# **Holistic Specifications for Robust Programs**

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#### **ACM Reference Format:**

#### 1 INTRODUCTION

Software guards our secrets, our money, our intellectual property, our reputation [?]. We entrust personal and corporate information to software which works in an *open* world, where it interacts with third party software of unknown provenance, possibly buggy and potentially malicious.

Thus, we expect and hope that our software will be *robust*: We expect and hope our software to behave correctly even if used by erroneous or malicious third parties. Robustness means something different for different software. We expect that our bank will only make payments from our account if *susan*: *I put in the* instructed by us or somebody authorized[?], and that space on a web given to an advertiser will not *ERC20 citation* be used to obtain access to our bank details[?].

The importance of robustness has lead to the design of many programming language mechanisms authorising which help write robust programs: constant fields or methods, private methods/fields, ownership[?] as well as the object capability paradigm[?], and its adoption in web systems [???] and programming languages such as Newspeak [?], Dart [?], Grace [??], Wyvern [?].

While such programming language mechanisms make it *possible* to write robust programs, they cannot *ensure* that programs are robust. To be able to do this, we need ways to specify what robustness means for the particular program, and ways to demonstrate that the particular program adheres to its specific robustness requirements.

There has been a plethora of work on the specification and verification of the functional correctness of programs. Such specifications describe what are essentially *sufficient* conditions for some effect to happen. For example, if you make a payment request to your bank, money will be transferred and as a result your funds will be reduced: the payment request is a sufficient condition for the reduction of funds. However, a bank client is also interested in *necessary* conditions: they want to be assured that no reduction in their funds will take place unless they themselves requested it.

Necessary conditions are essentially about things that will *not* happen. For example, there will be no reduction to the account's funds without the owner's explicit request: the request being made by the owner is the necessary condition - under no other circumstances will the funds be reduced.

We give a visual representation of the difference between sufficient and necessary conditions in Fig. 1. We represent the space of all theoretically possible behaviours as points in the rectangle, each function is a coloured oval and its possible behaviours are the points in the area of that oval. The sufficient conditions are described on a per-function basis. The necessary conditions, on the other

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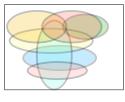
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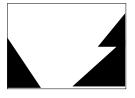
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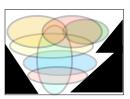
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hand are about the behaviour of a module as a whole, and describe what is guaranteed not to happen; they are depicted as black triangles.







sufficient spec.

necessary spec.

holistic spec.

Fig. 1. Sufficient and Necessary Conditions, and Full Specifications

We propose that necessary conditions should be explicitly stated. Specifications should be *holistic*, in the sense that they describe the overall behaviour of a module: not only the behaviour of each of its functions separately, but also emerging behaviours through combination of functions. A holistic specification should therefore consist of the sufficient as well as the necessary conditions, as depicted in right hand side diagram in Fig. 1. susan: When our module which has been specified holistically, executes, possibly interacting with other software, the behaviours represented by the black triangles cannot occur. In Section 7 we argue why necessary conditions are more than the complement of sufficient conditions.

Necessary conditions are guarantees upheld throughout program execution. Other systems which give such "permanent" guarantees are type systems, which ensure that well-formed programs always produce well-formed runtime configurations, or information flow control systems [?], which ensure that values classified as high will not be passed into contexts classified as low. Such guarantees are practical to check, but too coarse grained for the purpose of fine-grained, module-specific specifications.

Necessary conditions are akin to monitor or object invariants[??]. The difference between these and our holistic specifications is that object/monitor invariants can only reflect on the current state (*i.e.* the contents of the stack frame and the heap), while holistic specifications reflect on all aspects of execution.

In this paper we propose *Chainmail*, a specification language to express holistic specifications. *Chainmail* extends traditional program specification languages[??], with features which talk about:

**Permission** Which object may have access to which other objects. Accessibility is central since access to an object usually also grants access to the functions it provides.

**Control** What object called functions on other objects. This is useful in identifying the causes of certain effects - eg funds can only be reduced if the owner called a payment function.

**Authority** Which objects' state or properties may change. This is useful in describing effects, such as reduction of funds.

**Space** This is about which parts of the heap are considered when establishing some property, or when performing program execution and is related to, but different from memory footprints and separation logics.

**Time** Assertions about the past or the future.

The design of *Chainmail* was guided by the study of a sequence of examples from the OCAP literature and the smart contracts world: the membrane, the DOM, the Mint/Purse, the Escrow, the DAO and ERC20. We were satisfied to see that the same concepts were used to specify examples from different contexts. Holistic assertions often have the form of a guarantee that if some property ever hods in the future then some other property holds now. For example, if within a certain heap

Susan: I would stop after the firs sentence - the other points perhaps in relate work

Susan: These features sort of come from wonder whether we even want them in the introduction. I think if you do then something more about open systems, (that what is critical is controlling access from foreign code and that you need to be able to talk about that in the specification language) should

come first.

instead? Also, we need to stress that

these features was

not arbitrary.

some change is possible in the future, then this particular heap contains at least one object which has access to a specific other, privileged object. While many individual features of Chainmail can be found also in other work, we argue that their power and novelty for specifying open systems lies in their careful combination. Sophia: I think

A module satisfies such a holistic assertion if, for all other modules, the assertion is satisfied in all that James does runtime configurations reachable through execution of the two modules combined. This reflects the sentence. What open-world view.

The contributions of this paper are:

- the design of the holistic specification language *Chainmail*,
- the semantics of *Chainmail*,
- a validation of *Chainmail* through its application to a sequence of examples,
- a further validation of Chainmail through informal proofs of adherence of code to some of these specifications.

The rest of the paper is organized as follows: Section 2 motivates our work in terms of an example. Sections A contain a formal definition of  $\mathcal{L}_{00}$ , and Section 5 the semantics of assertions. Section ... related work .... Section xxxx concludes.

#### MOTIVATING EXAMPLE: THE BANK

Traditional functional specifications describe what objects are guaranteed to do. So long as a method is called in a state satisfying its preconditions, the method will complete its work and establish a state satisfying its postconditions. Thus, the pre-condition and the method call together form a sufficient condition for the method's effect.

As a motivating example, we consider a simplified banking application, with objects representing Accounts or Banks. As in [?], Accounts belong to Banks and hold money (here balances); with access to two Accounts of the same Bank on cane transfer any amount of money from the one to the other. We give a traditional specification in Figure 2.

```
function deposit(src, amt)
PRE: this, src:Account ∧ this≠src ∧ this.myBank=src.myBank ∧
      amt:N ∧ src.balance≥amt
POST: src.balance=src.balancepre-amt \land this.balance=this.balancepre+amt
function makeNewAccount(amt)
PRE: this:Account ∧ amt:N ∧ this.balance≥amt
POST: this.balance=this.balancepre-amt \land fresh result \land
      result: Account Λ this.myBank=result.myBank Λ result.balance=amt
function newAccount(amt)
PRE: this:Bank
POST: result: Account A result.myBank=this A result.balance=amt
```

Fig. 2. Functional specification of Bank and Account

The PRE-condition of deposit requires that the receiver and the first argument (this, scr) are Accounts and belong to the same bank, that amt is a number, and that src holds at leat amt moneys. The POST-condition mandates that amt has been transferred from src to the receiver. The function makeNewAccount specified below returns a fresh Account with the same bank, and transfers amt from the receiver Account to the new Account. Finally, the function newAccount when run by a Bank creates a new Account with corresponding amount of money in it.

:4 author

With such a specification the code below satisfies its assertions: assuming that acm\_acc and auth\_ascc are Accounts, and acm\_acc has a balance of 10,000 before an author is registered, then afterwards it will have a balance of 11,000 while the auth\_acc's balance will be f 500 from a starting balance of 1,500 (barely enough to buy a round of drinks at the conference hotel bar).

```
assume acm_acc,auth_scc: Account \Lambda acm_acc.balance=10000 \Lambda auth_acc.balance=1500 acm_acc.deposit(auth_acc,1000) assert acm_acc.balance=11000 \Lambda auth_acc.balance=500
```

This reasoning is fine in a closed world, where we only have to consider complete programs, where all the code in our programs (or any other systems with which they interact) is under our control. In an open world, however, things are more complex: our systems will be made up of a range of modules, many of which we do not control; and furthermore will have to interact with external systems which we certainly do not control. Returning to our author, say some time after registering by executing the code from earlier, they attempt to pay for a round at the bar. Under what circumstances can they be sure they have enough funds in their account?

To see the problem, what if the bank provided a steal method that emptied out every account in the bank and put them into a thief's account? If this method existed and if it was somehow called between registering at the conference and going to the bar, then the author (actually everyone using the same bank) woud find all their accounts empty (except the thief, of course).

The critical problem is that a bank implementation including a steal method would meet the functional specifications of the bank from fig. 2, so long as the methods deposit, makeNewAccount, and newAccount meet their specification.

