

Critical Thinking Module 2 Option 1

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CSC 580: Applying Machine Learning and Neural Networks - Capstone

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1) What is the accuracy of the model?

As can be seen in Figure 1, the accuracy of the model was 94.75% after twenty epochs. As can be seen, the model accuracy increases as the number of epochs increases. The accuracy seems to increase faster during the earlier epochs and slower during the later epochs. In fact, the accuracy seems to only marginally increase after the fifteenth epoch.

```
Training epoch 1  
Accuracy: 0.8919  
Training epoch 2  
Accuracy: 0.9112  
Training epoch 3  
Accuracy: 0.9224  
Training epoch 4  
Accuracy: 0.9281  
Training epoch 5  
Accuracy: 0.9319  
Training epoch 6  
Accuracy: 0.9328  
Training epoch 7  
Accuracy: 0.9369  
Training epoch 8  
Accuracy: 0.9365  
Training epoch 9  
Accuracy: 0.9392  
Training epoch 10  
Accuracy: 0.9392  
Training epoch 11  
Accuracy: 0.9425  
Training epoch 12  
Accuracy: 0.9419  
Training epoch 13  
Accuracy: 0.9426  
Training epoch 14  
Accuracy: 0.9451  
Training epoch 15  
Accuracy: 0.9459  
Training epoch 16  
Accuracy: 0.9434  
Training epoch 17  
Accuracy: 0.9451  
Training epoch 18  
Accuracy: 0.9466  
Training epoch 19  
Accuracy: 0.9485  
Training epoch 20  
Accuracy: 0.9475
```

Figure 1: Accuracy of the model over twenty epochs

2) What are some of the misclassified images?

As can be seen in Figure 2, many of the misclassified images have part of the handwritten digit distorted in some way. For example in sample 8, the lower part of the digit is much smaller than expected. In sample 80, the upper part of the digit has curves down. In sample 92, the digit is rotated approximately forty-five degrees. Finally in sample 115, the upper part of the digit is a bit larger than usual.

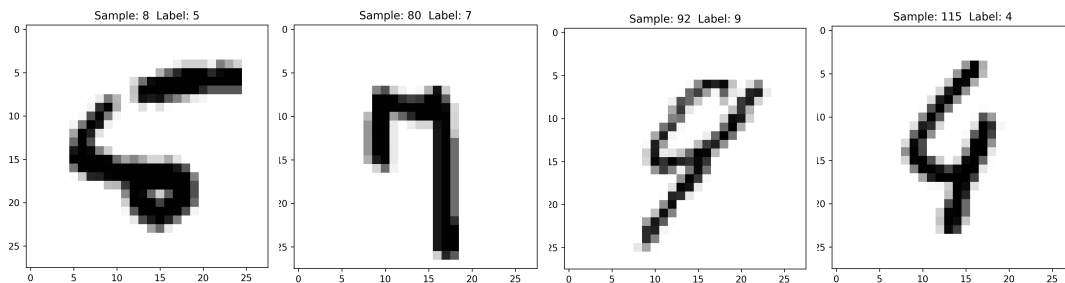


Figure 2: Misclassified images

3) How is the accuracy affected by using more hidden neurons? Fewer hidden neurons?

As can be seen in Figure 3, using only 64 hidden neurons resulted in lower accuracy. Hence, decreasing the amount of hidden neurons decreases the accuracy. Additionally, the training speed was much faster using only 64 hidden neurons compared to 512. As can be seen in Figure 6, using 4096 hidden neurons resulted in higher accuracy. Hence, increasing the amount of hidden neurons increases the accuracy. However, the training speed was much slower using 4096 hidden neurons compared to 512.

Training epoch 20
Accuracy: 0.9473

Figure 3: Accuracy of training 64 hidden neurons

Training epoch 20
Accuracy: 0.9475

Figure 4: Accuracy of training 512 hidden neurons

```
Training epoch 20  
Accuracy: 0.9686
```

Figure 5: Accuracy of training 4096 hidden neurons

4) How is the accuracy affected by using different learning rates? Try a range of at least four values.

