Homework 1: Image Processing

Submission Instructions: Before the deadline, export the completed notebook to PDF and upload it to GradeScope. The PDF should clearly show your code, and the result of running the code. Check the PDF to ensure that it is readable, the font-size is not small, and no information is cut-off. There will be no make-ups or extensions for corrupted/damaged/unreadable PDFs.

Names of Collaborators:

The below commands will download the images needed for this problem set. Make sure you run it before you get started.

```
In [27]: !wget -qN https://www.cs.columbia.edu/~vondrick/class/coms4732/hw1/noisy_image.jpg !wget -qN https://www.cs.columbia.edu/~vondrick/class/coms4732/hw1/edge_detection_image.jpg !wget -qN https://www.cs.columbia.edu/~vondrick/class/coms4732/hw1/cat.jpg !wget -qN https://www.cs.columbia.edu/~vondrick/class/coms4732/hw1/dog.jpg
```

Problem 1: Image Denoising

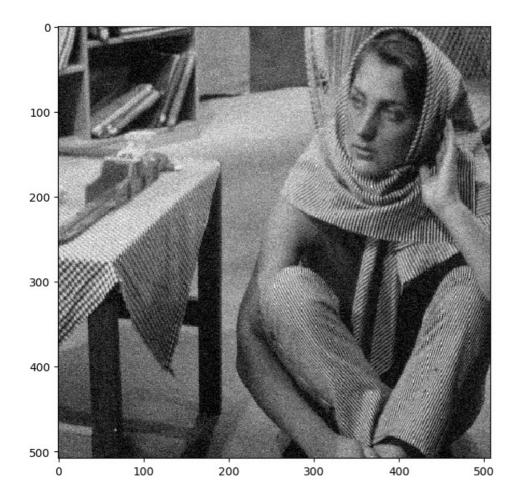
Taking pictures at night is challenging because there is less light that hits the film or camera sensor. To still capture an image in low light, we need to change our camera settings to capture more light. One way is to increase the exposure time, but if there is motion in the scene, this leads to blur. Another way is to use sensitive film that still responds to low intensity light. However, the trade-off is that this higher sensitivity increases the amount of noise captured, which often shows up as grain on photos. In this problem, your task is to clean up the noise with signal processing.

Visualizing the Grain

show image(im)

```
To start off, let's load up the image and visualize the image we want to denoise. In [28]:
```

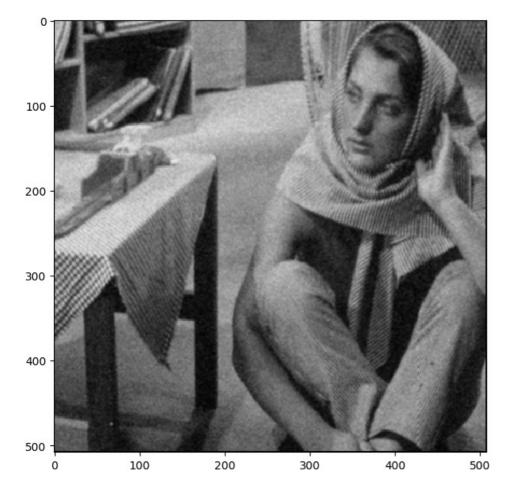
```
import numpy as np
import matplotlib.pyplot as plt
from PIL import Image
from IPython import display
from scipy.signal import convolve2d
from math import *
import time
%matplotlib inline
path to noisy image = '/Users/rajmani/Documents/research/Home/python/computer-vision/homeworks/hw1/noisy image.jpg'
plt.rcParams['figure.figsize'] = [7, 7]
def load image(filename):
  img = np.asarray(Image.open(filename))
  img = img.astype("float32") / 255.
  return img
def gray2rgb(image):
  return np.repeat(np.expand dims(image, 2), 3, axis=2)
def show image(img):
  if len(img.shape) == 2:
    img = gray2rgb(img)
  plt.imshow(img, interpolation='nearest')
# load the image
im = load_image(path_to_noisy_image)
im = im.mean(axis=2) # convert to grayscale
```



Problem 1a: Mean Filter using "for" loop

Let's try to remove this grain with a mean filter. For every pixel in the image, we want to take an average (mean) of the neighboring pictures. Implement this operation using "for" loops and visualize the result:

```
In [29]:
im_pad = np.pad(im, 5, mode='constant') # pad the border of the original image
im_out = np.zeros_like(im) # initialize the output image array
"" TODO: Implement a mean filter using "for" loop here (modify the im_out matrix). ""
def mean_filter(image, im_out, k=3):
    height, width = image.shape
    mid = k // 2
    for i in range(height - k + 1):
        for j in range(width - k + 1):
            im_out[i:k+i, j:k+j][mid, mid] = image[i:k+i, j:k+j].mean()
In [30]:
    mean_filter(im, im_out, 3)
In [31]:
    show_image(im_out)
```



Problem 1b: Implement the convolve image function.

