



Malaria Molecular Surveillance Study Design Workshop

Module 4: Power

Remember ...

		Conclusion about H_0	
		Fail to reject	Reject
Truth about H_0	True	True negative $1 - \alpha$	False positive α
	False		

α sets the **false positive rate** of a test. Using α we can control how often we incorrectly conclude that there is a real effect when there is none.

Power



In power analysis, we also specify an **alternative hypothesis**

H_0 : The population prevalence equals p_0

H_1 : The population prevalence equals p , which is different from p_0

Power



In power analysis, we also specify an **alternative hypothesis**

H_0 : The population prevalence equals p_0

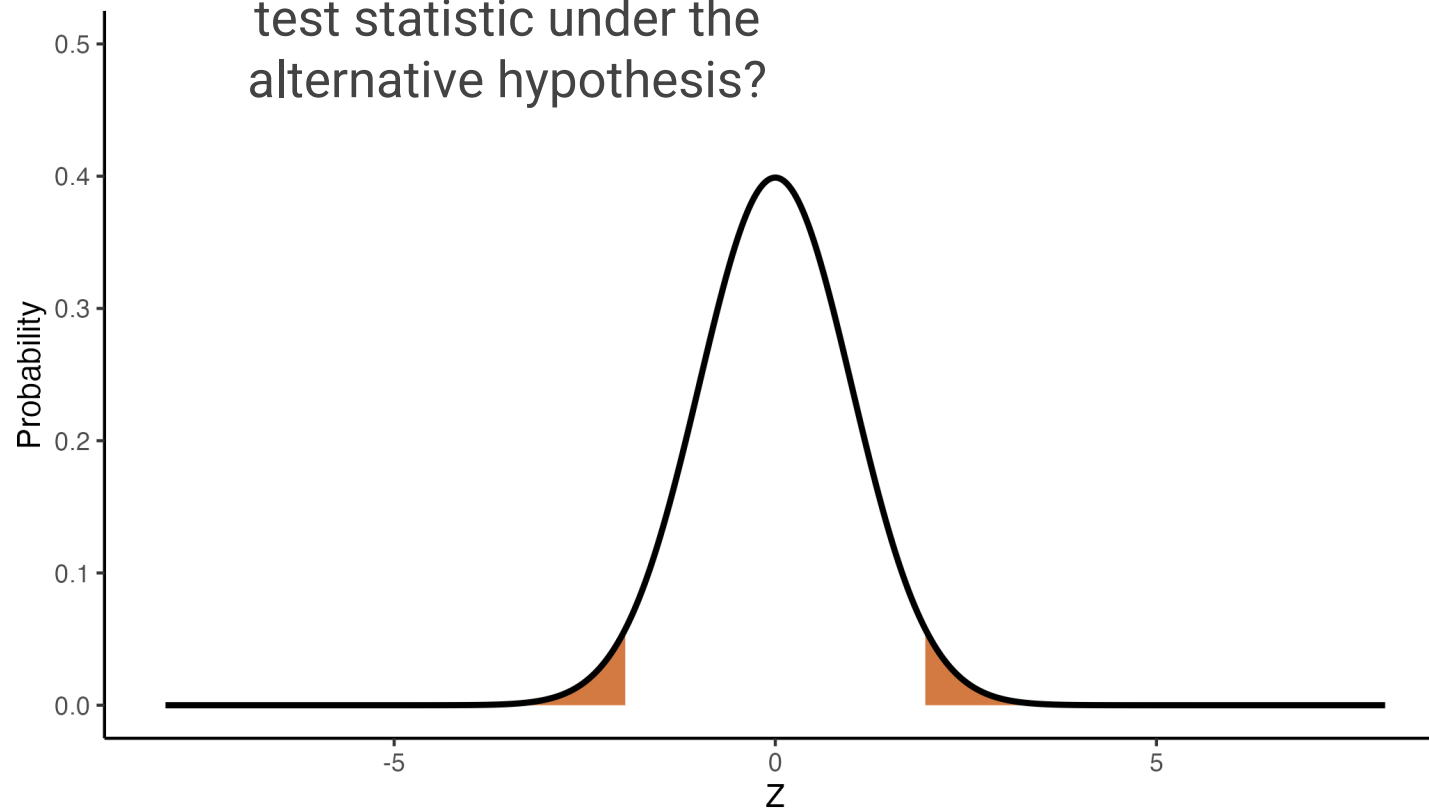
H_1 : The population prevalence equals p , which is different from p_0

For example...

I want to test if the prevalence of *pfprt* K76T mutations is significantly different from 10%. When powering this test, I assume the true prevalence of K76T mutations is 15%.