One obvious solution would be to return to a closed-world interpretation of specifications: we interpret specifications such as fig. 2 as *exact* in the sense that only implementations that meet the functional specification exactly, *with no extra methods or behaviour*, are considered as suitable implementations of the functional specification. The problem is that this solution is far too strong: it would for example rule out a bank that during maintenance was given a new method deposit that simply counted the number of deposits that had taken place, or a bank which occasionally sent notifications to its customers.

What we need is some way to permit bank implementations that send notifications to customers but to forbid implementations of steal, The key here is to capture the (implicit) assumptions underlying fig. 2, and to provide additional specifications that capture those assumptions. The following three requirements prevent methods like steal:

- (1) After creation, the *only* way an account's balance can be changed is if a client calls the deposit method with the account as the receiver or as an argument.
- (2) An account's balance can *only* be changed if a client has that particular account object.
- (3) Accounts and Banks are not leaked.

Compared with the functional specification we have seen so far, these assumptions capture *necessary* conditions rather than *sufficient* conditions. It is necessary that the deposit method is called to change an account's balance, and it is necessary that the particular account object can be passed as a parameter to that method. The function steal is inconsistent with requirement (1), as it reduces the balance of an Account without calling the function deposit. However, requirement (1) is not enough to protect our money. We need to (2) avoid that an Account's balance is modified without access to the particular Account, and (3) ensure that such accesses are not leaked.

Below we express these informal requirements through *Chainmail* assertions. Rather than specifying the behaviour of particular methods when they are called, we write invariants that range across the entire behaviour of the Bank/Account module:

```
(1) ≜ ∀a: Account. [ Change⟨a.balance⟩ →
∃o.[Was⟨ Calls⟨o, deposit, a, _⟩ _ ∨ Calls⟨o, deposit, _, a⟩ _ ⟩ ] ]
(2) ≜ ∀a: Account. ∀S: Set. [With⟨S, (Will⟨ Change⟨a.balance⟩⟩) ⟩ →
∃o. [o ∈ S ∧ External⟨o⟩ ∧ Access⟨o, a⟩] ]
(3) ≜ ∀a: Account. ∀S: Set. [ With⟨S, (Will⟨∃o.[External⟨o⟩ ∧ Access⟨o, a⟩] ⟩) ⟩ →
∃o'. [o' ∈ S ∧ External⟨o'⟩ ∧ Access⟨o', a⟩] ]
```

We will discuss the meaning of *Chainmail* assertions in more detail in the next sections, but give here a first impression, and discuss (1)-(3):

Assertion (1) says that if an account's balance changes (Change(a.balance)), then there must be some client object o that in the past (Was(...)) called the deposit method with a as a receiver or an an argument ( $Calls(o, deposit, \_, \_)$ ).

Assertion (2) similarly constrains any possible change to an account's balance: If at some future  $\frac{m some later}{section on that this}$  point the balance changes ( $Will\langle Change\langle ... \rangle \rangle$ ), and if this future change is observed with the  $\frac{assertion}{implicitly gives}$  configuration restricted to the objects from  $S(i.e.\ With\langle\ S,\ ...\ \rangle)$ , then at least one of these objects  $\frac{change}{implicitly gives}$  ( $S(i.e.\ With\langle\ S,\ ...\ \rangle)$ ) and has (direct) access to that account object ( $\mathcal{A}ccess\langle\ O,\ a\rangle$ ). Notice that while the change in the balance happens some time in the future, the external object  $S(i.e.\ S)$  has access to  $S(i.e.\ S)$  in the  $S(i.e.\ S)$  notice also, that the object which makes the call to deposit described in (1), and the object which has access to  $S(i.e.\ S)$  in the current configuration described in (2) need not be the same: It may well be that the latter passes (indirectly) to the former access to  $S(i.e.\ S)$ , which then makes the call to deposit.

It remains to think about how access to a Account may be obtained. This is the remit of assertion (3): Assertion (3) says that if at sometime in the future observed in the configuration restricted to S, some object  $\circ$  which is external has access to some account a, then in the current configuration some object from Shas access to a. Note that  $\circ$  and  $\circ'$  may but need not be the same object. Note also that  $\circ'$  has to exists and have access to a in the current configuration, but  $\circ$  need not exist in the current configuration – it may be allocated later.

A holistic specification for the bank account, then, would be our original sufficient functional specification from fig. 2 plus the necessary security policy specifications (1)-(3) from above. This holistic specification permits an implementation of the bank that also provides count and notify methods, but does not permit an implementation that also provides the steal method. First, the sophia: We said steal method clearly changes the balance of every account in the bank, but policy (1) requires that this earlier, do we any method that changes the balance of any account must be called deposit. Second, the steal method changes the balance of every account in the system, and will do so without the caller having a reference to most of those accounts, thus breaching policy (2).

Assertion (3) gives essential protection when dealing with foreign, untrusted code. When ansophia: 1 like the Account is given out to untrusted third parties, assertion (3) guarantees that this Account cannot paragraph. Please be used to obtain access to further Accounts. Thus, if the ACM does not trust the author, it will make more placed be used to obtain access to further Accounts. Thus, if the ACM does not trust the author, it will make more placed be used to obtain access to further Accounts. Thus, if the ACM does not trust the author, it will make more placed be used to obtain access to acm\_acc, which contains all of ACM's money. Instead, it will pass a secondary sophia: Assertion empty account, acm\_aux, into which the author will pay her fee, and from which the ACM will(3) is a corollary of (2), and thus transfer the money back into the main acm\_acc. Assertion (3) is crucial, because it guarantees that actually even if the author were malicious, she could not use acm\_aux to obtain access to acm\_acc of we say that? Do we way the story just using (2)?

In summary, our necessary specifications are invariants that describe the behaviour of a module as observed from its clients. These invariants are (usually) independent of the concrete implementation

:6 author

Sophia: This is james' original

point, made a bit more concrete. Please check sense. Sophia: would be

nice iof we had a

Sophia: TODO add – code is available somewhere

Sophia: TDOD add - code is available somewhere

Sophia: I think this para is great not sure it belongs

policies are expressed as

Hoare triples

single method

class being specified (as in

policies are expressed as temporal or spatial invariants

conforms to the specification must maintain even though any other code may be

invocation on an instance of the

XXXXX), Rholistic

here. While traditional

Sophia: TO ADD - in fact, in section XXXwe show two very different implementations of the Bank/Account specification which also satisfy (1)-(3). Our invariants can talk about space, time and control, and thus go beyond class invariants, which can only talk about relations between the values of the fields state of the objects.

### Chainmail **OVERVIEW**

whether it makes In this Section we give a brief and informal overview of Chainmail— a full exposition appears in Section 5. As well as "classical" assertions about variables and the heap (e.g. a1.myBank =a2.myBank), Chainmail incorporates assertions about access, control, authority, space, and time.

> Example Configurations We will explain these concepts in terms of examples coming from Bank/Account as in the previous Section. We will use the runtime configurations  $\sigma_1$  and  $\sigma_2$ shown in the left and right diagrams in Figure 3. In both diagrams the rounded boxes depict objects: green for those from the Bank/Account module, and grey for the "external", "client" objects. The transparent green rectangle shows which objects Bank/Account module. The object at 1 is a Bank, those at 2, 3 and 4 are Accounts, and those at 91, 92, 93 and 94 are "client" objects which belong to classes different than those from the Bank/Account module.

> The configurations differ in the internal representation of the objects. Configuration  $\sigma_1$  may arise from execution using a module  $M_{BA1}$ , where Account objects of have a field myBank pointing to their Bank, and an integer field balance – the code can be found in xxx.. Configuration  $\sigma_2$  may arise from execution using a module  $M_{BA2}$ , where Accounts have a myBank field, Bank objects have a ledger implemented though a sequence of Nodes, each of which has a field pointing to the Account, a field balance, and a field next - the code can be found in yy...

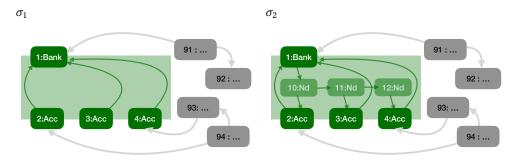


Fig. 3. Two runtime configurations for the Bank/Account example.

For the rest, assume variable identifiers  $b_1$ , and  $a_2-a_4$ , and  $u_{91}-u_{94}$  denoting objects 1, 2-4, and 91–94 respectively for both  $\sigma_1$  and  $\sigma_2$ . That is,  $\sigma_i(b_1)=1$ , and  $\sigma_i(a_2)=2$ ,  $\sigma_i(a_3)=3$ ,  $\sigma_i(a_4)=4$ , and  $\sigma_i(u_{91})=91$ ,  $\sigma_i(u_{92})=92$ ,  $\sigma_i(u_{93})=90$ ,  $\sigma_i(u_{94})=94$ , for i=1 or i=2.

Classical Assertions talk about the contents of the local variables (i.e. the topmost stack frame), and the fields of the various objects (*i.e.* the heap). For example, the assertion that a<sub>2</sub>.myBank=a<sub>3</sub>myBank, expresses that  $a_1$  and  $a_2$  have the same bank. In fact, this assertion is satisfied in both  $\sigma_1$  and  $\sigma_2$ , often describing a written formally as

..., 
$$\sigma_1 \models a_2$$
.myBank =  $a_3$ .myBank ...,  $\sigma_2 \models a_2$ .myBank =  $a_3$ .myBank

The term x:ClassId says that x is an object of class ClassId. For example

..., 
$$\sigma_1 \models a_2$$
.myBank =  $a_3$ .myBank.