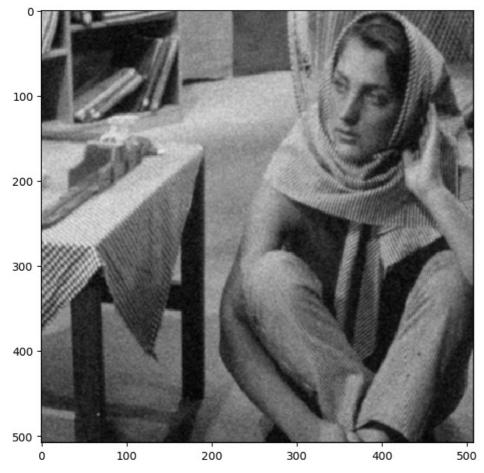
Convolution provides a mathematical way to apply filters to image. Implement the <code>convolve_image</code> function below using <code>for</code> loops. Your function should accept an image and a filter matrix, and return the result of convoling the image with the given filter matrix. Note: You cannot use a built-in convolution routine for this problem.

```
def convolve image(image main, filter matrix):
  "Convolve a 2D image using the filter matrix.
  Args:
     image: a 2D numpy array.
     filter_matrix: a 2D numpy array.
     the convolved image, which is a 2D numpy array same size as the input image.
  TODO: Implement the convolve_image function here.
  final image = np.zeros like(image main)
  kernel_dim = filter_matrix.shape[0]
  k = kernel dim
  pad = (kernel\_dim - 1) // 2
  image_main = np.pad(image_main, [(pad, pad)], mode="constant")
  height, width = image_main.shape
  filter matrix = np.fliplr(np.flipud(filter_matrix))
  for i in range(height - k + 1):
     for j in range(width - k + 1):
       final image[i, j] = (
          image_main[i : k + i, j : k + j].ravel().dot(filter_matrix.ravel())
  return final_image
In [33]:
import scipy as sp
```

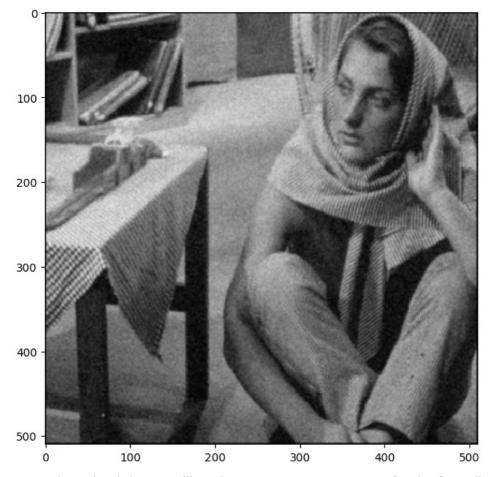
Problem 1c: Mean Filter with Convolution

Implement this same operation with a convolution instead. Fill in the mean filter matrix here, and visualize the convolution result.

In [34]:
mean_filt = np.ones(9).reshape(3, 3) * 1/9
Apply mean filter convolution using your convolve_image function and the mean_filt matrix.
In [35]:
show_image(convolve_image(im, mean_filt))



Compare your convolution result with the scipy.signal.convolve2d function (they should look the same). In [36]: show_image(convolve2d(im, mean_filt))



Note: In the sections below, we will use the scipy.signal.convolve2d function for grading. But fill free to test your convolve image function on other filters as well.

Problem 1d: Gaussian Filter

Instead of using a mean filter, let's use a Gaussian filter. Create a 2D Gaussian filter, and plot the result of the convolution.

