# Package 'fabMix'

October 3, 2018

Type Package

**Title** Overfitting Bayesian Mixtures of Factor Analyzers with Parsimonious Covariance and Unknown Number of Components

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#### **Description**

Model-based clustering of multivariate continuous data using Bayesian mixtures of factor analyzers (Papastamoulis, 2018 Computational Statistics and Data Analysis). The number of clusters is estimated using overfitting mixture models (Rousseau and Mengersen, 2011 Journal of the Royal Statistical Society B): suitable prior assumptions ensure that asymptotically the extra components will have zero posterior weight, therefore, the inference is based on the "alive" components. A Gibbs sampler is implemented in order to (approximately) sample from the posterior distribution of the overfitted mixture. A prior parallel tempering scheme is also available, which allows to run multiple parallel chains with different prior distributions on the mixture weights. These chains run in parallel and can swap states using a Metropolis-Hastings move. The number of factors is considered fixed and the optimal one can be estimated using the Bayesian Information Criterion. Eight different parameterizations give rise to parsimonious representations of the covariance per cluster (following Mc Nicholas and others, 2008 Statistics and Computing). Identifiability issues related to label switching are dealt by post-processing the simulated output with the Equivalence Classes Representatives algorithm (Papastamoulis 2010 Journal of Computational and Graphical Statistics, 2016 Journal of Statistical Software). Missing values are currently allowed for two model parameterizations.

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**Imports** Rcpp (>= 0.12.17), MASS, doParallel, foreach, label.switching, mvtnorm, doRNG, RColorBrewer, corrplot, mclust

LinkingTo Rcpp, RcppArmadillo

**NeedsCompilation** yes

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#### **Description**

Model-based clustering of multivariate continuous data using Bayesian mixtures of factor analyzers (Papastamoulis, 2018 Computational Statistics and Data Analysis). The number of clusters is estimated using overfitting mixture models (Rousseau and Mengersen, 2011 Journal of the Royal Statistical Society B): suitable prior assumptions ensure that asymptotically the extra components will have zero posterior weight, therefore, the inference is based on the "alive" components. A Gibbs sampler is implemented in order to (approximately) sample from the posterior distribution of the overfitted mixture. A prior parallel tempering scheme is also available, which allows to run multiple parallel chains with different prior distributions on the mixture weights. These chains run in parallel and can swap states using a Metropolis-Hastings move. The number of factors is considered fixed and the optimal one can be estimated using the Bayesian Information Criterion. Eight different parameterizations give rise to parsimonious representations of the covariance per cluster (following Mc Nicholas and others, 2008 Statistics and Computing). Identifiability issues related to label switching are dealt by post-processing the simulated output with the Equivalence Classes Representatives algorithm (Papastamoulis 2010 Journal of Computational and Graphical Statistics, 2016 Journal of Statistical Software). Missing values are currently allowed for two model parameterizations.

The main fuction of the package is fabMix.

# Author(s)

Panagiotis Papastamoulis

Maintainer: Panagiotis Papastamoulis <papapast@yahoo.gr>

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#### References

Fokoue, E. and Titterington, D.M. (2003). Mixtures of Factor Analysers: Bayesian Estimation and Inference by Stochastic Simulation. Machine Learing, 50(1): 73-94.

McNicholas, P.D. and Murphy, T.B. Statistics and Computing (2008) 18: 285. https://doi.org/10.1007/s11222-008-9056-0.

Papastamoulis P. and Iliopoulos G. (2010). An artificial allocations based solution to the label switching problem in Bayesian analysis of mixtures of distributions. Journal of Computational and Graphical Statistics, 19: 313-331.

Rousseau, J. and Mengersen, K. (2011). Asymptotic behaviour of the posterior distribution in overfitted mixture models. Journal of the Royal Statistical Society, Series B (methodological), 73(5): 689-710.

van Havre, Z., White, N., Rousseau, J. and Mengersen, K. (2015). Overfitting Bayesian Mixture Models with an Unknown Number of Components. PLOS ONE, 10(7): 1-27.

Papastamoulis, P. (2016). label.switching: An R Package for Dealing with the Label Switching Problem in MCMC Outputs. Journal of Statistical Software, 69(1), 1-24.

Papastamoulis, P. (2018). Overfitting Bayesian mixtures of factor analyzers with an unknown number of components. Computational Statistics and Data Analysis, 124: 220-234. DOI: 10.1016/j.csda.2018.03.007.

#### See Also

```
fabMix,plot.fabMix.object
```

#### **Examples**

```
# TOY EXAMPLE (very small numbers...)
library('fabMix')
n = 8
                     # sample size
                     # number of variables
p = 5
                     # number of factors
q = 2
K = 2
           # number of clusters
sINV_{diag} = 1/((1:p)) # diagonal of inverse variance of errors
set.seed(100)
syntheticDataset <- simData(sameLambda=TRUE,K.true = K, n = n, q = q, p = p,
sINV_values = sINV_diag)
colnames(syntheticDataset$data) <- paste0("x_",1:p)</pre>
qRange <- 1:2 # range of values for the number of factors
Kmax <- 20 # number of components for the overfitted mixture model
nChains <- 2 # number of parallel heated chains
# Run `fabMix` for a _small_ number of iterations for the
# `UUU` (maximal model) and `CCC` (minimal model) parameterizations,
# using the default prior parallel heating parameters `dirPriorAlphas`.
# NOTE: `dirPriorAlphas` may require some tuning in general.
set.seed(3)
fm <- fabMix( model = c("UUU", "CCC"), nChains = 2,</pre>
```

complete.log.likelihood

complete.log.likelihood

Complete log-likelihood function

# Description

Complete log-likelihood function

## Usage

```
complete.log.likelihood(x_data, w, mu, Lambda, SigmaINV, z)
```

#### **Arguments**

x_data	Data
W	Mixture weights
mu	Marginal means
Lambda	Factor loadings
SigmaINV	Precision matrix (inverse covariance)
Z	Allocation vector of the data to the mixture components

# Value

complete log-likelihood value

#### Author(s)

Panagiotis Papastamoulis

```
complete.log.likelihood_q0
```

Complete log-likelihood function for q=0

# Description

Complete log-likelihood function

# Usage

```
complete.log.likelihood_q0(x_data, w, mu, SigmaINV, z)
```

## **Arguments**

x\_data Data

w Mixture weightsmu Marginal means

SigmaINV Precision matrix (inverse covariance)

z Allocation vector of the data to the mixture components

#### Value

complete log-likelihood value

# Author(s)

Panagiotis Papastamoulis

```
complete.log.likelihood_q0_sameSigma
```

Complete log-likelihood function for q = 0

# **Description**

Complete log-likelihood function

```
complete.log.likelihood_q0_sameSigma(x_data, w, mu, SigmaINV, z)
```

#### **Arguments**

x\_data Data

w Mixture weightsmu Marginal means

SigmaINV Precision matrix (inverse covariance)

z Allocation vector of the data to the mixture components

#### Value

complete log-likelihood value

## Author(s)

Panagiotis Papastamoulis

complete.log.likelihood\_Sj

Complete log-likelihood function

# Description

Complete log-likelihood function

# Usage

```
complete.log.likelihood_Sj(x_data, w, mu, Lambda, SigmaINV, z)
```

## **Arguments**

x\_data Data

w Mixture weightsmu Marginal meansLambda Factor loadings

SigmaINV Precision matrix (inverse covariance) per component

z Allocation vector of the data to the mixture components

#### Value

complete log-likelihood value

#### Author(s)

Panagiotis Papastamoulis

# Description

This function simulates  $\mu$  and  $\Lambda$ .

# Usage

```
compute_A_B_G_D_and_simulate_mu_Lambda(SigmaINV,
    suff_statistics, OmegaINV, K, priorConst1, T_INV, v_r)
```

# **Arguments**

SigmaINV Precision matrix  $\Sigma^{-1}$ 

suff\_statistics

Sufficient statistics

OmegaINV Prior parameter:  $\Omega^{-1}$ 

K Number of overfitting mixture components

 $\begin{array}{ll} {\rm priorConst1} & {\rm Prior\ constant:}\ T^{-1}\xi \\ {\rm T\_INV} & {\rm Prior\ parameter:}\ T^{-1}\xi \end{array}$ 

v\_r This vector is used to set to zero the upper right  $(q-1) \times (q-1)$  diagonal block

of factor loadings for identifiability purposes.

#### Value

A list containing  $A, B, \Gamma, \Delta$  and a draw from the conditional distributions of  $\mu$  and  $\Lambda$ .

## Author(s)

Panagiotis Papastamoulis

```
\label{lem:compute_A_B_G_D_and_simulate_mu_Lambda_CCU} Computation\ and\ simulations\ for\ CCU
```

#### Description

This function simulates  $\mu$  and  $\Lambda$  for the CCU model.

```
compute_A_B_G_D_and_simulate_mu_Lambda_CCU(SigmaINV,
suff_statistics, OmegaINV, K, priorConst1, T_INV, v_r)
```

#### **Arguments**

SigmaINV Precision matrix  $\Sigma^{-1}$ 

suff\_statistics

OmegaINV

Sufficient statistics
Prior parameter:  $\Omega^{-1}$ 

K Number of overfitting mixture components

 $\begin{array}{ll} {\rm priorConst1} & {\rm Prior\ constant:}\ T^{-1}\xi \\ {\rm T\_INV} & {\rm Prior\ parameter:}\ T^{-1}\xi \end{array}$ 

v\_r This vector is used to set to zero the upper right  $(q-1) \times (q-1)$  diagonal block

of factor loadings for identifiability purposes.

