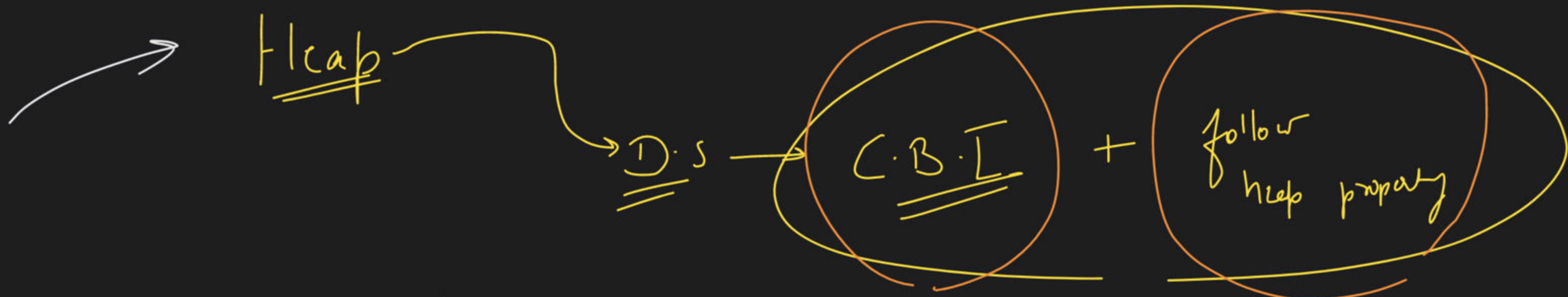


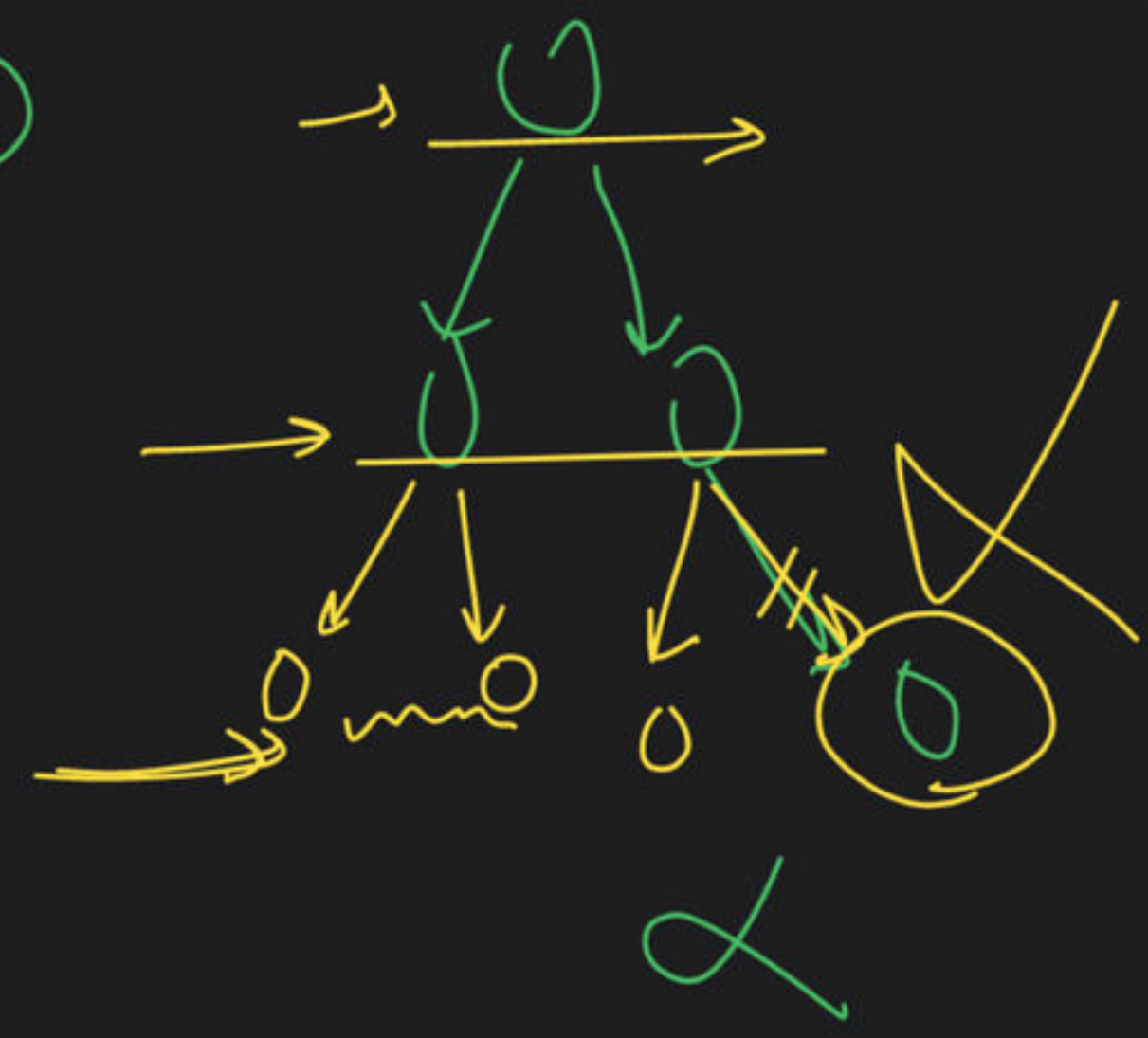
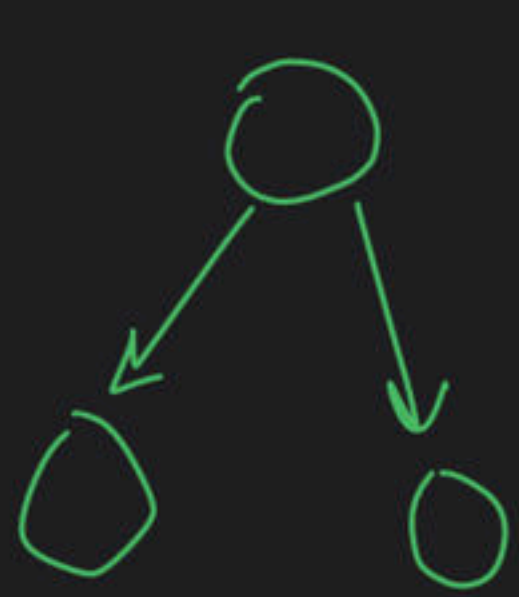
Heaps Class-1

