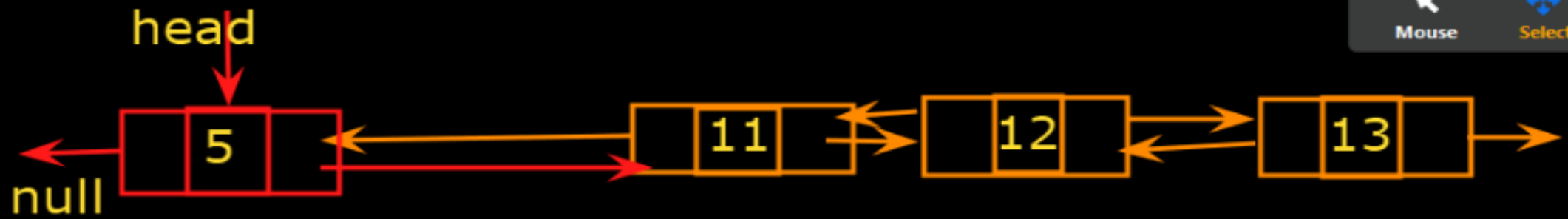
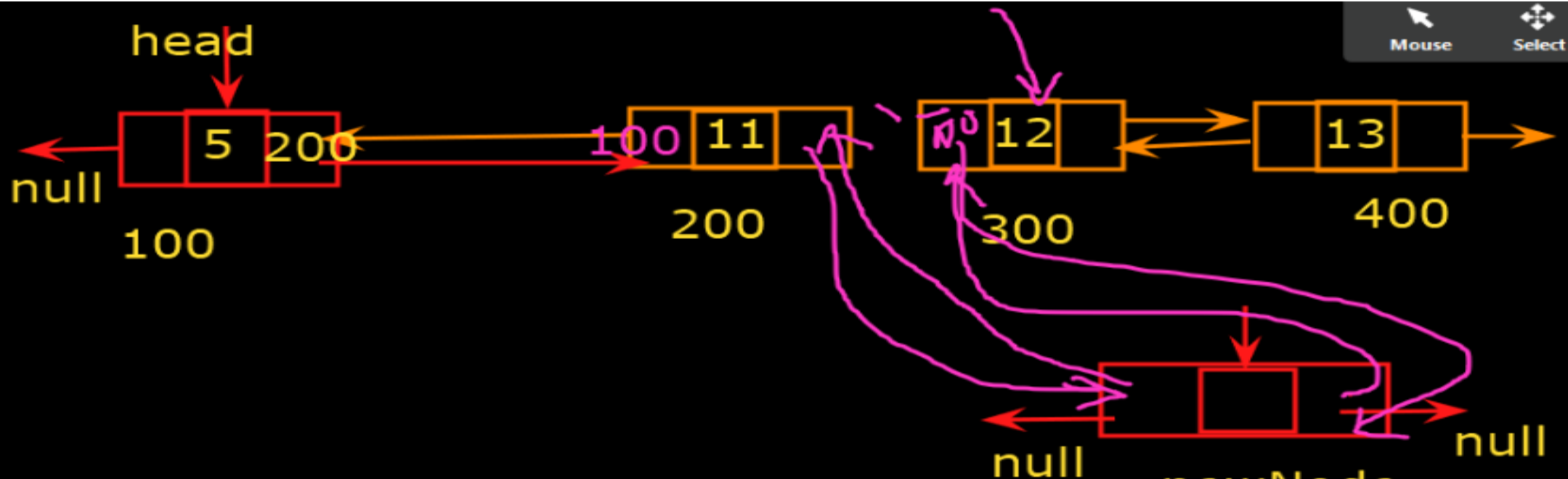


Algorithms & Data Structure

Kiran Waghmare



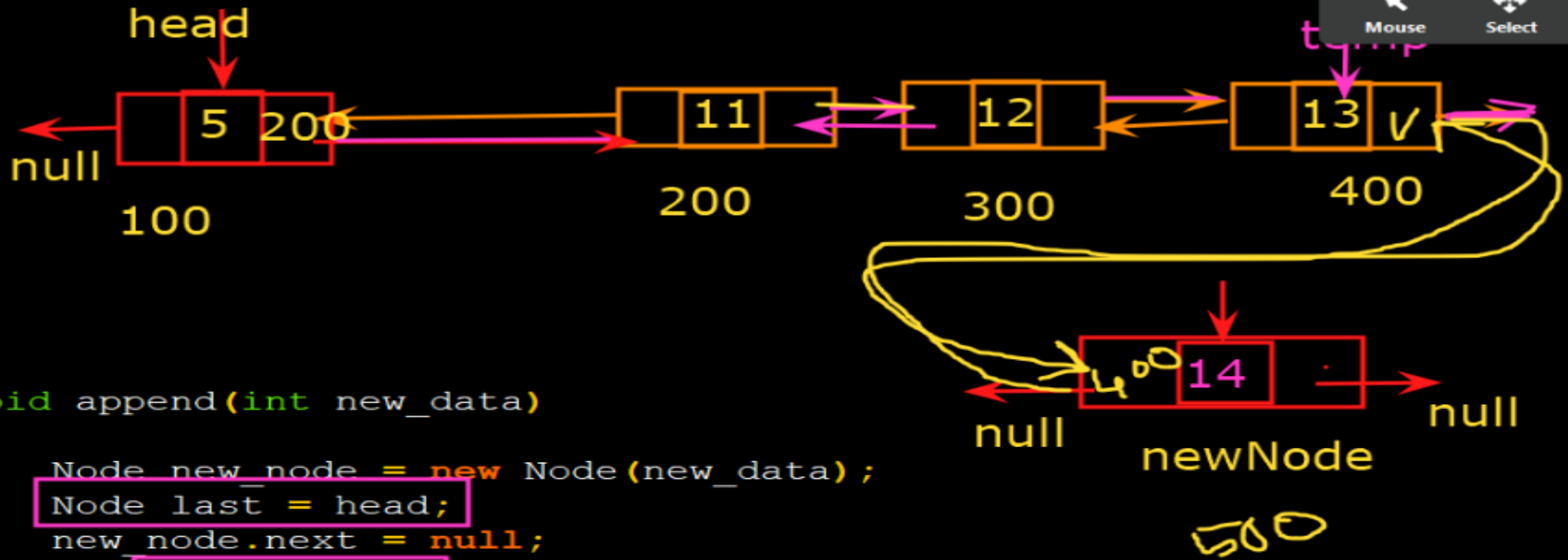
```
//Insertion at Beginning
public void insert(int new_data)
{
    Node new Node = new Node(new_data);
    new_Node.next = head;
    new_Node.prev = null;
    if (head != null)
        head.prev = new_Node;
    head = new_Node;
}
```



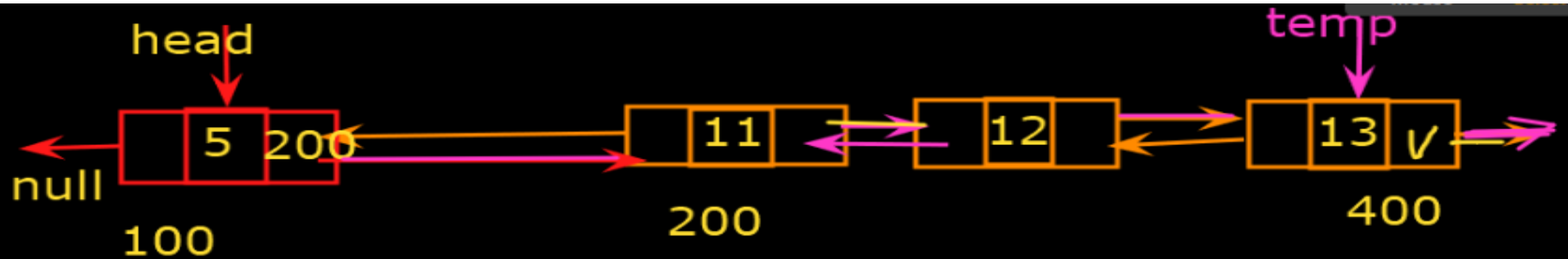
```

public void InsertAfter(Node prev_Node, int new_data,
{
    if (prev_Node == null) {
        System.out.println("The given previous node cannot be NULL ")
        return;
    }
    Node new_node = new Node(new_data);
    new_node.next = prev_Node.next;
    prev_Node.next = new_node;
    new_node.prev = prev_Node;
    if (new_node.next != null)
        new_node.next.prev = new_node;
}

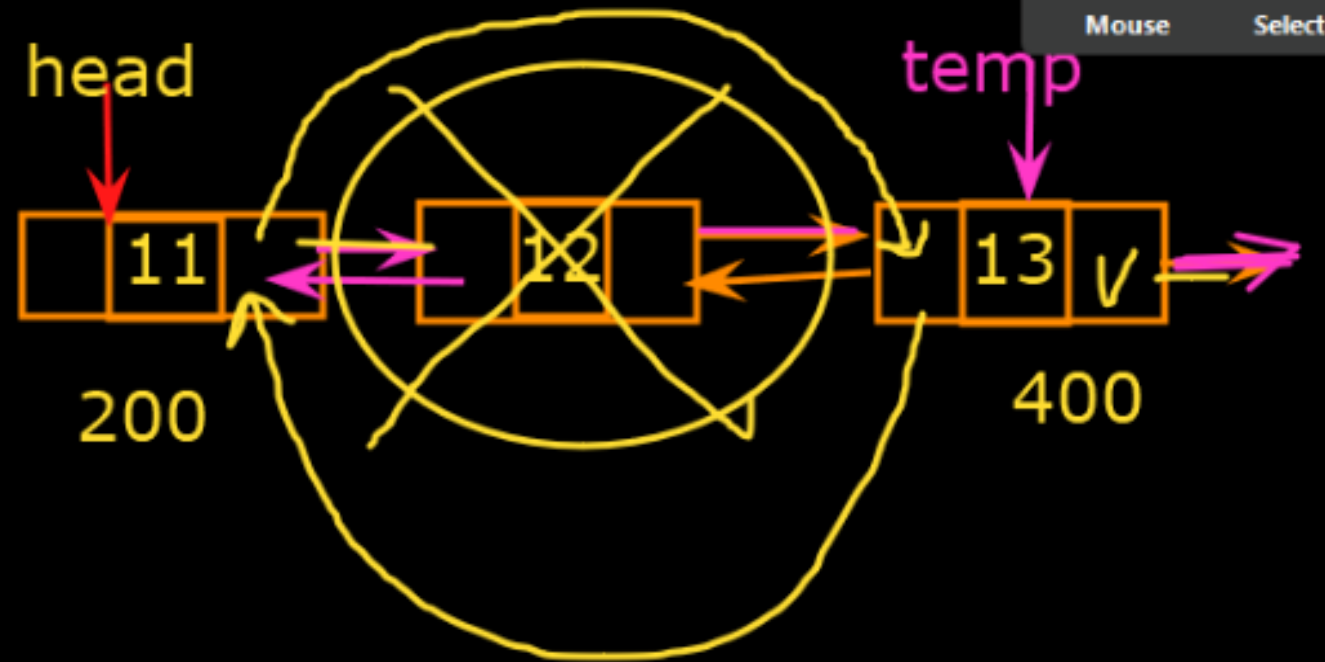
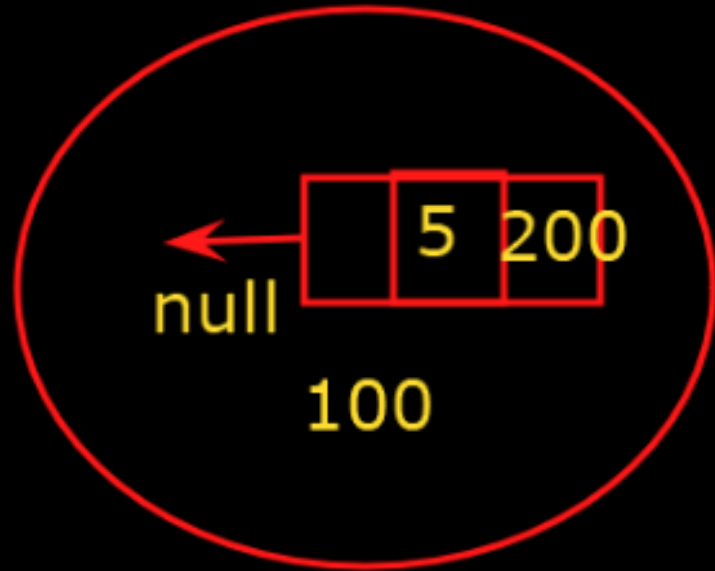
```

