDIC 7

#### Value

List of files written to outDir

#### Note

It is recommended to always use: normalize = TRUE (default). Tuning of dirPriorAlphas may be necessary to achieve reasonable acceptance rates of chain swaps. Also note that the output is not identifiable due to label switching and the user has to subsequently call the dealWithLabelSwitching\_same\_sigma function.

#### Author(s)

Panagiotis Papastamoulis

#### References

Papastamoulis, P. (2017). Overfitting Bayesian mixtures of factor analyzers with an unknown number of components. arXiv:1701.04605 [stat.ME]

#### See Also

dealWithLabelSwitching\_same\_sigma

getStuffForDIC	Compute information criteria	

#### **Description**

This function computes four information criteria for a given run of the fabMix algorithm, namely: AIC, BIC, DIC and DIC<sub>2</sub>. Given various runs with different number of factors, the selected model corresponds to the one with the smalled value of the selected criterion.

#### Usage

```
getStuffForDIC(x_data, outputFolder, q, burn, Km, normalize, discardLower)
```

#### **Arguments**

x_data	Observed data.
outputFolder	Name of the folder where the fabMix function has saved its output.
q	Number of factors. Note that this should coincide with the number of factors in the fabMix run.
burn	Discard observations as burn-in period (optional).
Km	Number of components in the overfitted mixture model. Note that this should coincide with the same entry in the fabMix run.

8 log\_dirichlet\_pdf

normalize Should the observed data be normalized? Note that this should coincide with

the same entry in the fabMix run. Default value: TRUE.

discardLower Discard draws with log-likelihood values lower than the specific quantile. This

applied only for the DIC computation.

#### **Details**

If necessary, more details than the description above

#### Value

The information criteria are saved to the informationCriteria\_map\_model.txt file in the code-outputFolder.

#### Note

It is well known that DIC tends to overfit, so it advised to compare models with different number of factors using AIC or BIC.

#### Author(s)

Panagiotis Papastamoulis

log\_dirichlet\_pdf

Log-density function of the Dirichlet distribution

#### **Description**

Log-density function of the Dirichlet distribution

#### Usage

```
log_dirichlet_pdf(alpha, weights)
```

## Arguments

alpha Parameter vector weights Vector of weights

#### Value

```
Log-density of the D(alpha_1, \ldots, \alpha_k) evaluated at w_1, \ldots, w_k.
```

#### Author(s)

myDirichlet 9

myDirichlet

Simulate from the Dirichlet distribution

## Description

Generate a random draw from the Dirichlet distribution  $D(\alpha_1, \ldots, \alpha_k)$ .

## Usage

```
myDirichlet(alpha)
```

#### **Arguments**

alpha

Parameter vector

#### Value

Simulated vector

#### Author(s)

Panagiotis Papastamoulis

observed.log.likelihood0

Log-likelihood of the mixture model

## Description

Log-likelihood of the mixture model evaluated only at the alive components.

#### Usage

```
observed.log.likelihood0(x_data, w, mu, Lambda, Sigma, z)
```

## Arguments

x\_data The observed data

w Vector of mixture weights mu Vector of marginal means

Lambda Factor loadings

Sigma Common covariance matrix of the errors per cluster

z Allocation vector

10 overfittingMFA

#### Value

Log-likelihood value

#### Author(s)

Panagiotis Papastamoulis

overfittingMFA

Basic MCMC sampler

#### **Description**

Gibbs sampling for fitting a mixture model of factor analyzers.

#### Usage

```
overfittingMFA(x_data, originalX, outputDirectory, Kmax, m, thinning, burn, g, h, alpha_prior, alpha_sigma, beta_sigma, start_values, q, zStart, gibbs_z)
```

#### **Arguments**

x\_data normalized data

originalX observed raw data (only for plotting purpose)

outputDirectory

Name of the output folder

Kmax Number of mixture components

m Number of iterationsthinning Thinning of chainburn Burn-in period

g Prior parameter g. Default value: g=2. h Prior parameter h. Default value: h=1.

alpha\_prior Parameters of the Dirichlet prior distribution of mixture weights.

alpha\_sigma Prior parameter  $\alpha$ . Default value:  $\alpha=2$ . beta\_sigma Prior parameter  $\beta$ . Default value:  $\beta=1$ .

start\_values Optional (not used)
q Number of factors.
zStart Optional (not used)

gibbs\_z Optional

#### Value

List of files

#### Author(s)

update\_all\_y

update_	all v	
upua te_	_атт_у	

Gibbs sampling for y

## Description

Gibbs sampling for y

## Usage

```
update_all_y(x_data, mu, SigmaINV, Lambda, z)
```

## Arguments

mu Marginal means
SigmaINV Precision matrix
Lambda Factor loadings
z Allocation vector

#### Value

A matrix with generated factors

## Author(s)

Panagiotis Papastamoulis

update	_OmegaINV
apaatt_	_Omcgaint

Gibbs sampling for  $\Omega^-1$ 

## Description

Gibbs sampling for  $\Omega^{-1}$ 

## Usage

```
update_OmegaINV(Lambda, K, g, h)
```

## Arguments

	_	
Lambda	Factor	loadings

K Number of components

g Prior parameterh Prior parameter

## Value

 $\Omega^{-1}$ 

#### Author(s)

Panagiotis Papastamoulis

update\_SigmaINV\_faster

Gibbs sampling for  $\Sigma^-1$ 

## Description

Gibbs sampling for  $\Sigma^{-1}$ 

## Usage

```
update_SigmaINV_faster(x_data, z, y, Lambda, mu, K, alpha_sigma, beta_sigma)
```

## Arguments

x\_data Data

z Allocation vector

y Factors

Lambda Factor loadings mu Marginal means

K Number of components

alpha\_sigma Prior parameter beta\_sigma Prior parameter

## Value

 $\Sigma^{-1}$ 

## Author(s)

update\_z4

update\_z4

Collapsed Gibbs for z

## Description

Collapsed Gibbs for z

## Usage

```
update_z4(w, mu, Lambda, SigmaINV, K, x_data)
```

## Arguments

w Mixture weightsmu Marginal meansLambda Factor loadingsSigmaINV Precision matrix

K Number of components

x\_data Data

## Value

Allocation vector

## Author(s)

Panagiotis Papastamoulis

update\_z\_b

Gibbs sampling for z

## Description

Gibbs sampling for z

#### Usage

```
update_z_b(w, mu, Lambda, y, SigmaINV, K, x_data)
```

14 update\_z\_b

## Arguments

w Mixture weights
 mu Marginal means
 Lambda Factor loadings
 y Matrix of factors
 SigmaINV Precision matrix

K Number of components

x\_data Data

#### Value

Allocation vector

## Author(s)

# **Index**

```
*Topic package
    fabMix-package, 2
complete.log.likelihood, 3
compute\_A\_B\_G\_D\_and\_simulate\_mu\_Lambda,
compute_sufficient_statistics, 4
dealWithLabelSwitching_same_sigma, 3, 5,
fabMix, 3, 6
fabMix-package, 2
getStuffForDIC, 3, 7
log\_dirichlet\_pdf, 8
myDirichlet, 9
observed.log.likelihood0,9
{\tt overfittingMFA}, {\color{red}10}
update_all_y, 11
update\_OmegaINV, \\ 11
update_SigmaINV_faster, 12
update_z4, 13
update_z_b, 13
```