Special class

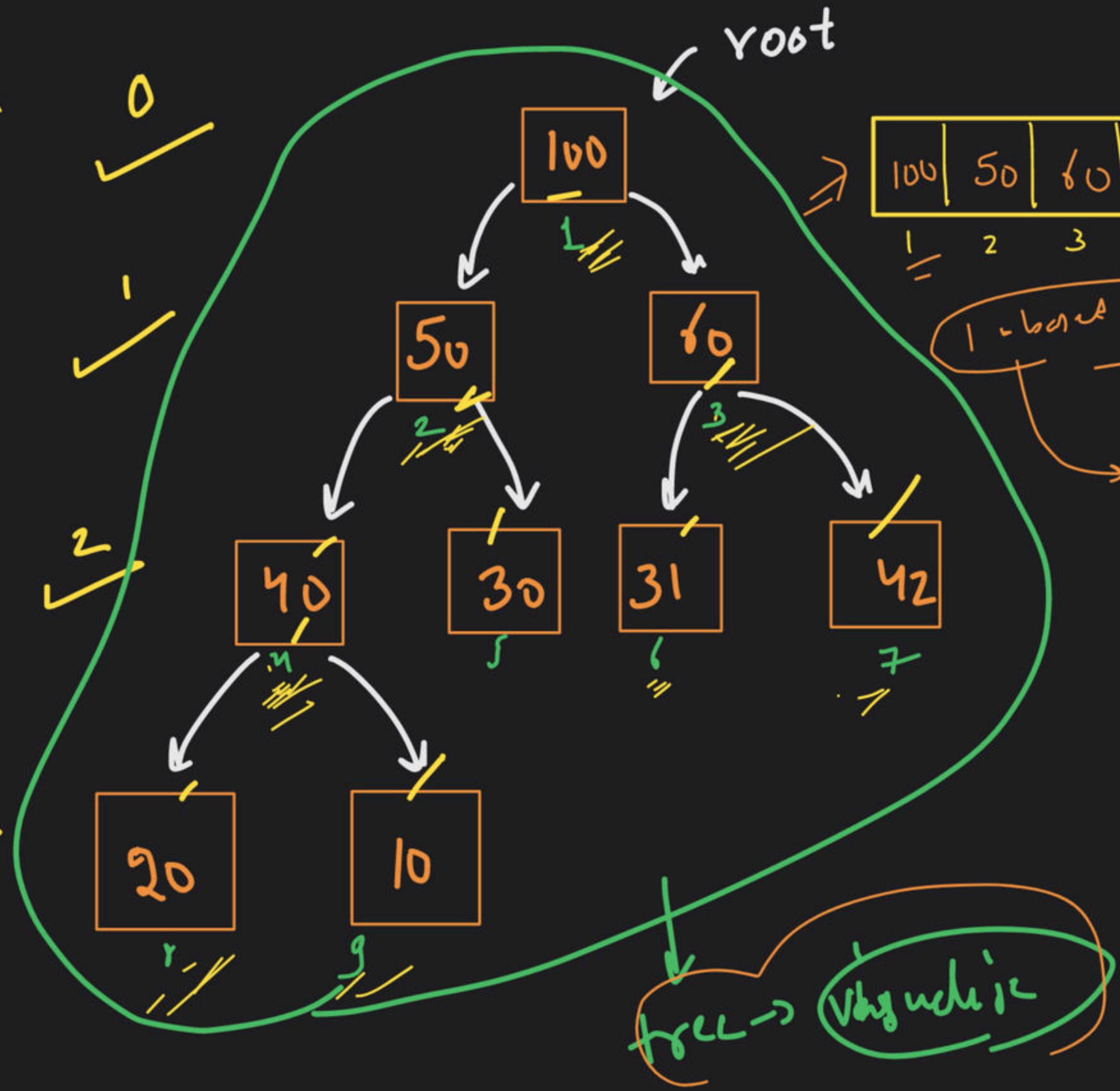


C.B.T → Complete Binary Tree

→ min heap
→ max heap



$7/2^2$
 $6/2^3$
 $5/2^4$
 $4/2^5$
 $3/2^6$
 $2/2^7$
 $1/2^8$
 $0/2^9$

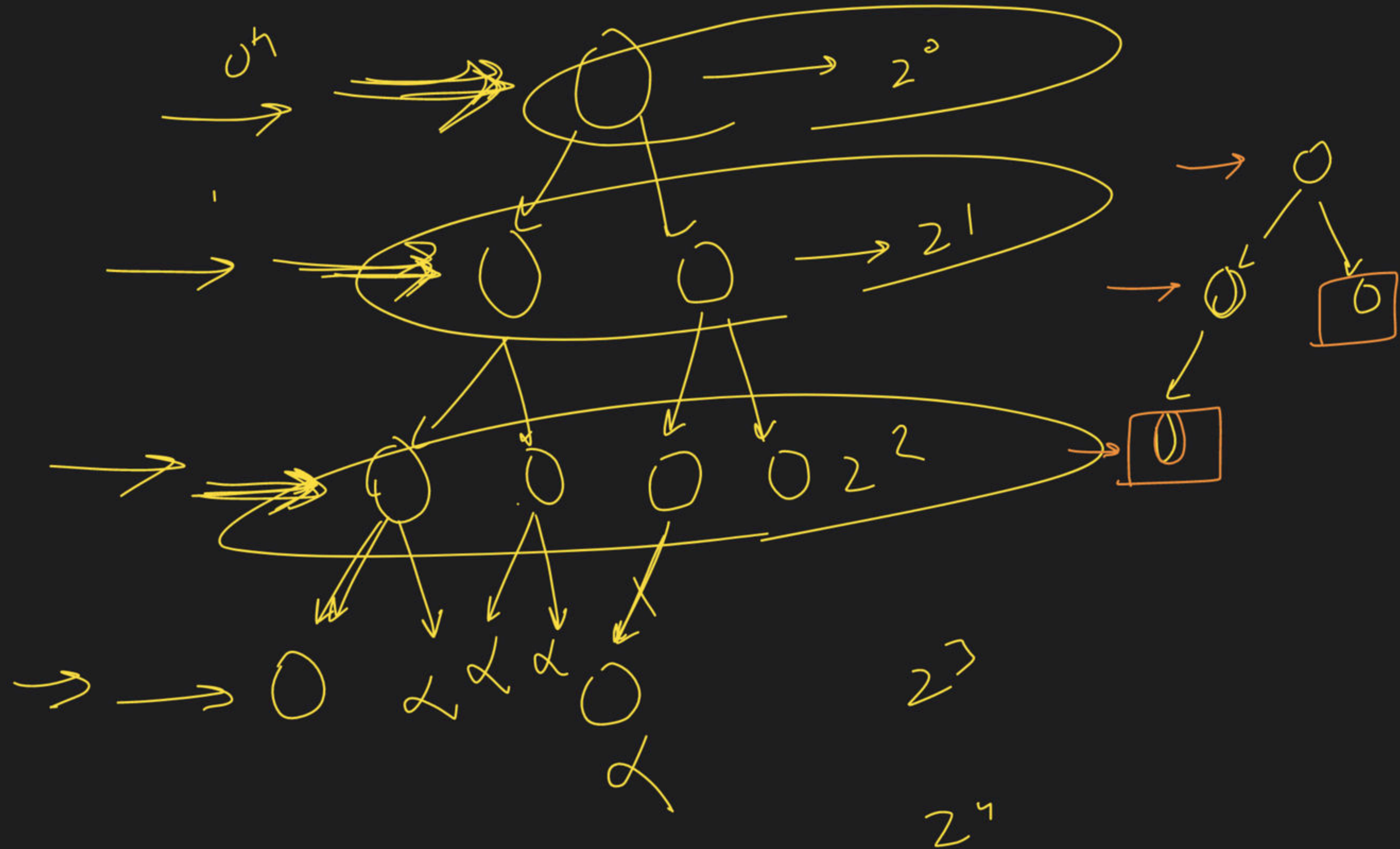


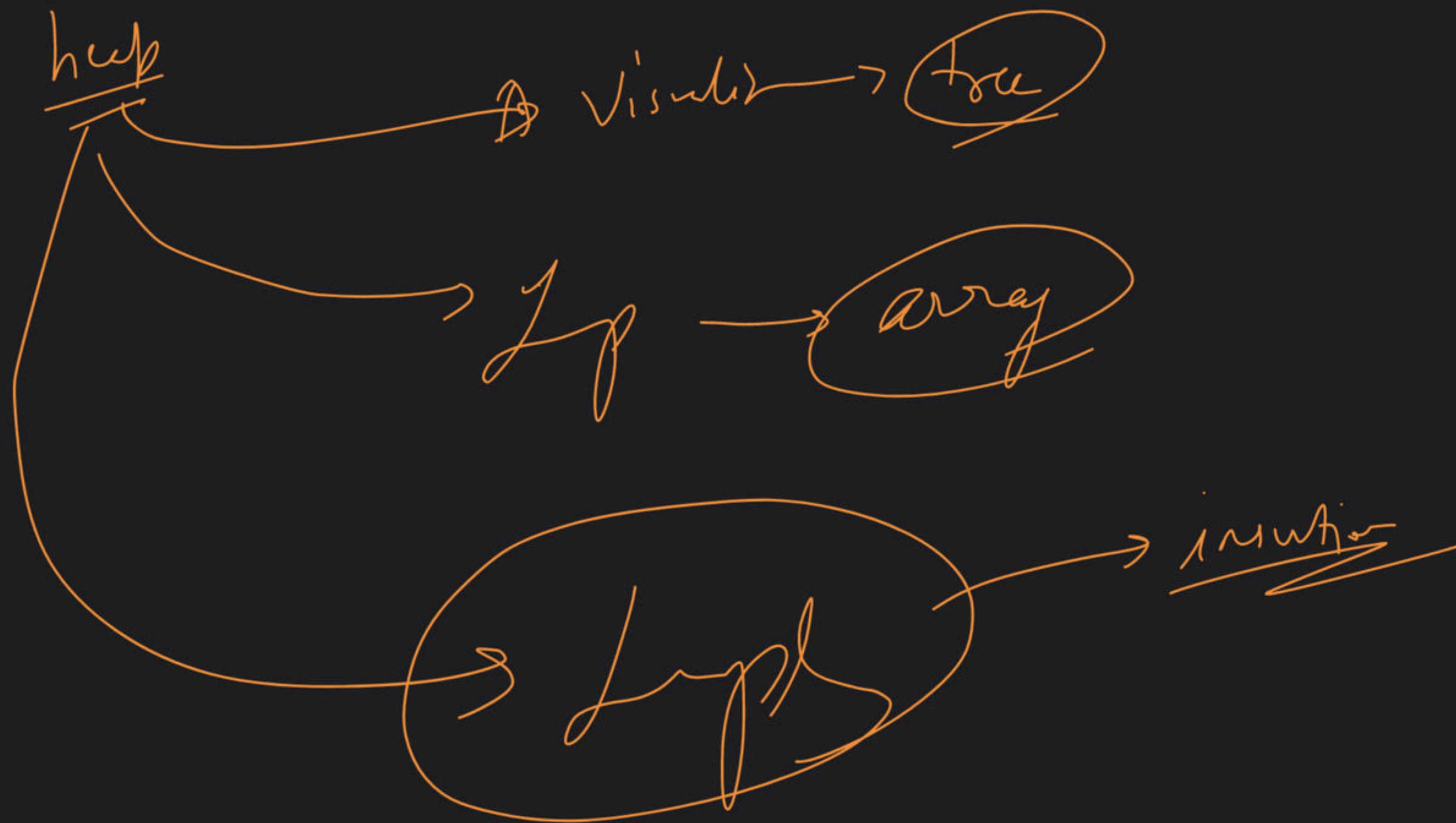
| | | | | | | | | |
|-----|----|----|----|----|----|----|----|----|
| 100 | 50 | 60 | 40 | 30 | 31 | 42 | 20 | 10 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |

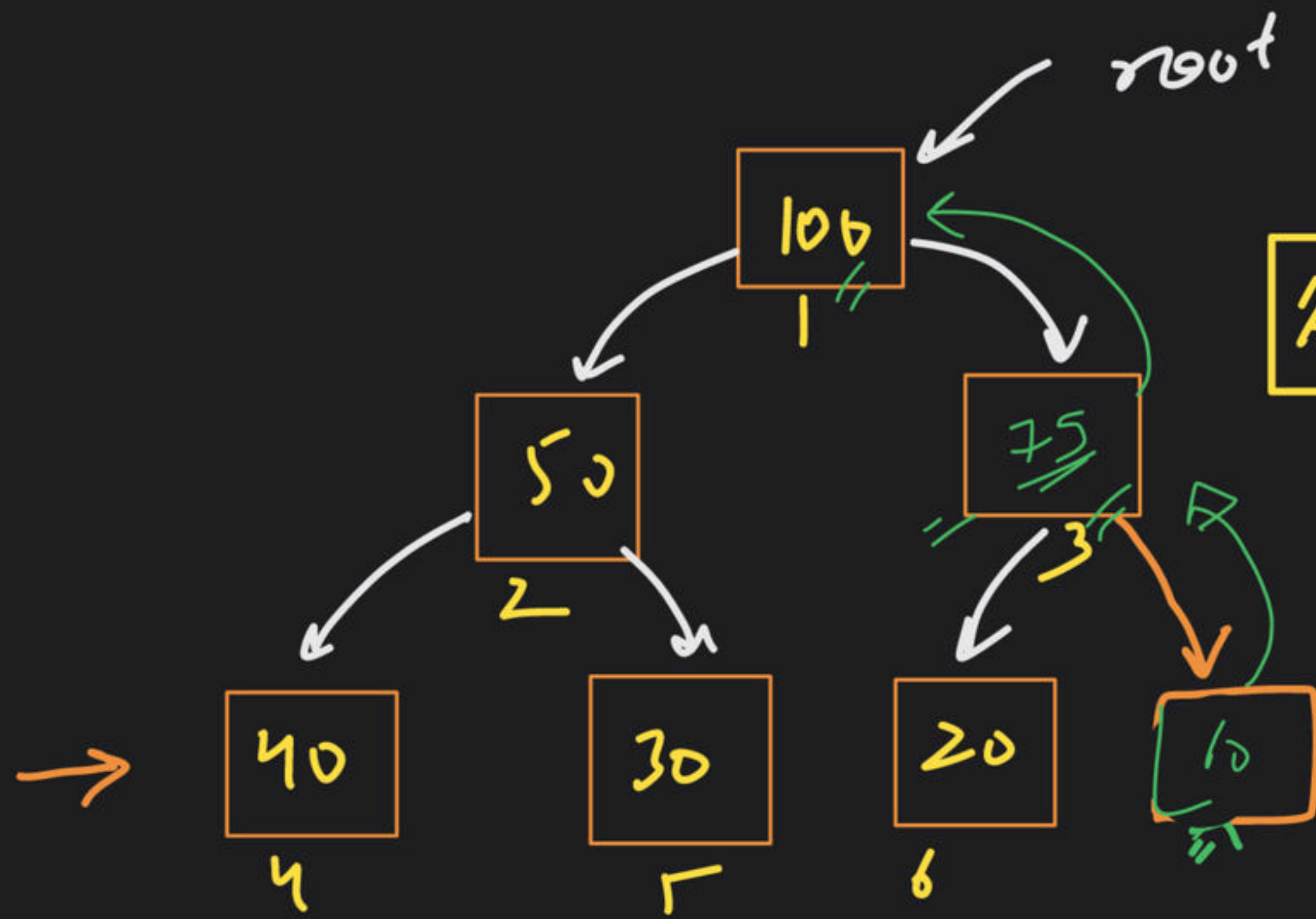
1-based indexing
 parent to child
 i \rightarrow left = $2i$
 i \rightarrow right = $2i+1$