Vol. 1, No. 1, Article . Publication date: March 2019. that a module that '

We support ghost fields, e.g.  $a_1$ . balance is a ghost field in  $\sigma_2$  since Accounts do not store a balance field. But its value can be defined so that for any a of class Account the value of a . balance is nd.balance such that nd is a Node, and nd.myAccount=a.

We also support the usual logical connectives, and so, we can express assertions such as

```
\foralla.[ a:Account \longrightarrow a.myBank:Bank \land a.balance \ge 0 ].
```

Sophia: All hell is loose here, as ghostfields require recursive defs, but I want to postpone these.

*Permission:* Access Our first holistic assertion,  $\mathcal{A}ccess\langle x,y\rangle$ , asserts that object x has a direct reference to another object y: either one of x's fields contains a reference to y, or the receiver of the currently executing method is x, and y is one of the arguments or a local variable. For example:

```
..., \sigma_1 \models \mathcal{A}ccess(a_2, b_1)
```

If  $\sigma_1$  was currently executing a call like  $a_2$ .deposit  $(a_2,100.00)$ , then we would have ...,  $\sigma_1 \models \mathcal{A}ccess(a_2,a_3)$ ,

Namely, during execution of that method,  $a_2$  has access to  $a_3$ , and could, if the method body chose to, store a reference to  $a_3$  in its own fields. Note that access is not symmetric, nor transitive:

```
..., \sigma_1 \not\models \mathcal{A}ccess\langle a_3, a_2 \rangle,

..., \sigma_2 \models \mathcal{A}ccess^*\langle a_2, a_3 \rangle,

..., \sigma_2 \not\models \mathcal{A}ccess\langle a_2, a_3 \rangle.
```

Sophia: ALL: does this clarify why we define access to take method execution into account?

that is a nice

Control: Calls The assertion Calls(x, y, m, zs) holds in program states where a method on objectsophia: it said " is x makes a method call y.m(zs) — that is it calls method m with object y as the receiver, and with control flow arguments zs. For example,

analogue of the access assertion" - access assertion"

```
..., \sigma_0 \models Calls(x, a_2, deposit, (a_3, 100.00)).
```

means that the receiver in  $\sigma_0$  is x, and the next statement to be executed is a<sub>2</sub>.deposit (a<sub>3</sub>, 100.00)  $_{\text{tree}}^{\text{simulation}}$ 

Authority – Changes and Internal/External The assertion Change(e) holds when the value of e insophia: Is it good the next configuration is different to the value in the current configuration. For example, if the code to put these being executed in  $\sigma_1$  started with a<sub>2</sub>.balance = a<sub>2</sub>.balance + 100.00, then:

```
..., \sigma_1 \models Change\langle a_2.balance \rangle.
```

Moreover, the assertion  $\mathcal{E}xternal(e)$  expresses that the object e does not belong to the module under consideration. For example,

```
M_{AB2}; ..., \sigma_2 \models External\langle u_{92} \rangle

M_{AB2}; ..., \sigma_2 \not\models External\langle a_2 \rangle

M_{AB2}; ..., \sigma_2 \not\models External\langle b_1.ledger \rangle
```

Notice the use of the *internal* module,  $M_{AB2}$ , needed to judge which objects are internal, and which are external.

Space: With The space assertion With(S, A) states that assertion A is true in a configuration is restricted to the objects from the set S. In other words, it restricts the set of objects which may be used to establish property A. For example, if  $S_1$  includes object 94, and  $S_2$  does not include it, then we have

```
..., \sigma_1 \models With\langle S_1, \exists o.[External\langle o \rangle \land Access\langle o, a_4 \rangle] \rangle
..., \sigma_1 \not\models With\langle S_2, \exists o.[External\langle o \rangle \land Access\langle o, a_4 \rangle] \rangle.
```

 $With\langle S, A \rangle$  is therefore *not* the footprint of the assertion A; it is more like the *fuel* given to establish sophia: TODO that assertion. Note that  $With\langle S, A \rangle$  does not imply  $With\langle S \cup S', A \rangle$ , nor the other direction. Anal's fuel

*Time: Next, Will, Prev, Was* We supports several temporal operators familiar from temporal logic  $(Next\langle A \rangle, \text{ and } Will\langle A \rangle, \text{ and } Prev\langle A \rangle, \text{ and } Was\langle A \rangle)$  to talk about the future or the past in one or any number of steps. The assertion  $Will\langle A \rangle$  expresses that after one or more execution steps A will hold. For example, if the code being executed in  $\sigma_2$  was method m() with receiver  $u_{94}$ , and

Sophia: TODO citation

:8 author

if  $\sigma_2(94, f_1) = 2$  and  $\sigma_2(94, f_2) = 93$ , and calling m2 on 93 returns 4, and the body of m was this. $f_1$ .deposit (this. $f_2$ .m2(),4.00),then

```
M_{BA2}; ..., \sigma_2 \models Will\langle Change\langle a_2.balance \rangle \rangle.
```

Putting these together We now look at some composite assertions which use ingredients from several families from above. The assertion below says that if the call to be made next is u<sub>94</sub>.m(), then the balance of a<sub>2</sub> will eventually change:

```
M_{BA2} \ ^{\circ}_{2} ..., \sigma_{2} \models Calls \langle ..., u_{94}, m, () \rangle \longrightarrow Will \langle Change \langle a_{2}.balance \rangle \rangle.
```

We now add space to the mix, and demonstrate that in general Will(With(S, A)) is different from With  $\langle S, Will(A) \rangle$ . Consider  $S_1$  consisting of objects 1, 2, 4, 93, and 94, and  $S_2$  consisting of objects 1, 2, 4. Assume also that  $\sigma_1$  contained the call m() with receiver  $u_{94}$ , that the code of m and m2 were as above. Then

```
M_{BA1}, ..., \sigma_1 \models With(S_1, Will(Change(a_2.balance)))
M_{BA1}; ..., \sigma_1 \not\models With(S_2, Will(Change(a_2.balance)))
M_{BA1}, ..., \sigma_1 \models Will(With(S_2, Change(a_2.balance)))
```

with  $\sigma_2$  as used in In summary, our holistic assertions draw from some concepts from object capabilities ( $\mathcal{A}ccess\langle\_,\_\rangle$ where we already for permission and Change $\langle \rangle$  for authority) as well as temporal logic (Will $\langle A \rangle$ , Was $\langle A \rangle$  and assume a mat the code in  $\sigma_2$  started friends), and the relation of our spatial connective (With(S, A)) with ownership and effect systems.

#### **OVERVIEW OF THE Chainmail FORMAL MODEL**

Having outlined the ingredients of our holistic specification language, the next question to ask is: power and novelty When does a module M satisfy such a holistic assertion A? Note that we use the term module to talk about repositories of code; in this work modules are mappings from class identifiers to class definitions. So, the question about modules satisfying assertions put formally is, when does

$$M \models A$$

hold?

Our answer has to reflect the fact that we are dealing with the *open world*, where M, our module, may be linked with arbitrary untrusted code. To reflect this we consider pairs of modules, M & M', where M is the module whose code is supposed to satisfy the assertion, and M' is another module which exercises the functionality of M. We call M the *internal*, and M' is the *external* module.

We can now answer our original question:  $M \models A$  holds if for all further, potentially adversarial, modules M' and in all runtime configurations  $\sigma$  which may be observed through execution of the code of M combined with that of M', the assertion A is satisfied. More formally, we define:

$$M \models A$$
 if  $\forall M'. \forall \sigma \in \mathcal{A}rising(M \ \ M'). [M \ \ M', \sigma \models A].$ 

somewhere, should In that sense, module M' represents all possible clients of M; and as it is arbitrarily chosen, it reflects the open world nature of our specifications.

> The judgement M  $\S$  M',  $\sigma \models A$  means that assertion A is satisfied by M  $\S$  M' and  $\sigma$ . As in traditional specification languages [??], satisfaction is judged in the context of runtime configuration  $\sigma$ ; but in addition, it is judged in the context of modules. The reason for this is that assertions may talk about possible future configurations. To determine the possible future configurations we need the class definitions – these are found in the modules.

> Note the distinction between the internal and the external module. The reason for this distinction is some assertions require object to be external, and also, because we model progrm execution as if all executions within a modue were atomic. We only record runtime configurations which are external to module M, i.e. those where the executing object (i.e. the current receiver) comes from module M'.

be nice to have a simpler example, what makes it difficult is the fact that MAB2-internal transitions are not

registered.

Sophia: It would

Sophia: The observer pattern example is very unfortunately cannot use it, because the calls are internal, and therefore not visible in the

current system.

