

# **Class 8: Static Embeddings**

Theme: Text

Computational Analysis of Text, Audio, and Images, Fall 2023

Aarhus University

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Aarhus University

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Recap:

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1. What's the main reason we need to vectorize text when using machine learning?

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	0	1	2	3	4	5	6
$\overline{\mathcal{D}_1}$	1	1	1	0	0	0	0
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#### Two drawbacks:

- → Sparse and inefficient representation
- → Similar words have orthogonal representations

We want a representation of words that are short and dense which capture meaning and relations

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How can we obtain that?

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1. Learning representations for 'downstream' tasks (e.g. classification)

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Word embeddings are widely used in political science nowadays:

- 1. Learning representations for 'downstream' tasks (e.g. classification)
- 2. Learning word usage and meaning (semantics) directly

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"Embeddings" are designed to represent words in a short and dense format while still maintaining meaning and relations:

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• General term that refers to representing discrete features (e.g. word, document, actors) as a real-valued vector with d-dimensions:  $X \in \mathbb{R}^d$ 

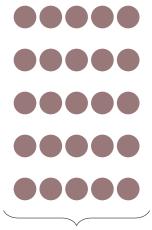
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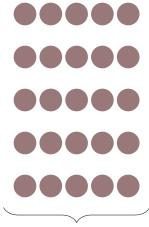
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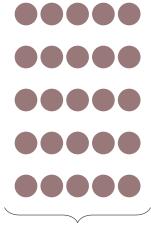
Collection of movies

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Collection of movies

Let's say we want to embed movies using d = 5 embeddings:

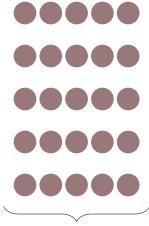


Collection of movies

Let's say we want to embed movies using d = 5 embeddings:

- 1. crime
- 2. comedy
- 3. drama
- 4. horror
- 5. romance

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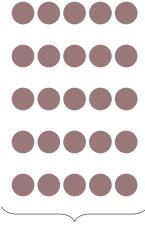


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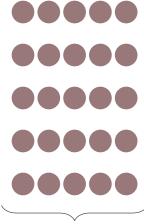
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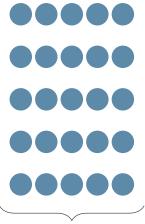
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- Dumb and Dumber (1994): [0.20, 0.90, 0.30, 0.01, 0.40]



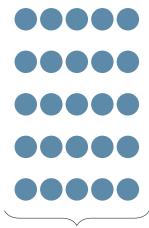
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- ▶ Not a probability distribution!

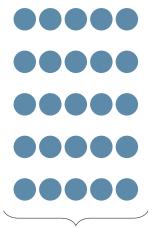


Collection of people



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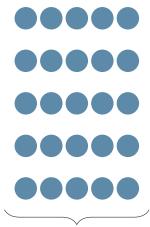
Person characteristics



Collection of people

#### Person characteristics

- 1. Age
- 2. Height (cm)
- 3. Weight (kg)
- 4. Skin color
- 5. Hair-color



Collection of people

#### Person characteristics

- 1. Age
- 2. Height (cm)
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- ▷ Embedding: [28, 184, 79, 0.1, 2]

The core idea about embeddings is that we want to represent words such that semantically related words are closer to each other

→ The distributional hypothesis:

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    - → "We know a word by the company it keeps" (Firth, 1957)
  - Formalizes the very intuitive idea that contexts give meaning to words
    - → Context ≠ co-occurrence

The semantic similarity conveyed by embeddings is a *powerful* and *flexible* tool:

• Semantic changes

- Semantic changes
- Semantic differences

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- Semantic differences
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- → How can we define similarity?
  - ▶ Cosine similarity!

#### Semantic Changes (Hamilton et al., 2016)

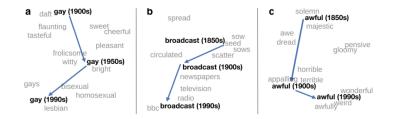
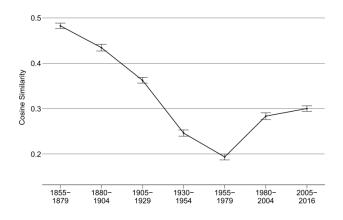
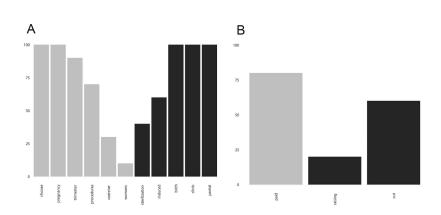


Figure 1: Two-dimensional visualization of semantic change in English using SGNS vectors.<sup>2</sup> a, The word gay shifted from meaning "cheerful" or "frolicsome" to referring to homosexuality. b, In the early 20th century broadcast referred to "casting out seeds"; with the rise of television and radio its meaning shifted to "transmitting signals". c, Awful underwent a process of pejoration, as it shifted from meaning "full of awe" to meaning "terrible or appalling" (Simpson et al., 1989).