child to parent
 $i \rightarrow n/2$
 i parent \rightarrow $n/2$

0-based
 i \rightarrow left = $2i+1$
 i \rightarrow right = $2i+2$







$\overline{F}_s \rightarrow \text{input}$

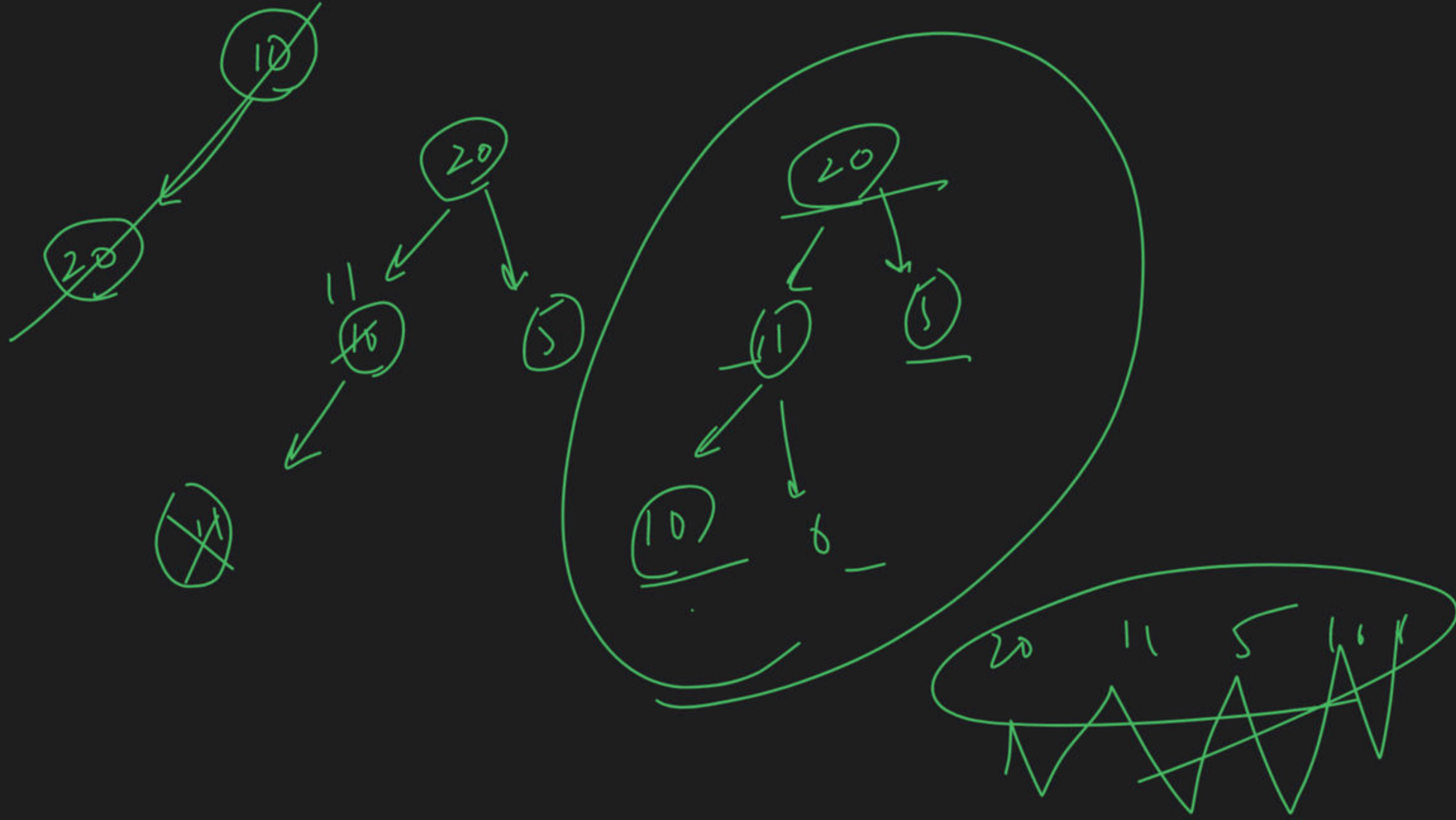
| | | | | | | |
|--------------|-----|----|----|----|----|----|
| 4 | 100 | 50 | 60 | 40 | 30 | 20 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 |

bad \rightarrow sweep
 chotte \rightarrow ignore/stop

insertion \rightarrow

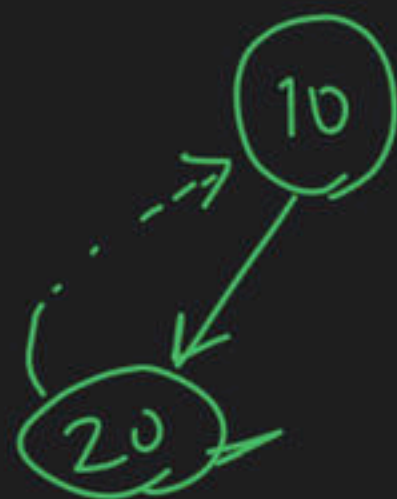
- ① insert \overline{F}_s at the vacant/available position
- ② correcting position

10 20 5 11 6

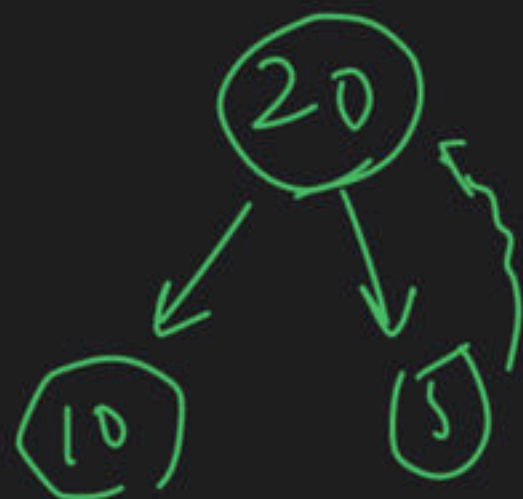
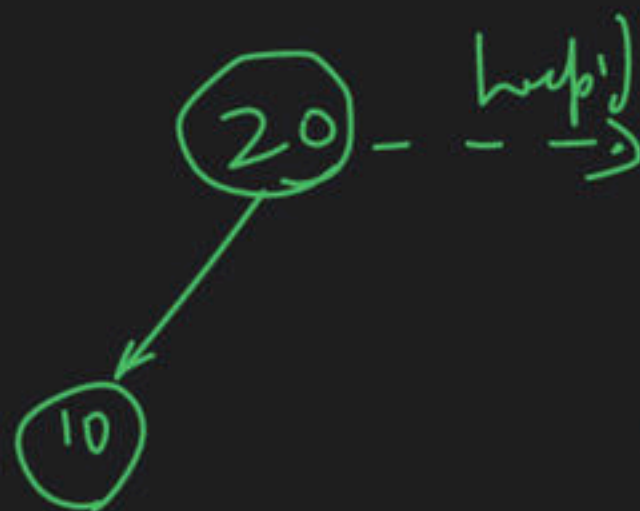


(10) 20 5 11 1

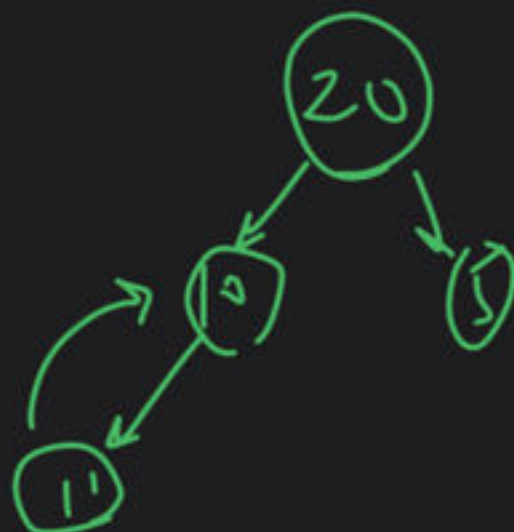
(10) \rightarrow heapify \rightarrow (10)



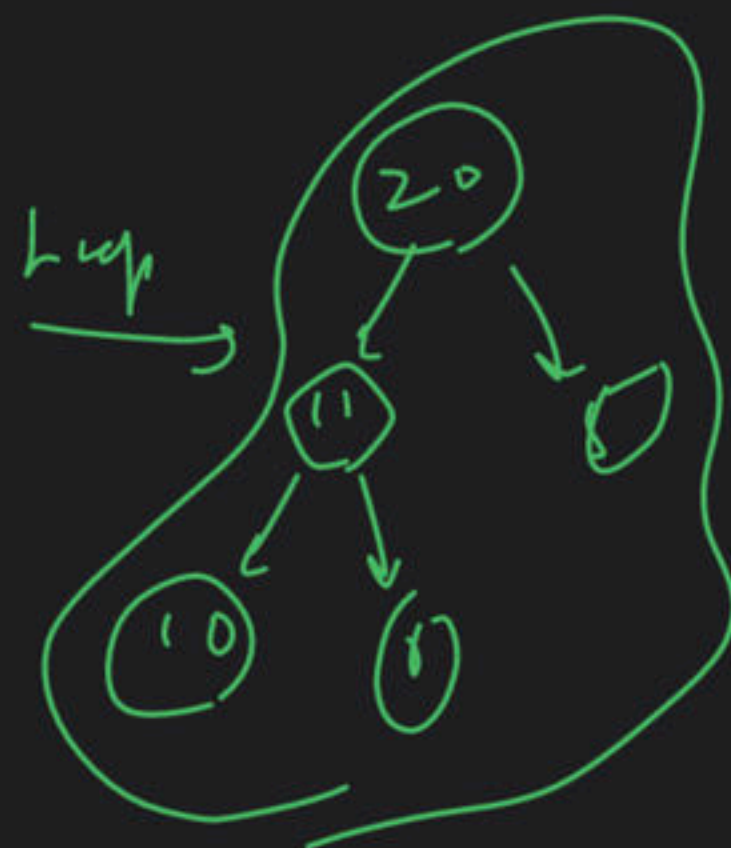
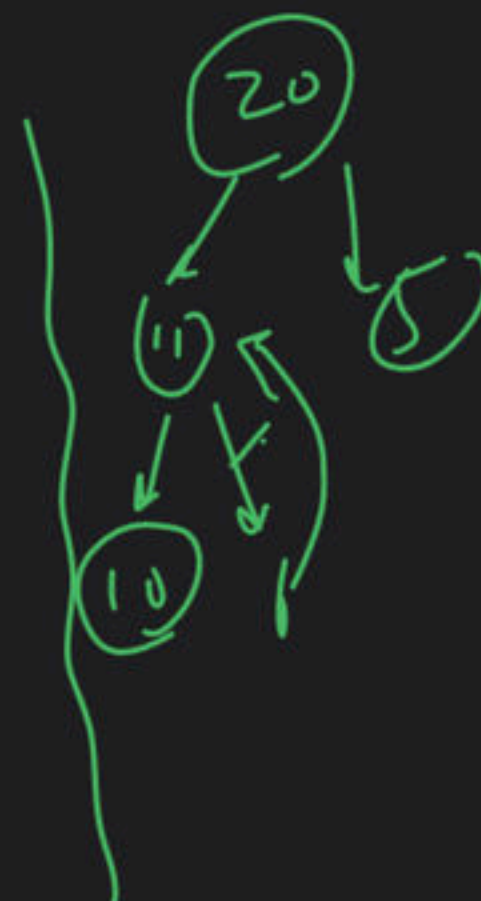
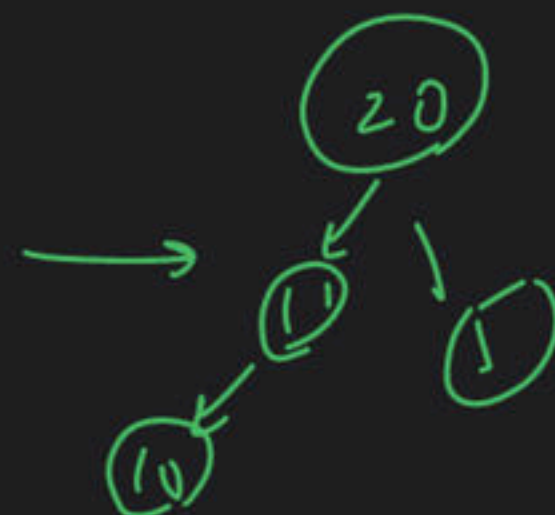
\rightarrow heapify \rightarrow



