

INITIALIZATION

$d = (e - c_b) / \|e - c_b\| \rightarrow$

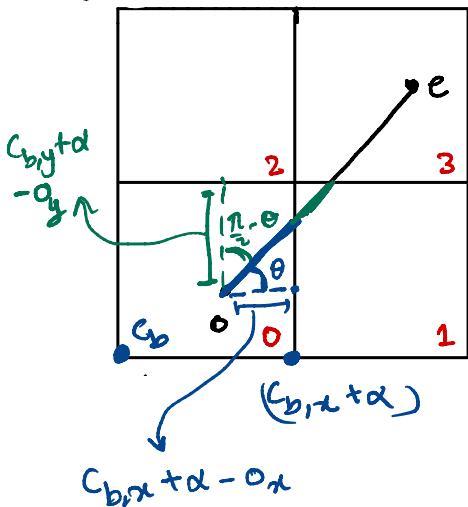
- $\frac{dx}{dy}$ any point on ray along x: $c_x + t dx$
- any point on ray along y: $c_y + t dy$

if $dx \geq 0$:

- if $dy \geq 0$: step_col = 1, step_row = 1
- else if $dy = 0$: step_col = 0, step_row = 0
- else: step_col = -1, step_row = -1

when to stop along row?

when along col?



$c_b + t dx$
 $-c_b + t dy$

lower left hand corner

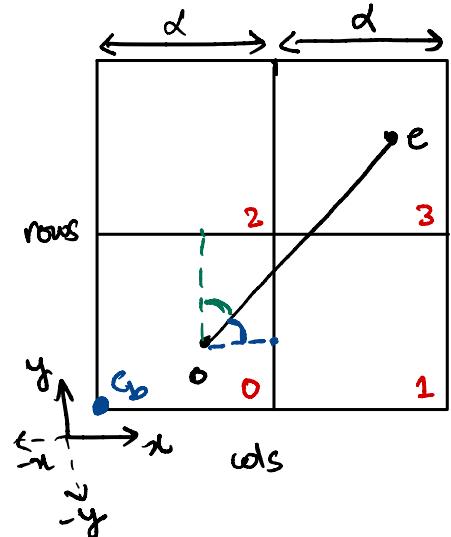
$c_{b,x}$
 $c_{b,y}$

$$\tan \theta = \frac{dy}{dx} = \frac{\sin \theta}{\cos \theta}$$

$$\cos \theta = \frac{c_{b,x} + \alpha - 0_x}{t \max X}$$

$$\frac{(c_{b,x} + \alpha - 0_x)}{dx} t \max X$$

$$\frac{(c_{b,y} + \alpha - 0_y)}{dy} t \max Y$$



UPDATE Loop

if $tMaxX < tMaxY$:

- ① step along col
- ② update $tMaxX$

else:

- ① step along row
- ② update $tMaxY$

$$\frac{(c_{bx,x} + \alpha - 0_x)}{dx}$$

$tMaxX$

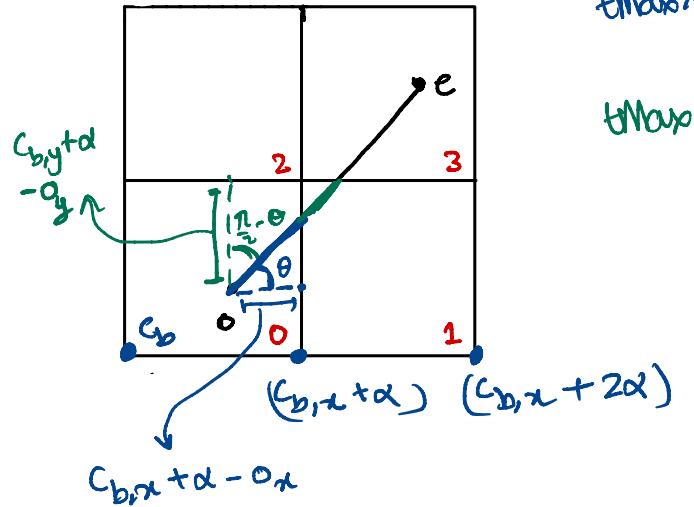
$$\frac{(c_{by,y} + \alpha - 0_y)}{dy}$$

$tMaxY$

• step-col
step-row

$$tMaxX = tMaxX + \frac{\alpha (step_col)}{dx}.$$

$$tMaxY = tMaxY + \frac{\alpha (step_row)}{dy}.$$



UPDATE Loop

if $tMaxX < tMaxY$:

① step along col

② update $tMaxX$

else:

① step along row

② update $tMaxY$

Numerical example

$$\alpha = 0.5 \quad \text{on } \partial\Omega$$

$$O = [0.27, 0.13]^T$$

$$e = [0.8, 0.75]^T$$

$$e - O = [0.8 - 0.27, 0.75 - 0.13]_{0.5}$$

$$= [0.53, 0.62]$$

$$dx = 0.65 \quad dy = 0.76$$

$$C_b = [0.0, 0.0]$$

$$C_{b,x}$$

$$C_{b,y}$$

$$tMaxX = tMaxX + \frac{\alpha (\text{step-col})}{dx}.$$

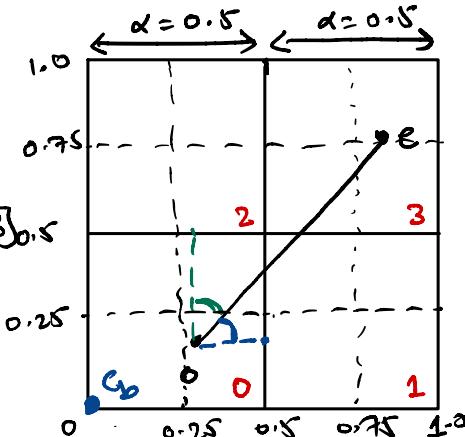
$$tMaxY = tMaxY + \frac{\alpha (\text{step-row})}{dy}.$$

step-col

step-row

$$\frac{(C_{b,x} + \alpha - O_x)}{dx} \\ tMaxX$$

$$\frac{(C_{b,y} + \alpha - O_y)}{dy} \\ tMaxY$$



cell 0

$$tMaxX = 0.35 \quad \left. \begin{array}{l} \text{go to cell 1} \\ \text{...} \end{array} \right\}$$

$$tMaxY = 0.49$$

cell 1

$$\text{updated } tMaxX = 1.12 \quad \left. \begin{array}{l} \text{go to cell 3} \\ \text{...} \end{array} \right\}$$

$$tMaxY = 0.49$$

Detect you are in "end" cell \rightarrow exit.

return $[0, 1, 3]$