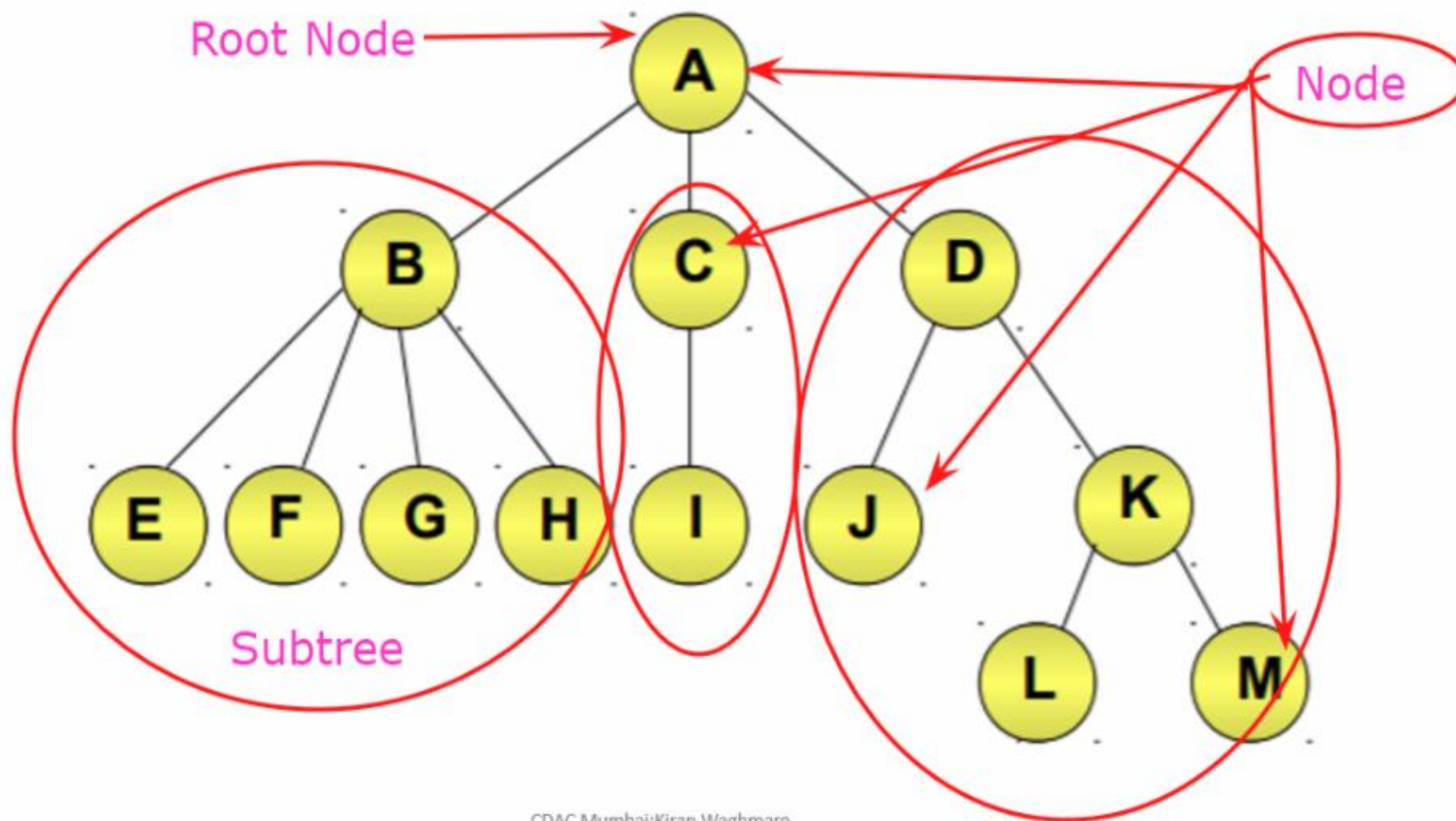


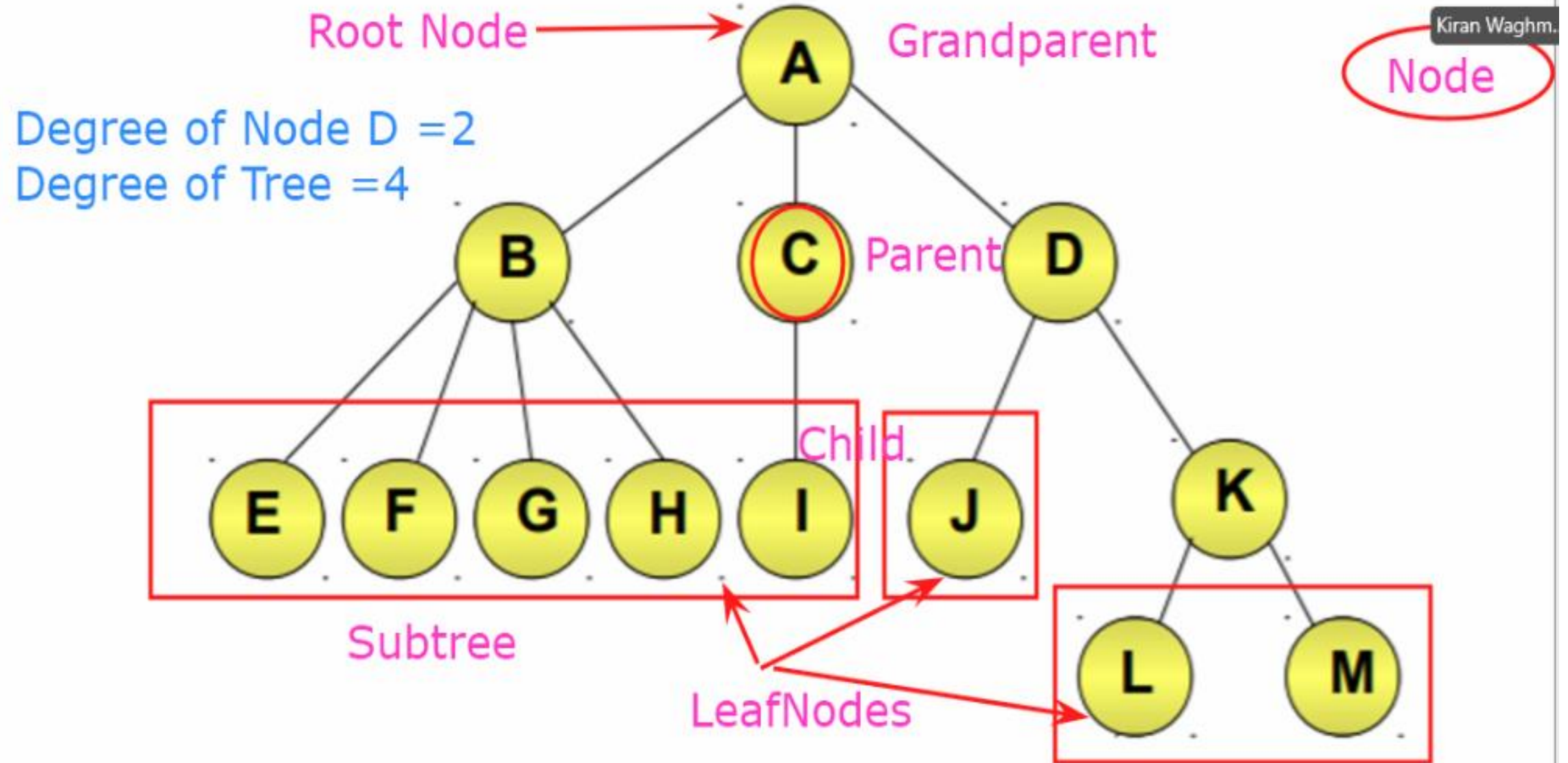
```
void append(int new_data)
{
    Node new_node = new Node(new_data);
    Node last = head;
    new_node.next = null;
    if (head == null) {
        new_node.prev = null;
        head = new_node;
        return;
    }
    while (last.next != null)
        last = last.next;
    last.next = new_node;
    new_node.prev = last;
}
```