Hint: You can first construct a one dimensional Gaussian, then use it to create a 2D dimensional Gaussian.

```
def gaussian_filter(sigma, k=20):

""

Args:
    sigma: the standard deviation of Gaussian kernel.
    k: controls size of the filter matrix.

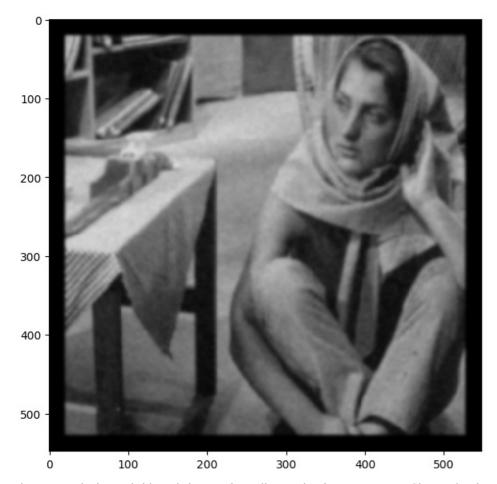
Returns:
    a 2D Gaussian filter matrix of the size (2k+1, 2k+1).

TODO: Implement a Gaussian filter here.

"

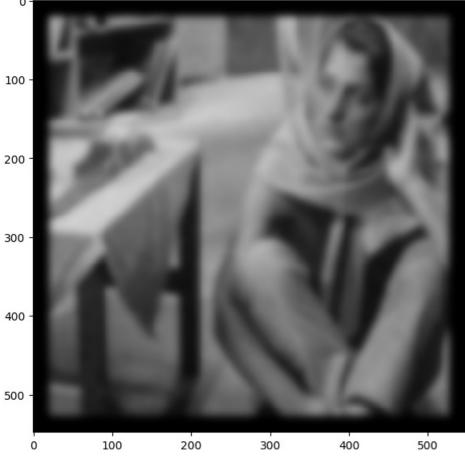
denom = 2 * sigma**2
    scale = 2 * np.pi * sigma**2
    oned_gauss = [np.exp(-x**2 / denom) / np.sqrt(scale) for x in range(-k, k + 1)]
    return np.outer(oned_gauss, oned_gauss)

show_image(convolve2d(im, gaussian_filter(2)))
```

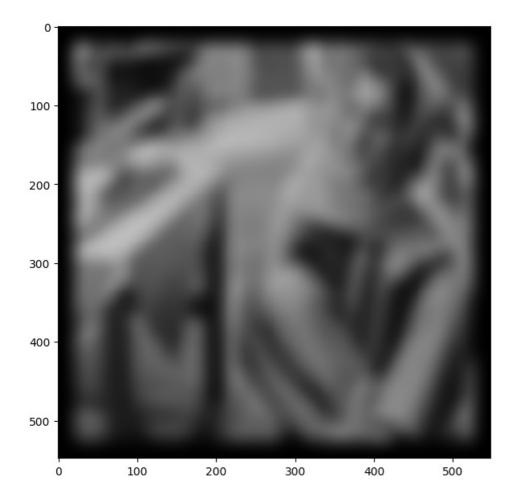


The amount the image is blurred changes depending on the sigma parameter. Change the sigma parameter to see what happens. Try a few different values.

In [38]: show_image(convolve2d(im, gaussian_filter(5)))



In [39]: show_image(convolve2d(im, gaussian_filter(10)))

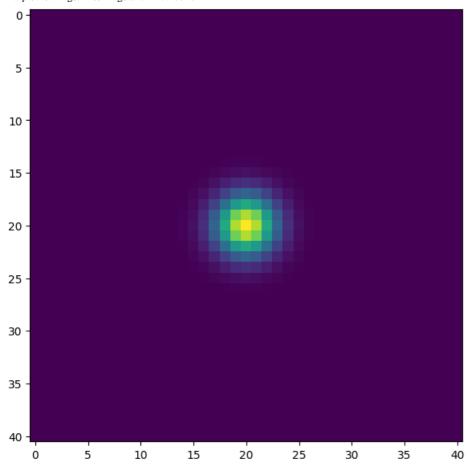


Problem 1e: Visualizing Gaussian Filter

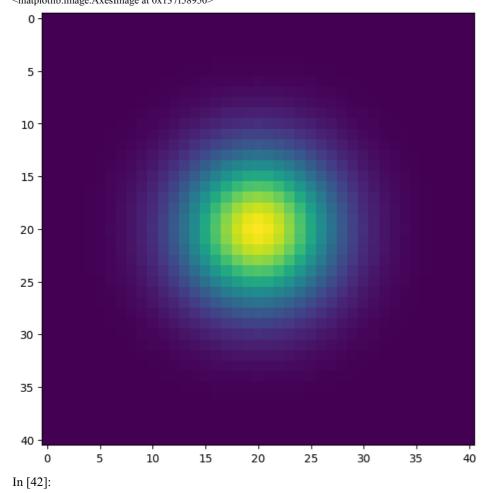
Try changing the sigma parameter below to visualize the Gaussian filter directly. This gives you an idea of how different sigma values create different convolved images.