heapify \rightarrow



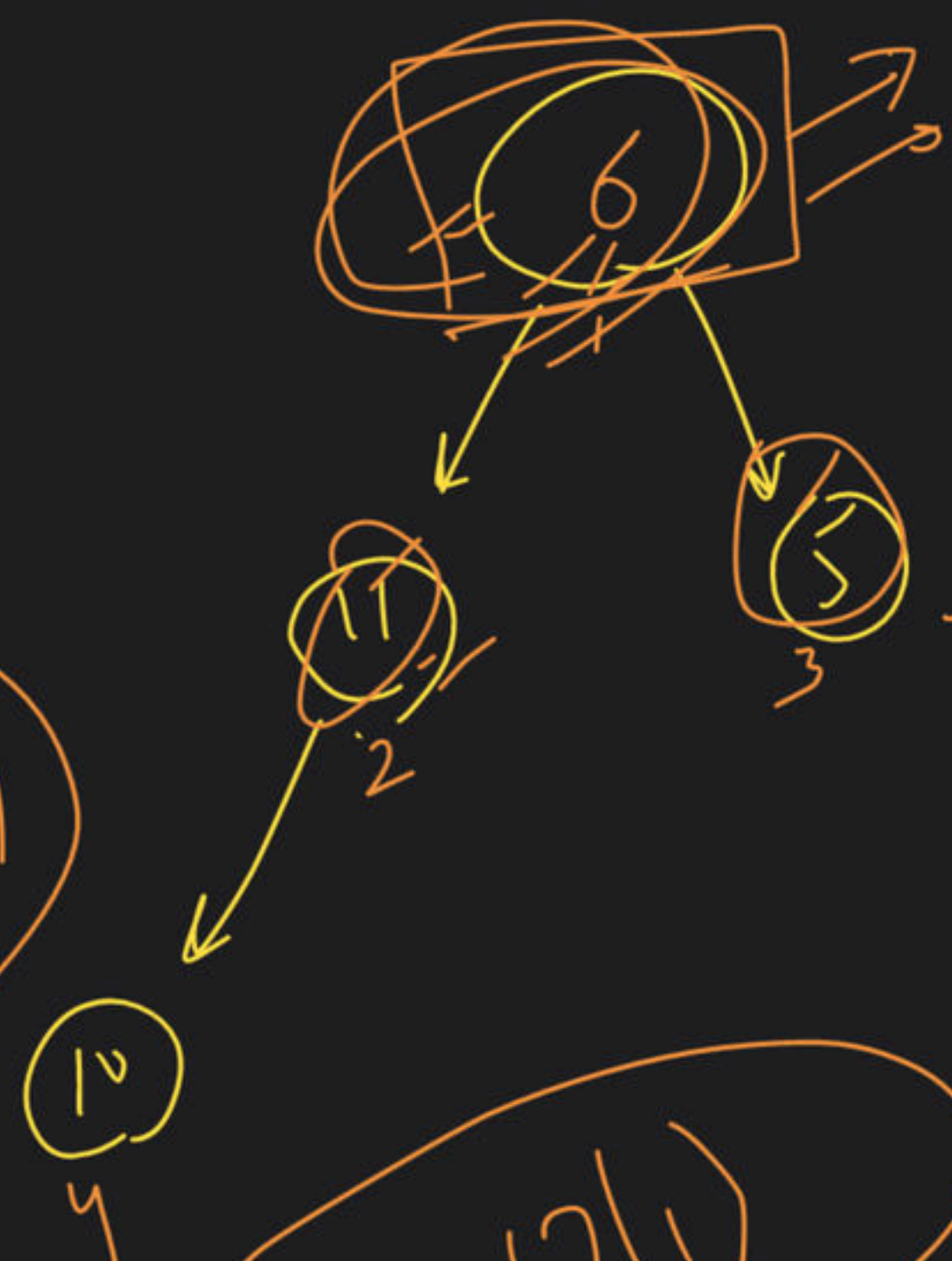
heapify \rightarrow



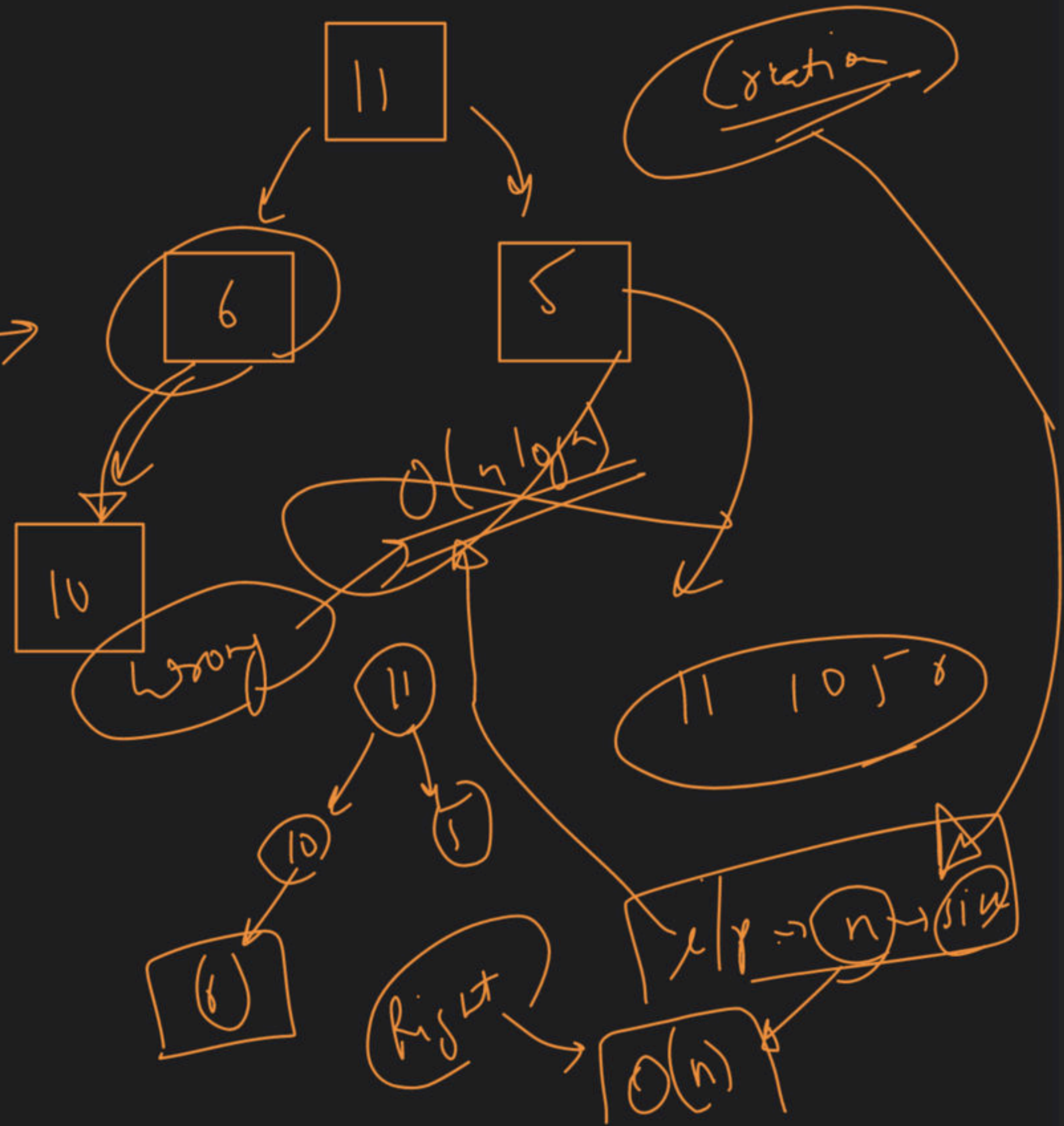
ans = 20

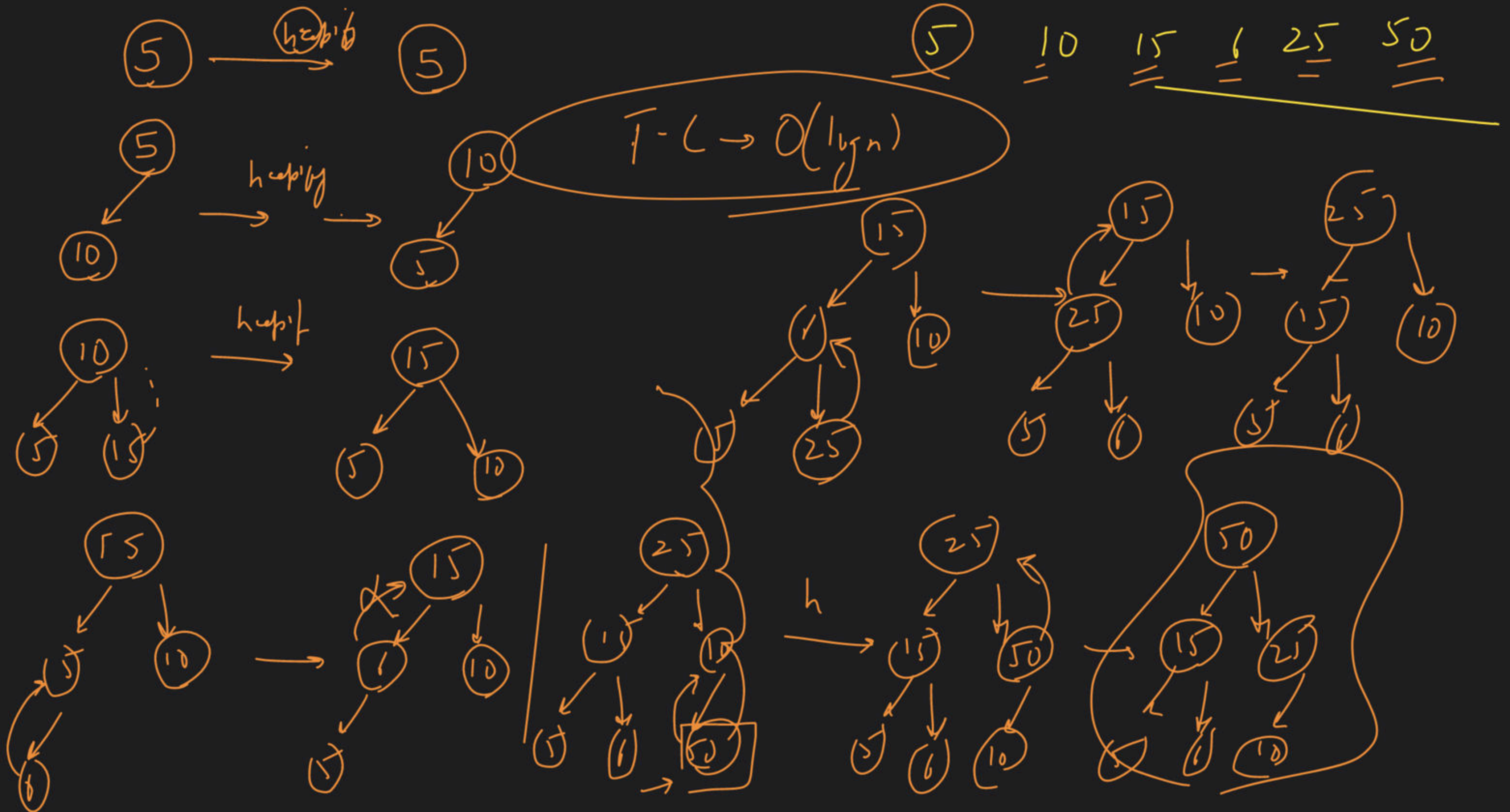
