

## Part 1: Algorithm Description

I based my algorithm on Nesterov's momentum approach and made 3 important modifications:

1. Adding a threshold and normalization term, where if the next step (calculated with the following logic:

```
If norm(v) > threshold
    v = v / norm(v)
```

```
End
```

Where v is the momentum/velocity term

This addition to the algorithm prevented divergence/instability on simple1, when the gradient (and consequently the step size for this gradient-descent method) was too large

2. I used a learning rate that decreased with step count rather than a constant learning rate. This is often used in proofs to guarantee convergence, and here it added some stability that prevented continuous oscillations in flatter regions of the cost landscape.

This decreasing learning rate, alpha, was calculated using:

```
tmp_vec = xi_vec + beta*v;
v = beta*v - (alpha^i)*g(tmp_vec); #adjusted Nestov's alg. to incorporate
```

decreasing learning rate

```
normThresh = 1;
if norm(v) > normThresh
    v = v / norm(v)
```

```
end
```

```
xpi_vec = xi_vec + v;
```

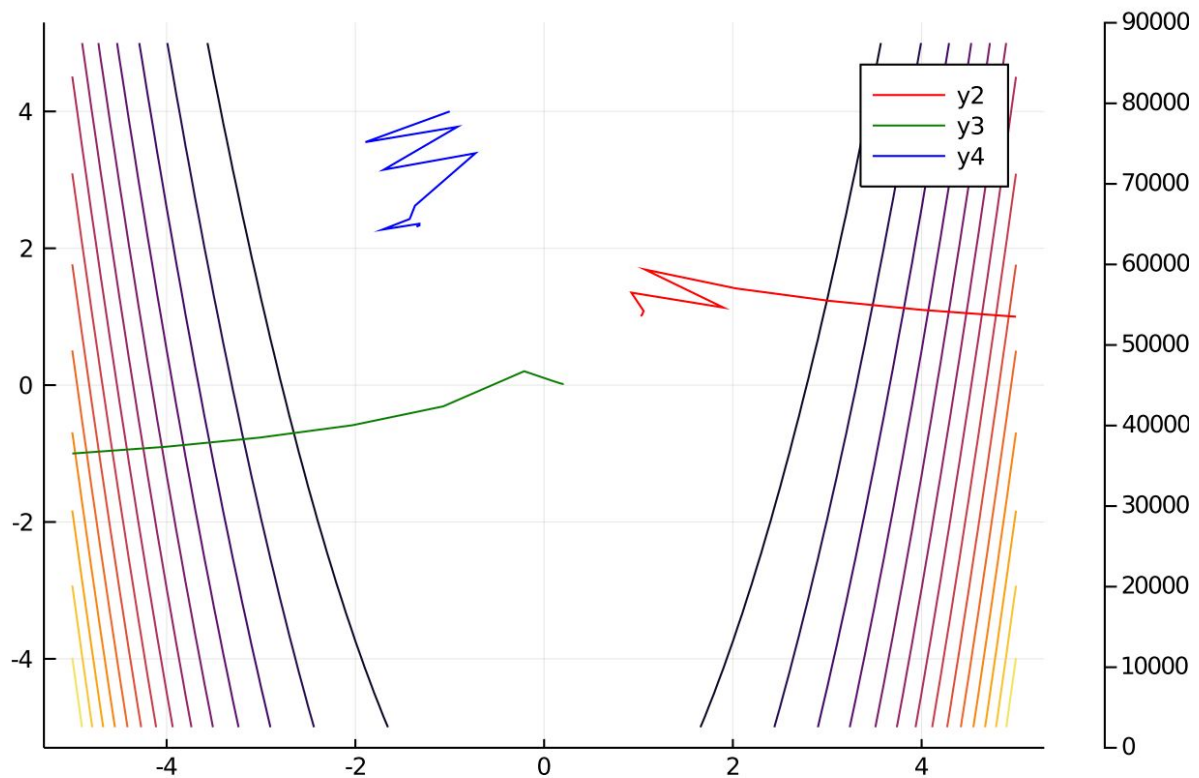
I always assigned alpha as  $0 < \alpha < 1$ , therefore with each step (i), the effect the gradient had and consequently, the step size, decreased as iterations increased

3. I added a logic step to adjust the beta (momentum decay) and (initial) alpha (learning rate) terms for simple1 problem, as the values that worked well for the other 4 problems did not converge in the steep parabola.