In [40]: plt.imshow(gaussian_filter(sigma=2))

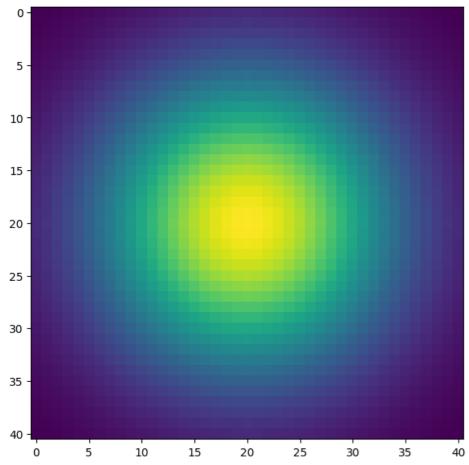
Out[40]: <matplotlib.image.AxesImage at 0x127f45710>



In [41]: plt.imshow(gaussian_filter(sigma=5)) Out[41]: <matplotlib.image.AxesImage at 0x137f58950>



Out[42]: <matplotlib.image.AxesImage at 0x14401c210>



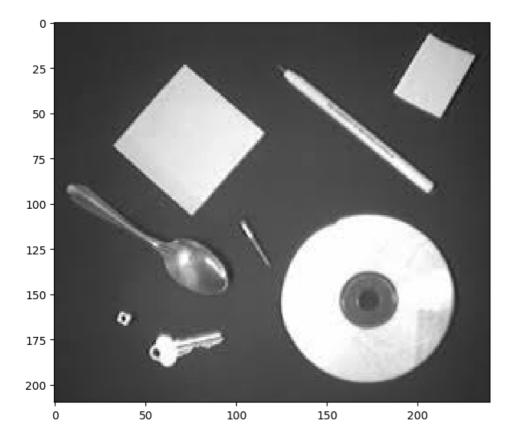
Problem 2: Edge Detection

There are a variety of filters that we can use for different tasks. One such task is edge detection, which is useful for finding the boundaries regions in an image. In this part, your task is to use convolutions to find edges in images. Let's first load up an edgy image.

In [43]:

 $path_to_edge_image = '/Users/rajmani/Documents/research/Home/python/computer-vision/homeworks/hw1/edge_detection_image.jpg' im = load_image(path_to_edge_image)$

im = im.mean(axis=2) # convert to grayscale
show image(im)

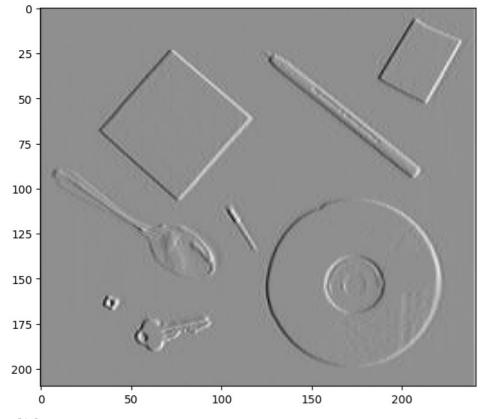


Problem 2a: Image Gradient Filters

Implement a filter to detect gradients, and convolve it with the image. Show the result.

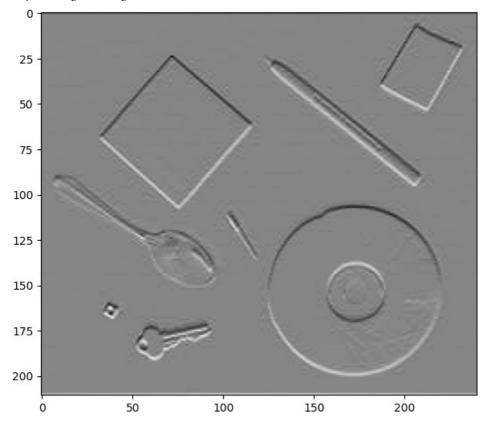
```
In [44]:
filtx = np.array([[-1, 1]])
#filty = np.array([[1, 1], [-1, -1]])
plt.imshow(convolve2d(im, filtx), cmap='gray')
Out[44]:
```