#### Value

A list containing A, B,  $\Gamma$ ,  $\Delta$  and a draw from the conditional distributions of  $\mu$  and  $\Lambda$ .

# Author(s)

Panagiotis Papastamoulis

```
\label{lem:compute_A_B_G_D_and_simulate_mu_Lambda_CUU} Computation\ and\ simulations\ for\ CUU
```

#### **Description**

This function simulates  $\mu$  and  $\Lambda$  for the CUU model.

#### Usage

```
compute_A_B_G_D_and_simulate_mu_Lambda_CUU(SigmaINV,
   suff_statistics, OmegaINV, K, priorConst1, T_INV, v_r)
```

# **Arguments**

SigmaINV Precision matrix  $\Sigma^{-1}$ 

suff\_statistics

Sufficient statistics

OmegaINV Prior parameter:  $\Omega^{-1}$ 

K Number of overfitting mixture components

 $\begin{array}{ll} {\rm priorConst1} & {\rm Prior\ constant:}\ T^{-1}\xi \\ {\rm T\_INV} & {\rm Prior\ parameter:}\ T^{-1}\xi \end{array}$ 

v\_r This vector is used to set to zero the upper right  $(q-1) \times (q-1)$  diagonal block

of factor loadings for identifiability purposes.

## Value

A list containing  $A, B, \Gamma, \Delta$  and a draw from the conditional distributions of  $\mu$  and  $\Lambda$ .

#### Author(s)

Panagiotis Papastamoulis

```
\label{eq:compute_ABGD_and_simulate_mu_Lambda_q0} Computation\ and\ simulations\ for\ q=0.
```

# Description

This function simulates  $\mu$ .

# Usage

```
compute_A_B_G_D_and_simulate_mu_Lambda_q0(SigmaINV,
suff_statistics, K, priorConst1, T_INV, v_r)
```

## **Arguments**

 $\begin{tabular}{ll} {\bf SigmaINV} & {\bf Precision \ matrix} \ \Sigma^{-1} \\ {\bf suff\_statistics} \end{tabular}$ 

Sufficient statistics

K Number of overfitting mixture components

priorConst1 Prior constant:  $T^{-1}\xi$  T\_INV Prior parameter:  $T^{-1}\xi$ 

v\_r This vector is used to set to zero the upper right  $(q-1) \times (q-1)$  diagonal block

of factor loadings for identifiability purposes.

# Value

A list containing  $A, B, \Gamma, \Delta$  and a draw from the conditional distributions of  $\mu$  and  $\Lambda$ .

#### Author(s)

Panagiotis Papastamoulis

 $\label{lem:compute_A_B_G_D_and_simulate_mu_Lambda_q0_sameSigma} Computation\ and\ simulations\ for\ q=0.$ 

#### **Description**

This function simulates  $\mu$ .

## Usage

```
compute_A_B_G_D_and_simulate_mu_Lambda_q0_sameSigma(SigmaINV,
suff_statistics, K, priorConst1, T_INV, v_r)
```

#### **Arguments**

 $\begin{array}{ll} {\rm SigmaINV} & {\rm Precision\; matrix}\; \Sigma^{-1} \\ {\rm suff\_statistics} \end{array}$ 

Sufficient statistics

K Number of overfitting mixture components

 $\begin{array}{ll} {\rm priorConst1} & {\rm Prior\ constant:}\ T^{-1}\xi \\ {\rm T\_INV} & {\rm Prior\ parameter:}\ T^{-1}\xi \end{array}$ 

v\_r This vector is used to set to zero the upper right  $(q-1) \times (q-1)$  diagonal block

of factor loadings for identifiability purposes.

# Value

A list containing  $A, B, \Gamma, \Delta$  and a draw from the conditional distributions of  $\mu$  and  $\Lambda$ .

#### Author(s)

Panagiotis Papastamoulis

```
\label{lem:compute_A_B_G_D_and_simulate_mu_Lambda_Sj} Computation\ and\ simulations
```

#### **Description**

This function simulates  $\mu$  and  $\Lambda$ .

```
compute_A_B_G_D_and_simulate_mu_Lambda_Sj(SigmaINV,
suff_statistics, OmegaINV, K, priorConst1, T_INV, v_r)
```

#### **Arguments**

SigmaINV Precision matrix  $\Sigma^{-1}$  per component

suff\_statistics

Sufficient statistics

OmegaINV Prior parameter:  $\Omega^{-1}$ 

K Number of overfitting mixture components

 $\begin{array}{ll} {\rm priorConst1} & {\rm Prior\ constant:}\ T^{-1}\xi \\ {\rm T\_INV} & {\rm Prior\ parameter:}\ T^{-1}\xi \end{array}$ 

v\_r This vector is used to set to zero the upper right  $(q-1) \times (q-1)$  diagonal block

of factor loadings for identifiability purposes.

## Value

A list containing  $A, B, \Gamma, \Delta$  and a draw from the conditional distributions of  $\mu$  and  $\Lambda$ .

#### Author(s)

Panagiotis Papastamoulis

compute\_sufficient\_statistics

Compute sufficient statistics

# Description

Compute sufficient statistics given y and z.

## Usage

```
compute_sufficient_statistics(y, z, K, x_data)
```

# **Arguments**

y Matrix of factors z Allocation vector

K Number of components

x\_data Data

# Value

A list with six entries of sufficient statistics.

# Author(s)

Panagiotis Papastamoulis

```
compute_sufficient_statistics_given_mu

Compute sufficient statistics given mu
```

# Description

Compute sufficient statistics given y and z.

# Usage

```
compute_sufficient_statistics_given_mu(y, z, K, x_data,mu)
```

# **Arguments**

У	Matrix of factors
z	Allocation vector
K	Number of components

x\_data Data

mu Means per component

#### Value

A list with six entries of sufficient statistics.

# Author(s)

Panagiotis Papastamoulis

```
\label{eq:compute_sufficient_statistics_q0} \textit{Compute sufficient statistics for } q = 0
```

# Description

Compute sufficient statistics given z.

# Usage

```
compute_sufficient_statistics_q0(z, K, x_data)
```

# Arguments

K Number of components

x\_data Data

#### Value

A list with six entries of sufficient statistics.

#### Author(s)

Panagiotis Papastamoulis

dealWithLabelSwitching

Apply label switching algorithms

## **Description**

This functions is a wrapper for the label. switching package and applies the ECR and ECR.ITERATIVE.1 algorithms. The model may have the same variance of error terms per cluster or not.

## Usage

```
dealWithLabelSwitching(sameSigma, x_data, outputFolder, q, burn,
z.true, compute_regularized_expression, Km)
```

#### **Arguments**

sameSigma Logical value indicating whether the parameterization with the same error vari-

ance per cluster is used.

x\_data Data

outputFolder Name of the folder where the fabMix function has saved its output

q Number of factors

burn Discard observations as burn-in period (optional).

z.true An (optional) vector of cluster assignments which is considered as the groun-

truth clustering of the data. Useful for direct comparisons against the real pa-

rameter values in simulated data.

compute\_regularized\_expression

Logical. Should regularized expression be computed?

Km Number of components in the overfitted mixture model.

## Value

The following files are produced in the output folder:

#### Author(s)

Panagiotis Papastamoulis

#### References

Papastamoulis, P. (2016). label.switching: An R Package for Dealing with the Label Switching Problem in MCMC Outputs. Journal of Statistical Software, 69(1), 1-24.

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fabMix	Main function		
--------	---------------	--	--

# Description

This function runs parallel chains under a prior tempering scheme of the Dirichlet prior distribution of mixture weights.

# Usage

```
fabMix(model, nChains, dirPriorAlphas, rawData, outDir, Kmax, mCycles,
burnCycles, g, h, alpha_sigma, beta_sigma, q, normalize,
thinning, zStart, nIterPerCycle, gibbs_z,
warm_up_overfitting, warm_up, overfittingInitialization,
progressGraphs, gwar, rmDir)
```

# Arguments

model	Any subset of "UUU" "CUU" "UCU" "CCU" "UCC" "UUC" "CUC", "CCC" indicating the fitted models. By default, all models are fitted.
nChains	The number of parallel heated chains. When 'dirPriorAlphas' is supplied, 'nChains' can be ignored.
dirPriorAlphas	vector of length nChains in the form of an increasing sequence of positive scalars. Each entry contains the (common) prior Dirichlet parameter for the corresponding chain. Default: $dirPriorAlphas = c(1, 1 + dN*(2:nChains - 1))/Kmax$ , where $dN = 1$ , for nChains > 1. Otherwise, $dirPriorAlphas = 1/Kmax$ .
rawData	The observed data as an $n \times p$ matrix. Clustering is performed on the rows of the matrix.
outDir	Name of the output folder. An error is thrown if this directory already exists.
Kmax	Number of components in the overfitted mixture. Default: 20.
mCycles	Number of MCMC cycles. Each cycle consists of nIterPerCycle MCMC iterations. At the end of each cycle a swap of the state of two randomly chosen adjacent chains is attempted.
burnCycles	Number of cycles that will be discarded as burn-in period.
g	Prior parameter $g$ . Default value: $g = 0.5$ .
h	Prior parameter $h$ . Default value: $h = 0.5$ .
alpha_sigma	Prior parameter $\alpha$ . Default value: $\alpha = 0.5$ .
beta_sigma	Prior parameter $\beta$ . Default value: $\beta = 0.5$ .
q	A vector containing the number of factors to be fitted.
normalize	Should the observed data be normalized? Default value: TRUE. (Recommended)
thinning	Optional integer denoting the thinning of the keeped MCMC cycles.
zStart	Optional starting value for the allocation vector.