~~data~~ $\log n$

~~min~~ $\log n$

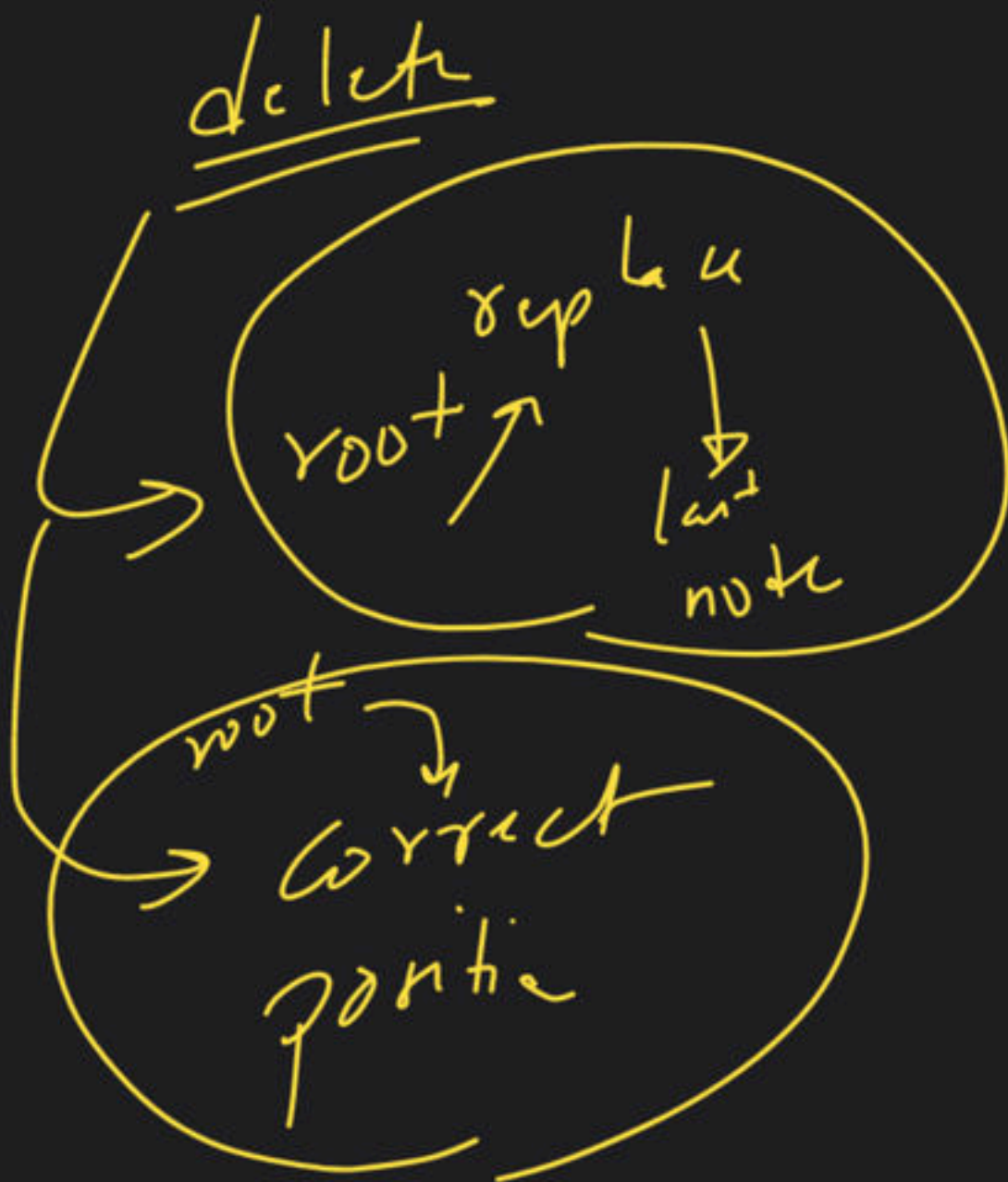
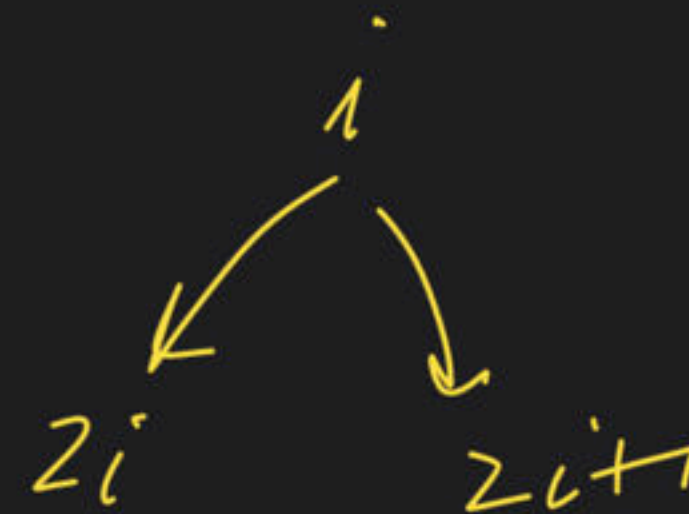
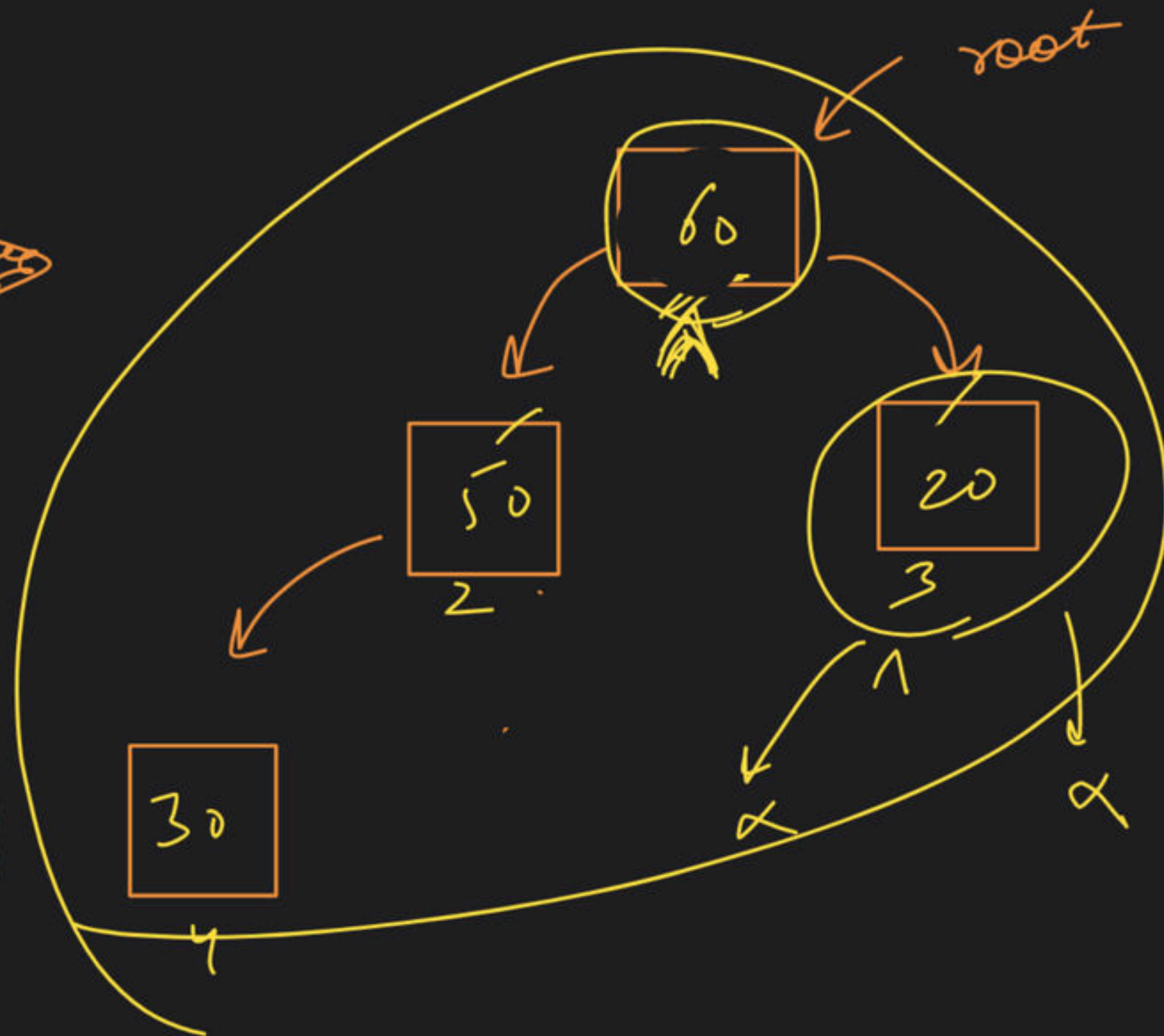