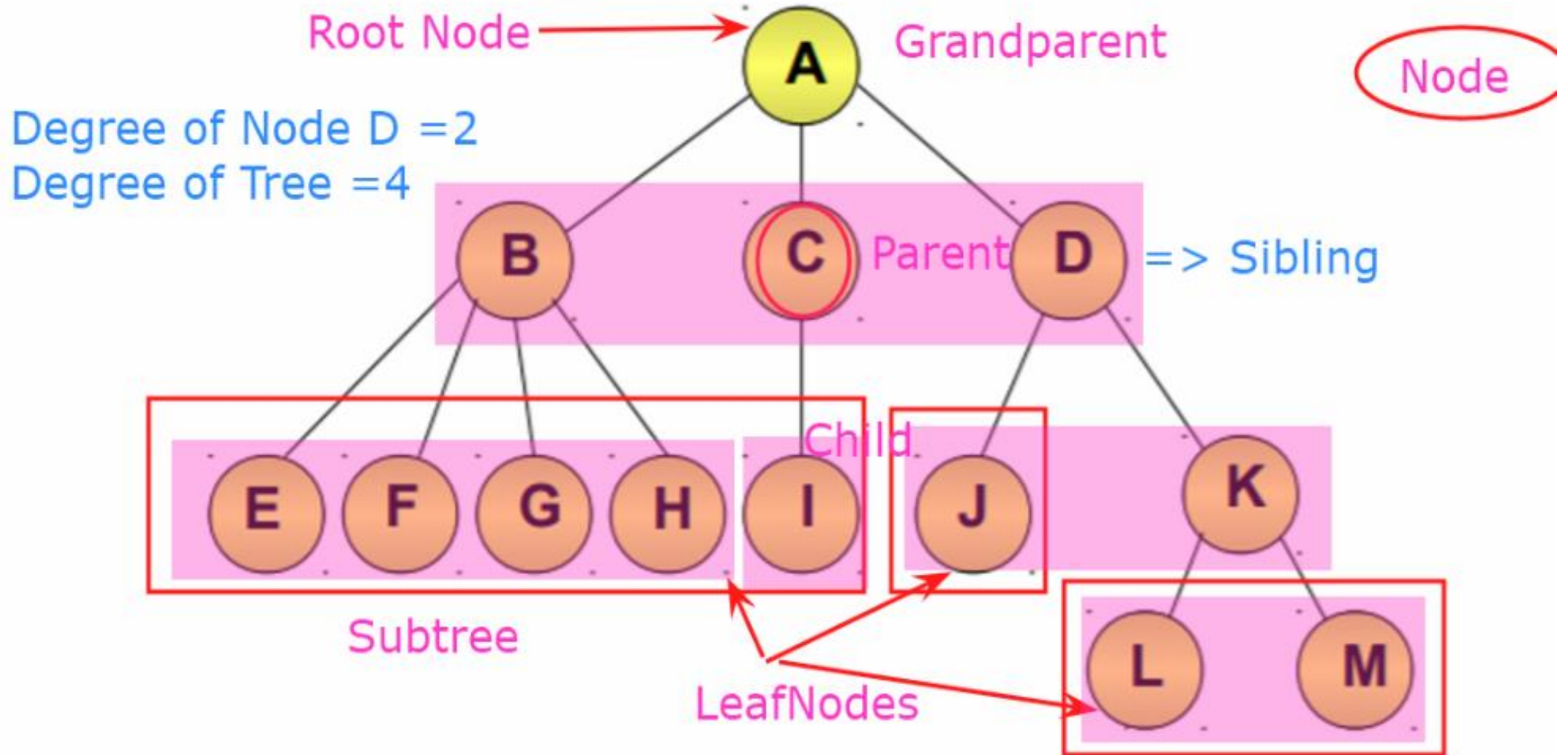


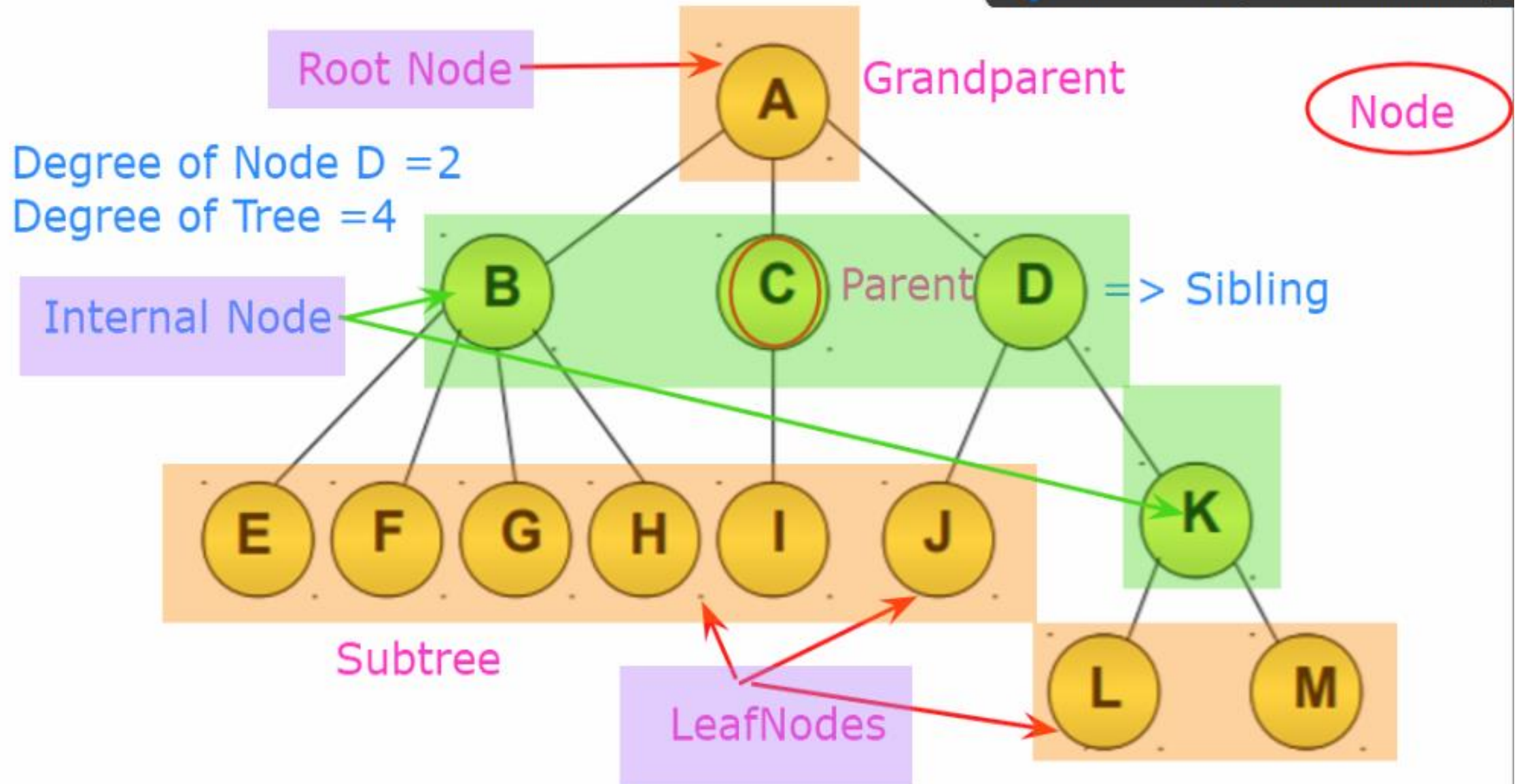
```
static void display()  
{  
    Node temp = head;  
    if (temp == null)  
        System.out.print("Doubly Linked list empty");  
  
    while (temp != null)  
    {  
        System.out.print(temp.data + " ");  
        temp = temp.next;  
    }  
    System.out.println();  
}
```