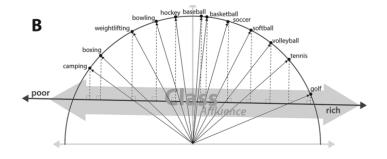
## "Equality" - "Social" Cosine Similarity (Rodman, 2020)



# Partisan Differences in Word Choice (Rodriguez and Spirling, 2022)

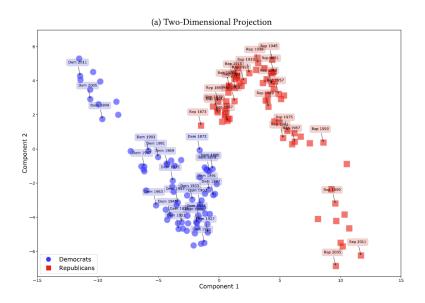


# Cultural Dimensions of Word Embeddings (Kozlowski et al., 2019)



## Ideology and Word Embeddings (Rheault and Cochrane, 2020)

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#### **Exercise**

Discuss with your neighbors how word embeddings can be combined with dictionaries.

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## **Analogies**

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- Starting at king means we are "walking" one step in the vector space along the gender dimension
- This means we can consider directions and not only distances

Discuss with your neighbor how we can construct neural networks that use the distributional hypothesis to generate embeddings:

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See tutorial for a hands-on example using PyTorch

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Word2Vec is one of the possible embedding algorithms that exist: learns *dense* representations that capture word *relations and meaning* 

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• Objective:

$$\frac{1}{T} \sum_{t=1}^{T} \sum_{-c \leq j \leq c, j \neq 0} \log(p(w_t \mid w_{t+j}))$$

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### **CBOW**

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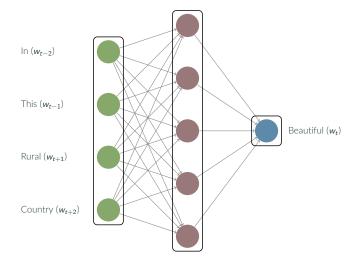
$$\frac{1}{T} \sum_{t=1}^{I} \sum_{-c < j < c, j \neq 0} \log(p(w_t \mid w_{t+j})) \qquad \frac{1}{T} \sum_{t=1}^{I} \sum_{-c < j < c, j \neq 0} \log(p(w_{t+j} \mid w_t))$$

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  - $p(w_{t+i} | w_t)$ : conditional probability context words given target word

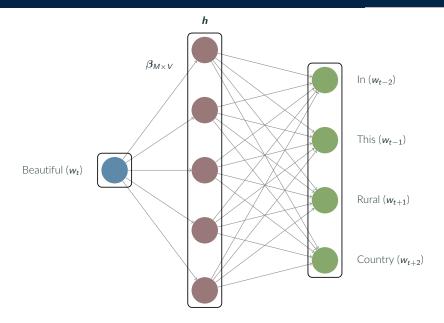
## **CBOW**

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# Skip-Gram

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Sentence: "I A mener vi altså ikke at skattelettelser og velfærd er

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Window size: 2

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Window size: 2

t-1 target



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Sentence: "I A mener vi altså ikke at skattelettelser og velfærd er modsætninger"

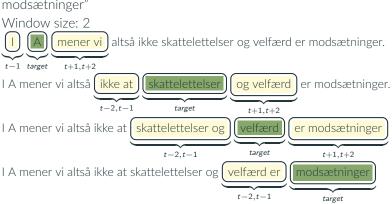
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t+1, t+2

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# **Negative Sampling**

## **Negative Sampling**





### **Positive Samples**



#### **Positive Samples**

- (ikke, skattelettelser)
- (at, skattelettelser)
- (og, skattelettelser)
- (velfærd, skattelettelser)



#### **Positive Samples**

- (ikke, skattelettelser)
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### **Negative Samples**

(???, skattelettelser)



#### **Positive Samples**

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- (kørekort, skattelettelser)
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- (zoo, skattelettelser)



#### **Positive Samples**

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- (???, skattelettelser)
- (kørekort, skattelettelser)
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The positive and negative samples constitute the training set – no labeling required! --> self-supervision

Working with embeddings in practice involves choosing between four "hyperparameters" (Rodriguez and Spirling, 2022):

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# See you next week!

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Computational Analysis of Text, Audio, and Images, Fall 2023 Aarhus University

### References i

- [1] W. L. Hamilton, J. Leskovec, and D. Jurafsky, "Diachronic word embeddings reveal statistical laws of semantic change," *arXiv* preprint arXiv:1605.09096, 2016.
- [2] E. Rodman, "A timely intervention: Tracking the changing meanings of political concepts with word vectors," *Political Analysis*, vol. 28, no. 1, pp. 87–111, 2020.
- [3] P. L. Rodriguez and A. Spirling, "Word embeddings: What works, what doesn't, and how to tell the difference for applied research," *The Journal of Politics*, vol. 84, no. 1, pp. 101–115, 2022.
- [4] A. C. Kozlowski, M. Taddy, and J. A. Evans, "The geometry of culture: Analyzing the meanings of class through word embeddings," *American Sociological Review*, vol. 84, no. 5, pp. 905–949, 2019.

### References ii

- [5] L. Rheault and C. Cochrane, "Word embeddings for the analysis of ideological placement in parliamentary corpora," *Political Analysis*, vol. 28, no. 1, pp. 112–133, 2020.
- [6] T. Mikolov, I. Sutskever, K. Chen, G. S. Corrado, and J. Dean, "Distributed representations of words and phrases and their compositionality," *Advances in neural information processing systems*, vol. 26, 2013.