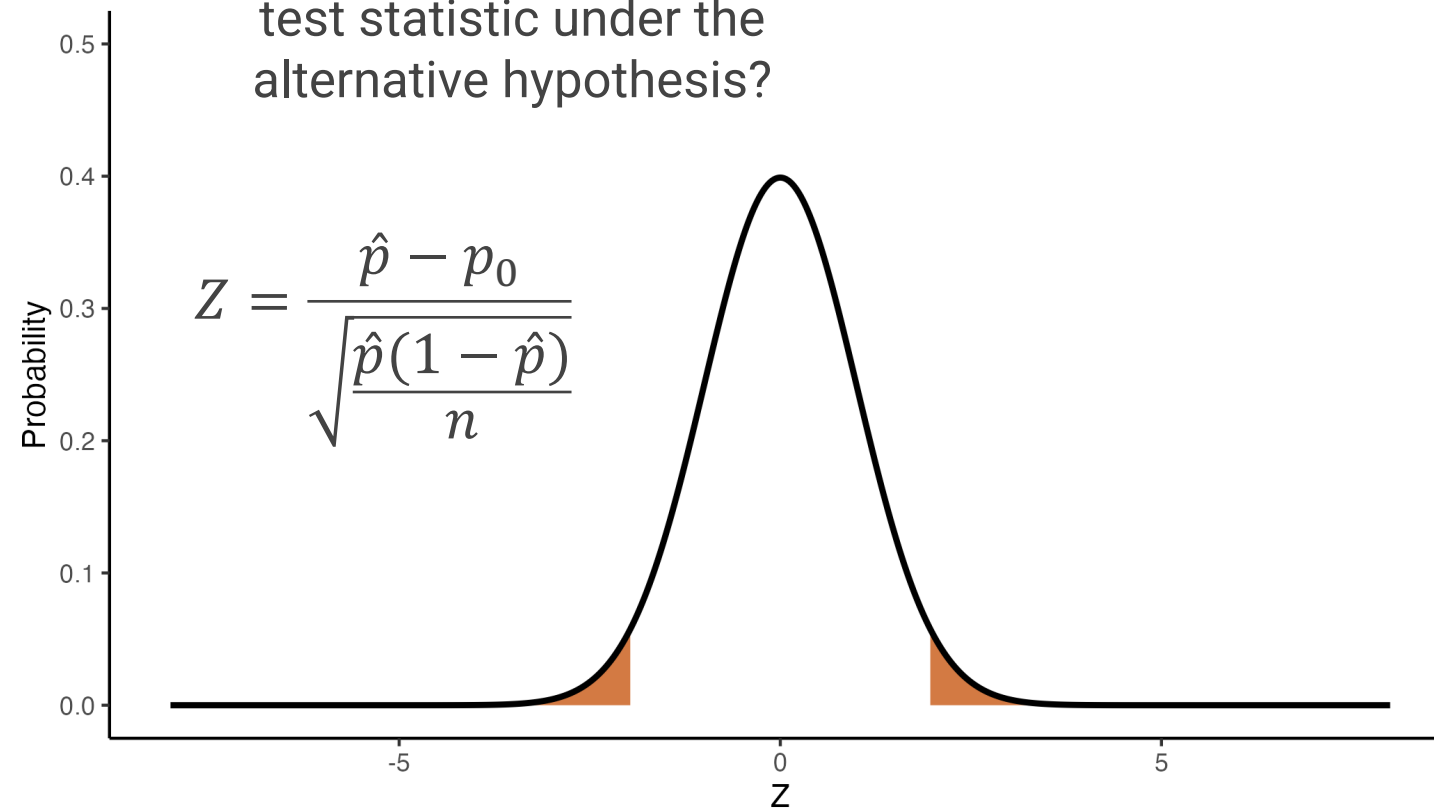
Power

What is the distribution of my test statistic under the alternative hypothesis?