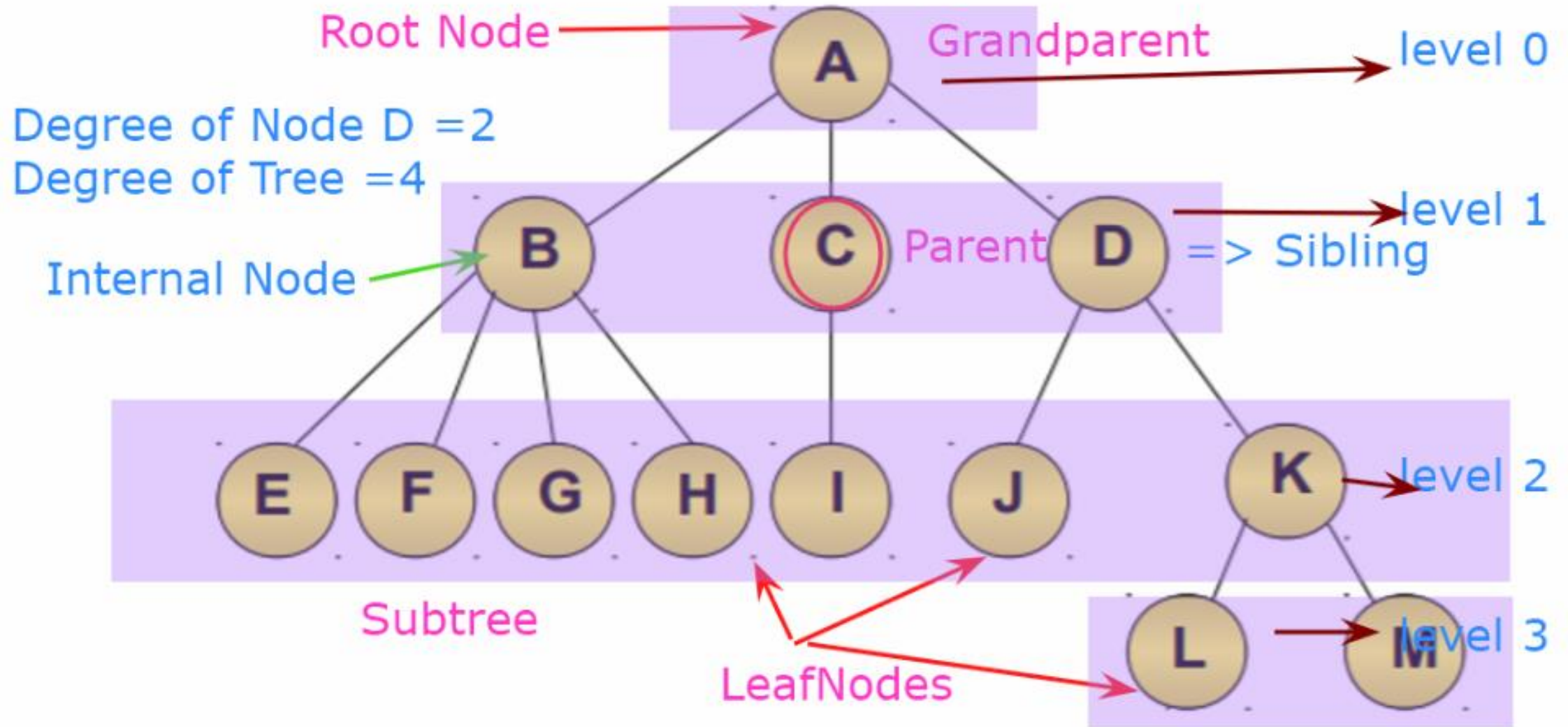












Depth

Height

Root Node

level 0

$h=3$

Parent

level 1

$h=2$

level 2

$h=0$

$h=0$

$h=0$

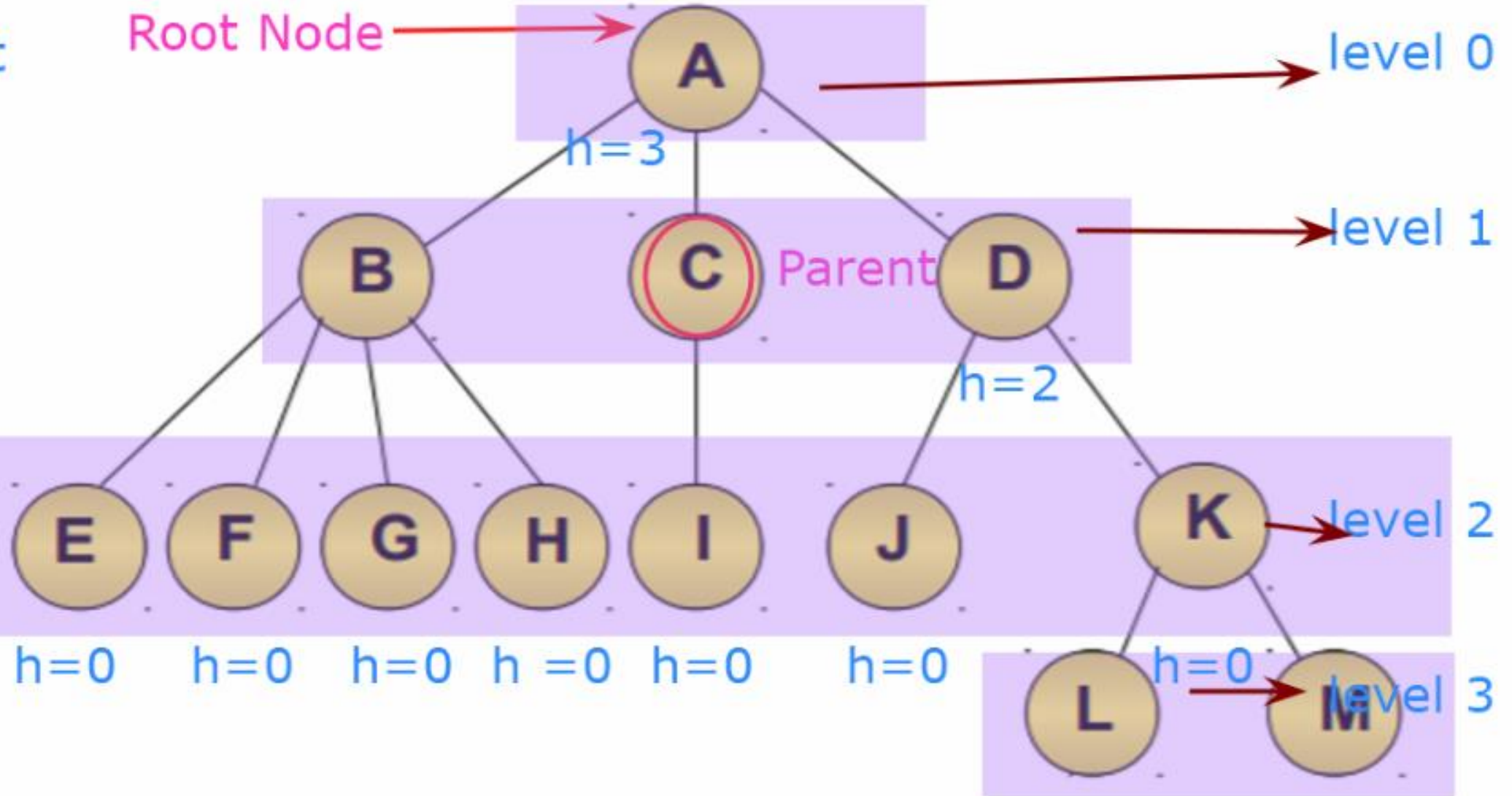
$h=0$

$h=0$

$h=0$

$h=0$

level 3

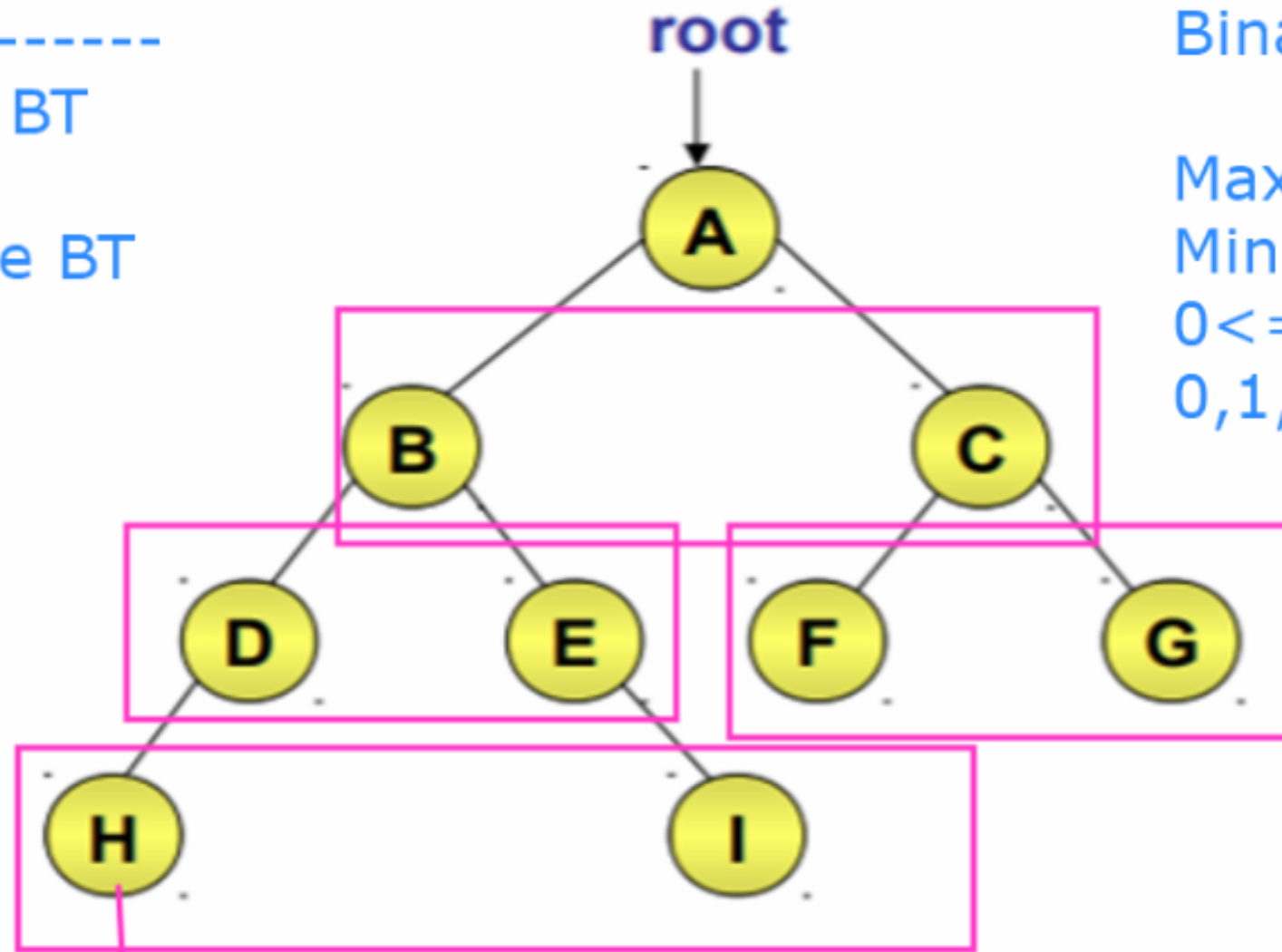


Types of BT

1. Strictly BT
2. Full BT
3. Complete BT

Binary Tree

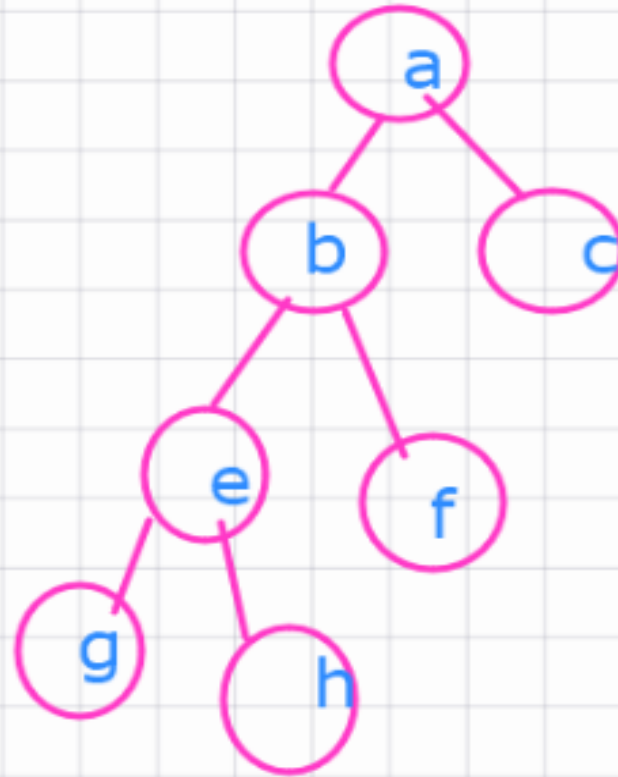
Max: 2
Min: 0
 $0 \leq 2$
0, 1, 2



Tree ---> BT ---> Strictly, Full, Complete

Types of BT

- 1. Strictly BT
- 2. Full BT
- 3. Complete BT



Binary Tree

Max: 2

Min: 0

$0 \leq 2$

0, 1, 2

Strictly BT : every node, except for the leaf node, has non empty left and right children (2 children)