<matplotlib.image.AxesImage at 0x144103f90>



In [45]: plt.imshow(convolve2d(im, filtx.T), cmap='gray')

Out[45]: <matplotlib.image.AxesImage at 0x144177550>



Noise

The issue with the basic gradient filters is that it is sensitive to noise in the image. Let's add some Gaussian noise to the image below, and visualize what happens. The edges should be hard to see.

```
In [46]:
```

im = load_image(path_to_edge_image)

im = im.mean(axis=2)

im = im + 0.2*np.random.randn(*im.shape)

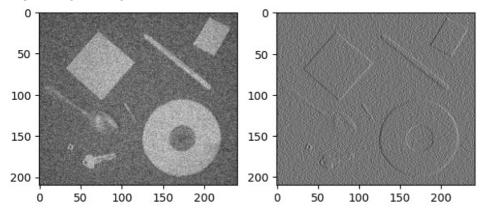
f, axarr = plt.subplots(1,2)

axarr[0].imshow(im, cmap='gray')

axarr[1].imshow(convolve2d(im, filtx), cmap='gray')

Out[46]:

<matplotlib.image.AxesImage at 0x1440e6510>



Problem 2b: Laplacian Filters

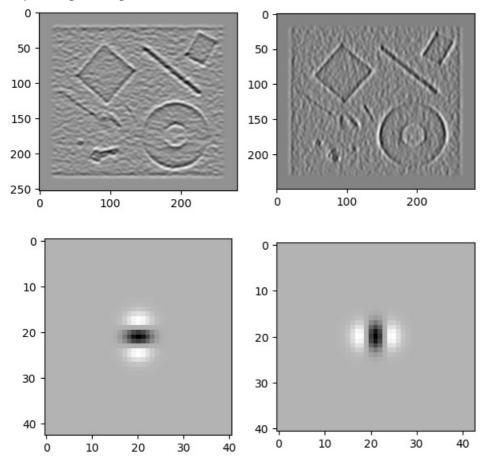
Laplacian filters are edge detectors that are robust to noise (Why is this? Think about how the filter is constructed.). Implement a Laplacian filter below for both horizontal and vertical edges.

In [47]:

```
lap x filt = convolve2d(convolve2d(gaussian filter(2), filtx), filtx)
lap y filt = convolve2d(convolve2d(gaussian filter(2), filtx.T), filtx.T)
f, axarr = plt.subplots(2,2)
axarr[0,0].imshow(convolve2d(im, lap_y_filt), cmap='gray')
axarr[0,1].imshow(convolve2d(im, lap_x_filt), cmap='gray')
axarr[1,0].imshow(lap_y_filt, cmap='gray')
axarr[1,1].imshow(lap x filt, cmap='gray')
```

Out[47]:

<matplotlib.image.AxesImage at 0x1442cf710>



Problem 3: Hybrid Images

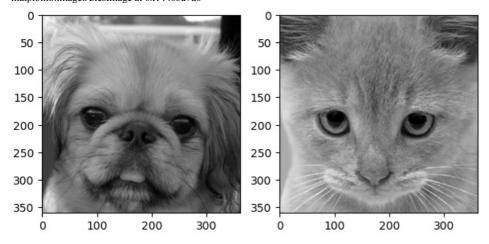
Hybrid images is a technique to combine two images in one. Depending on the distance you view the image, you will see a different image. This is done by merging the high-frequency components of one image with the low-frequency components of a second image. In this problem, you are going to use the Fourier transform to make these images. But first, let's visualize the two images we will merge together.

In [48]:

from numpy.fft import fft2, fftshift, ifftshift, ifft2 path_to_dog_image = '/Users/rajmani/Documents/research/Home/python/computer-vision/homeworks/hw1/dog.jpg' path to cat image = '/Users/rajmani/Documents/research/Home/python/computer-vision/homeworks/hw1/cat.jpg' dog = load image(path to dog image).mean(axis=-1)[:, 25:-24] cat = load image(path to cat image).mean(axis=-1)[:, 25:-24]

f, axarr = plt.subplots(1,2)axarr[0].imshow(dog, cmap='gray') axarr[1].imshow(cat, cmap='gray')