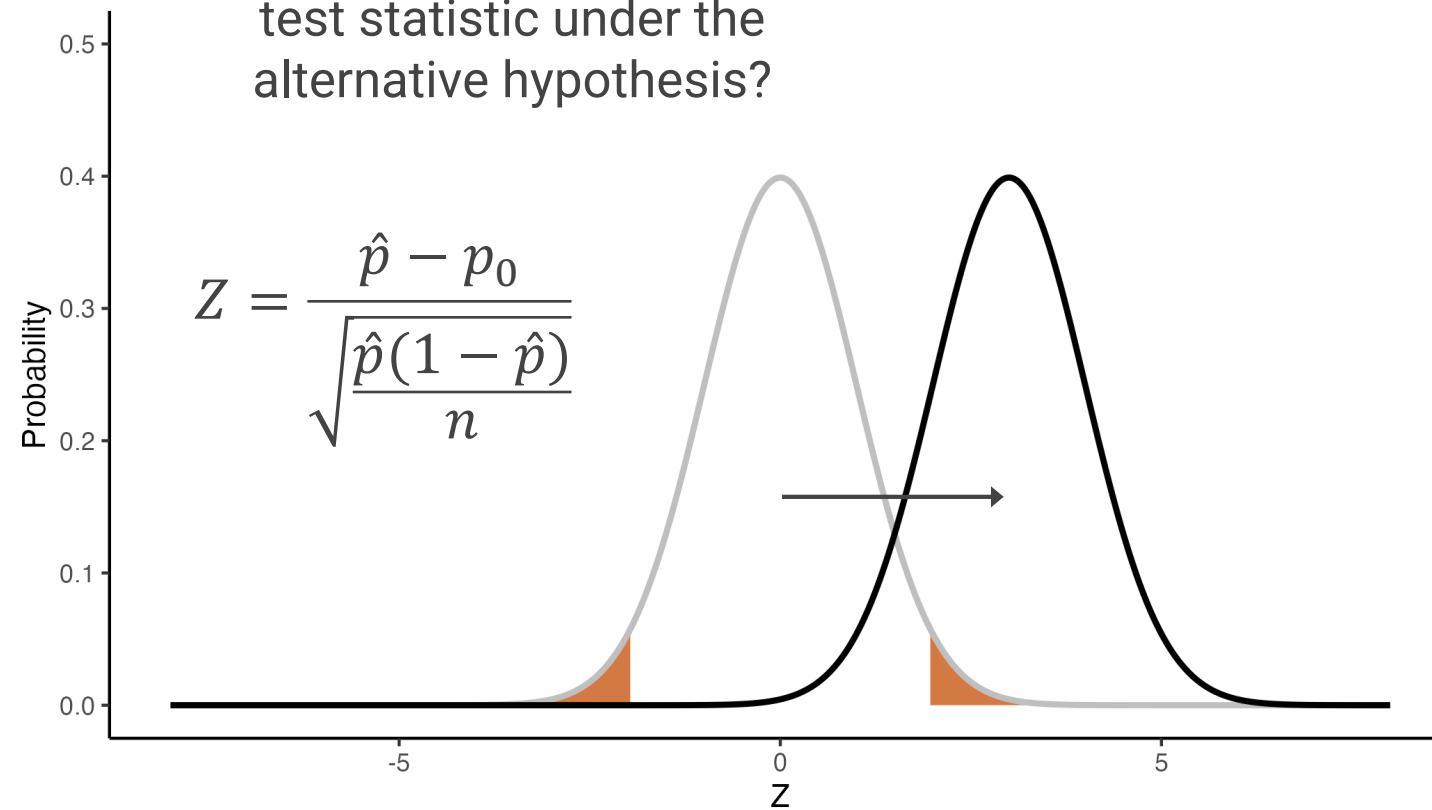
Power

What is the distribution of my test statistic under the alternative hypothesis?