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nIterPerCycle Number of iteration per MCMC cycle. Default value: 10.

gibbs\_z Select the gibbs sampling scheme for updating latent allocations of mixture model. Default value: 1.

warm\_up\_overfitting

Number of iterations for the overfitting initialization scheme. Default value: 500.

warm\_up Number of iterations that will be used to initialize the models before starting proposing switchings. Default value: 5000.

overfittingInitialization

Logical value indicating whether the chains are initialized via the overfitting initialization scheme. Default: TRUE.

progressGraphs Logical value indicating whether to plot successive states of the chains while the sampler runs. Default: FALSE.

gwar Initialization parameter. Default: 0.05.

rmDir Logical value indicating whether to delete the outDir directory. Default: TRUE.

#### **Details**

Let  $X_i$ ;  $i=1,\ldots,n$  denote independent p-dimensional random vectors. Let  $Y_i \in R^q$  with q < p denote the latent factor for observation  $i=1,\ldots,n$ . In the typical factor analysis model, each observation is modelled as  $X_i = \mu + \Lambda Y_i + \varepsilon_i$ , with  $\varepsilon_i \sim \mathcal{N}(0, \Sigma)$ , where  $\varepsilon_i$  and  $Y_i$  are assumed independent,  $i=1,\ldots,n$ . The  $p \times q$  matrix  $\Lambda$  consists of the factor loadings. Assume that there are K clusters and let  $Z_i$  denotes the latent allocation of observation i to one amongs the k clusters, with prior probability  $P(Z_i = k) = w_k, k = 1, \ldots, K$ , independent for  $i=1,\ldots,n$ . Following McNicholas et al (2008), the following parameterizations are used:

UUU model:  $(\boldsymbol{X}_i|Z_i=k)=\boldsymbol{\mu}_k+\boldsymbol{\Lambda}_k\boldsymbol{Y}_i+\boldsymbol{\varepsilon}_i, \text{ with } \boldsymbol{\varepsilon}_i\sim\mathcal{N}(0,\boldsymbol{\Sigma}_k)$ 

UCU model:  $(\boldsymbol{X}_i|Z_i=k)=\boldsymbol{\mu}_k+\boldsymbol{\Lambda}_k\boldsymbol{Y}_i+\boldsymbol{\varepsilon}_i, \text{ with } \boldsymbol{\varepsilon}_i\sim\mathcal{N}(0,\boldsymbol{\Sigma})$ 

UUC model:  $(\boldsymbol{X}_i|Z_i=k)=\boldsymbol{\mu}_k+\boldsymbol{\Lambda}_k\boldsymbol{Y}_i+\boldsymbol{\varepsilon}_i, \text{ with } \boldsymbol{\varepsilon}_i\sim\mathcal{N}(0,\sigma_k\boldsymbol{I}_p)$ 

UCC model:  $(\boldsymbol{X}_i|Z_i=k)=\boldsymbol{\mu}_k+\boldsymbol{\Lambda}_k\boldsymbol{Y}_i+\boldsymbol{\varepsilon}_i,$  with  $\boldsymbol{\varepsilon}_i\sim\mathcal{N}(0,\sigma\boldsymbol{I}_p)$ 

CUU model:  $(\boldsymbol{X}_i|Z_i=k)=\boldsymbol{\mu}_k+\boldsymbol{\Lambda}\boldsymbol{Y}_i+\boldsymbol{\varepsilon}_i,$  with  $\boldsymbol{\varepsilon}_i\sim\mathcal{N}(0,\boldsymbol{\Sigma}_k)$ 

CCU model:  $(\boldsymbol{X}_i|Z_i=k) = \boldsymbol{\mu}_k + \boldsymbol{\Lambda}\boldsymbol{Y}_i + \boldsymbol{\varepsilon}_i$ , with  $\boldsymbol{\varepsilon}_i \sim \mathcal{N}(0, \boldsymbol{\Sigma})$ 

CUC model:  $(X_i|Z_i=k) = \mu_k + \Lambda Y_i + \varepsilon_i$ , with  $\varepsilon_i \sim \mathcal{N}(0, \sigma_k I_p)$ 

CCC model:  $(\boldsymbol{X}_i|Z_i=k)=\boldsymbol{\mu}_k+\boldsymbol{\Lambda}\boldsymbol{Y}_i+\boldsymbol{\varepsilon}_i, \text{ with } \boldsymbol{\varepsilon}_i\sim\mathcal{N}(0,\sigma\boldsymbol{I}_p)$ 

In all cases,  $\varepsilon_i$  and  $Y_i$  are assumed independent,  $i=1,\ldots,n$ . Note that  $\Sigma_k$  and  $\Sigma$  denote positive definite matrices,  $I_p$  denotes the  $p \times p$  identity matrix and  $\sigma_k$ ,  $\sigma$  denote positive scalars.

#### Value

An object of class fabMix.object, that is, a list consisting of the following entries:

bic Bayesian Information Criterion per model and number of factors.

class The estimated single best clustering of the observations according to the selected model.

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n\_Clusters\_per\_model

The most probable number of clusters (number of non-empty components of the overfitted mixture) per model and number of factors.

posterior\_probability

The posterior probability of the estimated allocations according to the selected model.

covariance\_matrix

The estimated posterior mean of the covariance matrix per cluster according to

the selected model.

mu The estimated posterior mean of the mean per cluster according to the selected

model.

weights The estimated posterior mean of the mixing proportions according to the se-

lected model.

selected\_model

Data frame containing the parameterization, number of clusters and factors of

the selected model.

mcmc A list containing the MCMC draws for the parameters of the selected models.

All component-specific parameters have been reordered according to the ECR

algorithm in order to undo the label switching problem.

data The observed data.

#### Note

It is recommended to always use: normalize = TRUE (default). Tuning of dirPriorAlphas may be necessary to achieve reasonable acceptance rates of chain swaps. Note that the output is reordered in order to deal with the label switching problem, according to the ECR algorithm applied by dealWithLabelSwitching function.

# Author(s)

Panagiotis Papastamoulis

#### References

McNicholas, P.D. and Murphy, T.B. Stat Comput (2008) 18: 285. https://doi.org/10.1007/s11222-008-9056-0.

Papastamoulis, P. (2018). Overfitting Bayesian mixtures of factor analyzers with an unknown number of components. Computational Statistics and Data Analysis, 124: 220-234. DOI: 10.1016/j.csda.2018.03.007.

#### See Also

```
plot.fabMix.object
```

## **Examples**

```
## Not run:
library('fabMix')
```

 $fabMix\_CxC$ 

```
n = 90
                      # sample size
                      # number of variables
p = 50
q = 2
                     # number of factors
K = 3
           # number of clusters
sINV_diag = 1/((1:p)) # diagonal of inverse variance of errors
set.seed(100)
syntheticDataset <- simData(sameLambda=FALSE,K.true = K, n = n, q = q, p = p,</pre>
sINV_values = sINV_diag)
colnames(syntheticDataset$data) <- paste0("x_",1:p)</pre>
qRange <- 1:3 # range of values for the number of factors
Kmax <- 20 # number of components for the overfitted mixture model
nChains <- 8 # number of parallel heated chains
set.seed(3)
fm <- fabMix( rawData = syntheticDataset$data,</pre>
nChains = nChains, outDir = "fabMixExample",
        Kmax = Kmax, mCycles = 500, burnCycles = 100, q = qRange)
# Now print a run summary and produce some plots.
print(fm)
plot(fm, what = "BIC")
plot(fm, what = "classification_pairs")
## End(Not run)
```

fabMix\_CxC

Function to estimate the CUC and CCC models

#### **Description**

This function runs parallel chains under a prior tempering scheme of the Dirichlet prior distribution of mixture weights.

#### Usage

```
fabMix_CxC(sameSigma, dirPriorAlphas, rawData, outDir, Kmax, mCycles,
burnCycles, g, h, alpha_sigma, beta_sigma, q, normalize,
thinning, zStart, nIterPerCycle, gibbs_z,
warm_up_overfitting, warm_up, overfittingInitialization,
progressGraphs, gwar, cccStart)
```

#### **Arguments**

sameSigma

Logical value denoting the parameterization of the error variance per component. If TRUE, the parameterization CCU is fitted. Otherwise, the parameterization CUU is fitted.

fabMix\_CxC

dirPriorAlphas The prior Dirichlet parameters for each chain.

rawData The observed data as an  $n \times p$  matrix. Clustering is performed on the rows of

the matrix.

outDir Name of the output folder.