Tree ---> BT ---> Strictly, Full, Complete

Types of BT

1. Strictly BT
2. Full BT
3. Complete BT

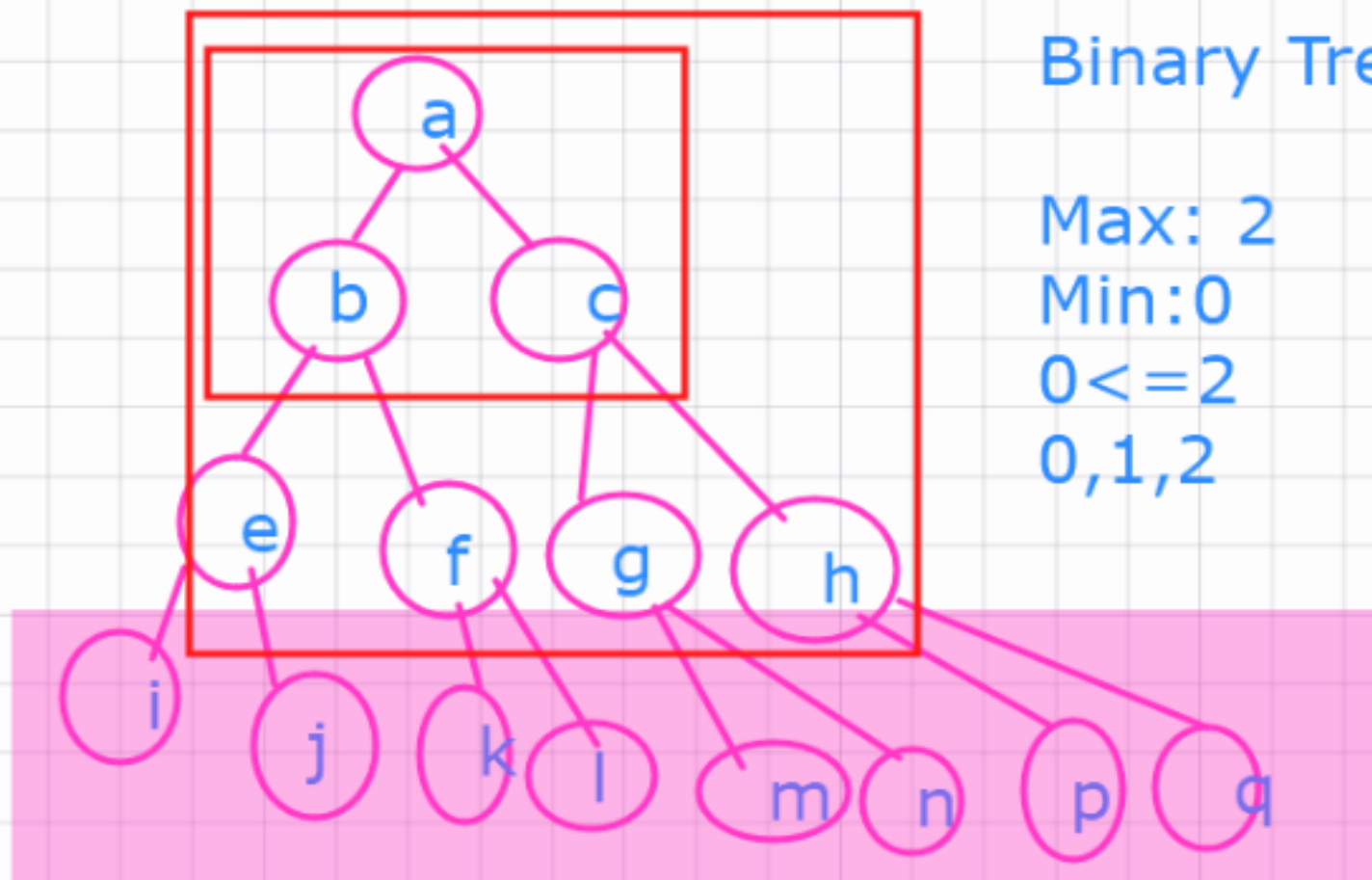
Binary Tree

Max: 2

Min: 0

$0 \leq 2$

0, 1, 2



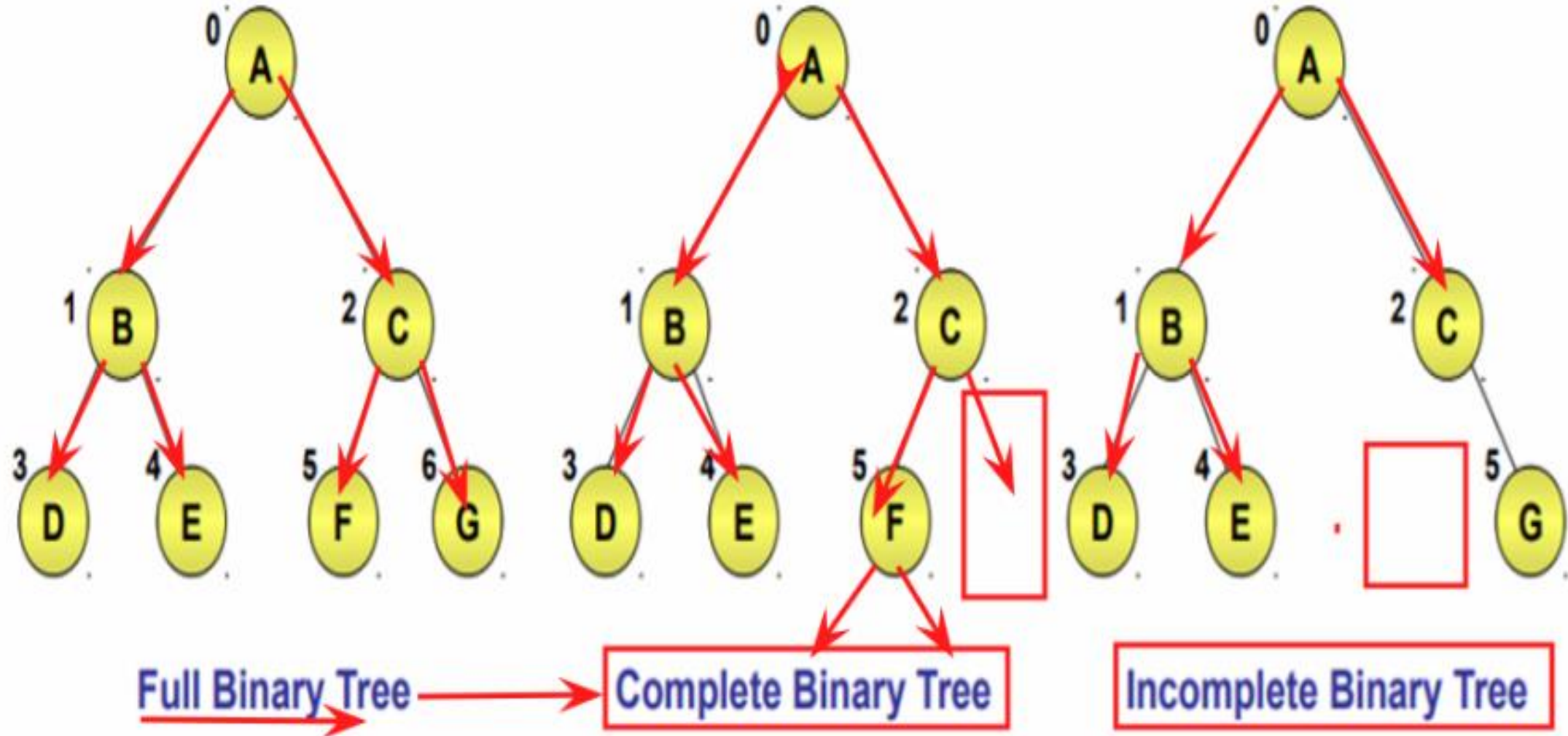
Full BT :