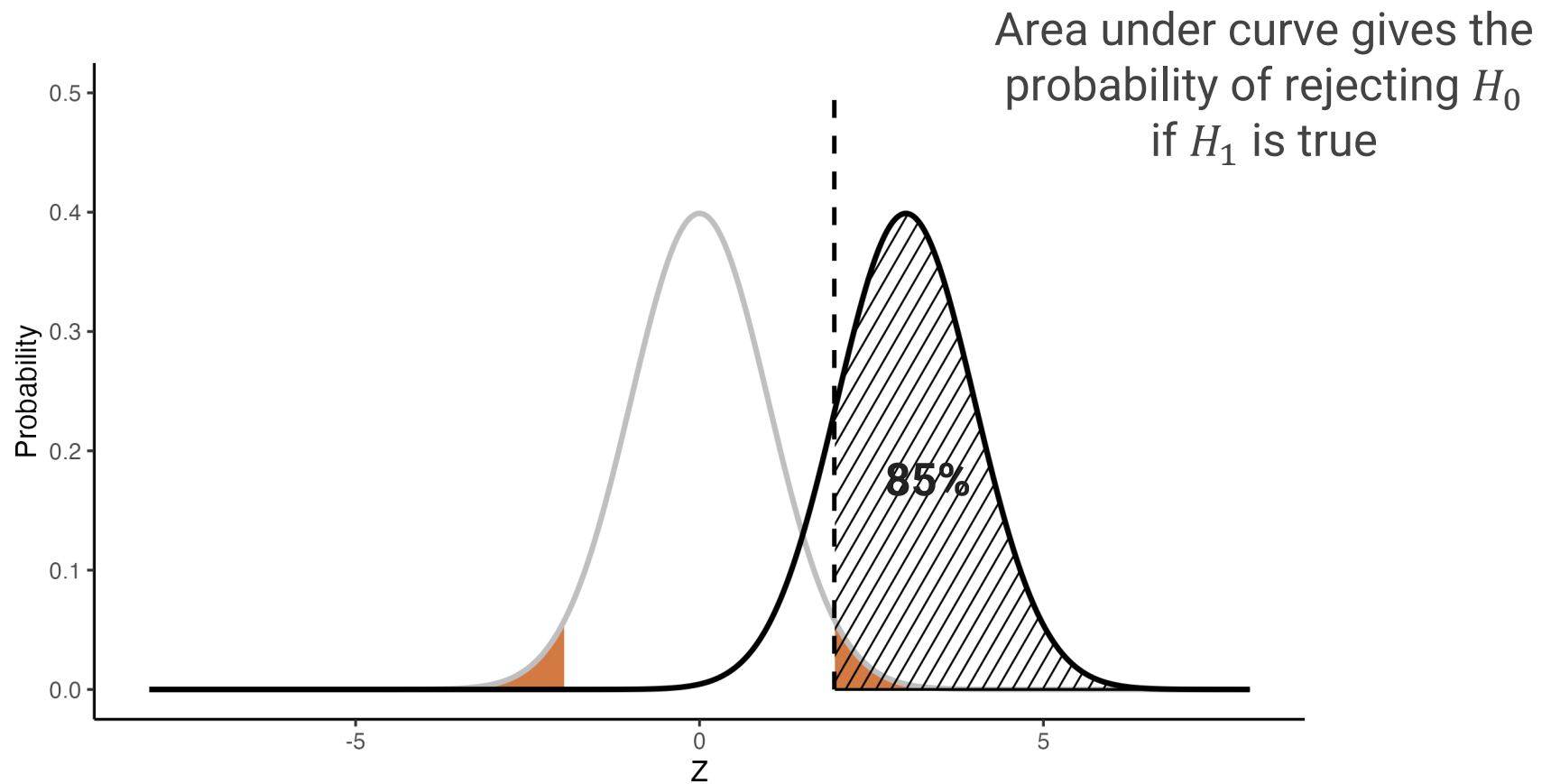


Power

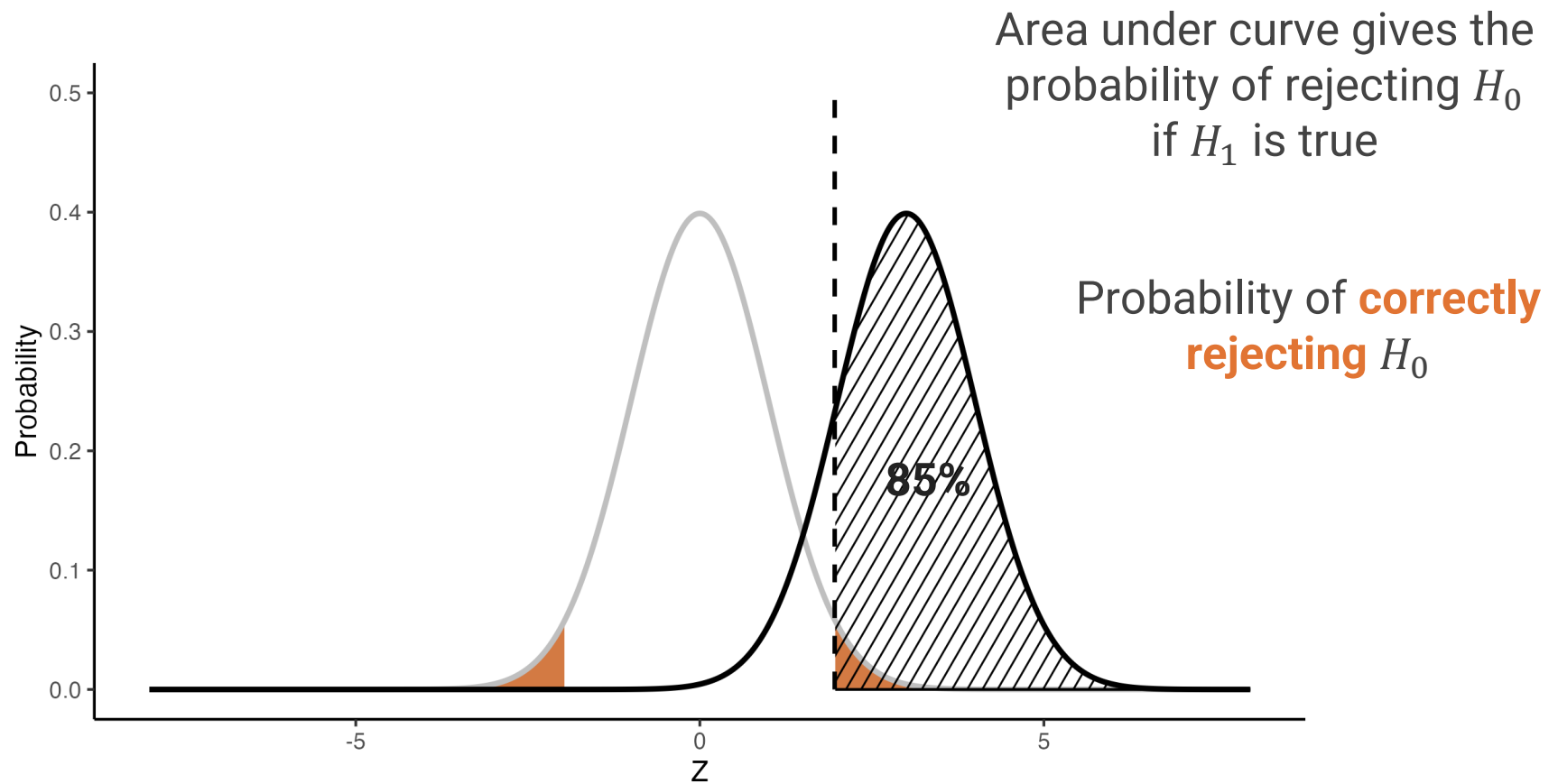
What is the distribution of my test statistic under the alternative hypothesis?