Kmax Number of components in the overfitted mixture. Default: 20.

mCycles Number of MCMC cycles. Each cycle consists of nIterPerCycle MCMC it-

erations. At the end of each cycle a swap of the state of two randomly chosen

adjacent chains is attempted.

burnCycles Number of cycles that will be discarded as burn-in period.

g Prior parameter g. Default value: g=2. h Prior parameter h. Default value: h=1. alpha\_sigma Prior parameter  $\alpha$ . Default value:  $\alpha=2$ . beta\_sigma Prior parameter  $\beta$ . Default value:  $\beta=1$ .

Number of factors q, where  $1 \le q \le L$ . An error is thrown if the Ledermann

bound (L) is exceeded.

normalize Should the observed data be normalized? Default value: TRUE. thinning Optional integer denoting the thinning of the keeped MCMC cycles.

zStart Optional starting value for the allocation vector.

nIterPerCycle Number of iteration per MCMC cycle. Default value: 10.

gibbs\_z Select the gibbs sampling scheme for updating latent allocations of mixture

model. Default value: 1.

warm\_up\_overfitting

Number of iterations for the overfitting initialization scheme. Default value:

100.

warm\_up Number of iterations that will be used to initialize the models before starting

proposing switchings. Default value: 500.

over fitting Initialization

Logical value indicating whether the chains are initialized via the overfitting

initialization scheme. Default: TRUE.

progressGraphs Logical value indicating whether to plot successive states of the chains while the

sampler runs. Default: FALSE.

gwar Initialization parameter. Default: 0.05. cccStart Initialization from the CCC model.

## Value

List of files written to outDir

#### Note

It is recommended to always use: normalize = TRUE (default). Tuning of dirPriorAlphas may be necessary to achieve reasonable acceptance rates of chain swaps. Also note that the output is not identifiable due to label switching and the user has to subsequently call the dealWithLabelSwitching function.

20 fabMix\_CxU

#### Author(s)

Panagiotis Papastamoulis

#### See Also

fabMix

fabMix\_CxU

Function to estimate the CCU and CUU models

## **Description**

This function runs parallel chains under a prior tempering scheme of the Dirichlet prior distribution of mixture weights.

#### Usage

```
fabMix_CxU(sameSigma, dirPriorAlphas, rawData, outDir, Kmax, mCycles,
burnCycles, g, h, alpha_sigma, beta_sigma, q, normalize,
thinning, zStart, nIterPerCycle, gibbs_z,
warm_up_overfitting, warm_up, overfittingInitialization,
progressGraphs, gwar)
```

# Arguments

sameSigma		parameterization of		

nent. If TRUE, the parameterization CCU is fitted. Otherwise, the parameteriza-

tion CUU is fitted.

dirPriorAlphas The prior Dirichlet parameters for each chain.

rawData The observed data as an  $n \times p$  matrix. Clustering is performed on the rows of

the matrix.

outDir Name of the output folder.

Kmax Number of components in the overfitted mixture. Default: 20.

mCycles Number of MCMC cycles. Each cycle consists of nIterPerCycle MCMC it-

erations. At the end of each cycle a swap of the state of two randomly chosen

adjacent chains is attempted.

burnCycles Number of cycles that will be discarded as burn-in period.

g Prior parameter g. Default value: g=2. h Prior parameter h. Default value: h=1. alpha\_sigma Prior parameter  $\alpha$ . Default value:  $\alpha=2$ . beta\_sigma Prior parameter  $\beta$ . Default value:  $\beta=1$ .

Number of factors q, where  $1 \le q \le L$ . An error is thrown if the Ledermann

bound (L) is exceeded.

normalize Should the observed data be normalized? Default value: TRUE. thinning Optional integer denoting the thinning of the keeped MCMC cycles.

zStart Optional starting value for the allocation vector.

nIterPerCycle Number of iteration per MCMC cycle. Default value: 10.

gibbs\_z Select the gibbs sampling scheme for updating latent allocations of mixture

model. Default value: 1.

warm\_up\_overfitting

Number of iterations for the overfitting initialization scheme. Default value:

100.

warm\_up Number of iterations that will be used to initialize the models before starting

proposing switchings. Default value: 500.

overfittingInitialization

Logical value indicating whether the chains are initialized via the overfitting

initialization scheme. Default: TRUE.

progressGraphs Logical value indicating whether to plot successive states of the chains while the

sampler runs. Default: FALSE.

gwar Initialization parameter. Default: 0.05.

#### Value

List of files written to outDir

# Note

It is recommended to always use: normalize = TRUE (default). Tuning of dirPriorAlphas may be necessary to achieve reasonable acceptance rates of chain swaps. Also note that the output is not identifiable due to label switching and the user has to subsequently call the dealWithLabelSwitching function.

#### Author(s)

Panagiotis Papastamoulis

#### See Also

fabMix

fabMix\_missing\_values Function to estimate the UUU or UCU models in case of missing values

#### **Description**

This function runs parallel chains under a prior tempering scheme of the Dirichlet prior distribution of mixture weights. Missing values are simulated from their full conditional posterior distribution.

#### Usage

fabMix\_missing\_values(sameSigma, dirPriorAlphas, rawData, outDir, Kmax, mCycles, burnCycles, g, h, alpha\_sigma, beta\_sigma, q, normalize, thinning, zStart, nIterPerCycle, gibbs\_z, warm\_up, progressGraphs, gwar)

#### **Arguments**

sameSigma Logical value denoting the parameterization of the error variance per compo-

nent. If sameSigma = TRUE, the parameterization UCU is fitted, otherwise the

UUU model is fitted.

dirPriorAlphas The prior Dirichlet parameters for each chain.

rawData The observed data as an  $n \times p$  matrix. Clustering is performed on the rows of

the matrix.

outDir Name of the output folder.

Kmax Number of components in the overfitted mixture. Default: 20.

mCycles Number of MCMC cycles. Each cycle consists of nIterPerCycle MCMC it-

erations. At the end of each cycle a swap of the state of two randomly chosen

adjacent chains is attempted.

burnCycles Number of cycles that will be discarded as burn-in period.

g Prior parameter g. Default value: g=2. h Prior parameter h. Default value: h=1. alpha\_sigma Prior parameter  $\alpha$ . Default value:  $\alpha=2$ . beta\_sigma Prior parameter  $\beta$ . Default value:  $\beta=1$ .

q Number of factors q, where  $1 \le q \le L$ . An error is thrown if the Ledermann

bound (L) is exceeded.

normalize Should the observed data be normalized? Default value: TRUE. thinning Optional integer denoting the thinning of the keeped MCMC cycles.

zStart Optional starting value for the allocation vector.

nIterPerCycle Number of iteration per MCMC cycle. Default value: 10.

gibbs\_z Select the gibbs sampling scheme for updating latent allocations of mixture

model. Default value: 1.

warm\_up NUmber of iterations that will be used to initialize the models before starting

proposing switchings. Default value: 500.

progressGraphs Logical value indicating whether to plot successive states of the chains while the

sampler runs. Default: FALSE.

gwar Initialization parameter. Default: 0.05.

#### Value

List of files written to outDir

fabMix\_UxC 23

#### Note

It is recommended to always use: normalize = TRUE (default). Tuning of dirPriorAlphas may be necessary to achieve reasonable acceptance rates of chain swaps. Also note that the output is not identifiable due to label switching and the user has to subsequently call the dealWithLabelSwitching function.

#### Author(s)

Panagiotis Papastamoulis

fabMix\_UxC

Function to estimate the UUC and UCC models

#### **Description**

This function runs parallel chains under a prior tempering scheme of the Dirichlet prior distribution of mixture weights.

#### Usage

```
fabMix_UxC(sameSigma, dirPriorAlphas, rawData, outDir, Kmax, mCycles,
burnCycles, g, h, alpha_sigma, beta_sigma, q, normalize,
thinning, zStart, nIterPerCycle, gibbs_z,
warm_up_overfitting, warm_up, overfittingInitialization,
progressGraphs, gwar)
```

# Arguments

sameSigma	Logical value	denoting the	parameterization of	the error	variance per compo-
-----------	---------------	--------------	---------------------	-----------	---------------------

nent. If TRUE, the parameterization CCU is fitted. Otherwise, the parameteriza-

tion CUU is fitted.

dirPriorAlphas The prior Dirichlet parameters for each chain.

rawData The observed data as an  $n \times p$  matrix. Clustering is performed on the rows of

the matrix.

outDir Name of the output folder.

Kmax Number of components in the overfitted mixture. Default: 20.

mCycles Number of MCMC cycles. Each cycle consists of nIterPerCycle MCMC it-

erations. At the end of each cycle a swap of the state of two randomly chosen

adjacent chains is attempted.

burnCycles Number of cycles that will be discarded as burn-in period.

g Prior parameter g. Default value: g=2. h Prior parameter h. Default value: h=1. alpha\_sigma Prior parameter  $\alpha$ . Default value:  $\alpha=2$ . beta\_sigma Prior parameter  $\beta$ . Default value:  $\beta=1$ . 24  $fabMix\_UxC$ 

Number of factors q, where  $1 \leq q \leq L$ . An error is thrown if the Ledermann

bound (L) is exceeded.

normalize Should the observed data be normalized? Default value: TRUE.

thinning Optional integer denoting the thinning of the keeped MCMC cycles.

zStart Optional starting value for the allocation vector.

nIterPerCycle Number of iteration per MCMC cycle. Default value: 10.

gibbs\_z Select the gibbs sampling scheme for updating latent allocations of mixture

model. Default value: 1.

warm\_up\_overfitting

Number of iterations for the overfitting initialization scheme. Default value:

100.

warm\_up Number of iterations that will be used to initialize the models before starting

proposing switchings. Default value: 500.

overfittingInitialization

Logical value indicating whether the chains are initialized via the overfitting

initialization scheme. Default: TRUE.

progressGraphs Logical value indicating whether to plot successive states of the chains while the

sampler runs. Default: FALSE.

gwar Initialization parameter. Default: 0.05.

