# Phylogenetic inference using maximum likelihood

### **Comparative Genomic Analyses**

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# Phylogeny inference

Sequences evolve according to an unknown tree, so within the phylogenetic framework, we want to estimate it.

- tree structure or topology
- branch lengths
- model of sequence evolution (JC, GTR ...) and respective parameters

## Maximum likelihood principle

The likelihood function tells us the probability of the data given a set of parameters.

$$L = p(D|\tau,\theta)$$

- D is a set of aligned sequences
- ightharpoonup au represents the tree: branch lengths and topology
- lacktriangledown represents the model of evolution parameters: substitution rates

## Maximum likelihood principle

Some parameters produce the sequences with higher probability than others.

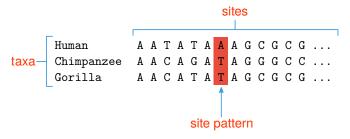
we want the tree topology, branch lengths, and model parameters that best explain the observed the sequences: i.e.,  $\hat{\tau}$  and  $\hat{\theta}$  that maximize the **likelihood function** 

$$L = p(D|\hat{\tau}, \hat{\theta})$$

 $ightharpoonup \hat{\tau}$  and  $\hat{\theta}$  are the maximum likelihood estimates

## Alignment and site patterns

A sequence alignment includes information from N taxa and S sites.



▶ a site pattern includes information from a single site an alignment is a collection of site patterns

# Alignment and site patterns

The probability of the whole alignment can be obtained from the probability of each site pattern.

$$p(D| au, heta) = \prod_{i=1}^{S} p(d_i| au, heta)$$

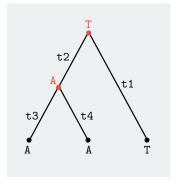
- $\triangleright$  D is the whole alignment and  $d_i$  the *i*-th site pattern
- assume independent evolution at each site

The goal is to compute the probability of each and every observed site patterns in an alignment of N sequences.

$$p(D|\tau,\theta) = p(\{AAA\}|\tau,\theta) \times p(\{AAA\}|\tau,\theta) \times p(\{TCC\}|\tau,\theta)...$$

ightharpoonup calculating  $p(d_i|\tau,\theta)$  is a small likelihood problem

The probability of a site pattern given the tree, the model of evolution and the ancestral states.



$$p(\{A,T,T\}|\tau,\theta) = p(T \to T|t_1) \times p(T \to A|t_2) \times p(A \to A|t_3) \times p(A \to A|t_4)$$

#### **Exercise**

The pyrimidine  $Y = \{C, T\}$  and purine  $P = \{A, G\}$  content in a certain site of a protein coding genes, was observed for three species:  $\{S_1, S_2, S_3\} = \{P, P, Y\}$ . Despite one does not know the species tree and the ancestral states, six scenarios for the evolution of this site were proposed:

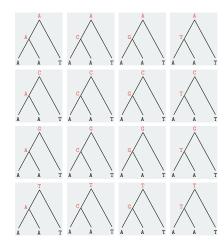
Y				P			Y		
1				1			1		
						-			
PΙ		1	PΙ			Υ		1	
1	1	1	- 1	1	1	- 1	1	1	
S1	S2	S3	S1	S2	S3	S1	S2	S3	
P			Υ				P		
1		1				1			
						-			
PΙ		1	Υļ	Υ		Υļ	Υļ		
		1							
1	1	1		1	1	1	1	1	
S1		S2		S3	S2	S1	S3	S2	

Assuming that transitions between pyrimidines and purines occur with probability

what is the most likely scenario?

We know how to calculate the likelihood of a site patterns when the ancestral states and the topology are both known.

- the ancestral states are unknown
- ▶ there are n − 1 internal nodes in a tree with n taxa meaning that there are 4<sup>n-1</sup> possible sets of ancestral states
- efficient algorithms exist:
  Felsenstein's pruning algorithm
   Felsenstein (1981)



### A possible approach to finding the maximum likelihood tree:

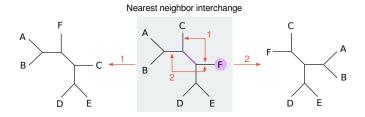
- maximizing the likelihood of an alignment for a given tree and model parameters is feasible, but we want the tree that best describes the data
- try out several trees and find the one that maximizes the likelihood function

Searching for the maximum likelihood tree has some computational limitations:

- there is a huge space of possible topologies
- testing all possible trees is just impossible, even for moderately sized data sets

Number of taxa	possible unrooted trees
3	1
5	15
10	2 027 025
50	8.5 x 10 <sup>74</sup>
100	5.1 x 10 <sup>182</sup>

Because testing all the possible trees is not computationally feasible, several algorithms are used to suggest reasonable trees.



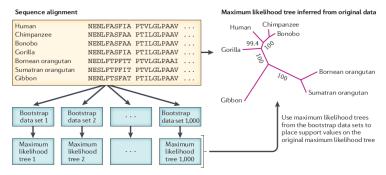
► **full-tree arrangement operations**: change the structure of a given tree within its neighborhood

Several measures are used to assess the certainty of a tree or its clades: the most widely used approach is the **bootstrapping**.

Efron (1979) and Felsenstein (1985)

- pseudo-alignments are created by subsetting the alignment
- pseudo-trees are inferred for each pseudo-alignment
- bootstraps represent the number of times a certain clade is present in the pseudo-trees

### Bootstrapping phylogenetic trees:



Yang & Rannala (2012)

### Literature

**The Phylogenetic Handbook** by Lemey, Salemi and Vandamme (2009) Cambridge University Press

► Chapter 6: sections 6.1, 6.2 and 6.3, 6.4 and 6.5