Sophia: some delicate issues prev. paragraph, assumed that the with u94.m () what can we do? Sophia: While

many individual features of Chainmail can 4 be found also in other work, we argue that their for specifying open systems lies in their careful combination James: Hmm. a

Sophia: TODO: add references

here

James: don't forget the whole AOPmonitoring/specs stuff, just for fun (HELM contracts!!! (vs

Meyer Contracts James: we say something like: the goal is to

specifations with possible over a basic Hoare language

Sophia: Is is

sentence

superfluous now? Sophia: In contrast to what we said on Friday's conf call we do not need to put any

restrictions on M' -, Vol. 1, No. 1, Article . Publication date: March 2019.

required. Sophia: TODO

disjointness is

Thus, program execution is a judgment of the form

$$M \otimes M', \sigma \leadsto \sigma'$$

we ignore all intermediate steps whose receivers are internal to M. Thus, our executions correspond to some form of visible states semantics. Similarly, when considering  $\mathcal{A}rising(M \ ^{\circ}, M')$ , *i.e.* the sophia: TODO: configurations arising from executions in  $M \ ^{\circ}, M'$ , we can take method bodies defined in M or in M', but here. we will only consider the runtime configurations which are external to M.

As a notational convenience, we keep the code to be executed as a component of the runtime configuration. Thus,  $\sigma$  consists of a stack of frames and a heap, and each frame consists of a variable map and a continuation. The variable map is a mapping from variables to addresses or to set of addresses – the latter are needed to deal with assertions which quantify over footprints, as e.g. (1) and (2) from section 2.

To give meaning to assertions with footprint restrictions such as e.g.  $With\langle S, A \rangle$ , we define restrictions on the configuration. Thus  $\sigma \downarrow_{\sigma(S)}$  is the same as  $\sigma$  but with the domain of the heap restricted to the addresses from  $\sigma(S)$ . And then we define

$$M ; M', \sigma \models With(S, A)$$
 if  $M ; M', \sigma \downarrow_{\sigma(S)} \models A$ 

The meaning of assertions therefore may depend on the variable map, eg  $\times$  may be pointing to a different object in .... TODO The treatment of time in combination with the fact that the meaning od assertions TODO

#### 5 ASSERTIONS

We now define the syntax of expressions and assertions.

## 5.1 Syntax of Assertions

DEFINITION 1 (ASSERTIONS). The syntax of expressions (e) and assertions (A) is:

```
e ::= true | false | null | x | e.f

A ::= e | e = e | e : ClassId | e \in S |
A \to A | A \land A | A \lor A | \neg A | \forall x.A | \forall S : SET.A | \exists x.A | \exists S : SET.A |
External\langle x \rangle | \mathcal{A}ccess\langle x,y \rangle | Change\langle e \rangle | Calls\langle x,y,m,zS \rangle |
Next\langle A \rangle | \mathcal{W}ill\langle A \rangle | \mathcal{P}rev\langle A \rangle | \mathcal{W}as\langle A \rangle
```

As we discussed in section TODO validity of assertions has the format  $M \ ^\circ_9 M'$ ,  $\sigma \models A$ , where M is the internal module, whose internal workings are opaque to the external, client module M'. We break the definition into four parts: In definition 3 we define validity of basic assertions which reflect over the contents of the frame or the heap. In definition 4 we define validity of basic assertions which reflect over the contents of the frame or the heap.

#### 5.2 Satisfaction of Assertions - standard

DEFINITION 2 (INTERPRETATIONS FOR SIMPLE EXPRESSIONS). For any runtime configuration,  $\sigma$ , and any  $k \in \mathbb{N}$ , and any simple expression,  $\varepsilon$ , we define its interpretation as follows:

- [true] $_{\sigma} \triangleq$  true, and [false] $_{\sigma} \triangleq$  false, and [null] $_{\sigma} \triangleq$  null
- $[x]_{\sigma} \triangleq \phi(x)$  if  $\sigma = (\phi \cdot \_, \_)$
- $[e.f]_{\sigma} \triangleq \chi([e]_{\sigma}, f)$  if  $\sigma = (-, \chi)$

<sup>&</sup>lt;sup>1</sup>Note that the operators  $\land$ ,  $\lor$ ,  $\neg$  and  $\forall$  could have been defined through the usual shorthands, *e.g.*,  $\neg A$  is short for  $A \rightarrow \texttt{false}$  *etc.*, but here we give full definitions instead.SD: Perhaps we should just do that, it make the defs implicit

:10 author

LEMMA 5.1 (INTERPRETATION CORRESPONDS TO EXECUTION). For any simple expression e, module M, runtime configuration  $\sigma$ , and value v:

•  $[e]_{\sigma} = v \text{ if and only if } M, \sigma[\text{contn} \mapsto e] \rightsquigarrow v.$ 

PROOF. by structural induction over the definition of e.

DEFINITION 3 (BASIC ASSERTIONS). We define when a configuration satisfies basic assertions, consisting of expressions.

- $M ; M', \sigma \models e \quad if \quad [e]_{\sigma} = true.$
- $M ; M', \sigma \models e = e' \quad if \quad [e]_{\sigma} = [e']_{\sigma}.$
- $M \, \mathrm{\r{G}} \, \mathrm{M}', \sigma \models \mathrm{e} : \mathrm{ClassId}$  if  $\mathrm{Class}([\mathrm{e}]_{\sigma})_{\sigma} = \mathrm{ClassId}$ .
- $M ; M', \sigma \models e \in S$  if  $[e]_{\sigma} \in [S]_{\sigma}$ .

We now define satisfaction of assertions which involve logical connectives and existential or universal quantifiers.

DEFINITION 4 (ASSERTIONS WITH LOGICAL CONNECTIVES AND QUANTIFIES). We now consider For modules M, M', assertions A, A', variables x and S, configuration  $\sigma$ , we define:

- $M : M', \sigma \models \exists x.A \quad if \quad M : M', \sigma[z \mapsto \alpha] \models A[x/z]$ 
  - for some  $\alpha \in dom(\sigma)$ , and z free in  $\sigma$  and A.

•  $M ; M', \sigma \models \forall S : SET.A \quad if \quad M ; M', \sigma[Q \mapsto R] \models A[S/Q]$ 

for all sets of addresses  $R \subseteq dom(\sigma)$ , and all Q free in  $\sigma$  and A.

- M ; M',  $\sigma \models \exists S : SET. A$  if M ; M',  $\sigma[Q \mapsto R] \models A[S/Q]$  for some set of addresses  $R \subseteq dom(\sigma)$ , and Q free in  $\sigma$  and A.
- $M \otimes M', \sigma \models \forall x.A$  if  $\sigma[z \mapsto \alpha] \models A[x/z]$  for all  $\alpha \in dom(\sigma)$ , and some z free in  $\sigma$  and A.
- $\bullet \ \ \texttt{M}\ \ \mathring{\texttt{S}}\ \texttt{M}', \sigma \models A \to A' \quad \ \ \textit{if} \quad \ \ \texttt{M}\ \ \mathring{\texttt{S}}\ \texttt{M}', \sigma \models A \ \textit{implies}\ \ \texttt{M}\ \ \mathring{\texttt{S}}\ \ \texttt{M}', \sigma \models A'$
- $M \circ M', \sigma \models A \wedge A'$  if  $M \circ M', \sigma \models A$  and  $M \circ M', \sigma \models A'$ .
- $M \circ M', \sigma \models A \vee A'$  if  $M \circ M', \sigma \models A \text{ or } M \circ M', \sigma \models A'$ .
- $M \stackrel{\circ}{,} M', \sigma \models \neg A$  if  $M \stackrel{\circ}{,} M', \sigma \models A$  does not hold.

# 5.3 Satisfaction of Assertions - Space

And now, we consider the assertions which involve space and control:

DEFINITION 5 (SATISFACTION OF ASSERTIONS ABOUT SPACE-1). For any modules M, M', assertions A, A', variables x and x, we define

- M  $^{\circ}$  M',  $\sigma \models \mathcal{A}ccess(x, y)$  if
  - $[x]_{\sigma} = [y]_{\sigma}$ , or
  - $\lfloor x.f \rfloor_{\sigma} = \lfloor y \rfloor_{\sigma}$  for some field f, or
  - $[x]_{\sigma}$ = $[this]_{\sigma}$  and  $[y]_{\sigma}$ = $[z]_{\sigma}$ , and z appears in  $\sigma$ .contn.
- M  $\circ$  M',  $\sigma \models Calls(x, y, m, zs)$  if  $\sigma.contn=u.m(v)$ ; for some variables u and v, and

```
[\text{this}]_{\sigma} = [x]_{\sigma}, and [y]_{\sigma} = [u]_{\sigma}, and [z]_{\sigma} = [v]_{\sigma}.
```

- $M : M', \sigma \models With(S, A)$  if  $M : M', \sigma \downarrow_S \models A$ .
- $M \stackrel{\circ}{,} M', \sigma \models \mathcal{E}xternal(e)$  if  $Class([e]_{\sigma})_{\sigma} \notin dom(M)$

 $\mathcal{A}ccess\langle x, y \rangle$  expresses that x has a *direct* path to y. It says that in the current frame, either xand y are aliases, or xpoints to an object which has a field whose value is the same as that of y, or x is the currently executing object and y is a local variable or formal parameter z which appears in the code in the continuation ( $\sigma$ .contn). The latter requirement ensures that that variables which were

introduced into the variable map in order to give meaning to existentially quantified assertions are not considered.