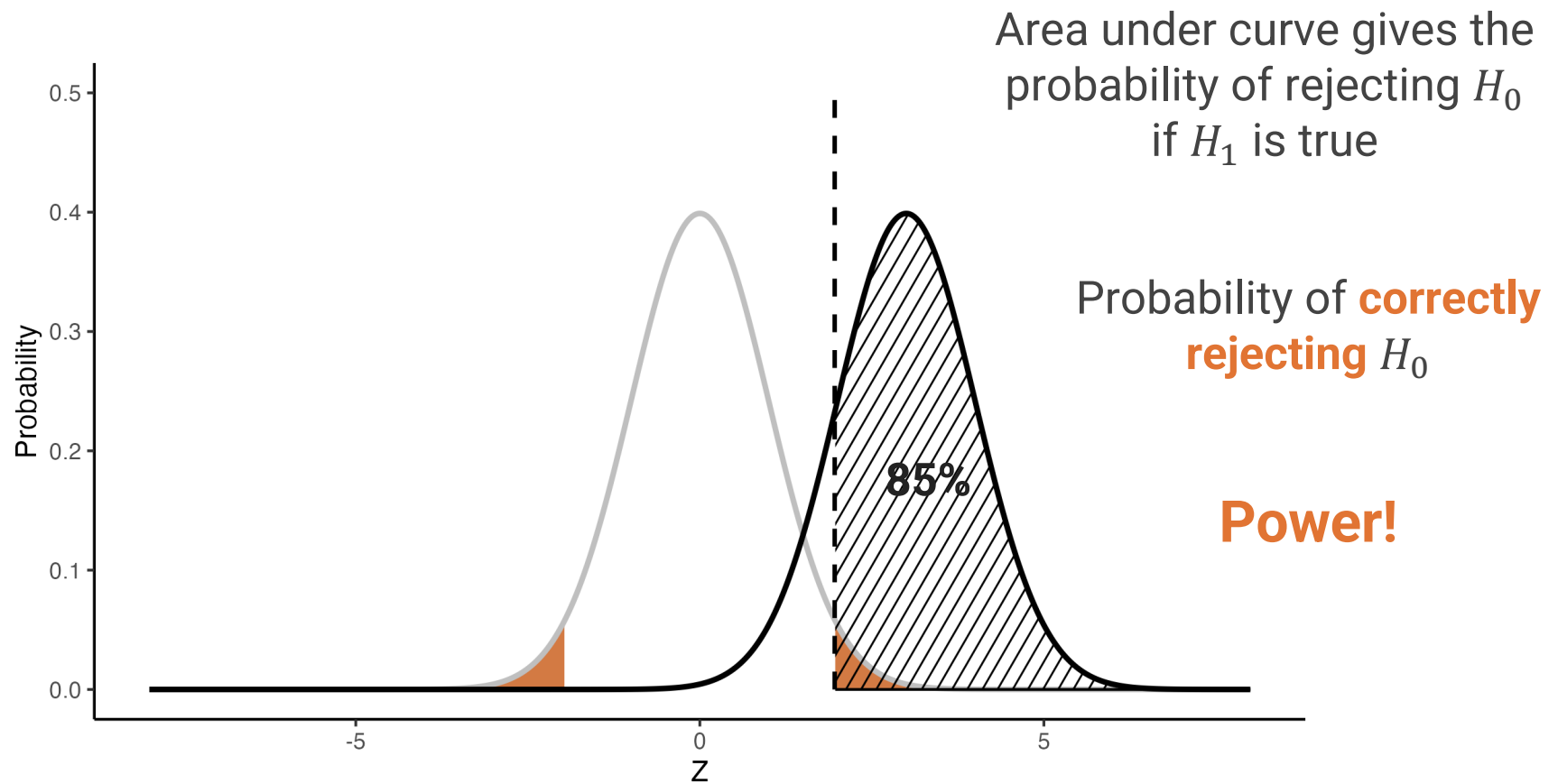
Power



Power



Power



Power



		Conclusion about H_0	
		Fail to reject	Reject
Truth about H_0	True	True negative $1 - \alpha$	False positive α
	False		

Power

		Conclusion about H_0	
		Fail to reject	Reject
Truth about H_0	True	True negative $1 - \alpha$	False positive α
	False	False negative	True positive

Power

		Conclusion about H_0	
		Fail to reject	Reject
Truth about H_0	True	True negative $1 - \alpha$	False positive α