**Part2: Contour plots and paths**

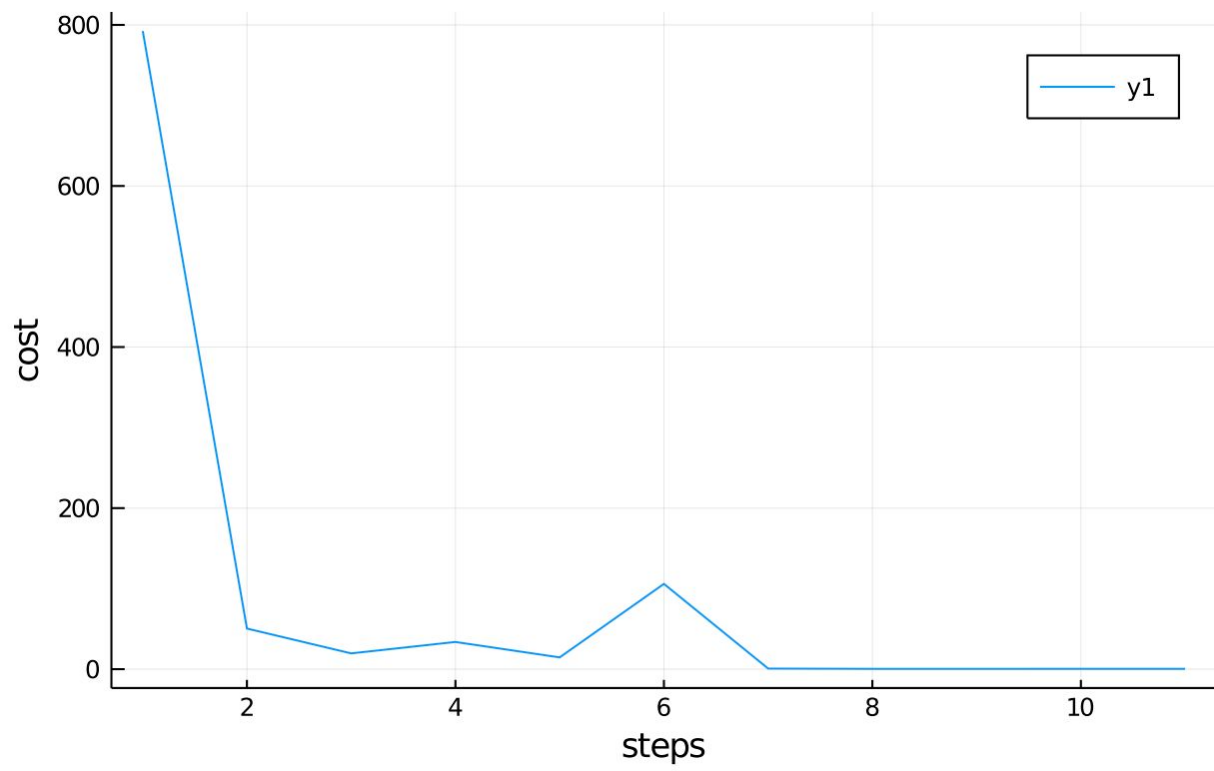
3 different initial conditions for the RosenBrock function, for y2,  $x_0 = (5, 1)$ , for y23  $x_0 = (-5, -1)$ , for y4,  $x_0 = (4, -1)$ ,

Clearly my algorithm found the bottom of the bowl (getting close to the optimum) when it started on the steeper gradient sections and oscillated more substantially in the flatter region.

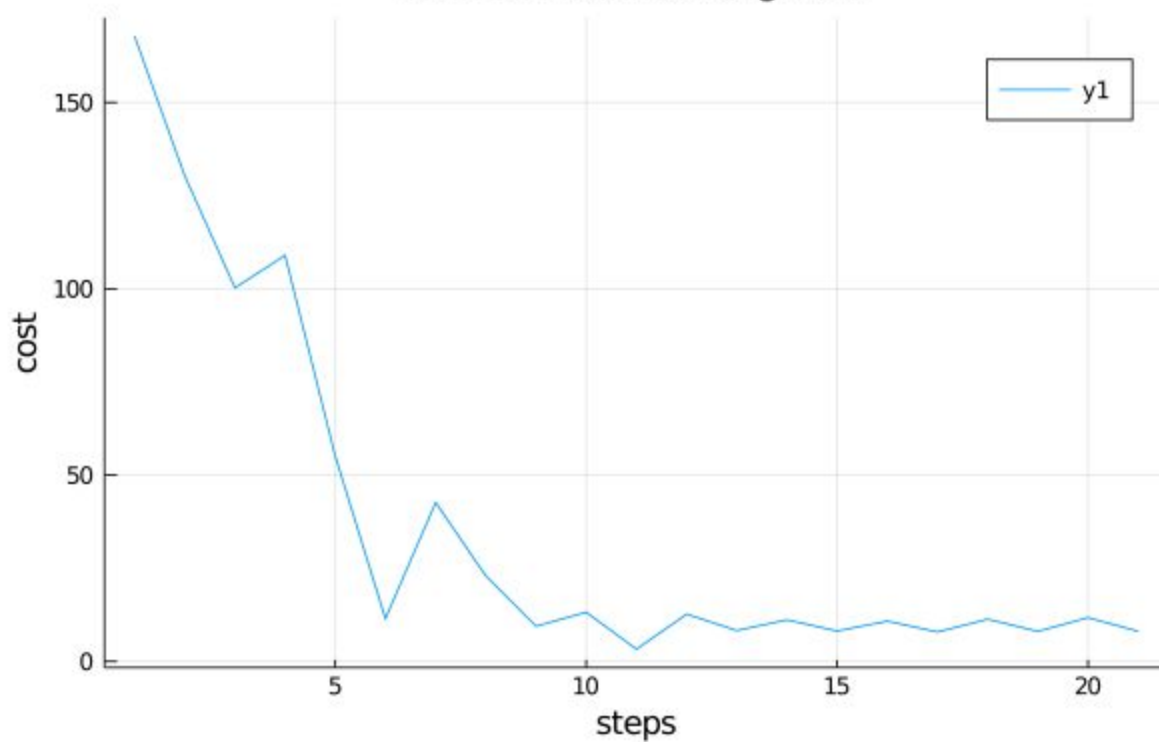


## Part 3: Convergence Plots

## Rosenbrock convergence



himmelblau convergence



Powell convergence