On the other hand, an assertion of the form With(S, A) promises that A holds in subconfiguration, whose heap is restricted to the objects from S.

DEFINITION 6 (RESTRICTION OF RUNTIME CONFIGURATIONS). The restriction operator  $\downarrow$  applied to a runtime configuration  $\sigma$  and a set R is defined as follows:

• 
$$\sigma \downarrow_S \triangleq (\psi, \chi')$$
, if  $\sigma = (\psi, \chi)$ , and  $dom(\chi') = \lfloor S \rfloor_{\sigma}$ , and  $\forall \alpha \in dom(\chi') \cdot \chi(\alpha) = \chi'(\alpha) \blacksquare^2$ 

DEFINITION 7 (SATISFACTION OF ASSERTIONS ABOUT SPACE-2). For any modules M, M', assertion A, set variable S, and configuration  $\sigma$ , we define

• 
$$M ; M', \sigma \models With(S, A)$$
 if  $M ; M', \sigma \downarrow_S \models A$ .

Perhaps With(S, A) is the most intriguing of our holistic assertions. It allows us to restrict the set of objects that are considered when ...

### 5.4 Satisfaction of Assertions - Time

Finally, we consider assertions involving time. To do this, we need an auxiliary concept:  $\triangleleft$  the adaptation of a runtime configuration to the scope of another one. This operator is needed to the changes of scope during execution. For example, the assertion Will(x.f = 3) is satisfied in the current configuration if in some future configuration the field f of the object that is pointed at by f in the current configuration has the value f. Note that in the future configuration, f may be pointing to a different object, or may even no longer be in scope (e.g. if a nested call is executed). Therefore, we introduce the operator f which combines runtime configurations: f and f dataset the second configuration to the top frame's view of the former: it returns a new configuration whose stack has the top frame as taken from f and where the contin has been consistently renamed, while the heap is taken from f. This allows us to interpret expressions in the newer (or older) configuration f but with the variables bound according to the top frame from f; e.g. we can obtain that value of f in configuration f even if f was out of scope. The consistent renaming of the code allows the correct modelling of execution (as needed, for the semantics of nested time assertions, as e.g. in f will f and f in the configuration f is a configuration, as e.g. in f in the configuration f is a configuration of f in the configuration f in the configuration f is a configuration of f in the configuration f in the configuration f is a configuration f in the configuration f

Definition 8 (Adaptation of Runtime Configurations). For runtime configurations  $\sigma$ ,  $\sigma'$ .:

```
• \sigma \triangleleft \sigma' \triangleq (\phi'' \cdot \psi', \chi') if \sigma = (\phi \cdot \_, \_), and \sigma' = (\phi' \cdot \psi', \chi'), and \phi = (\text{contn}, \beta), and \phi' = (\text{contn'}, \beta'), and \phi'' = (\text{contn'}[\text{zs/zs'}], \beta[\text{zs'} \mapsto \beta'(\text{zs})]), where \text{zs} = dom(\beta), and \text{zs'} is a set of variables with the same cardinality as zs, and all variables in zs' are fresh in \beta and in \beta'.
```

That is, in the new frame  $\phi''$  from above, we keep the same continuation as from  $\sigma'$  but rename all variables with fresh names prgzs', and in the variable map we comnine that from  $\sigma$  and  $\sigma'$  but avoid names clashes through the renaming  $[zs' \mapsto \beta'(zs)]$ . With this auxiliary definition, we can now define satisfaction of assertions with involve time:

DEFINITION 9 (ASSERTIONS OVER TIME). For any modules M, M', assertions A, A', variables X and X, we define

<sup>&</sup>lt;sup>2</sup>SD: I had written instead  $[Class(\alpha)_{\chi'} = Class(\alpha)_{\chi} \land \forall f. \chi'(\alpha, f) = \chi(\alpha, f)]$ , but I do not see why

:12 author

```
• M \circ M', \sigma \models Change(e) if \exists \sigma'. [M \circ M', \sigma \leadsto \sigma' \land [e]_{\sigma} \neq [e]_{\sigma \neq \sigma'}].

• M \circ M', \sigma \models Next(A) if \exists \sigma'. [M \circ M', \phi \leadsto \sigma' \land M \circ M', \sigma \triangleleft \sigma' \models A],

and where \phi is so that \sigma = (\phi \cdot \_, \_).

• M \circ M', \sigma \models Will(A) if \exists \sigma'. [M \circ M', \phi \leadsto^* \sigma' \land M \circ M', \sigma \triangleleft \sigma' \models A],

and where \phi is so that \sigma = (\phi \cdot \_, \_).

• M \circ M', \sigma \models Prev(A) if \forall \sigma_1, \sigma_2. [Initial(\sigma_1) \land M \circ M', \sigma \leadsto^* \sigma_2 \land M \circ M', \sigma_2 \leadsto \sigma

\longrightarrow M \circ M', \sigma \models Was(A) if \forall \sigma_1, ..., \sigma_n. [Initial(\sigma_1) \land \sigma_n = \sigma \land \forall i \in [1...n). M \circ M', \sigma_i \leadsto \sigma_{i+1}

\longrightarrow \exists j \in [1...n-1). M \circ M', \sigma \triangleleft \sigma_j \models A]^4
```

Thus,  $M \circ M'$ ,  $\sigma \models Will(A)$  holds if A holds in some configuration  $\sigma'$  which arises from execution of  $\phi$ , where  $\phi$  is the top frame of  $\sigma$ . By requiring that  $\phi \leadsto^* \sigma'$  rather than  $\sigma \leadsto^* \sigma'$  we are restricting the set of possible future configurations to just those that are caused by the top frame. Namely, we do not want to also consider the effect of enclosing function calls. This allows us to write more natural specifications when giving necessary conditions for some future effect.

### 5.5 Entailment and Equivalence

We define equivalence of assertions in the usual sense: two assertions are equivalent if they are satisfied in the context of the same configurations. Similarly, an assertion entails another assertion, iff all configurations which satisfy the former also satisfy the latter.

DEFINITION 10 (EQUIVALENCE AND ENTAILMENTS OF ASSERTIONS).

- $A \equiv A'$  if  $\forall \sigma. \forall M, M'$ . [  $M \otimes M', \sigma \models A$  if and only if  $M \otimes M', \sigma \models A'$ ].
- $A \subseteq A'$  if  $\forall \sigma. \forall M, M'$ . [  $M \otimes M', \sigma \models A$  implies  $M \otimes M', \sigma \models A'$  ].

LEMMA 5.2 (ASSERTIONS ARE CLASSICAL-1). For all runtime configurations  $\sigma$ , assertions A and A', and modules M and M', we have

```
(1) M \circ M', \sigma \models A \text{ or } M \circ M', \sigma \models \neg A
```

- (2)  $M \stackrel{\circ}{,} M', \sigma \models A \land A'$  if and only if  $M \stackrel{\circ}{,} M', \sigma \models A$  and  $M \stackrel{\circ}{,} M', \sigma \models A'$
- (3)  $M \circ M', \sigma \models A \vee A'$  if and only if  $M \circ M', \sigma \models A \text{ or } \sigma \models A'$
- (4)  $M \circ M', \sigma \models A \land \neg A \text{ never holds.}$
- (5)  $M \circ M', \sigma \models A \text{ and } M \circ M', \sigma \models A \rightarrow A' \text{ implies } M \circ M', \sigma \models A'.$

PROOF. By application of the corresponding definitions from ??.

LEMMA 5.3 (ASSERTIONS ARE CLASSICAL-2). For assertions A, A', and A'' the following equivalences hold

```
(1) A \wedge \neg A \equiv \text{false}
```

(2) 
$$A \lor \neg A \equiv \text{true}$$

(3) 
$$A \wedge A' \equiv A' \wedge A$$

$$(4) A \vee A' \equiv A' \vee A$$

$$(5) (A \lor A') \lor A'' \equiv A \lor (A' \lor A'')$$

(6) 
$$(A \lor A') \land A'' \equiv (A \land A') \lor (A \land A'')$$

$$(7) (A \wedge A') \vee A'' \equiv (A \vee A') \wedge (A \vee A'')$$

$$(8) \neg (A \land A') \equiv \neg A \lor \neg A''$$

$$(9) \neg (A \lor A') \equiv \neg A \land \neg A''$$

<sup>&</sup>lt;sup>3</sup>past includes the present, perhaps change this

<sup>&</sup>lt;sup>4</sup>past includes the present, perhaps change this

П

```
 \begin{array}{lll} (10) \ \neg (\exists x.A) & \equiv \ \forall x.(\neg A) \\ (11) \ \neg (\exists k: \mathbb{N}.A) & \equiv \ \forall k: \mathbb{N}.(\neg A) \\ (12) \ \neg (\exists fs: FLD^k.A) & \equiv \ \forall fs: FLD^k.(\neg A) \\ (13) \ \neg (\forall x.A) & \equiv \ \exists x.\neg(A) \\ (14) \ \neg (\forall k: \mathbb{N}.A) & \equiv \ \exists k: \mathbb{N}.\neg(A) \\ (15) \ \neg (\forall fs: FLD^k.A) & \equiv \ \exists fs: FLD^k.\neg(A) \\ \end{array}
```

PROOF. All points follow by application of the corresponding definitions from ??.