Out[48]: <matplotlib.image.AxesImage at 0x14403a7d0>



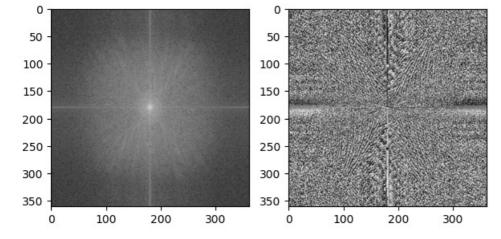
Problem 3a: Fourier Transform

In the code box below, compute the Fourier transform of the two images. You can use the fft2 function. You can also use the fftshift function, which may help in the next section.

```
In [49]:
cat_fft = np.fft.fftshift(np.fft.fft2(cat))
dog_fft = np.fft.fftshift(np.fft.fft2(dog))

# Visualize the magnitude and phase of cat_fft. This is a complex number, so we visualize
# the magnitude and angle of the complex number.
# Curious fact: most of the information for natural images is stored in the phase (angle).
f, axarr = plt.subplots(1,2)
axarr[0].imshow(np.log(np.abs(cat_fft)), cmap='gray')
axarr[1].imshow(np.angle(cat_fft), cmap='gray')
```

Out[49]: <matplotlib.image.AxesImage at 0x1444b6390>



Problem 3b: Low and High Pass Filters

By masking the Fourier transform, you can compute both low and high pass of the images. In Fourier space, write code below to create the mask for a high pass filter of the cat, and the mask for a low pass filter of the dog. Then, convert back to image space and visualize these images.

You may need to use the functions ifft2 and ifftshift.

```
In [50]:
def circular_mask(height, width):
    center = (height // 2, width // 2)
    radius = height // 25
    Y, X = np.ogrid[:height, :width]
    xnorm = (X - center[0]) ** 2
    ynorm = (Y - center[1]) ** 2
    dist_from_center = np.sqrt(xnorm + ynorm)
    mask = dist_from_center <= radius
    return mask</pre>
```

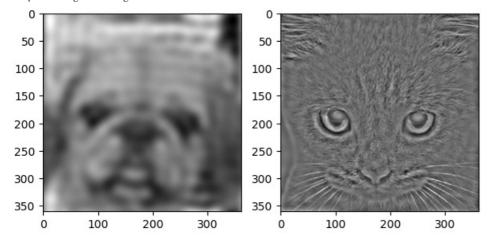
```
high_mask = np.where(circular_mask(*cat_fft.shape) == False, True, False) low_mask = circular_mask(*dog_fft.shape)
```

"" TODO: Apply the high pass filter on the cat and convert back to image space. "" cat_filtered = ifft2(ifftshift(cat_fft * high_mask)).real

"" TODO: Apply the low pass filter on the dog and convert back to image space. "" dog_filtered = ifft2(ifftshift(dog_fft * low_mask)).real

f, axarr = plt.subplots(1,2) axarr[0].imshow(dog_filtered, cmap='gray') axarr[1].imshow(cat_filtered, cmap='gray') Out[51]:

<matplotlib.image.AxesImage at 0x1444a5850>



Problem 3c: Hybrid Image Results

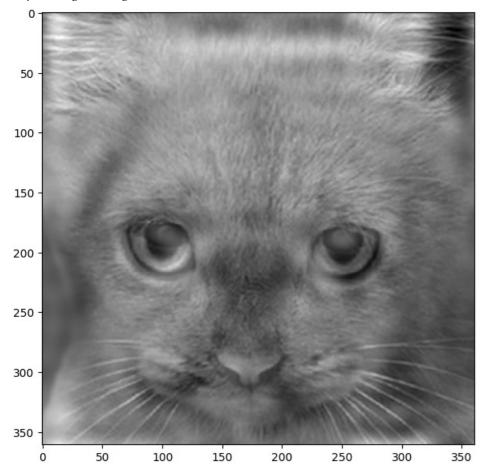
Now that we have the high pass and low pass fitlered images, we can create a hybrid image by adding them. Write the code to combine the images below, and visualize the hybrd image.

Depending on whether you are close or far away from your monitor, you should see either a cat or a dog. Try creating a few different hybrid images from your own photos or photos you found. Submit them, and we will show the coolest ones in class.

In [52]: hybrid = cat_filtered + dog_filtered

plt.imshow(hybrid, cmap='gray')

Out[52]: <matplotlib.image.AxesImage at 0x127f10990>



Acknowledgements

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