#### Value

List of files written to outDir

#### Note

It is recommended to always use: normalize = TRUE (default). Tuning of dirPriorAlphas may be necessary to achieve reasonable acceptance rates of chain swaps. Also note that the output is not identifiable due to label switching and the user has to subsequently call the dealWithLabelSwitching function.

## Author(s)

Panagiotis Papastamoulis

#### See Also

fabMix

fabMix\_UxU 25

fabMix_UxU	Function to estimate the UUU and UCU model

# Description

This function runs parallel chains under a prior tempering scheme of the Dirichlet prior distribution of mixture weights.

# Usage

```
fabMix_UxU(sameSigma, dirPriorAlphas, rawData, outDir, Kmax, mCycles,
burnCycles, g, h, alpha_sigma, beta_sigma, q, normalize,
thinning, zStart, nIterPerCycle, gibbs_z,
warm_up_overfitting, warm_up, overfittingInitialization,
progressGraphs, gwar)
```

# Arguments

sameSigma	Logical value denoting the parameterization of the error variance per component. If TRUE, the parameterization $\Sigma_1=\ldots=\Sigma_K$ is fitted.
dirPriorAlphas	The prior Dirichlet parameters for each chain.
rawData	The observed data as an $n \times p$ matrix. Clustering is performed on the rows of the matrix.
outDir	Name of the output folder.
Kmax	Number of components in the overfitted mixture. Default: 20.
mCycles	Number of MCMC cycles. Each cycle consists of nIterPerCycle MCMC iterations. At the end of each cycle a swap of the state of two randomly chosen adjacent chains is attempted.
burnCycles	Number of cycles that will be discarded as burn-in period.
g	Prior parameter $g$ . Default value: $g = 2$ .
h	Prior parameter $h$ . Default value: $h = 1$ .
alpha_sigma	Prior parameter $\alpha$ . Default value: $\alpha = 2$ .
beta_sigma	Prior parameter $\beta$ . Default value: $\beta = 1$ .
q	Number of factors $q$ , where $1 \leq q \leq L$ . An error is thrown if the Ledermann bound $(L)$ is exceeded.
normalize	Should the observed data be normalized? Default value: TRUE.
thinning	Optional integer denoting the thinning of the keeped MCMC cycles.
zStart	Optional starting value for the allocation vector.
nIterPerCycle	Number of iteration per MCMC cycle. Default value: 10.
gibbs_z	Select the gibbs sampling scheme for updating latent allocations of mixture

model. Default value: 1.

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warm\_up\_overfitting

Number of iterations for the overfitting initialization scheme. Default value:

100.

warm\_up Number of iterations that will be used to initialize the models before starting

proposing switchings. Default value: 500.

overfittingInitialization

Logical value indicating whether the chains are initialized via the overfitting

initialization scheme. Default: TRUE.

progressGraphs Logical value indicating whether to plot successive states of the chains while the

sampler runs. Default: FALSE.

gwar Initialization parameter. Default: 0.05.

#### Value

List of files written to outDir

#### Note

It is recommended to always use: normalize = TRUE (default). Tuning of dirPriorAlphas may be necessary to achieve reasonable acceptance rates of chain swaps. Also note that the output is not identifiable due to label switching and the user has to subsequently call the dealWithLabelSwitching function.

#### Author(s)

Panagiotis Papastamoulis

#### See Also

fabMix

getStuffForDIC

Compute information criteria

#### **Description**

This function computes four information criteria for a given run of the fabMix algorithm, namely: AIC, BIC, DIC and DIC<sub>2</sub>. Given various runs with different number of factors, the selected model corresponds to the one with the smalled value of the selected criterion.

#### Usage

getStuffForDIC(sameSigma, sameLambda, isotropic,  $x_{data}$ , outputFolder, q, burn, Km, normalize, discardLower)

getStuffForDIC 27

# **Arguments**

sameSigma	Logical value indicating whether the parameterization with the same variance of errors per component is used. Default: TRUE.
sameLambda	Logical value indicating whether the parameterization with same loadings per component is used. Default: FALSE.
isotropic	Logical value indicating whether the parameterization with isotropic error variance per component is used. Default: FALSE.
x_data	Observed data.
outputFolder	Name of the folder where the fabMix function has saved its output.
q	Number of factors. Note that this should coincide with the number of factors in the fabMix run.
burn	Discard observations as burn-in period (optional).
Km	Number of components in the overfitted mixture model. Note that this should coincide with the same entry in the fabMix run.
normalize	Should the observed data be normalized? Note that this should coincide with the same entry in the fabMix run. Default value: TRUE.
discardLower	Discard draws with log-likelihood values lower than the specific quantile. This applied only for the DIC computation.

# **Details**

If necessary, more details than the description above

#### Value

The information criteria are saved to the informationCriteria\_map\_model.txt file in the code-outputFolder.

# Note

It is well known that DIC tends to overfit, so it advised to compare models with different number of factors using AIC or BIC.

## Author(s)

Panagiotis Papastamoulis

28 myDirichlet

log\_dirichlet\_pdf

Log-density function of the Dirichlet distribution

# Description

Log-density function of the Dirichlet distribution

# Usage

```
log_dirichlet_pdf(alpha, weights)
```

# Arguments

alpha Parameter vector weights Vector of weights

#### Value

```
Log-density of the D(alpha_1, \ldots, \alpha_k) evaluated at w_1, \ldots, w_k.
```

## Author(s)

Panagiotis Papastamoulis

myDirichlet

Simulate from the Dirichlet distribution

# Description

Generate a random draw from the Dirichlet distribution  $D(\alpha_1, \ldots, \alpha_k)$ .

# Usage

```
myDirichlet(alpha)
```

## **Arguments**

alpha

Parameter vector

# Value

Simulated vector

## Author(s)

Panagiotis Papastamoulis

observed.log.likelihood0

Log-likelihood of the mixture model

## **Description**

Log-likelihood of the mixture model evaluated only at the alive components.

## Usage

```
observed.log.likelihood0(x_data, w, mu, Lambda, Sigma, z)
```

## **Arguments**

x\_data The observed data

w Vector of mixture weightsmu Vector of marginal means

Lambda Factor loadings

Sigma Common covariance matrix of the errors per cluster

z Allocation vector

## Value

Log-likelihood value

#### Author(s)

Panagiotis Papastamoulis

```
observed.log.likelihood0_q0_sameSigma
```

Log-likelihood of the mixture model for q=0 and same variance of errors

## **Description**

Log-likelihood of the mixture model evaluated only at the alive components.

```
observed.log.likelihood0_q0_sameSigma(x_data, w, mu, Sigma, z)
```

#### **Arguments**

x\_data The observed data

w Vector of mixture weightsmu Vector of marginal means

Sigma Covariance matrix of the errors per cluster

z Allocation vector

#### Value

Log-likelihood value

## Author(s)

Panagiotis Papastamoulis

observed.log.likelihood0\_Sj

Log-likelihood of the mixture model

# Description

Log-likelihood of the mixture model evaluated only at the alive components.

# Usage

```
observed.log.likelihood0_Sj(x_data, w, mu, Lambda, Sigma, z)
```

## **Arguments**

x\_data The observed data

w Vector of mixture weightsmu Vector of marginal means

Lambda Factor loadings

Sigma Covariance matrix of the errors per cluster

z Allocation vector

#### Value

Log-likelihood value

#### Author(s)

Panagiotis Papastamoulis

```
observed.log.likelihood0_Sj_q0 \label{eq:likelihood} \textit{Log-likelihood of the mixture model for } q=0
```

# Description

Log-likelihood of the mixture model evaluated only at the alive components.