Notice that satisfaction is not preserved with growing configurations; for example, the assertion  $\forall x.[x: \texttt{Purse} \rightarrow x.\texttt{balance} > 100]$  may hold in a smaller configuration, but not hold in an extended configuration. Nor is it preserved with configurations getting smaller; consider  $e.g. \exists x.[x: \texttt{Purse} \land x.\texttt{balance} > 100]$ .

Finally, we define satisfaction of assertions by modules: A module M satisfies an assertion A if for all modules M', in all configurations arising from executions of M  $^{\circ}_{9}$  M', the assertion A holds.

DEFINITION 11. For any module M, and assertion A, we define:

•  $M \models A$  if  $\forall M' . \forall \sigma \in \mathcal{R}rising(M \ \ M') . M \ \ M', \sigma \models A$ 

### 6 ANOTHER EXAMPLE - ATTENUATING THE DOM

Attenuation is ability to provide an untrusted client restricted access to an object's functionality. This section now needs is usually achieved through the introduction of an intermediate object. Such intermediate objects — it has moved to protection proxies [?] — are a common design pattern, and their security properties and have been studied at length in the object capabilities literature [??], and Devrise et. al. proposed specifications

protection proxies [?] — are a common design pattern, and their security properties and have been studied at length in the object capabilities literature [??], and Devrise et. al. proposed specifications for attenuation for the DOM [?].

In this section we revisit that example, and use it to motivate the need for holistic specifications,

In this section we revisit that example, and use it to motivate the need for holistic specifications, and to give an informal introduction to our for holistic language Chainmail II. We also argue that compared with Devrise et al., our specifications xxxx.

Sophia: TO

This example deals with a tree of DOM nodes. Access to a DOM node gives access to all its complete parent and children nodes, and the ability to modify the properties of any accessible node. As the top nodes of the tree usually contain privileged information (such as web content showing your banking details), while the lower nodes contain less crucial information (such as advertisements for BREXIT), we want to be able to limit access given to third parties to only the lower part of the DOM tree, (so that Jacob Rees-Mogg cannot access your bank account). We do this via attenuation through a Wrapper, which has a field node pointing to a Node, and a field height which restricts the range of Nodes which may be modified through the use of the particular Wrapper. Namely, when you hold a Wrapper you can modify the property of all the descendants of the height-th ancestors of the node of that particular Wrapper. It is not difficult to write such a Wrapper; a possible implementation appears in Figure ?? in appendix ??.

Figure 4 shows Wrapper objects attenuating the use of Nodes. The function usingWrappers has as parameter an object of unknown provenance, here called unknwn. On lines 2-7 we create a tree consisting of nodes n1, n2, ... n6, depicted as blue circles on the right-hand-side of the Figure. On line 8 we create a wrapper of n5 with height 1. This means that the wrapper w may be used to modify n3, n5 and n6 (*i.e.* the objects in the green triangle), while it cannot be used to modify n1, n2, and 4 (*i.e.* the objects within the blue triangle). On line 8 we call a function named untrusted on the unknown object, and pass w as argument.

Even though we know nothing about the unknown object or its untrusted function, and even though the call gives to unknown access to w, which in turn has transitively access to all Node-s

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```
func usingWrappers(unknwn) {
   n1=Node(null, "fixed");
   n2=Node(n1, "robust");
   n3=Node(n2, "volatile");
   n4=Node(n2, "const");
   n5=Node(n3, "variable");
   n6=Node(n3, "ethereal");
   w=Wrapper(n5,1);

unknwn.untrusted(w);

assert n2.property=="robust"
...
}
```

Fig. 4. Wrappers protecting Nodes

in the tree, we know that the untrusted function is guaranteed not to line 10 will not affect the property fields of the nodes n1, n2, and n4. Thus, the assertion on line 12 is guaranteed to succeed. The question is how do we specify Wrapper, so as to be able to make such an argument.

A specification of the class Wrapper in the traditional style, e.g. [?] (c.f. appendix ??) consists of pairs of pre- and post- conditions for each of the functions of that class. Each such pair gives a sufficient condition for some effect to take place: for example the call w.setProperty(i,prp) where i is smaller than w.height is a sufficient condition to modify property of the i-th parent of w.node. But we do not know what other ways there may be to modify a node's property. A broken wrapper could accidently permit access to nodes one or two levels about the expected height due to off-by one errors. More seriously, a malicious wrapper could offer a back-door public accessor method that leaks the underlying DOM object through the wrapper, return direct access to any of the other nodes in the DOM, or even to queue a task to delete every property at midnight GMT on 29 March 2019. All of these errors are possible while preserving the pre- and post- conditions expected of a Wrapper. What is needed here is some way to specify the necessary conditions under which some change could be made: if some external client is to change a node's property, then that client must have either direct access to a node in that DOM tree, or indirect access via a wrapper configured so that it can change the affected node. Thus,

The necessary condition for the modification of nd.property for some nd of class Node is either access to some Node in the same tree, or access to a w of class Wrapper where the w.height-th parent of w is an ancestor of nd.

With such a specification we can prove that the assertion on line 12 will succeed. Crucially, we can ensure that all future updates of the Wrapper class must continue to meet that specification, guaranteeing the protection of the Node data. To give a flavour of *Chainmail*, we use it express the requirement from above:

say the following, or does it break the flow? "Moreover, on line 10 we do not know which functions are called on w." KJX: I put that in and expanded on it. We need to explain the issues I think I do not see

where it is

, Vol. 1, No. 1, Article . Publication date: March 2019.

```
\exists w : Wrapper. \exists k : \mathbb{N}. (\mathcal{A}ccess(o, w) \land nd.parnt^k = w.node.parnt^w.height) ]]
```

That is, if the value of nd.property is modified ( $Change\langle\_\rangle$ ) at some future point ( $Will\langle\_\rangle$ ) and if reaching that future point involves no more objects than those from set S (i.e.  $With\langle$  S,  $\_\rangle$ ), then at least one (o) of the objects in S is not a Node nor a Wrapper, and o has direct access to some node ( $Access\langle o, nd'\rangle$ ), or to some wrapper w and the w.height-th parent of w is an ancestor of nd (that is, parnt  $^k=w.node.parnt^w.height$ ). Definitions of these concepts appear later (Definition ??), but note that our "access" is intransitive:  $Access\langle x,y\rangle$  holds if either x has a field pointing to y, or x is the receiver and y is one of the arguments in the executing method call.

In the next sections we proceed with a formal model of our model. In the appendix we discuss more – and simpler – examples. We chose the DOM for the introduction, in order to give a flavour of the *Chainmail* features.

#### 7 DISCUSSION

Necessary conditions vs the complement of the sufficient conditions? One might ask whether the necessary conditions are different from the complement of all the sufficient conditions. In other words, the possible behaviours of a module is the union of all possible behaviours of each individual function, and the necessary conditions is their complement, We described this in the left hand side of the diagram in Figure 1: we represent the space of all theoretically possible behaviours as points in the rectangle, each function is a coloured oval and its possible behaviours are the points in the area of that oval. Then, the necessary conditions are all the points outside the ovals.

This view is mathematically sound but it is impractical, brittle wrt software maintenance, and weak wrt reasoning in the open world.

It is impractical, because it suggests that when interested in a necessity guarantee one would need to read the specifications of all the functions in a module. In view of the number of these functions, and also the number of behaviours emerging from their combination, this can be a very large undertaking. What if the bank did indeed enforce that only the account owner may withdraw funds, but had another function which allowed the manager to appoint an account supervisor, and another which allowed the account supervisor to assign owners?

It is brittle wrt software maintenance, because it gives no guidance to the team maintaining a piece of software: if the necessary conditions which were implicitly in the developers' intentions are not explicitly described, subsequent developers may inadvertenty add functions which break these intentions.

It is weak wrt reasoning in the open world because if does not give any guarantees about objects' when these are passed as arguments to calls into unknown code. For example, what guarantees can we make about the top of the DOM tree when we pass to an unknown advertiser a wrapper pointing to lower parts of the tree.

*Design choices.* For our underlying language, we have chosen a class based language; we used classes, because we concentrate on class-based, object-oriented programming. But we believe that the ideas are also applicable to other kinds of languages.

#### **APPENDIX - EXAMPLES**



<sup>&</sup>lt;sup>5</sup>SD: Note that the file rest.tex contains more material.

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### A THE LANGUAGE $\mathcal{L}_{00}$

#### A.1 Modules and Classes

 $\mathcal{L}_{oo}$  programs are described through modules, which are repositories of code. Since we study class based oo languages, code is represented as classes, and modules are mappings from identifiers to class descriptions.

DEFINITION 12 (MODULES). We define Module as the set of mappings from identifiers to class descriptions (the latter defined in Definition 13):

```
Module \triangleq \{ M \mid M : Identifier \longrightarrow ClassDescr \}
```

Classes, as defined below, consist of field and method definitions. Note that  $\mathcal{L}_{oo}$  is untyped. Method bodies consist of sequences of statements; these can be field read or field assignments, object creation, method calls, and return statements. All else, *e.g.* booleans, conditionals, loops, can be encoded.

Note also that field read or write is only allowed if the target object is this – as, e.g., in Smalltalk – this is encapsulation: the syntax allows an object to read/write its own fields, but forbids it from reading/writing any other object's fields.