$$2^d - 1$$

$$d=3$$

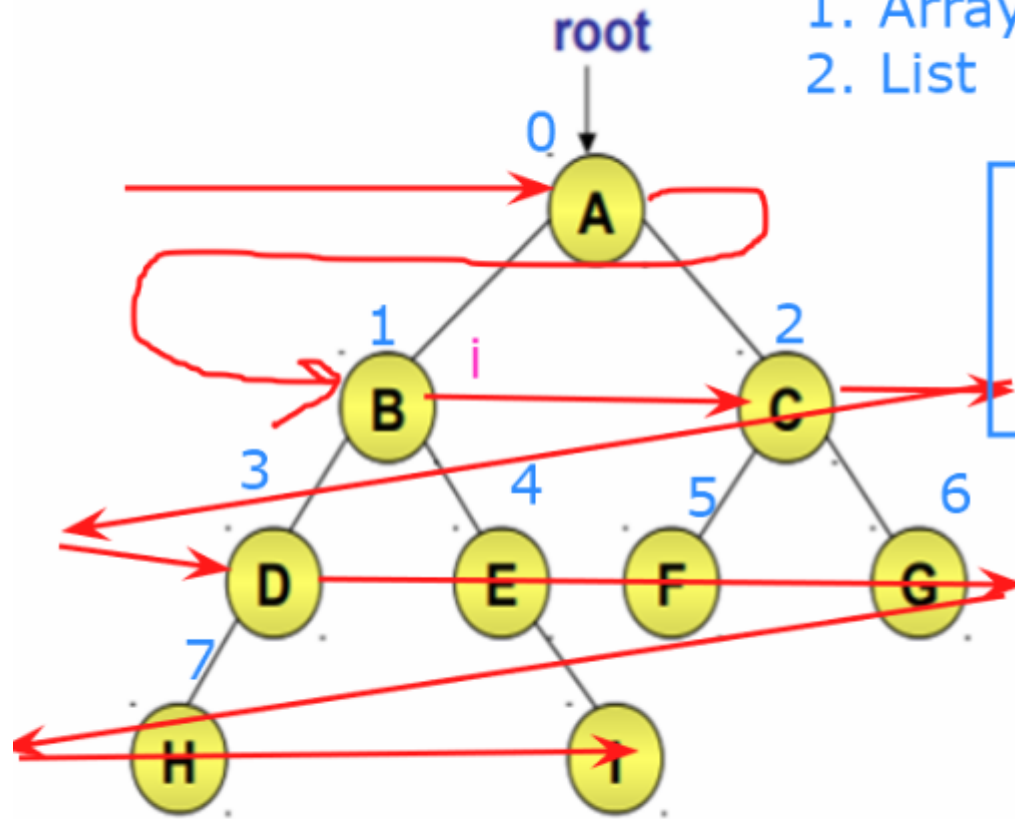
$$\text{No. of nodes: } 2^3 - 1 = 7$$

Tree ---> BT ---> Strictly, Full, Complete



Representation of BT

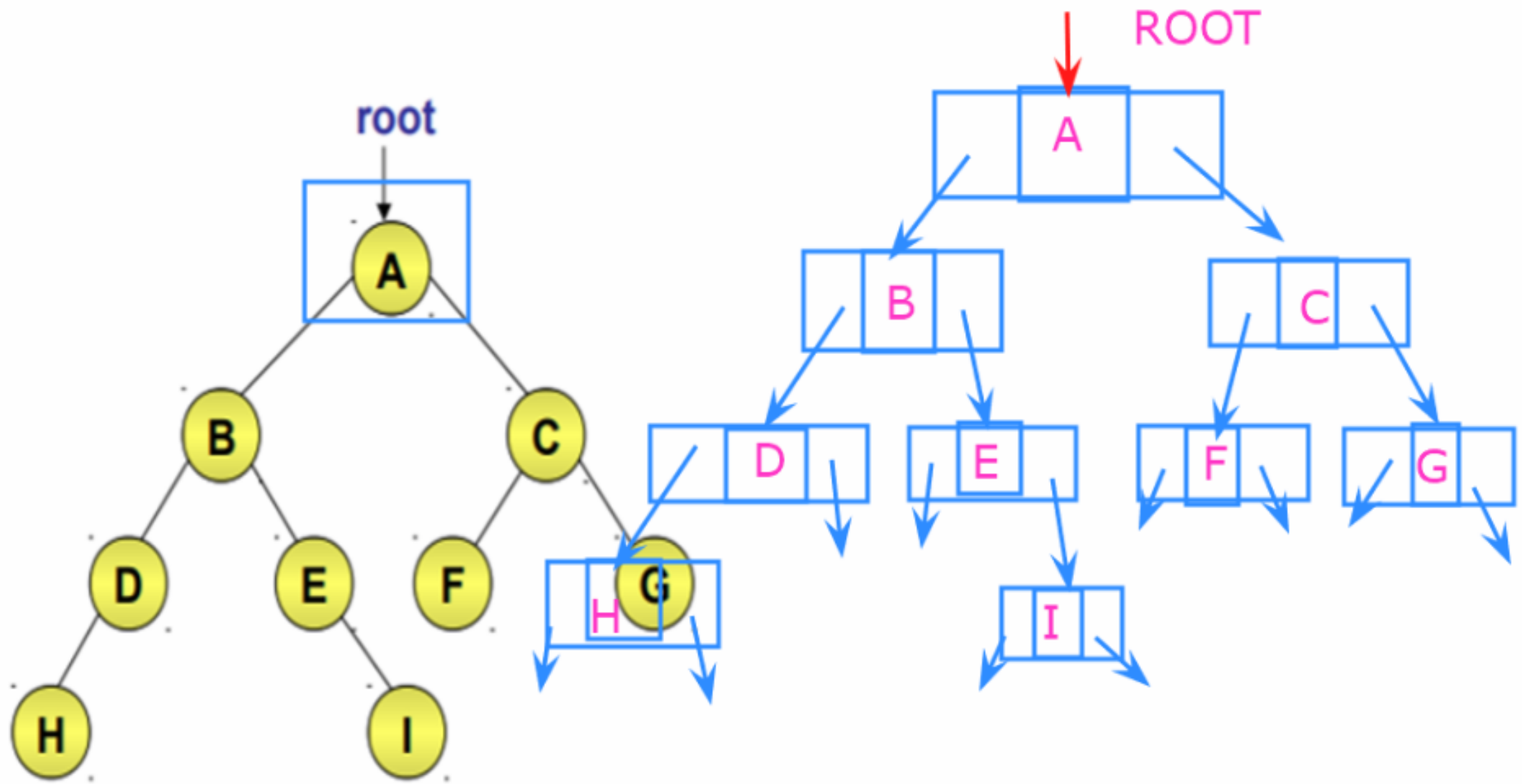
1. Array
2. List



Parent(i) = $(i-1)/2$
LeftChild(i) = $(2*i)+1$
RightChild(i) = $(2*i)+2$

Node B = $i=1$
Parent = A
LC = D
RC = E

0	A
1	B
2	C
3	D
4	E
5	F
6	G
7	H
8	



```

class BT
{
    Node root;
static class Node
{
    int data;
    Node left, right;

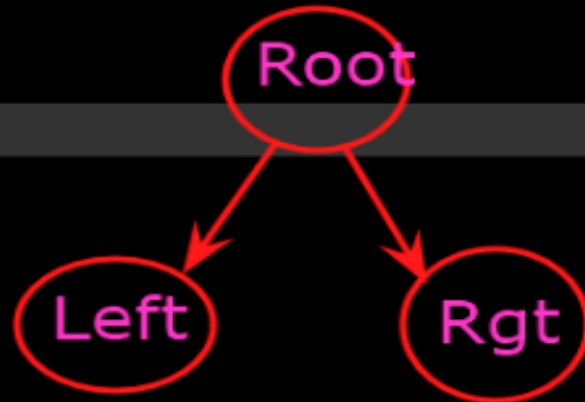
    Node(int d)
    {
        data = d;
        left = right = null;
    }
}
}

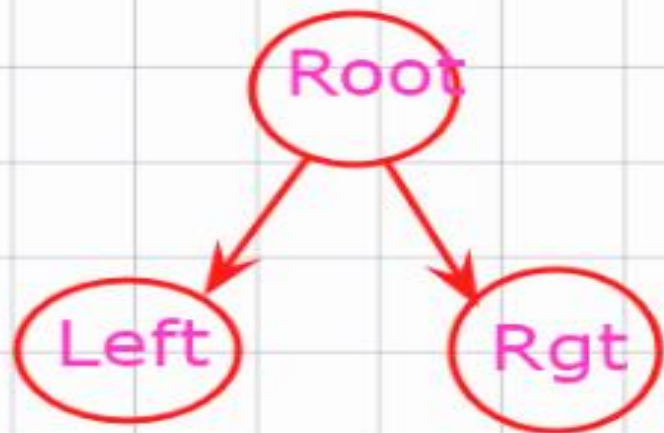
```



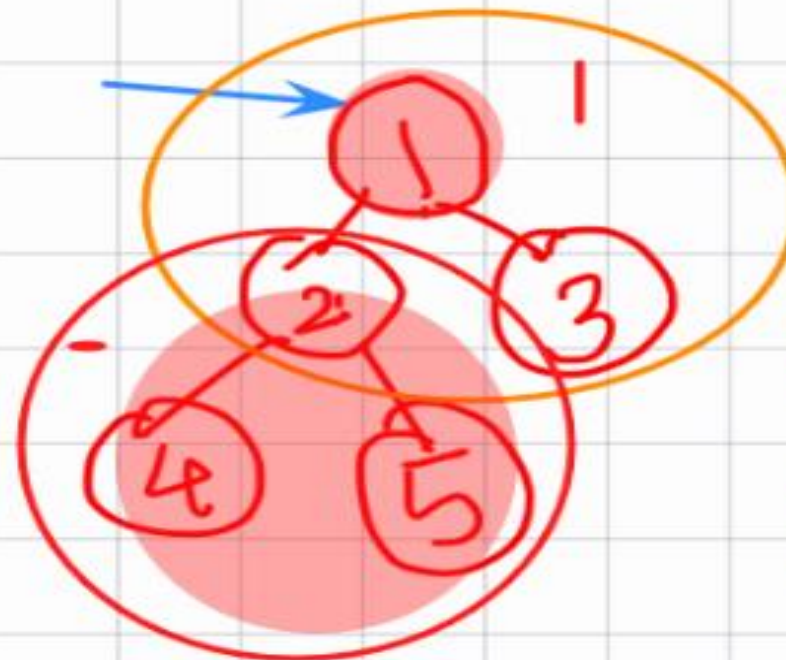
Tree Traversal

-
1. Inorder: Left, Root, Rgt
 2. Preorder: Root, Left, Rgt
 3. Postorder: Left, Rgt, Root

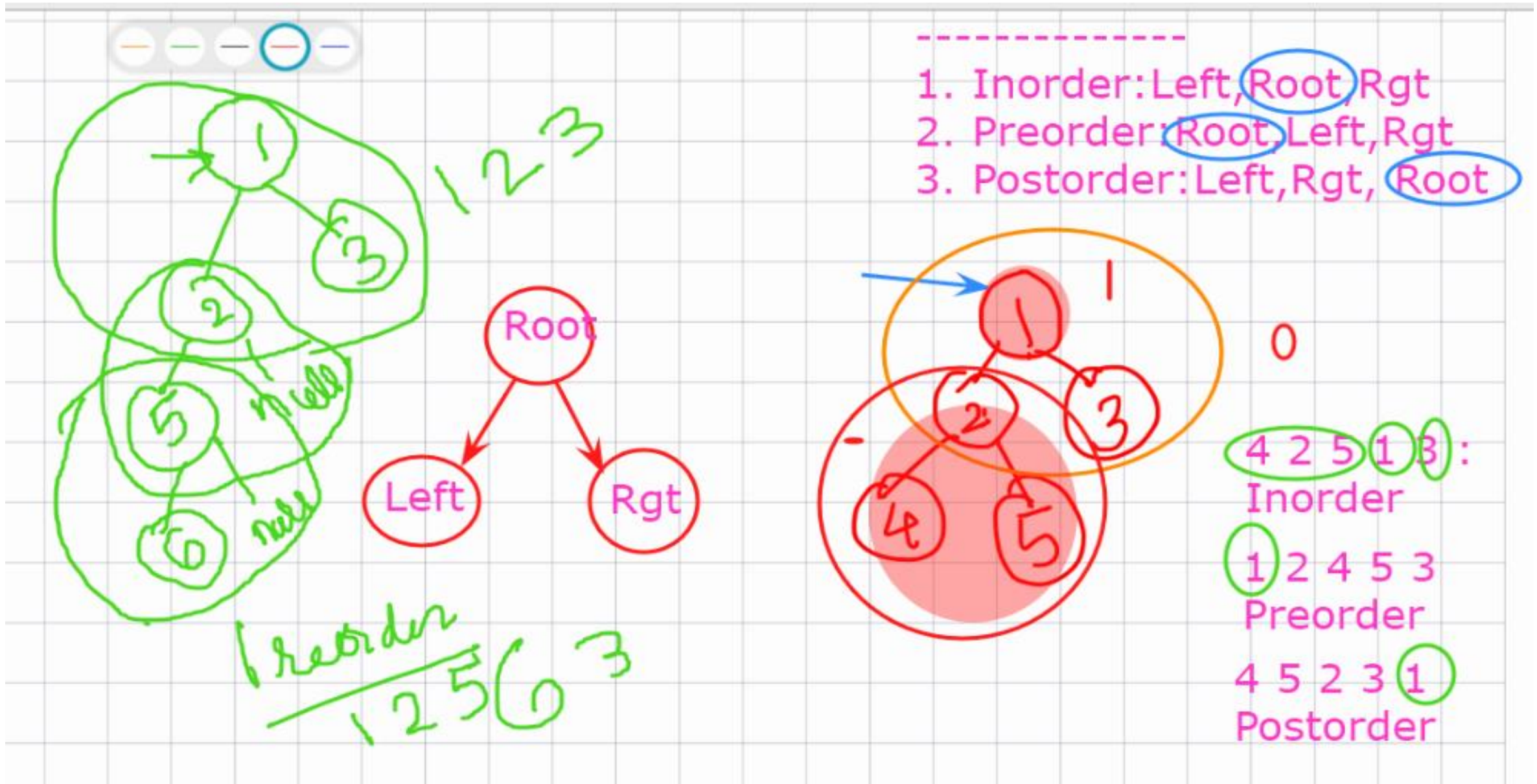




-
1. Inorder: Left, Root, Rgt
 2. Preorder: Root, Left, Rgt
 3. Postorder: Left, Rgt, Root