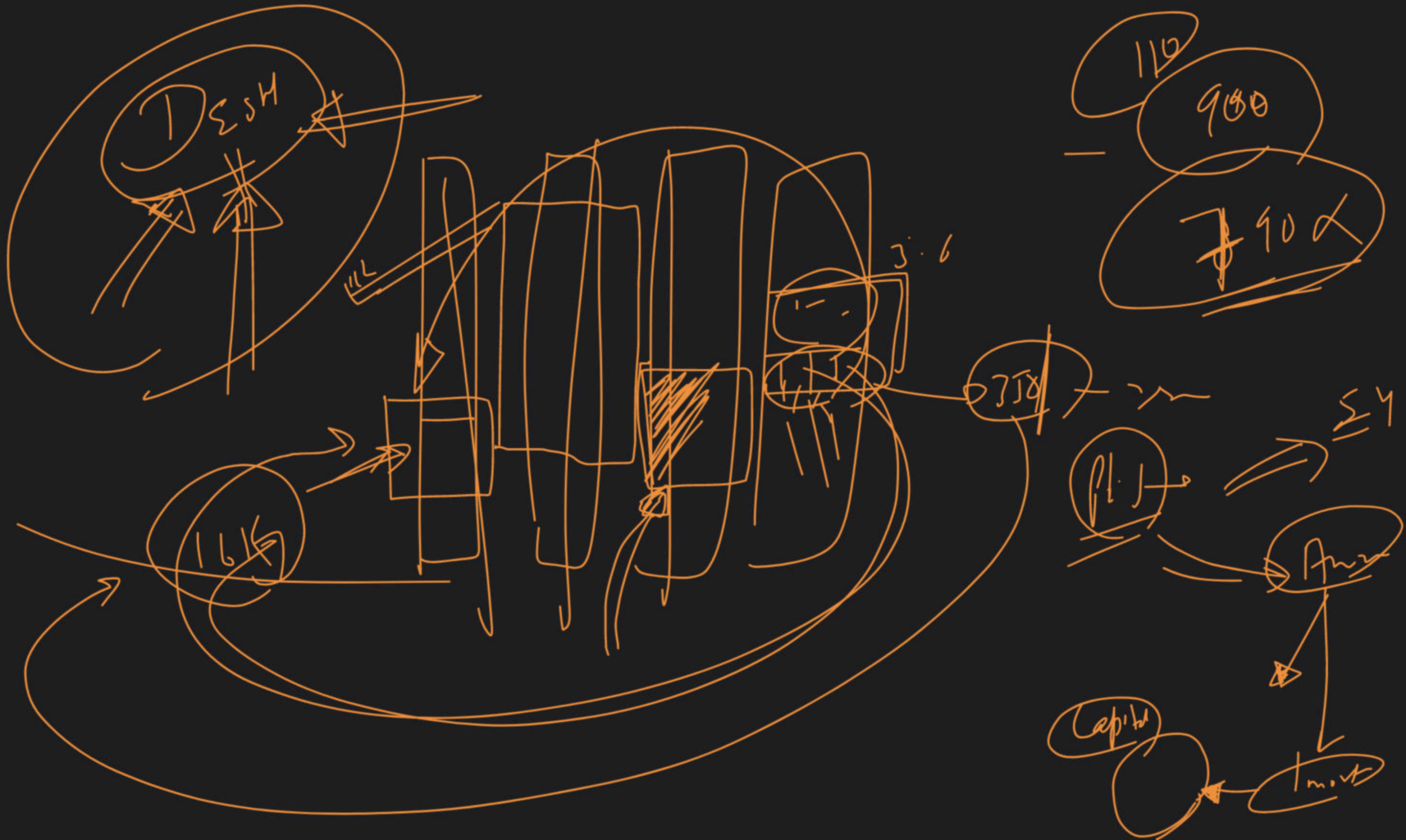
Man $\rightarrow O(1)$
Min $\rightarrow O(1)$