# Usage

```
observed.log.likelihood0_Sj_q0(x_data, w, mu, Sigma, z)
```

# Arguments

x_data	The observed data
W	Vector of mixture weights
mu	Vector of marginal means
Sigma	Covariance matrix of the errors per cluster
Z	Allocation vector

#### Value

Log-likelihood value

# Author(s)

Panagiotis Papastamoulis

overfittingMFA	Basic MCMC sampler	
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# Description

Gibbs sampling for fitting a mixture model of factor analyzers.

```
overfittingMFA(x_data, originalX, outputDirectory, Kmax, m, thinning, burn,
g, h, alpha_prior, alpha_sigma, beta_sigma,
start_values, q, zStart, gibbs_z)
```

#### **Arguments**

x\_data normalized data

originalX observed raw data (only for plotting purpose)

outputDirectory

Name of the output folder

Kmax Number of mixture components

m Number of iterationsthinning Thinning of chainburnBurn-in period

g Prior parameter g. Default value: g=2. h Prior parameter h. Default value: h=1.

alpha\_prior Parameters of the Dirichlet prior distribution of mixture weights.

alpha\_sigma Prior parameter  $\alpha$ . Default value:  $\alpha=2$ . beta\_sigma Prior parameter  $\beta$ . Default value:  $\beta=1$ .

q Optional (not used)
q Number of factors.
zStart Optional (not used)

gibbs\_z Optional

#### Value

List of files

## Author(s)

Panagiotis Papastamoulis

overfittingMFA\_CCC Basi

Basic MCMC sampler for CCC

#### **Description**

Gibbs sampling for fitting a CCC mixture model of factor analyzers.

```
overfittingMFA_CCC(x_data, originalX, outputDirectory, Kmax, m, thinning, burn, g, h, alpha_prior, alpha_sigma, beta_sigma, start_values, q, zStart, gibbs_z)
```

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#### **Arguments**

x\_data normalized data

originalX observed raw data (only for plotting purpose)

outputDirectory

Name of the output folder

Kmax Number of mixture components

m Number of iterationsthinning Thinning of chainburnBurn-in period

g Prior parameter g. Default value: g=2. h Prior parameter h. Default value: h=1.

alpha\_prior Parameters of the Dirichlet prior distribution of mixture weights.

alpha\_sigma Prior parameter  $\alpha$ . Default value:  $\alpha=2$ . beta\_sigma Prior parameter  $\beta$ . Default value:  $\beta=1$ .

q Optional (not used)
q Number of factors.
zStart Optional (not used)

gibbs\_z Optional

#### Value

List of files

# Author(s)

Panagiotis Papastamoulis

overfittingMFA\_CCU

Basic MCMC sampler for CCU

#### **Description**

Gibbs sampling for fitting a CCU mixture model of factor analyzers.

```
overfittingMFA_CCU(x_data, originalX, outputDirectory, Kmax, m, thinning, burn, g, h, alpha_prior, alpha_sigma, beta_sigma, start_values, q, zStart, gibbs_z)
```

#### **Arguments**

x\_data normalized data

originalX observed raw data (only for plotting purpose)

outputDirectory

Name of the output folder

Kmax Number of mixture components

m Number of iterationsthinning Thinning of chainburnBurn-in period

g Prior parameter g. Default value: g=2. h Prior parameter h. Default value: h=1.

alpha\_prior Parameters of the Dirichlet prior distribution of mixture weights.

alpha\_sigma Prior parameter  $\alpha$ . Default value:  $\alpha=2$ . beta\_sigma Prior parameter  $\beta$ . Default value:  $\beta=1$ .

q Optional (not used)
q Number of factors.
zStart Optional (not used)

gibbs\_z Optional

## Value

List of files

## Author(s)

Panagiotis Papastamoulis

overfittingMFA\_CUC Basic

Basic MCMC sampler for CUC

#### **Description**

Gibbs sampling for fitting a CUC mixture model of factor analyzers.

```
overfittingMFA_CUC(x_data, originalX, outputDirectory, Kmax, m, thinning, burn, g, h, alpha_prior, alpha_sigma, beta_sigma, start_values, q, zStart, gibbs_z)
```

overfittingMFA\_CUU 35

#### **Arguments**

x\_data normalized data

originalX observed raw data (only for plotting purpose)

outputDirectory

Name of the output folder

Kmax Number of mixture components

m Number of iterationsthinning Thinning of chainburnBurn-in period

g Prior parameter g. Default value: g=2. h Prior parameter h. Default value: h=1.

alpha\_prior Parameters of the Dirichlet prior distribution of mixture weights.

alpha\_sigma Prior parameter  $\alpha$ . Default value:  $\alpha=2$ . beta\_sigma Prior parameter  $\beta$ . Default value:  $\beta=1$ .

q Optional (not used)
q Number of factors.
zStart Optional (not used)

gibbs\_z Optional

#### Value

List of files

# Author(s)

Panagiotis Papastamoulis

overfittingMFA\_CUU

Basic MCMC sampler for CUU

#### **Description**

Gibbs sampling for fitting a CUU mixture model of factor analyzers.

```
overfittingMFA_CUU(x_data, originalX, outputDirectory, Kmax, m, thinning, burn, g, h, alpha_prior, alpha_sigma, beta_sigma, start_values, q, zStart, gibbs_z)
```

#### **Arguments**

x\_data normalized data

originalX observed raw data (only for plotting purpose)

outputDirectory

Name of the output folder

Kmax Number of mixture components

m Number of iterationsthinning Thinning of chainburn Burn-in period

g Prior parameter g. Default value: g=2. h Prior parameter h. Default value: h=1.

alpha\_prior Parameters of the Dirichlet prior distribution of mixture weights.

alpha\_sigma Prior parameter  $\alpha$ . Default value:  $\alpha=2$ . beta\_sigma Prior parameter  $\beta$ . Default value:  $\beta=1$ .

start\_values Optional (not used)
q Number of factors.
zStart Optional (not used)

gibbs\_z Optional

# Value

List of files

#### Author(s)

Panagiotis Papastamoulis

overfittingMFA\_missing\_values

Basic MCMC sampler for the case of missing data

## Description

Gibbs sampling for fitting a mixture model of factor analyzers.

```
overfittingMFA_missing_values(missing_entries, x_data, originalX, outputDirectory, Kmax, m, thinning, burn, g, h, alpha_prior, alpha_sigma, beta_sigma, start_values, q, zStart, gibbs_z)
```

overfittingMFA\_Sj 37

#### **Arguments**

missing\_entries

list which contains the row number (1st entry) and column indexes (subsequent

entries) for every row containing missing values.

x\_data normalized data

originalX observed raw data (only for plotting purpose)

outputDirectory

Name of the output folder

Kmax Number of mixture components

m Number of iterationsthinning Thinning of chainburnBurn-in period

g Prior parameter g. Default value: g=2. h Prior parameter h. Default value: h=1.

alpha\_prior Parameters of the Dirichlet prior distribution of mixture weights.

alpha\_sigma Prior parameter  $\alpha$ . Default value:  $\alpha=2$ . beta\_sigma Prior parameter  $\beta$ . Default value:  $\beta=1$ .

start\_values Optional (not used)
q Number of factors.
zStart Optional (not used)

gibbs\_z Optional

#### Value

List of files

#### Author(s)

Panagiotis Papastamoulis

overfittingMFA\_Sj

Basic MCMC sampler using different error variance per component

#### **Description**

Gibbs sampling for fitting a mixture model of factor analyzers.

```
overfittingMFA_Sj(x_data, originalX, outputDirectory, Kmax, m, thinning, burn, g, h, alpha_prior, alpha_sigma, beta_sigma, start_values, q, zStart, gibbs_z)
```

x\_data normalized data

originalX observed raw data (only for plotting purpose)

outputDirectory

Name of the output folder

Kmax Number of mixture components

m Number of iterationsthinning Thinning of chainburnBurn-in period

g Prior parameter g. Default value: g=2. h Prior parameter h. Default value: h=1.

alpha\_prior Parameters of the Dirichlet prior distribution of mixture weights.

alpha\_sigma Prior parameter  $\alpha$ . Default value:  $\alpha=2$ . beta\_sigma Prior parameter  $\beta$ . Default value:  $\beta=1$ .

start\_valuesOptional (not used)qNumber of factors.zStartOptional (not used)

gibbs\_z Optional

#### Value

List of files

#### Author(s)

Panagiotis Papastamoulis

overfittingMFA\_Sj\_missing\_values

Basic MCMC sampler for the case of missing data and different error variance

# Description

Gibbs sampling for fitting a mixture model of factor analyzers.

```
overfittingMFA_Sj_missing_values(missing_entries, x_data, originalX,
outputDirectory, Kmax,
m, thinning, burn, g, h, alpha_prior, alpha_sigma,
beta_sigma, start_values, q, zStart, gibbs_z)
```

overfittingMFA\_UCC 39

#### Arguments

missing\_entries

list which contains the row number (1st entry) and column indexes (subsequent

entries) for every row containing missing values.

x\_data normalized data

originalX observed raw data (only for plotting purpose)

outputDirectory

Name of the output folder

Kmax Number of mixture components

m Number of iterationsthinning Thinning of chainburnBurn-in period

g Prior parameter g. Default value: g=2. h Prior parameter h. Default value: h=1.

alpha\_prior Parameters of the Dirichlet prior distribution of mixture weights.

alpha\_sigma Prior parameter  $\alpha$ . Default value:  $\alpha=2$ . beta\_sigma Prior parameter  $\beta$ . Default value:  $\beta=1$ .

start\_values Optional (not used)
q Number of factors.
zStart Optional (not used)

gibbs\_z Optional

#### Value

List of files

#### Author(s)

Panagiotis Papastamoulis

overfittingMFA\_UCC

Basic MCMC sampler for CCC

#### **Description**

Gibbs sampling for fitting a UCC mixture model of factor analyzers.

```
overfittingMFA_UCC(x_data, originalX, outputDirectory, Kmax, m, thinning, burn, g, h, alpha_prior, alpha_sigma, beta_sigma, start_values, q, zStart, gibbs_z)
```

x\_data normalized data

originalX observed raw data (only for plotting purpose)

outputDirectory

Name of the output folder

Kmax Number of mixture components

m Number of iterationsthinning Thinning of chainburnBurn-in period

g Prior parameter g. Default value: g=2. h Prior parameter h. Default value: h=1.