	False	False negative $1 - \text{Power}$	True positive Power

Power

		Conclusion about H_0	
		Fail to reject	Reject
Truth about H_0	True	True negative $1 - \alpha$	False positive α
	False	False negative $1 - \text{Power}$	True positive Power

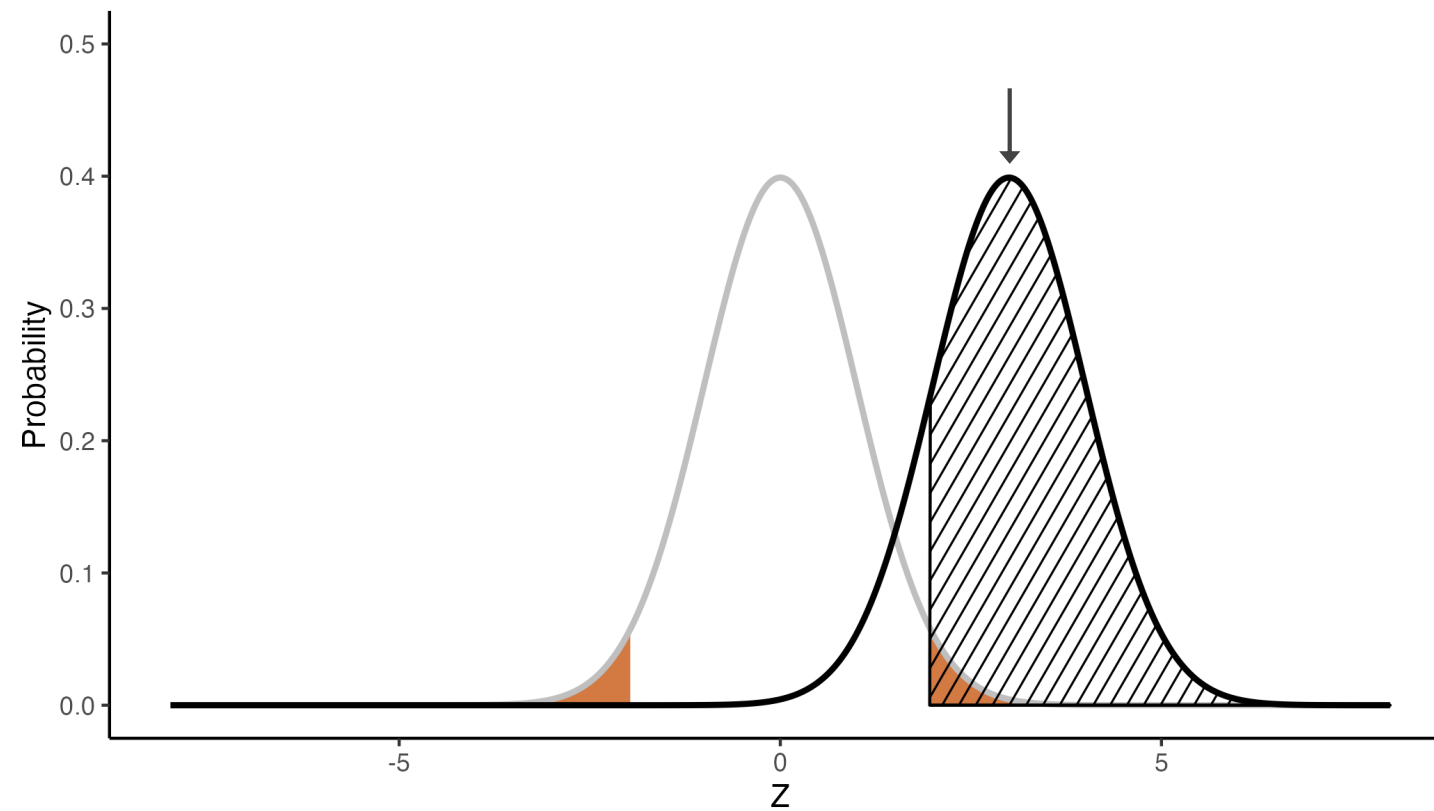
Power is the probability of **correctly rejecting** the null hypothesis. It is the chance that we find something interesting, given that it is there.