```
DEFINITION 13 (CLASSES). We define the syntax of class descriptions below. ClassDescr ::= class ClassId { (fieldf)* (method MethBody)* } MethBody ::= m(x*) { Stmts } Stmts ::= Stmt | Stmt; Stmts Stmt ::= this.f:= x | x:= this.f | x:= x.m(x*) | x:= new C(x^*) | return x x, f, m ::= Identifier
```

where we use metavariables as follows:  $x \in VarId \ f \in FldId \ m \in MethId \ C \in ClassId$ 

We define a method lookup function,  $\mathcal{M}$  which returns the corresponding method definition given a class C and a method identifier m.

DEFINITION 14 (LOOKUP). For a class identifier C and a method identifier m:

```
\mathcal{M}(\mathbb{M},\mathbb{C},\mathbb{m}) \triangleq \left\{ \begin{array}{l} \mathbb{m} \left( \, \mathbb{p}_1, ... \mathbb{p}_n \right) \left\{ \, \mathit{Stmts} \right\} \\ & \mathit{if} \, \mathbb{M}(\mathbb{C}) = \mathsf{class} \, \mathbb{C} \, \left\{ \, ... \mathsf{method} \, ... \, \mathbb{m} \left( \, \mathbb{p}_1, ... \mathbb{p}_n \right) \left\{ \, \mathit{Stmts} \right\} \, ... \, \right\} . \\ & \mathit{undefined}, \quad \mathit{otherwise}. \end{array} \right.
```

### A.2 The Operational Semantics of $\mathcal{L}_{\infty}$

We will now define execution of  $\mathcal{L}_{oo}$  code. We start by defining the runtime entities, and runtime configurations,  $\sigma$ , which consist of heaps and stacks of frames. The frames are pairs consisting of a continuation, and a mapping from identifiers to values. The continuation represents the code to be executed next, and the mapping gives meaning to the formal and local parameters.

DEFINITION 15 (RUNTIME ENTITIES). We define addresses, values, frames, stacks, heaps and runtime configurations.

- We take addresses to be an enumerable set, Addr, and use the identifier α ∈ Addr to indicate an address.
- Values, v, are either addresses, or sets of addresses or null:  $v \in \{\text{null}\} \cup \text{Addr} \cup \mathcal{P}(\text{Addr}).$
- Continuations are either statements (as defined in Definition 13) or a marker, x:= ●, for a nested call followed by statements to be executed once the call returns.

Continuation ::= Stmts |  $x := \bullet$ ; Stmts

- Frames,  $\phi$ , consist of a code stub and a mapping from identifiers to values:  $\phi \in CodeStub \times Ident \rightarrow Value$ ,
- Stacks,  $\psi$ , are sequences of frames,  $\psi := \phi \mid \phi \cdot \psi$ .
- Objects consist of a class identifier, and a partial mapping from field identifier to values:  $Object = ClassID \times (FieldId \rightarrow Value).$
- Heaps,  $\chi$ , are mappings from addresses to objects:  $\chi \in Addr \to Object$ .
- Runtime configurations,  $\sigma$ , are pairs of stacks and heaps,  $\sigma := (\psi, \chi)$ .

Note that values may be sets of addresses. Such values are never part of the execution of  $\mathcal{L}_{00}$ , but are used to give semantics to assertions – we shall see that in Definition ??.

Next, we define the interpretation of variables (x) and field look up (this.f) in the context of frames, heaps and runtime configurations; these interpretations are used to define the operational semantics and also the validity of assertions, later on in Definition ??:

DEFINITION 16 (INTERPRETATIONS). We first define lookup of fields and classes, where  $\alpha$  is an address, and f is a field identifier:

- $\chi(\alpha, f) \triangleq fldMap(\alpha, f)$  if  $\chi(\alpha) = (\_, fldMap)$ .
- $C lass(\alpha)_{\chi} \triangleq C \quad if \quad \chi(\alpha) = (C, \_)$

We now define interpretations as follows:

- $[x]_{\phi} \triangleq \phi(x)$
- [this.f] $_{(\phi,\chi)} \triangleq v$ , if  $\chi(\phi(\text{this})) = (\_,fldMap)$  and fldMap(f) = v

For ease of notation, we also use the shorthands below:

- $[x]_{(\phi \cdot \psi, \chi)} \triangleq [x]_{\phi}$
- $[\text{this.f}]_{(\phi,\psi,\chi)} \triangleq [\text{this.f}]_{(\phi,\chi)}$
- $Class(\alpha)_{(\psi, \gamma)} \triangleq Class(\alpha)_{\gamma}$

In the definition of the operational semantics of  $\mathcal{L}_{00}$  we use the following notations for lookup and updates of runtime entities:

DEFINITION 17 (LOOKUP AND UPDATE OF RUNTIME CONFIGURATIONS). We define convenient shorthands for looking up in runtime entities.

- Assuming that  $\phi$  is the tuple (stub, varMap), we use the notation  $\phi$ .contn to obtain stub.
- Assuming a value v, and that  $\phi$  is the tuple (stub, varMap), we define  $\phi$ [contn  $\mapsto$  stub'] for updating the stub, i.e. (stub', varMap). We use  $\phi[x \mapsto v]$  for updating the variable map, i.e. (stub,  $varMap[x \mapsto v]$ ).
- Assuming a heap  $\chi$ , a value v, and that  $\chi(\alpha) = (C, fieldMap)$ , we use  $\chi[\alpha, f \mapsto v]$  as a shorthand for updating the object, i.e.  $\chi[\alpha \mapsto (C, fieldMap[f \mapsto v]]$ .

Execution of a statement has the form M,  $\sigma \leadsto \sigma'$ , and is defined in figure 5.

DEFINITION 18 (EXECUTION). of one or more steps is defined as follows:

- The relation M,  $\sigma \rightsquigarrow \sigma'$ , it is defined in Figure 5.
- $\mathbb{M}$ ,  $\sigma \rightsquigarrow^* \sigma'$  holds, if a)  $\sigma = \sigma'$ , or b) there exists a  $\sigma''$  such that  $\mathbb{M}$ ,  $\sigma \rightsquigarrow^* \sigma''$  and  $\mathbb{M}$ ,  $\sigma'' \rightsquigarrow \sigma'$ .

# A.3 Definedness of execution, and extending configurations

Note that interpretations and executions need not always be defined. For example, in a configuration Toby: We defer the whose top frame does not contain x in its domain,  $[x]_{\phi}$  is undefined. We define the relation  $\sigma \sqsubseteq \sigma'$  definition of initial

configurations to Definition ?? later :18 author

methCall OS