alpha\_prior Parameters of the Dirichlet prior distribution of mixture weights.

alpha\_sigma Prior parameter  $\alpha$ . Default value:  $\alpha=2$ . beta\_sigma Prior parameter  $\beta$ . Default value:  $\beta=1$ .

q Optional (not used)
q Number of factors.
zStart Optional (not used)

gibbs\_z Optional

#### Value

List of files

#### Author(s)

Panagiotis Papastamoulis

overfittingMFA\_UUC

Basic MCMC sampler for UUC

#### **Description**

Gibbs sampling for fitting a UUC mixture model of factor analyzers.

```
overfittingMFA_UUC(x_data, originalX, outputDirectory, Kmax, m, thinning, burn, g, h, alpha_prior, alpha_sigma, beta_sigma, start_values, q, zStart, gibbs_z)
```

overfitting\_q0 41

#### **Arguments**

x\_data normalized data

originalX observed raw data (only for plotting purpose)

outputDirectory

Name of the output folder

Kmax Number of mixture components

m Number of iterationsthinning Thinning of chainburnBurn-in period

g Prior parameter g. Default value: g=2. h Prior parameter h. Default value: h=1.

alpha\_prior Parameters of the Dirichlet prior distribution of mixture weights.

alpha\_sigma Prior parameter  $\alpha$ . Default value:  $\alpha=2$ . beta\_sigma Prior parameter  $\beta$ . Default value:  $\beta=1$ .

start\_values Optional (not used)
q Number of factors.
zStart Optional (not used)

gibbs\_z Optional

#### Value

List of files

#### Author(s)

Panagiotis Papastamoulis

 $\label{eq:mcmc} \textit{overfitting\_q0} \qquad \qquad \textit{MCMC sampler for } q = 0$ 

# Description

Gibbs sampling for fitting a mixture model with diagonal covariance structure.

```
overfitting_q0(x_data, originalX, outputDirectory, Kmax, m, thinning, burn, g, h, alpha_prior, alpha_sigma, beta_sigma, start_values, q, zStart, gibbs_z)
```

x\_data normalized data

originalX observed raw data (only for plotting purpose)

outputDirectory

Name of the output folder

Kmax Number of mixture components

m Number of iterationsthinning Thinning of chainburnBurn-in period

g Prior parameter g. Default value: g=2. h Prior parameter h. Default value: h=1.

alpha\_prior Parameters of the Dirichlet prior distribution of mixture weights.

alpha\_sigma Prior parameter  $\alpha$ . Default value:  $\alpha=2$ . beta\_sigma Prior parameter  $\beta$ . Default value:  $\beta=1$ .

q Optional (not used)
q Number of factors.
zStart Optional (not used)

gibbs\_z Optional

#### Value

List of files

#### Author(s)

Panagiotis Papastamoulis

overfitting\_q0\_sameSigma

MCMC sampler for q = 0 and same error variance parameterization

#### Description

Gibbs sampling for fitting a mixture model with diagonal covariance structure.

```
overfitting_q0_sameSigma(x_data, originalX, outputDirectory, Kmax, m, thinning, burn, g, h, alpha_prior, alpha_sigma, beta_sigma, start_values, q, zStart, gibbs_z)
```

plot.fabMix.object 43

#### **Arguments**

x\_data normalized data

originalX observed raw data (only for plotting purpose)

outputDirectory

Name of the output folder

Kmax Number of mixture components

m Number of iterationsthinning Thinning of chainburn Burn-in period

g Prior parameter g. Default value: g=2. h Prior parameter h. Default value: h=1.

alpha\_prior Parameters of the Dirichlet prior distribution of mixture weights.

alpha\_sigma Prior parameter  $\alpha$ . Default value:  $\alpha=2$ . beta\_sigma Prior parameter  $\beta$ . Default value:  $\beta=1$ .

start\_values Optional (not used)
q Number of factors.
zStart Optional (not used)

gibbs\_z Optional

#### Value

List of files

#### Author(s)

Panagiotis Papastamoulis

# Description

This function plots fabMix function.

```
## S3 method for class 'fabMix.object'
plot(x, what, variableSubset, ...)
```

44 print.fabMix.object

#### **Arguments**

x An object of class fabMix.object, which is returned by the fabMix function.

what One of the "BIC", "classification\_matplot", "classification\_pairs", "correlation",

"regularized\_expression". The plot will display the BIC values per model and number of factors (along with the most probable number of clusters as text), a matplot per cluster for the selected model, scatterplots pairs, the estimated correlation matrix per cluster, and the estimated regularized expression of each

variable to the factor space for the selected model, respectively.

variableSubset An optional subset of the variables. By default, all variables are selected.

... ignored.

#### **Details**

When the BIC values are plotted, a number indicates the most probable number of "alive" clusters. The pairwise scatterplots (what = "classification\_pairs") are created using the coordProj function of the mclust package. The what = "correlation" is plotted using the corrplot package. Note that the what = "classification\_matplot" plots the original data (before scaling and centering). On the other hand, the option what = "classification\_pairs" plots the centered and scaled data.

#### Author(s)

Panagiotis Papastamoulis

#### References

Luca Scrucca and Michael Fop and Thomas Brendan Murphy and Adrian E. Raftery (2017). mclust 5: clustering, classification and density estimation using Gaussian finite mixture models. The R Journal, 8(1): 205–233.

Taiyun Wei and Viliam Simko (2017). R package "corrplot": Visualization of a Correlation Matrix (Version 0.84). Available from https://github.com/taiyun/corrplot

# Description

This function prints a summary of objects returned by the fabMix function.

```
## S3 method for class 'fabMix.object'
print(x, printSubset, ...)
```

readLambdaValues 45

# Arguments

x An object of class fabMix.object, which is returned by the fabMix function.

printSubset Logical indicating whether to print the header or the whole matrix of estimates.

Default value: TRUE.

... ignored.

#### **Details**

The function prints the estimated distribution of the number of clusters, the estimated number of observations assigned to each cluster after post-processing the output with three label switching algorithms, as well as the header of the posterior mean estimates of  $\theta_{kj}$  (probability of success for cluster k and feature j) (conditionally on the most probable number of clusters).

#### Author(s)

Panagiotis Papastamoulis

readLambdaValues

Read Lambda values.

# Description

Function to read Lambda values from file.

#### Usage

```
readLambdaValues(myFile,K,p,q)
```

#### **Arguments**

myFile File containing Lambda values

K Number of components

p Number of variables

q Number of factors

#### Value

 $K \times p \times q$  array of factor loadings.

#### Author(s)

46 simData

simData	Synthetic data generator	

#### **Description**

Simulate data from a multivariate normal mixture using a mixture of factor analyzers mechanism.

#### Usage

```
simData(sameSigma, sameLambda, p, q, K.true, n, loading_means, loading_sd, sINV_values)
```

#### **Arguments**

Logical. sameSigma Logical. sameLambda The dimension of the multivariate normal distribution (p > 1). Number of factors. It should be strictly smaller than p. q K.true The number of mixture components (clusters). Sample size. loading\_means A vector which contains the means of blocks of factor loadings. Default: loading\_means = c(-30, -20, -10, 10, 20, 30). loading\_sd A vector which contains the standard deviations of blocks of factor loadings. Default: loading\_sd <- rep(2, length(loading\_means)).</pre> sINV\_values A vector which contains the values of the diagonal of the (common) inverse covariance matrix, if sigmaTrue = TRUE. An  $K \times p$  matrix which contains the values of the diagonal of the inverse covariance matrix per component, if sigmaTrue = FALSE. Default: sINV\_values = rgamma(p, shape = 1, rate = 1).

#### Value

A list with the following entries:

data	$n \times p$ array containing the simulated data.
class	n-dimensional vector containing the class of each observation.
factorLoadings	$K.true \times p \times q$ -array containing the factor loadings $\Lambda_{krj}$ per cluster $k$ , feature $r$ and factor $j$ , where $k=1,\ldots,K; r=1,\ldots,p; j=1,\ldots,q$ .
means	$K.true \times p$ matrix containing the marginal means $\mu_{kr}, \ k=1,\ldots,K; \ r=1,\ldots,p.$
variance	$p \times p$ diagonal matrix containing the variance of errors $\sigma_{rr}$ , $r=1,\ldots,p$ . Note that the same variance of errors is assumed for each cluster.
factors	$n \times q$ matrix containing the simulated factor values.
weights	K.true-dimensional vector containing the weight of each cluster.