→ 1 Deletion

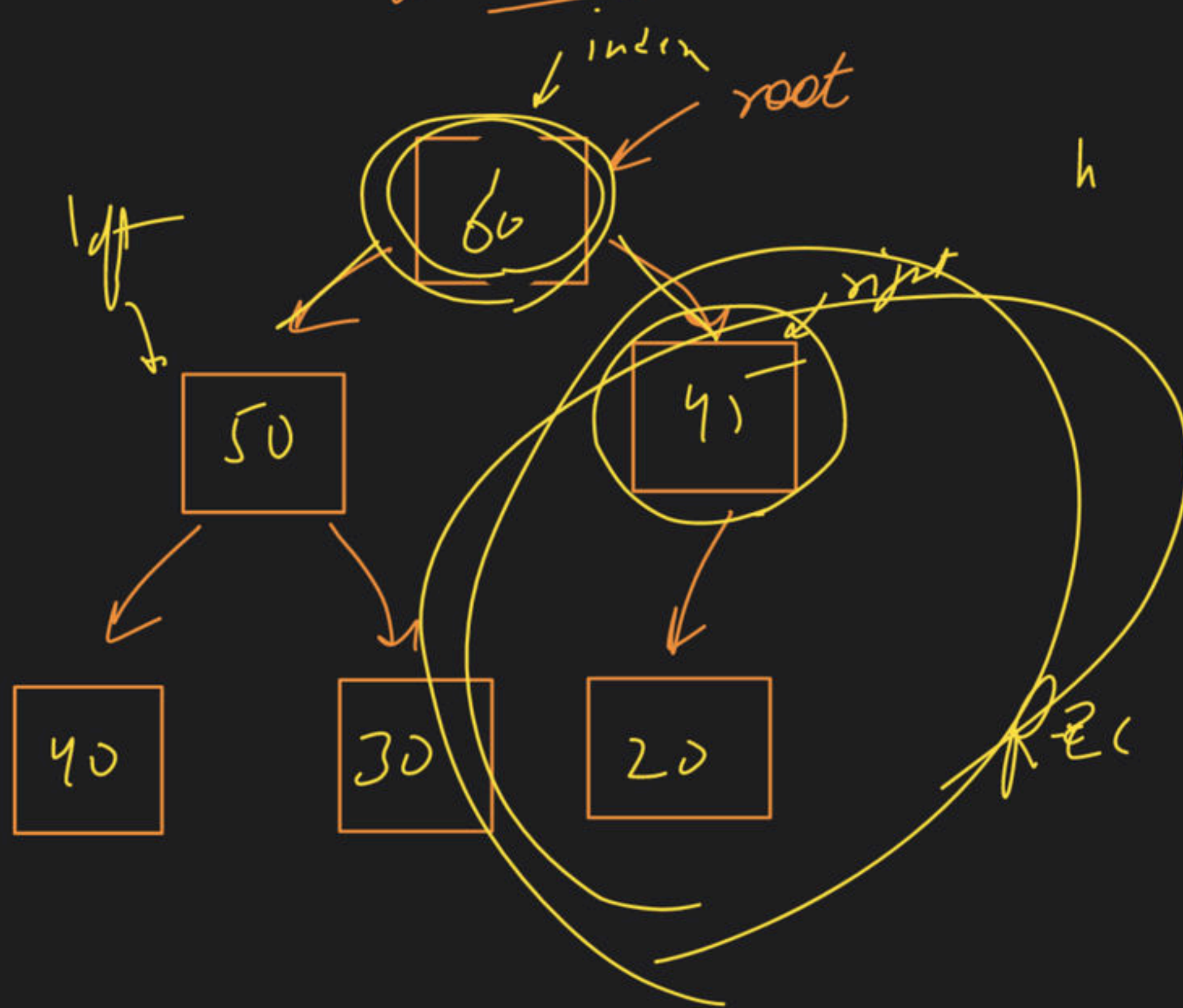


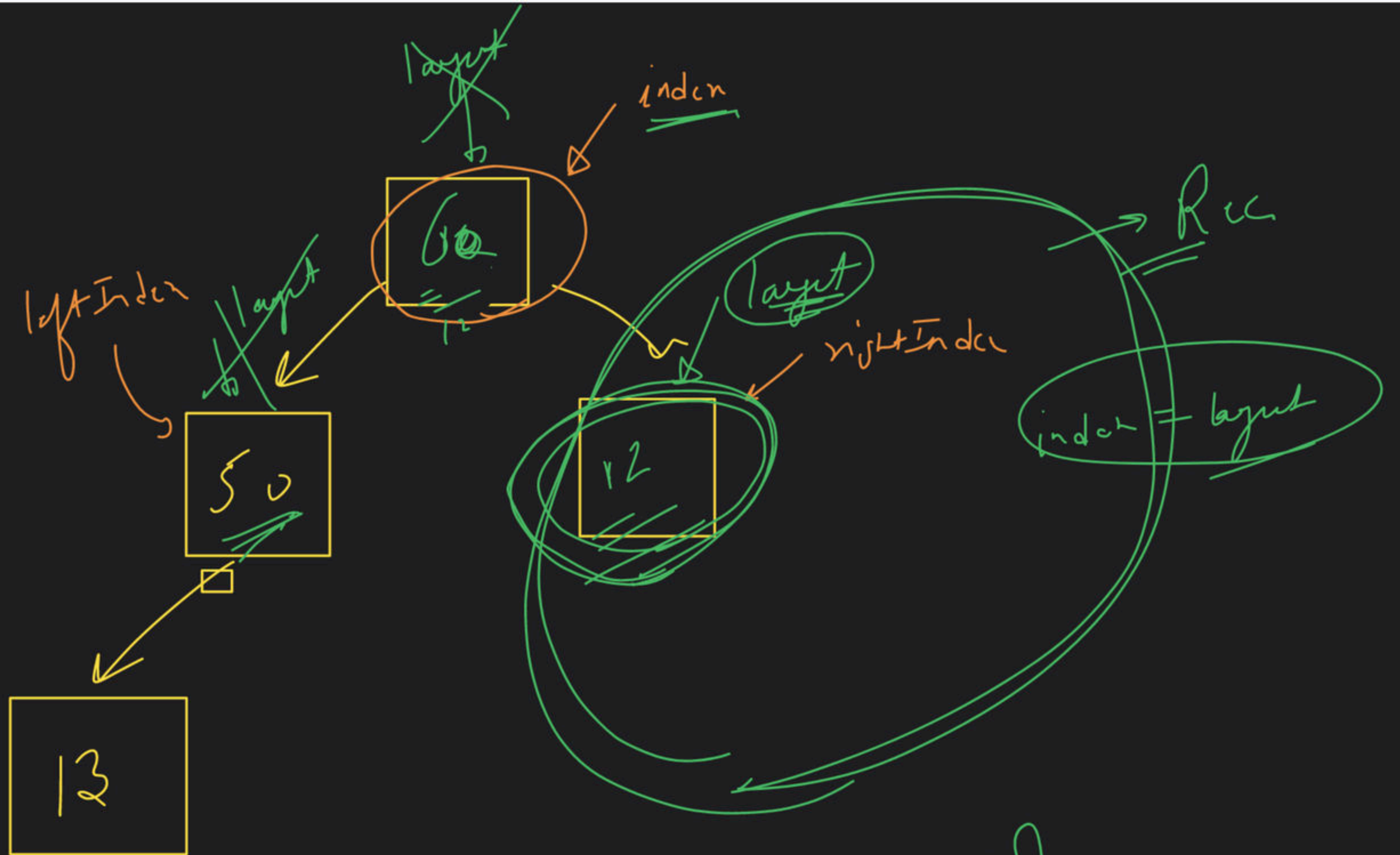


Vishal

Dahiy

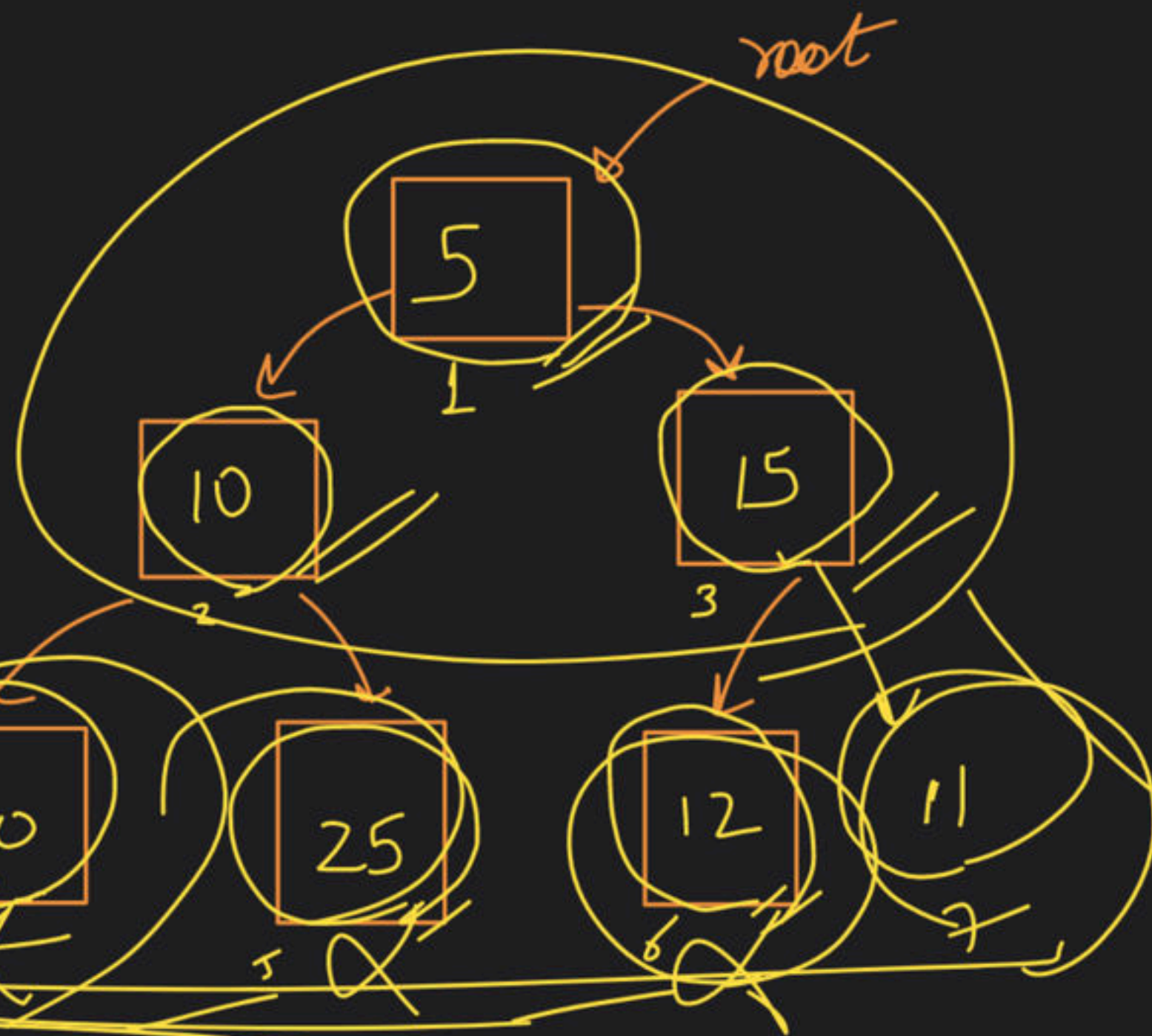
Heapify (arr, n, index)





leftIndex = 2 * i?

$n=6$
 $\left(\frac{n}{2} + 1\right) \rightarrow \frac{6}{2} + 1 = 4$
 $7, 11, 15, 21, 25, 31, 35, 39, 43, 47, 51, 55, 59, 63, 67, 71, 75, 79, 83, 87, 91, 95, 99$

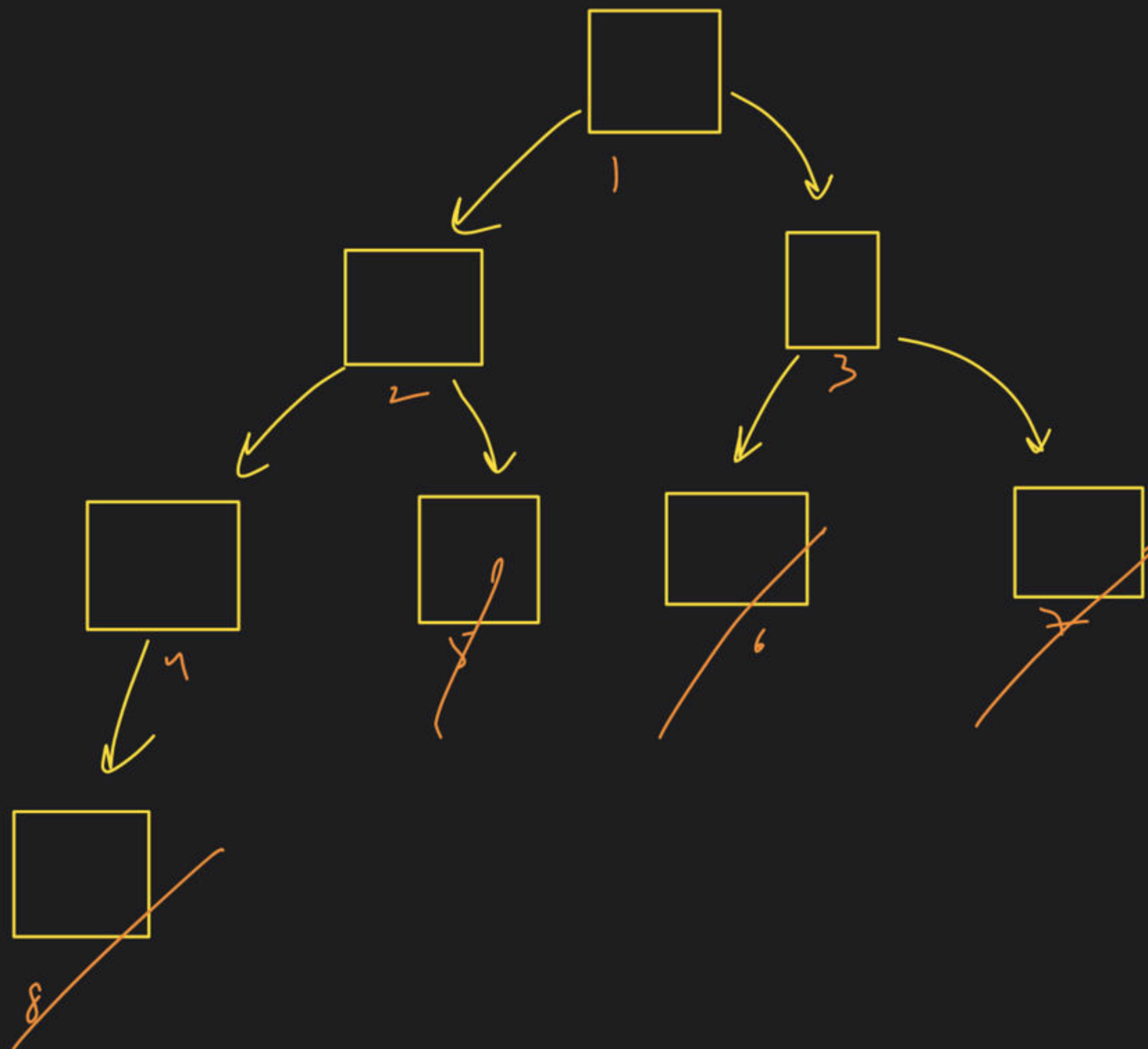


| | | | | | |
|---|----|----|----|----|----|
| 5 | 10 | 15 | 20 | 25 | 12 |
|---|----|----|----|----|----|

Leaf Node \rightarrow Valid Heap

$\left(\frac{n}{2} + 1\right)^{th}$ node \rightarrow leaf node

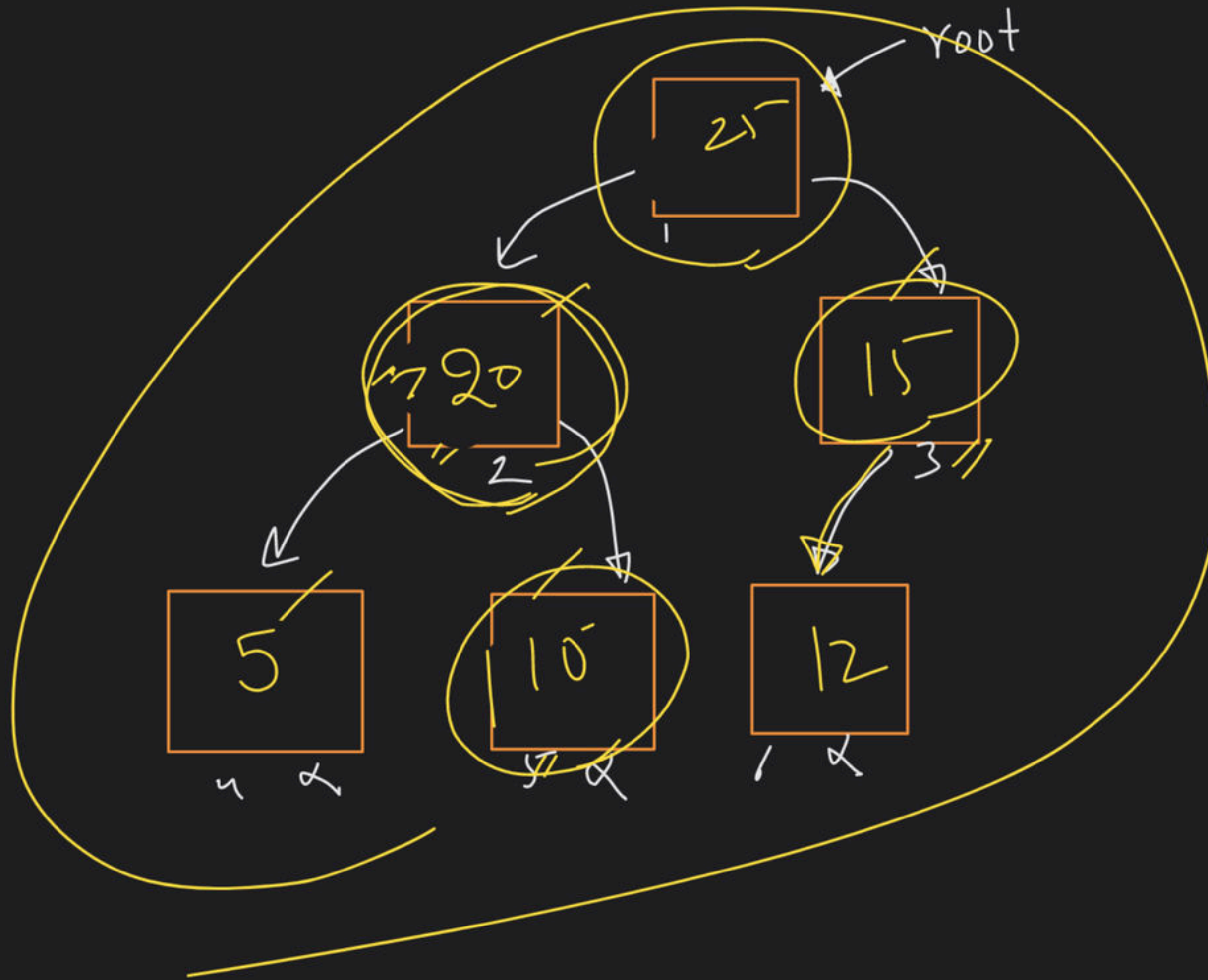
~~\rightarrow for $\left(\frac{n}{2} + 1\right)^{th}$~~



