

1.6 Signed Binary Numbers

1. Representation of Signed and Unsigned Binary Numbers

- **Unsigned Numbers:** Represent only positive integers (including zero). All bits are used to represent the magnitude.
- **Signed Numbers:** Represent both positive and negative integers.
 - The **leftmost bit (MSB)** represents the sign:
 - * 0 indicates a positive number.
 - * 1 indicates a negative number.
- **Example:**
 - 01001 (Unsigned) = 9 (Signed) = +9
 - 11001 (Unsigned) = 25 (Signed) = −9

2. Signed Number Representations

(a) Signed-Magnitude Representation

- Leftmost bit is the **sign bit**.
- Remaining bits represent the **magnitude**.
- Example (8 bits):

$$+9 = 00001001$$

$$-9 = 10001001$$

(b) 1's Complement Representation

- Negative numbers are represented by **flipping all bits** of the positive number.
- Example:

$$+9 = 00001001$$

$$-9 = 11110110$$

(c) 2's Complement Representation

- Obtain by adding 1 to the 1's complement.
- Simplifies arithmetic operations.
- Example:

$$+9 = 00001001$$

$$-9 = 11110111$$

3. Arithmetic Operations

(a) Addition in 2's Complement

- Add numbers including the sign bit.
- Discard carry out of the MSB.
- Example:

$$\begin{array}{rcl} & & (+6) + (-13) : \\ 00000110 + 11110011 & = & 11111001 \quad (Result = -7) \end{array}$$

(b) Subtraction in 2's Complement

- Take 2's complement of the subtrahend and add it to the minuend.
- Discard carry out of the MSB.
- Example:

$$\begin{array}{rcl} & & (-6) - (-13) : \\ 11111010 + 00001101 & = & 00000111 \quad (Result = +7) \end{array}$$

4. Overflow Conditions

- Occurs when the result exceeds the range that can be represented with the given number of bits.
- Detection Rule:
 - Adding two positive numbers gives a negative result.
 - Adding two negative numbers gives a positive result.