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# Note

The marginal variance for cluster k is equal to  $\Lambda_k\Lambda_k^T+\Sigma.$ 

# Author(s)

Panagiotis Papastamoulis

update\_all\_y

Gibbs sampling for y

# Description

Gibbs sampling for y

# Usage

```
update_all_y(x_data, mu, SigmaINV, Lambda, z)
```

# Arguments

x\_data Data

mu Marginal means
SigmaINV Precision matrix
Lambda Factor loadings
z Allocation vector

# Value

A matrix with generated factors

# Author(s)

48 update\_OmegaINV

update\_all\_y\_Sj

Gibbs sampling for y

# Description

Gibbs sampling for y

# Usage

```
update_all_y_Sj(x_data, mu, SigmaINV, Lambda, z)
```

# Arguments

x\_data Data

mu Marginal means

SigmaINV Precision matrix per component

Lambda Factor loadings z Allocation vector

#### Value

A matrix with generated factors

# Author(s)

Panagiotis Papastamoulis

update\_OmegaINV

Gibbs sampling for  $\Omega^-1$ 

# Description

Gibbs sampling for  $\Omega^{-1}$ 

# Usage

```
update_OmegaINV(Lambda, K, g, h)
```

# Arguments

Lambda	Factor loadings

K Number of components

g Prior parameterh Prior parameter

# Value

 $\Omega^{-1}$ 

# Author(s)

Panagiotis Papastamoulis

update\_OmegaINV\_Cxx

Gibbs sampling for  $\Omega^-1$  for Cxx model

# Description

Gibbs sampling for  $\Omega^{-1}$  for Cxx model

# Usage

```
update_OmegaINV_Cxx(Lambda, K, g, h)
```

# Arguments

Lambda	Factor loadings	
K	Number of components	
g	Prior parameter	
h	Prior parameter	

# Value

 $\Omega^{-1}$ 

# Author(s)

```
update_SigmaINV_faster
```

Gibbs sampling for  $\Sigma^{\hat{}}-1$ 

# Description

Gibbs sampling for  $\Sigma^{-1}$ 

# Usage

```
update_SigmaINV_faster(x_data, z, y, Lambda, mu, K, alpha_sigma, beta_sigma)
```

# Arguments

x_data	Data
--------	------

z Allocation vector

y Factors

Lambda Factor loadings mu Marginal means

K Number of components

alpha\_sigma Prior parameter beta\_sigma Prior parameter

#### Value

 $\Sigma^{-1}$ 

# Author(s)

Panagiotis Papastamoulis

```
update_SigmaINV_faster_q0
```

Gibbs sampling for  $\Sigma^-1$  per component for q=0

# Description

Gibbs sampling for  $\Sigma^{-1}$  per component

```
update_SigmaINV_faster_q0( z, mu, K, alpha_sigma, beta_sigma, x_data)
```

z Allocation vectormu Marginal means

K Number of components

alpha\_sigma Prior parameter beta\_sigma Prior parameter

x\_data Data

#### Value

 $\Sigma^{-1}$ 

#### Author(s)

Panagiotis Papastamoulis

```
update_SigmaINV_faster_q0_sameSigma  
 {\it Gibbs\ sampling\ for\ } \Sigma^{\hat{}}-1\ per\ component\ for\ q=0
```

# Description

Gibbs sampling for  $\Sigma^{-1}$  per component

# Usage

```
update_SigmaINV_faster_q0_sameSigma( z, mu, K, alpha_sigma, beta_sigma, x_data)
```

#### **Arguments**

z Allocation vector mu Marginal means

K Number of components

alpha\_sigma Prior parameter beta\_sigma Prior parameter

x\_data Data

#### Value

 $\Sigma^{-1}$ 

#### Author(s)

```
update_SigmaINV_faster_Sj {\it Gibbs\ sampling\ for\ } \Sigma^{\hat{}} - 1\ per\ component
```

# Description

Gibbs sampling for  $\Sigma^{-1}$  per component

# Usage

```
update_SigmaINV_faster_Sj(x_data, z, y, Lambda, mu, K, alpha_sigma, beta_sigma)
```

# Arguments

x\_data Data

z Allocation vector

y Factors

Lambda Factor loadings mu Marginal means

K Number of components

alpha\_sigma Prior parameter beta\_sigma Prior parameter

#### Value

 $\Sigma^{-1}$ 

# Author(s)

Panagiotis Papastamoulis

update\_SigmaINV\_xCC Gibbs sampling for  $\Sigma^-1$  for xCC models

# Description

Gibbs sampling for  $\Sigma^{-1}$  for xCC models

```
update_SigmaINV_xCC(x_data, z, y, Lambda, mu, K, alpha_sigma, beta_sigma)
```

x\_data Data

z Allocation vector

y Factors

Lambda Factor loadings mu Marginal means

K Number of components

alpha\_sigma Prior parameter beta\_sigma Prior parameter

#### Value

 $\Sigma^{-1}$ 

#### Author(s)

Panagiotis Papastamoulis

update\_SigmaINV\_xUC

Gibbs sampling for  $\Sigma^-1$  per component for xUC models

# Description

Gibbs sampling for  $\Sigma^{-1}$  per component for xUC models

#### Usage

```
update_SigmaINV_xUC(x_data, z, y, Lambda, mu, K, alpha_sigma, beta_sigma)
```

# Arguments

x\_data Data

z Allocation vector

y Factors

Lambda Factor loadings mu Marginal means

K Number of components

alpha\_sigma Prior parameter beta\_sigma Prior parameter

#### Value

 $\Sigma^{-1}$ 

54 update\_z2\_Sj

#### Author(s)

Panagiotis Papastamoulis

update\_z2

Collapsed Gibbs for z using matrix inversion lemma

# Description

Collapsed Gibbs for z using matrix inversion lemma

# Usage

```
update_z2(w, mu, Lambda, SigmaINV, K, x_data)
```

#### **Arguments**

w Mixture weightsmu Marginal meansLambda Factor loadingsSigmaINV Precision matrix

K Number of components

x\_data Data

#### Value

Allocation vector

#### Author(s)

Panagiotis Papastamoulis

update\_z2\_Sj

Collapsed Gibbs for z using matrix inversion lemma

# Description

Collapsed Gibbs for z using matrix inversion lemma

```
update_z2_Sj(w, mu, Lambda, SigmaINV, K, x_data)
```

update\_z4 55

#### **Arguments**

w Mixture weightsmu Marginal meansLambda Factor loadings

SigmaINV Precision matrix per component

K Number of components

x\_data Data

#### Value

Allocation vector

# Author(s)

Panagiotis Papastamoulis

update\_z4  $Collapsed\ Gibbs\ for\ z$ 

# Description

Collapsed Gibbs for  $\boldsymbol{z}$ 

# Usage

```
update_z4(w, mu, Lambda, SigmaINV, K, x_data)
```

# Arguments

w Mixture weightsmu Marginal meansLambda Factor loadingsSigmaINV Precision matrix

K Number of components

x\_data Data

#### Value

Allocation vector

#### Author(s)

56 update\_z\_b

update\_z4\_Sj

Collapsed Gibbs for z

# Description

Collapsed Gibbs for z

# Usage

```
update_z4_Sj(w, mu, Lambda, SigmaINV, K, x_data)
```

# Arguments

w Mixture weightsmu Marginal meansLambda Factor loadings

SigmaINV Precision matrix per component

K Number of components

x\_data Data

# Value

Allocation vector

# Author(s)

Panagiotis Papastamoulis

update\_z\_b

Gibbs sampling for z

# Description

Gibbs sampling for z

```
update_z_b(w, mu, Lambda, y, SigmaINV, K, x_data)
```

 $update\_z\_b\_Sj$  57

#### **Arguments**

w Mixture weightsmu Marginal meansLambda Factor loadingsy Matrix of factorsSigmaINV Precision matrix

K Number of components

x\_data Data

#### Value

Allocation vector

# Author(s)

Panagiotis Papastamoulis

update\_z\_b\_Sj

Gibbs sampling for z

# Description

Gibbs sampling for z

# Usage

```
update_z_b_Sj(w, mu, Lambda, y, SigmaINV, K, x_data)
```

#### **Arguments**

w Mixture weightsmu Marginal meansLambda Factor loadingsy Matrix of factors

SigmaINV Precision matrix per component

K Number of components

x\_data Data

#### Value

Allocation vector

# Author(s)

update\_z\_q0

Gibbs sampling for z for q = 0

#### **Description**

Gibbs sampling for z

#### Usage

```
update_z_q0(w, mu, SigmaINV, K, x_data)
```

# Arguments

w Mixture weightsmu Marginal means

SigmaINV Precision matrix per component

K Number of components

x\_data Data

# Value

Allocation vector

#### Author(s)

Panagiotis Papastamoulis

```
update_z_q0_sameSigma Gibbs sampling for z for q = 0
```

# Description

Gibbs sampling for z

# Usage

```
update\_z\_q0\_sameSigma(w, mu, SigmaINV, K, x\_data)
```

# Arguments

w Mixture weights mu Marginal means

SigmaINV Precision matrix per component

K Number of components

x\_data Data

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#### Value

Allocation vector

#### Author(s)

Panagiotis Papastamoulis

waveDataset1500

Wave dataset

#### **Description**

A subset of 1500 randomly sampled observations from the wave dataset (version 1), available from the UCI machine learning repository. It contains 3 classes of waves (variable class with values "1", "2" and "3") and 21 attributes. Each class is generated from a combination of 2 of 3 base waves with noise.

#### Usage

waveDataset1500

#### **Format**

A data frame with 1500 rows and 22 columns. The first column denotes the class of each observa-

#### **Source**

https://archive.ics.uci.edu/ml/datasets/Waveform+Database+Generator+(Version+1)

# References

Lichman, M. (2013). UCI Machine Learning Repository http://archive.ics.uci.edu/ml. Irvine, CA: University of California, School of Information and Computer Science.

Breiman, L., Friedman, J.H., Olshen, R.A. and Stone, C.J. (1984). Classification and Regression Trees. Wadsworth International Group: Belmont, California.

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