Power

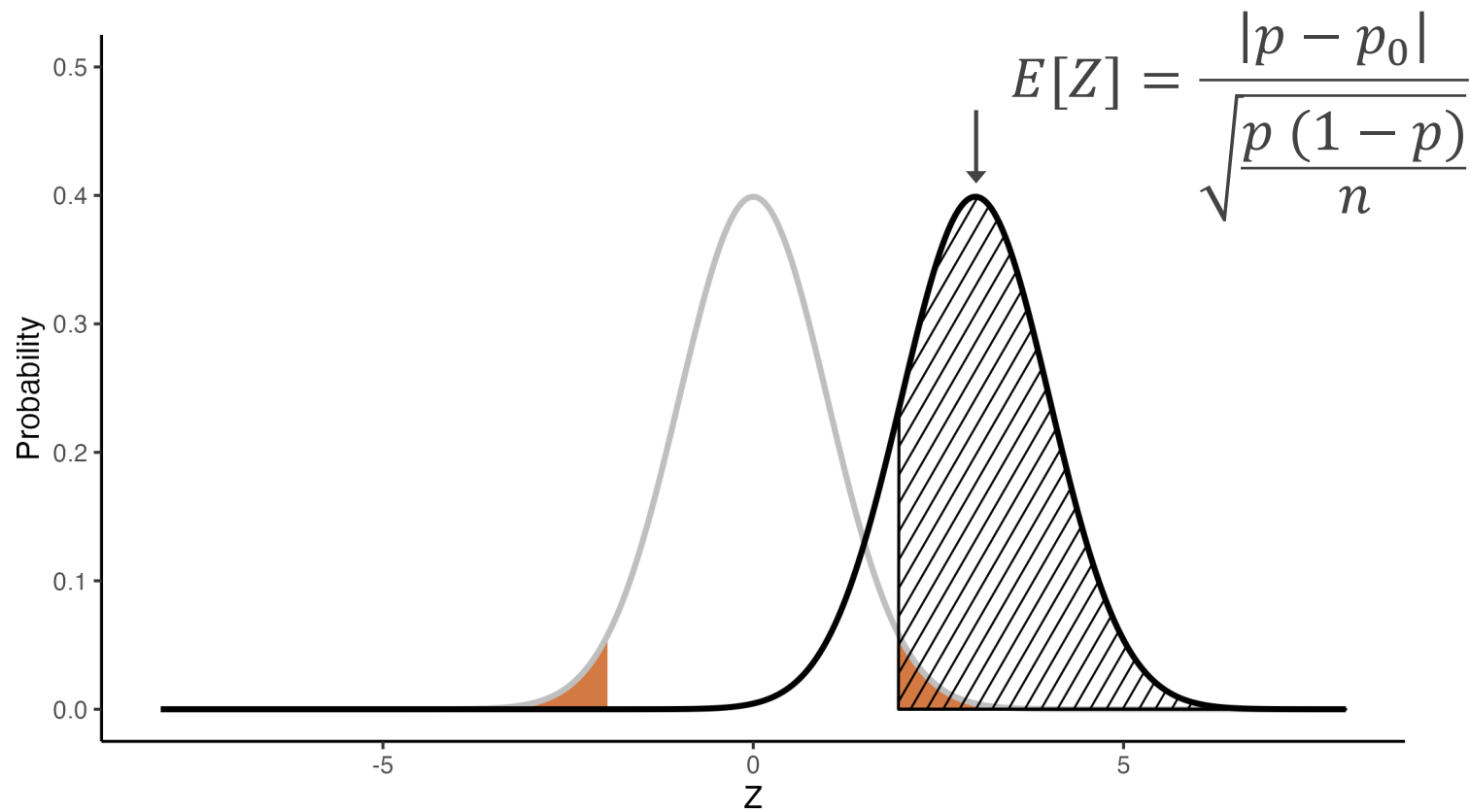
		Conclusion about H_0	
		Fail to reject	Reject
Truth about H_0	True	True negative $1 - \alpha$	False positive α
	False	False negative β	True positive $1 - \beta$