4 2 5 1 3 :
Inorder
1 2 4 5 3
Preorder
4 5 2 3 1
Postorder



```

{
    BT t1 = new BT();
    t1.root = new Node();
    t1.root.left = new Node();
    t1.root.right = new Node();
    t1.root.left.left = new Node();
    t1.root.left.right = new Node();

    System.out.println("Inorder Traversal:");
    t1.Inorder();
    System.out.println("Preorder Traversal:");
    t1.Preorder();
    System.out.println("Postorder Traversal:");
    t1.Postorder();
    System.out.println("Level Order Traversal:");
}
}

```

Command Prompt

C:\ADS>javac BT.java

C:\ADS>java BT

C:\ADS>javac BT.java

C:\ADS>java BT

Tree Traversal:

14 12 15 11 13 ✓

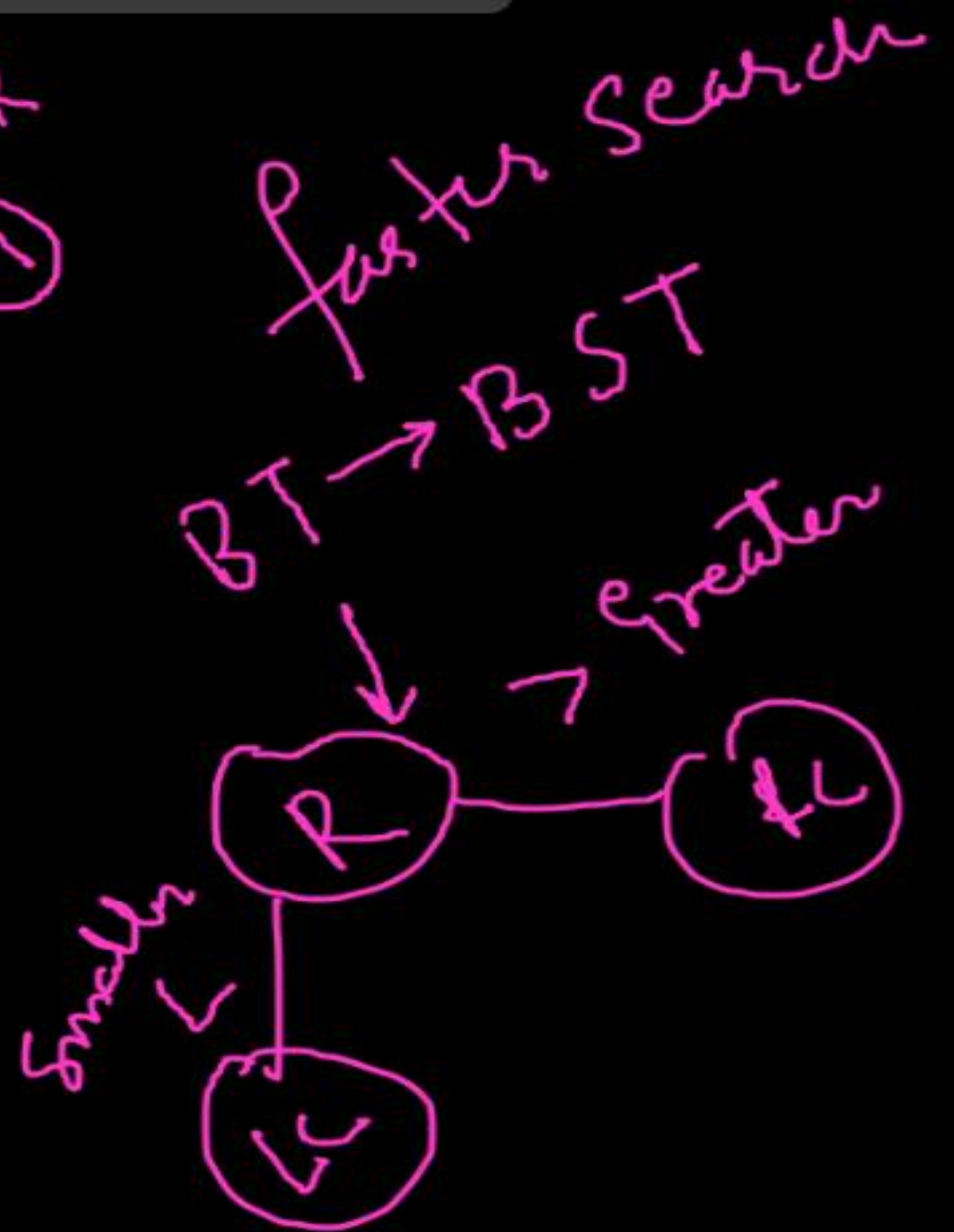
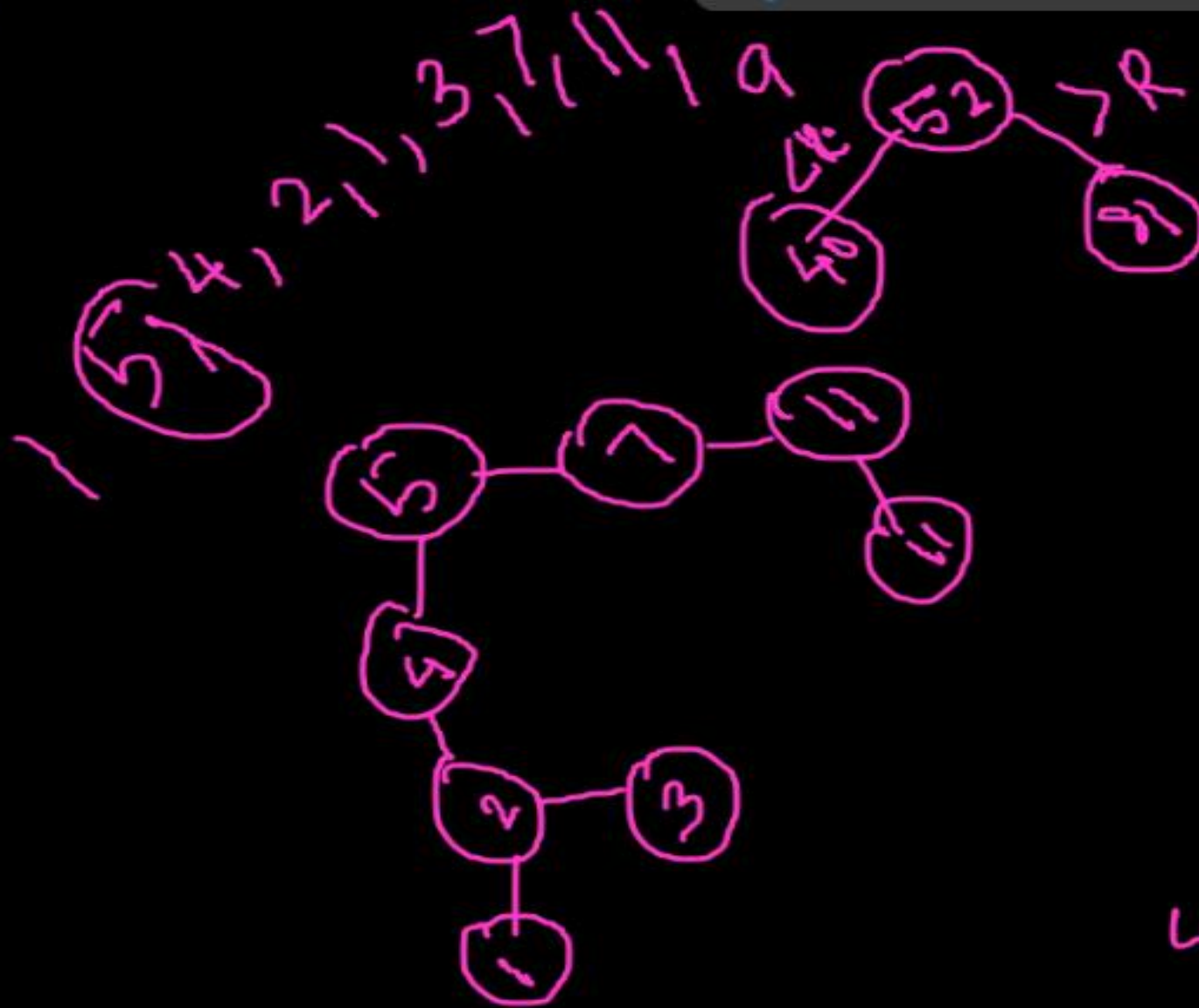
11 12 14 15 13 ✓