```
\phi.contn = x:= x<sub>0</sub>.m(par<sub>1</sub>,...par<sub>n</sub>); Stmts
[x_0]_{\phi} = \alpha
\mathcal{M}(M, Class(\alpha)_{\gamma}, m) = m(par_1, \dots par_n) \{ Stmts_1 \}
\phi'' = (\operatorname{Stmts}_1, (\operatorname{this} \mapsto \alpha, \operatorname{par}_1 \mapsto [\operatorname{x}_1]_{\phi}, \dots \operatorname{par}_n \mapsto [\operatorname{x}_n]_{\phi}))
M, (\phi \cdot \psi, \chi) \sim (\phi'' \cdot \phi[\text{contn} \mapsto x := \bullet; \text{Stmts}] \cdot \psi, \chi)
                                                                                                      varAssgn OS
\phi.contn = x:= this.f; Stmts
\mathbb{M}, (\phi \cdot \psi, \chi) \sim (\phi[\text{contn} \mapsto \text{Stmts}, \mathbf{x} \mapsto [\text{this.f}]_{\phi, \chi}] \cdot \psi, \chi)
                                                                                                      fieldAssgn_OS
\phi.contn = this.f:=x; Stmts
 \stackrel{\text{\tiny f.}}{\text{\tiny M}}, (\phi \cdot \psi, \chi) \, \sim \, (\phi[\text{contn} \mapsto \text{Stmts}] \cdot \psi, \chi[[\text{this}]_{\phi}, f \mapsto [\text{x}]_{\phi, \chi}]) 
                                                                                                      objCreate_OS
\phi.contn = x:=new C(x<sub>1</sub>,...x<sub>n</sub>); Stmts
\alpha new in \chi
f_1, ... f_n are the fields declared in M(C)
\mathbb{M}, (\phi \cdot \psi, \chi) \sim (\phi[\mathsf{contn} \mapsto \mathsf{Stmts}, \mathsf{x} \mapsto \alpha] \cdot \psi, \chi[\alpha \mapsto (\mathsf{C}, \mathsf{f}_1 \mapsto \lfloor \mathsf{x}_1 \rfloor_{\phi}, ... \mathsf{f}_n \mapsto \lfloor \mathsf{x}_n \rfloor_{\phi})])
                                                                                                      return OS
\phi.contn = return x; Stmts or \phi.contn = return x
\phi'.contn = x':=•; Stmts'
\mathbb{M}, (\phi \cdot \phi' \cdot \psi, \chi) \sim (\phi'[\mathsf{contn} \mapsto \mathsf{Stmts'}, \mathsf{x'} \mapsto [\mathsf{x}]_{\phi}] \cdot \psi, \chi)
```

Fig. 5. Operational Semantics

to express that  $\sigma$  has more information than  $\sigma'$ , and then prove that more defined configurations preserve interpretations:

DEFINITION 19 (EXTENDING RUNTIME CONFIGURATIONS). The relation  $\sqsubseteq$  is defined on runtime configurations as follows. Take arbitrary configurations  $\sigma$ ,  $\sigma'$ ,  $\sigma''$ , frame  $\phi$ , stacks  $\psi$ ,  $\psi'$ , heap  $\chi$ , address  $\alpha$  free in  $\chi$ , value v and object o, and define  $\sigma \sqsubseteq \sigma'$  as the smallest relation such that:

- $\sigma \sqsubseteq \sigma$
- $(\phi[x \mapsto v] \cdot \psi, \chi) \sqsubseteq (\phi \cdot \psi, \chi)$
- $(\phi \cdot \psi \cdot \psi', \chi) \sqsubseteq (\phi \cdot \psi, \chi)$
- $(\phi, \chi[\alpha \mapsto o) \sqsubseteq (\phi \cdot \psi, \chi)$
- $\sigma' \sqsubseteq \sigma''$  and  $\sigma'' \sqsubseteq \sigma$  imply  $\sigma' \sqsubseteq \sigma$

LEMMA A.1 (PRESERVATION OF INTERPRETATIONS AND EXECUTIONS). If  $\sigma' \sqsubseteq \sigma$ , then

- If  $\lfloor x \rfloor_{\sigma}$  is defined, then  $\lfloor x \rfloor_{\sigma'} = \lfloor x \rfloor_{\sigma}$ .
- If [this.f] $_{\sigma}$  is defined, then [this.f] $_{\sigma'}$ =[this.f] $_{\sigma}$ .
- If  $C \operatorname{lass}(\alpha)_{\sigma}$  is defined, then  $C \operatorname{lass}(\alpha)_{\sigma'} = C \operatorname{lass}(\alpha)_{\sigma}$ .
- If  $M, \sigma \rightsquigarrow^* \sigma''$ , then there exists a  $\sigma''$ , so that  $M, \sigma' \rightsquigarrow^* \sigma'''$  and  $\sigma''' \sqsubseteq \sigma''$ .

### A.4 Module linking

When studying validity of assertions in the open world we are concerned with whether the module under consideration makes a certain guarantee when executed in conjunction with other modules. To answer this, we need the concept of linking other modules to the module under consideration. Linking, o, is an operation that takes two modules, and creates a module which corresponds to the union of the two. We place some conditions for module linking to be defined: We require that the two modules do not contain implementations for the same class identifiers,

DEFINITION 20 (MODULE LINKING). The linking operator  $\circ$ : Module  $\times$  Module  $\longrightarrow$  Module from 21 think what the is defined as follows:

$$M \circ M' \triangleq \begin{cases} M \circ_{aux} M', & if \ dom(M) \cap dom(M') = \emptyset \\ undefined & otherwise. \end{cases}$$
and where,

• For all C:  $(M \circ_{aux} M')(C) \triangleq M(C)$  if  $C \in dom(M)$ , and M'(C) otherwise.

The lemma below says that linking is associative and commutative, and preserves execution.

LEMMA A.2 (PROPERTIES OF LINKING). For any modules M, M' and M'', and runtime configura aux; any idea how tions  $\sigma$ , and  $\sigma'$  we have:

- $(M \circ M') \circ M'' = M \circ (M' \circ M'')$ .
- $M \circ M' = M' \circ M$ .
- M,  $\sigma \leadsto \sigma'$ , and MoM' is defined, implies MoM',  $\sigma \leadsto \sigma'$

### A.5 Module pairs and visible states semantics

A module M adheres to an invariant assertion A, if it satisfies A in all runtime configurations that can be reached through execution of the code of M when linked to that of any other module M', and which are *external* to M. We call external to M those configurations which are currently executing code which does not come from M. This allows the code in M to break the invariant internally and temporarily, provided that the invariant is observed across the states visible to the external client M'.

Therefore, we define execution in terms of an internal module M and an external module M', through the judgment M  $\S$  M',  $\sigma \leadsto \sigma'$ , which mandates that  $\sigma$  and  $\sigma'$  are external to M, and that there exists an execution which leads from  $\sigma$  to  $\sigma'$  which leads through intermediate configurations  $\sigma_2$ , ...  $\sigma_{n+1}$  which are all internal to M, and thus unobservable from the client. In a sense, we "pretend" that all calls to functions from M are executed atomically, even if they involve several intermediate, internal steps.

DEFINITION 21. Given runtime configurations  $\sigma$ ,  $\sigma'$ , and a module-pair  $M_{\theta}^{\alpha}M'$  we define execution where M is the internal, and M' is the external module as below:

- $M \ \ \ M', \sigma \leadsto \sigma'$  if there exist  $n \ge 2$  and runtime configurations  $\sigma_1, ... \sigma_n$ , such that
  - $-\sigma = \sigma_1$ , and  $\sigma_n = \sigma'$ .
  - $M \circ M'$ ,  $\sigma_i \rightsquigarrow \sigma'_{i+1}$ , for  $1 \le i \le n-1$
  - $Class([this]_{\sigma})_{\sigma} \notin dom(M)$ , and  $Class([this]_{\sigma'})_{\sigma'} \notin dom(M)$ ,
  - $Class([this]_{\sigma_i})_{\sigma_i} \in dom(M), for 2 \le i \le n-2$

In the definition above n is allowed to have the value 2. In this case the final bullet is trivial and there exists a direct, external transition from  $\sigma$  to  $\sigma'$ . Our definition is related to the concept of visible states semantics, but differs in that visible states semantics select the configurations at which an invariant is expected to hold, while we select the states which are considered for executions which are expected to satisfy an invariant. Our assertions can talk about several states (through the use

the aux come fragment calculus disjointedness is

neater Sophia: aux is defined in last line of Def. below. In the Frag Calculus the modules were not mappings, so we did not need something like

:20 author

of the  $Will\langle \rangle$  and  $Was\langle \rangle$  connectives), and thus, the intention of ignoring some intermediate configurations can only be achieved if we refine the concept of execution.

The following lemma states that linking external modules preserves execution

LEMMA A.3 (LINKING MODULES PRESERVES EXECUTION). For any modules M, M', and M'', whose domains are pairwise disjoint, and runtime configurations  $\sigma$ ,  $\sigma'$ ,

- $M \stackrel{\circ}{\circ} M', \sigma \rightsquigarrow \sigma' \text{ implies } M \stackrel{\circ}{\circ} (M' \circ M''), \sigma \rightsquigarrow \sigma'.$
- $M \stackrel{\circ}{\circ} M', \sigma \leadsto \sigma' \text{ implies } (M \circ M'') \stackrel{\circ}{\circ} M', \sigma \leadsto \sigma'.$

PROOF. For the second guarantee we use the fact that  $M \ ^\circ M', \sigma \leadsto \sigma'$  implies that all intermediate configurations are internal to M and thus also to  $M \circ M''$ .

We can now answer the question as to which runtime configurations are pertinent when judging a module's adherence to an assertion. First, where does execution start? We define *initial* configurations to be those which may contain arbitrary code stubs, but which contain no objects. Objects will be created, and further methods will be called through execution of the code in  $\phi$ .contn. From such initial configurations, executions of code from M  $\,^\circ_1$ M' creates a set of *arising* configurations, which, as we will see in Definition 11, are pertinent when judging M's adherence to assertions.

DEFINITION 22 (INITIAL AND ARISING CONFIGURATIONS). are defined as follows:

- Initial $\langle (\psi, \chi) \rangle$ , if  $\psi$  consists of a single frame  $\phi$  with  $dom(\phi) = \{ \text{this} \}$ , and  $| \text{this} |_{\phi} = \text{null}$ , and  $dom(\chi) = \emptyset$ .
- $\mathcal{A}rising(\mathbb{M}; \mathbb{M}') = \{ \sigma \mid \exists \sigma_0. [Initial(\sigma_0) \land \mathbb{M}; \mathbb{M}', \sigma_0 \leadsto^* \sigma ] \}$

<sup>&</sup>lt;sup>6</sup>Explain better? Use the term "atomic"?