As can be seen in Figure 7, Figure 8, and Figure 9, changing the learning rate between 0.05 to 1 did very little to impact the accuracy of the model. As can be seen in Figure 6, a lower learning rate of 0.005 resulted in a lower accuracy after 20 epochs because the model did not get fully trained. The accuracy may have improved after 20 epochs, but 20 epochs was not long enough to train the 0.005 learning rate. As can be seen in Figure 7, the learning rate that resulted in the best accuracy for twenty epochs was 0.05.

```
Training epoch 20  
Accuracy: 0.9138
```

Figure 6: Accuracy after 20 epochs with a learning rate of 0.005

```
Training epoch 20  
Accuracy: 0.95
```

Figure 7: Accuracy after 20 epochs with a learning rate of 0.05

```
Training epoch 20  
Accuracy: 0.9475
```

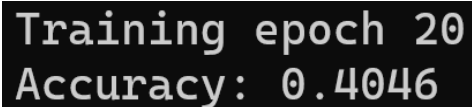
Figure 8: Accuracy after 20 epochs with a learning rate of 0.5

```
Training epoch 20  
Accuracy: 0.9493
```

Figure 9: Accuracy after 20 epochs with a learning rate of 1

5) How is accuracy affected by adding another hidden layer?

In the two hidden layer model, my first hidden layer had an output dimensionality of one hundred. The second hidden layer had a dimensionality of ten. As can be seen in Figure 10, accuracy after 20 epochs was much lower with the hidden layers. By adding another layer, the complexity of the model increases. There are more trainable parameters when another hidden layer is added.

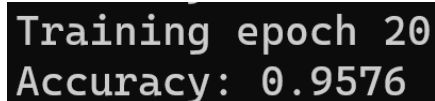


```
Training epoch 20
Accuracy: 0.4046
```

Figure 10: Accuracy at epoch 20 with a second hidden layer

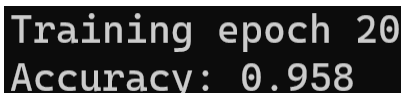
6) How is accuracy affected by using different batch sizes? Try at least three different batch sizes.

As can be seen in Figure 11, Figure 12, Figure 13, and Figure 14, the two smallest batch sizes had the best accuracy and the largest batch size had the worst accuracy. Hence, accuracy seems to improve with smaller batch sizes. However, it seems that as batch size decreases, the training time increases. The smaller batch sizes took much longer to train than the larger batch sizes.



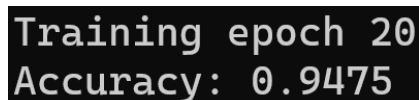
```
Training epoch 20
Accuracy: 0.9576
```

Figure 11: Accuracy after 20 epochs with a batch size of 10



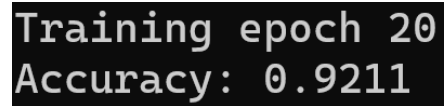
```
Training epoch 20
Accuracy: 0.958
```

Figure 12: Accuracy after 20 epochs with a batch size of 30



```
Training epoch 20
Accuracy: 0.9475
```

Figure 13: Accuracy after 20 epochs with a batch size of 100

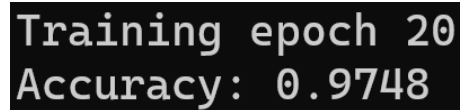


Training epoch 20
Accuracy: 0.9211

Figure 14: Accuracy after 20 epochs with a batch size of 1000

7) What is the best accuracy you can get from this multi-layer perceptron?

As can be seen in Figure 15, the best accuracy I was able to get from the multi-layer perceptron was 97.48%. I used a learning rate of 0.05, a batch size of 30, and 4096 hidden neurons. The model took a very long time to train, but it resulted in the best accuracy.



Training epoch 20
Accuracy: 0.9748

Figure 15: Best accuracy after 20 epochs