14 15 12 13 11 ✓

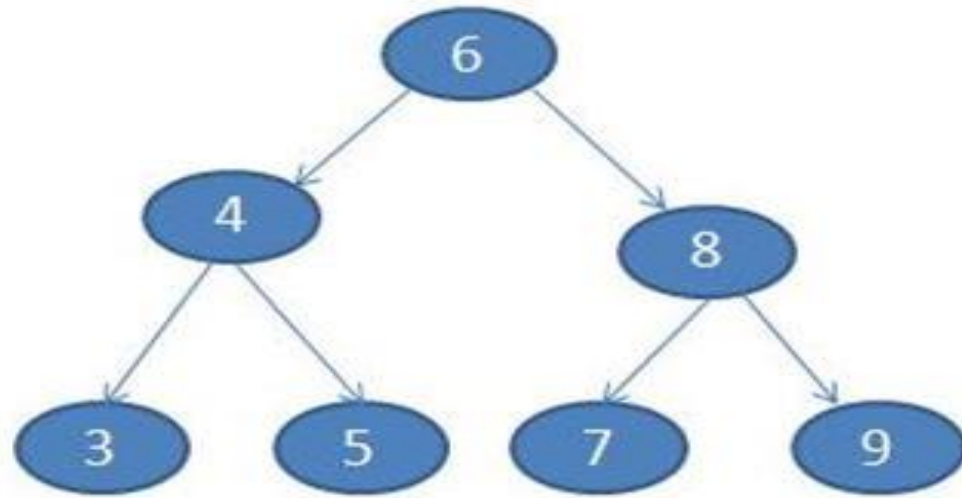
C:\ADS>



}



Tree Traversal



Preorder: Root-Left-Right

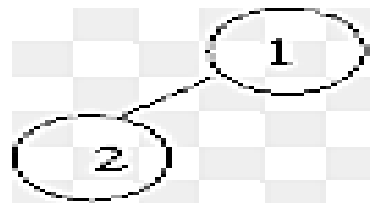
Inorder: Left-Root-Right

Postorder: Left-Right-Root

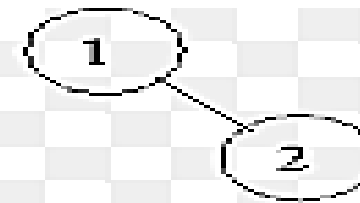
Preorder : 6, 4, 3, 5, 8, 7, 9

Inorder : 3, 4, 5, 6, 7, 8, 9

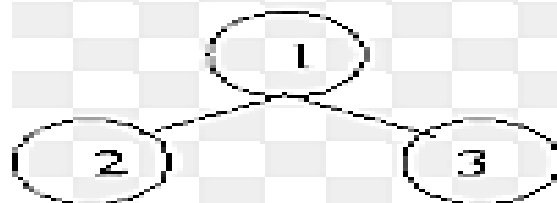
Postorder: 3, 5, 4, 7, 9, 8, 6



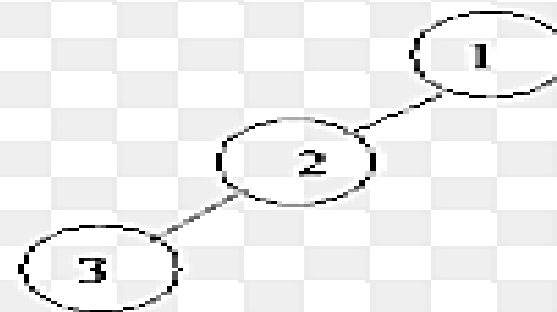
Pre: 12
Post: 21
In: 21



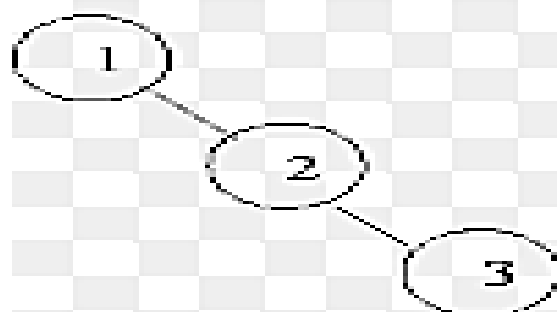
Pre: 12
Post: 21
In: 12



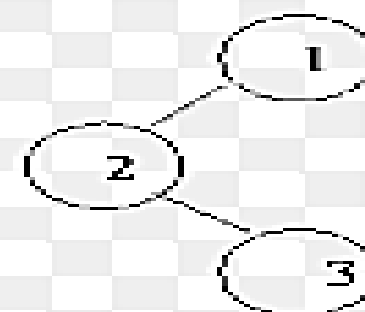
Pre: 123
Post: 231
In: 213



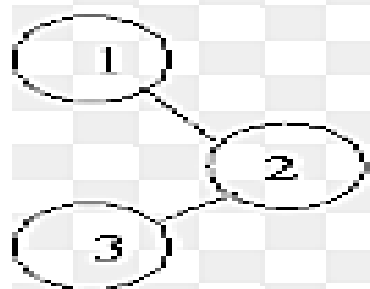
Pre: 123
Post: 321
In: 321



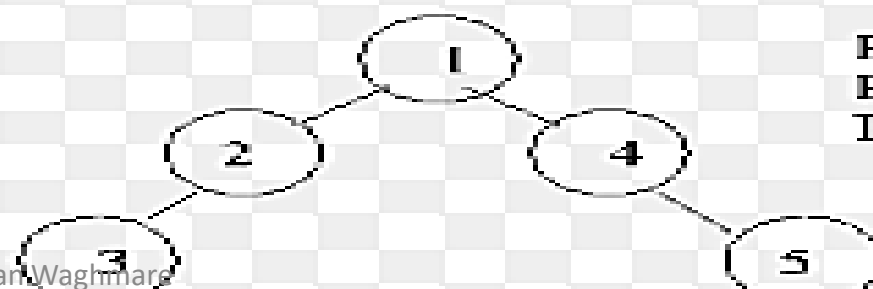
Pre: 123
Post: 321
In: 123



Pre: 123
Post: 321
In: 231

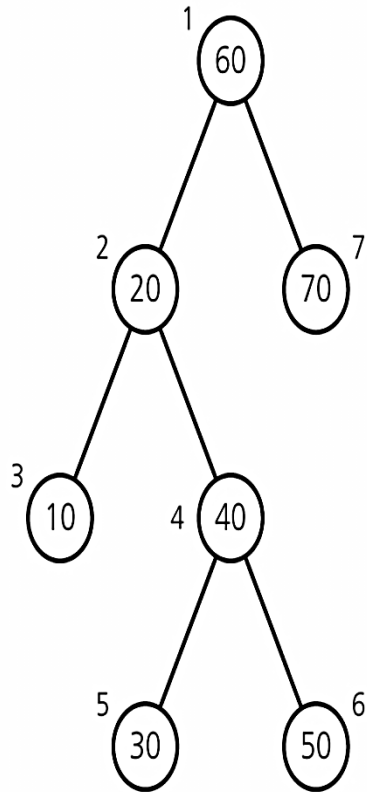


Pre: 123
Post: 321
In: 132

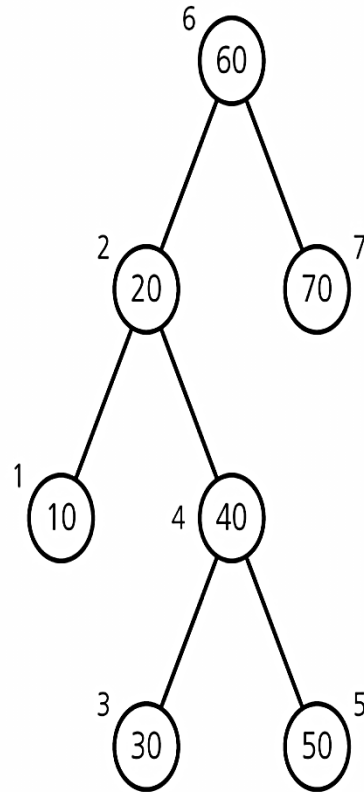


Pre: 12345
Post: 32541
In: 32145

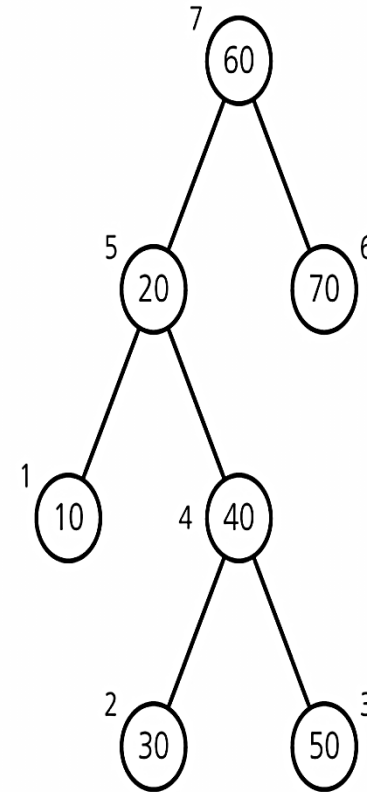
Binary Tree Traversals



(a) Preorder: 60, 20, 10, 40, 30, 50, 70



(b) Inorder: 10, 20, 30, 40, 50, 60, 70

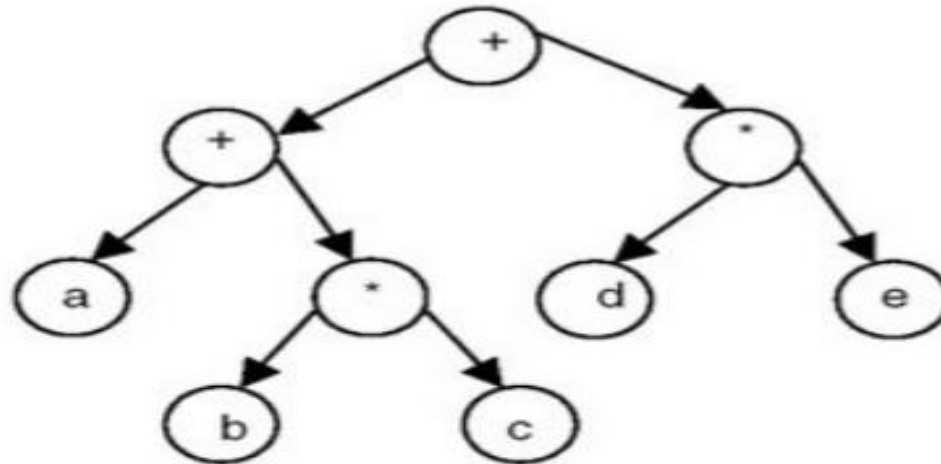


(c) Postorder: 10, 30, 50, 40, 20, 70, 60

(Numbers beside nodes indicate traversal order.)

Expression Binary Tree Traversal

If an expression is represented as a binary tree, the inorder traversal of the tree gives us an infix expression, whereas the postorder traversal gives us a postfix expression as shown in Figure.



Inorder : a + b * c + d * e

postorder : abc*+de*+

**Q. Example : Construct a Binary Search Tree by inserting the following sequence of numbers...
10,12,5,4,20,8,7,15 and 13**