$$\frac{8}{2} + 1 \longrightarrow 8$$

$$\frac{4}{1} + 1 \longrightarrow 8$$

$$5 \longrightarrow 8$$



$$L.N \rightarrow \frac{n}{2} + 1 \rightarrow n$$

$$\frac{6}{2} + 1 \rightarrow 4$$

$$3 + 1 \rightarrow 4$$

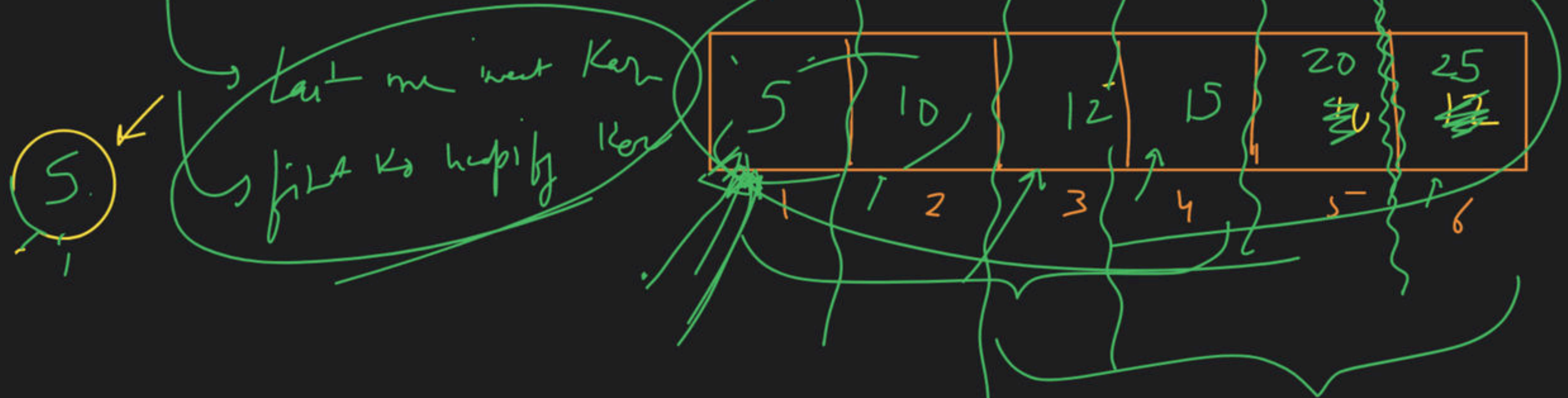
$$4 \rightarrow 6$$

$$for \left(\frac{n}{2} \rightarrow 1 \right)$$

$$for \left(\frac{6}{2} \rightarrow 1 \right)$$

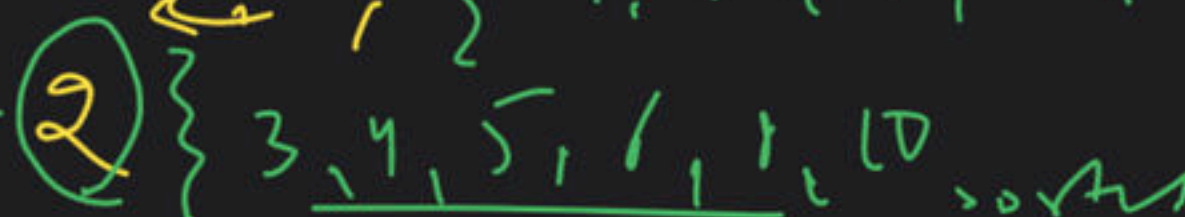
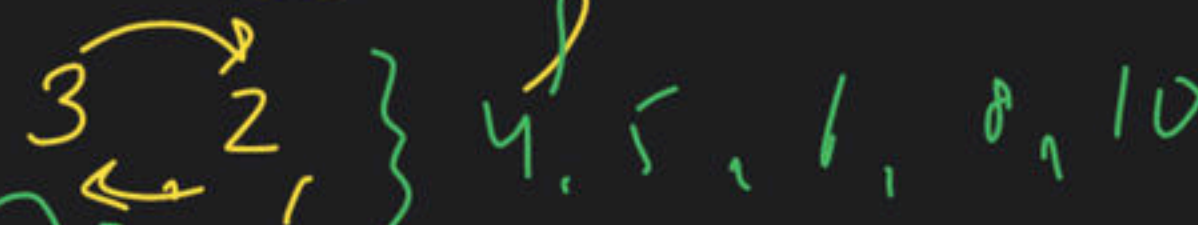
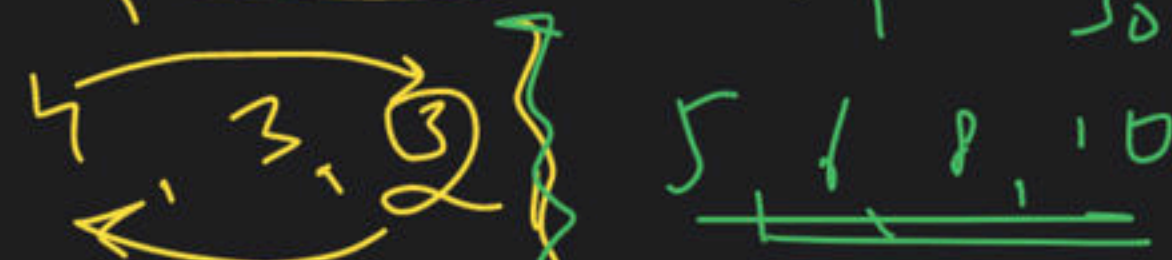
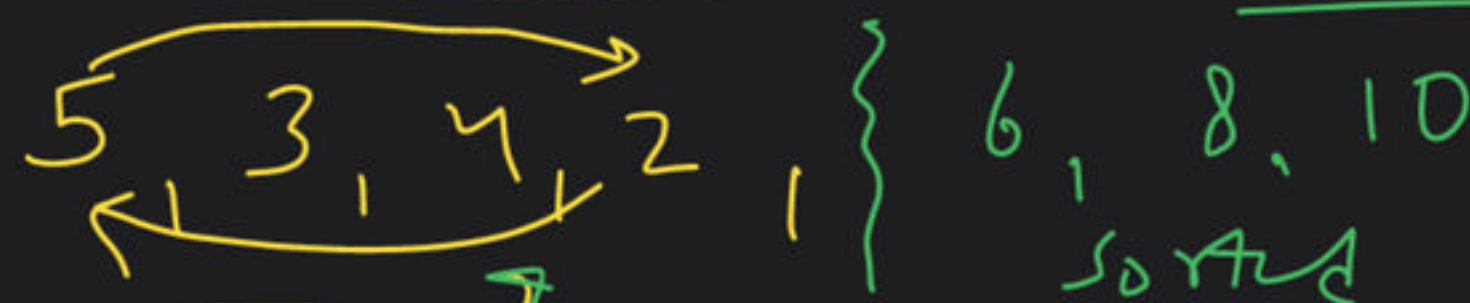
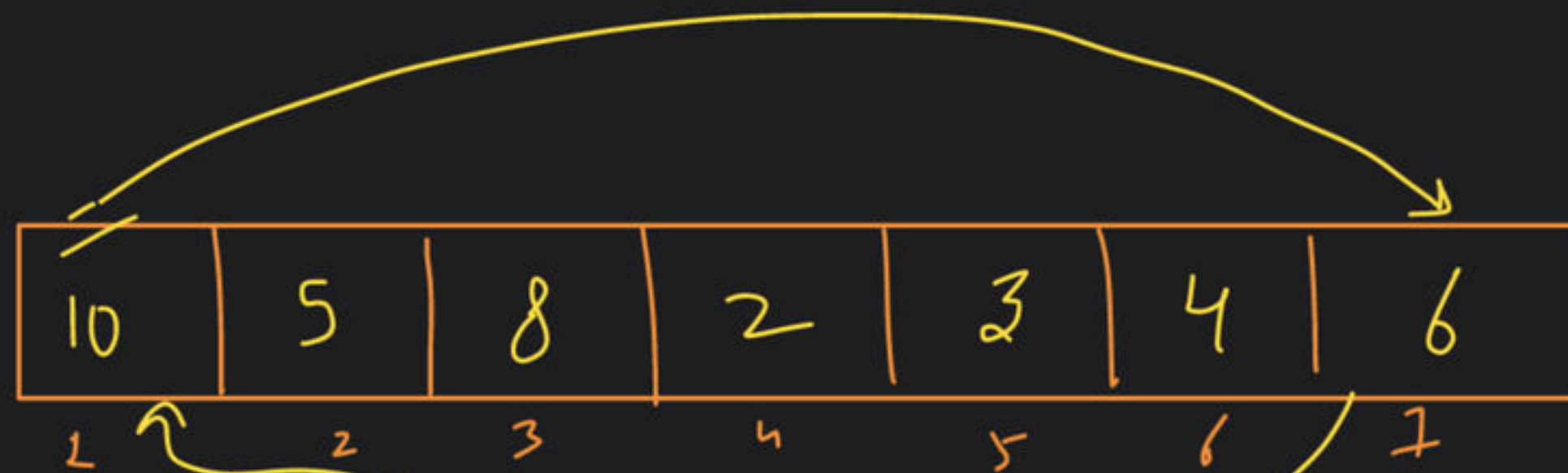
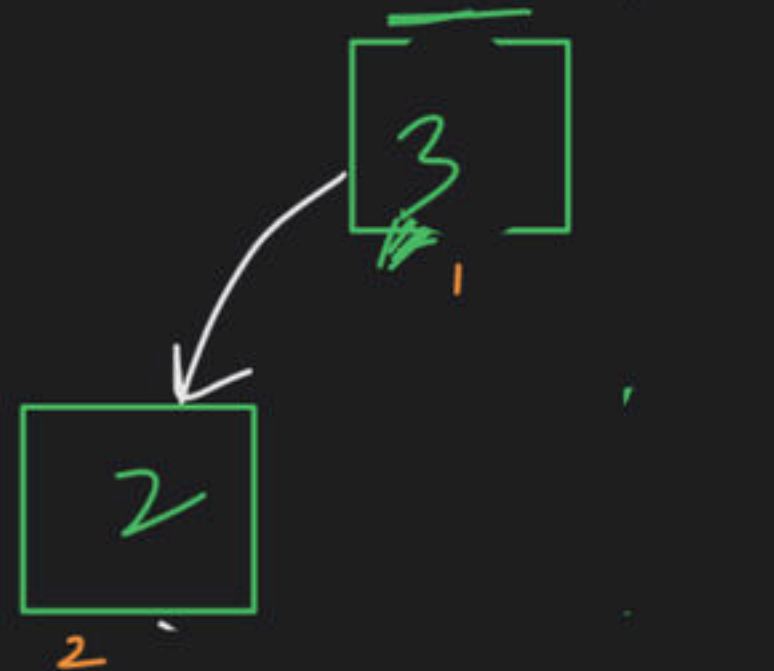
$$for \left(3 \rightarrow 1 \right)$$

Heap Sort



5 10 12 15 20 25

1 Dry Run



2, 3, 4, 5, 6, 8, 10