Power is the probability of **correctly rejecting** the null hypothesis. It is the chance that we find something interesting, given that it is there.

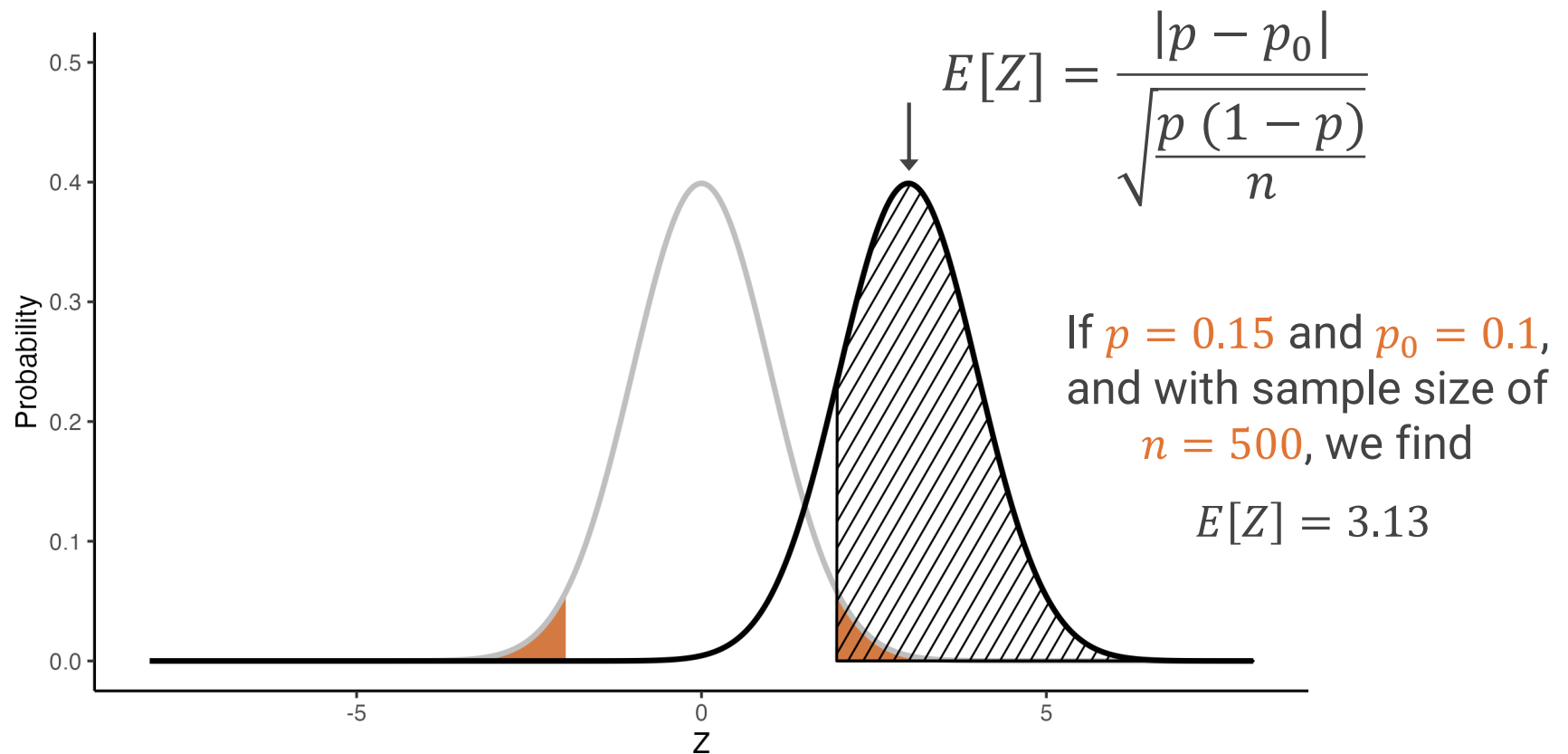
How do we calculate power?



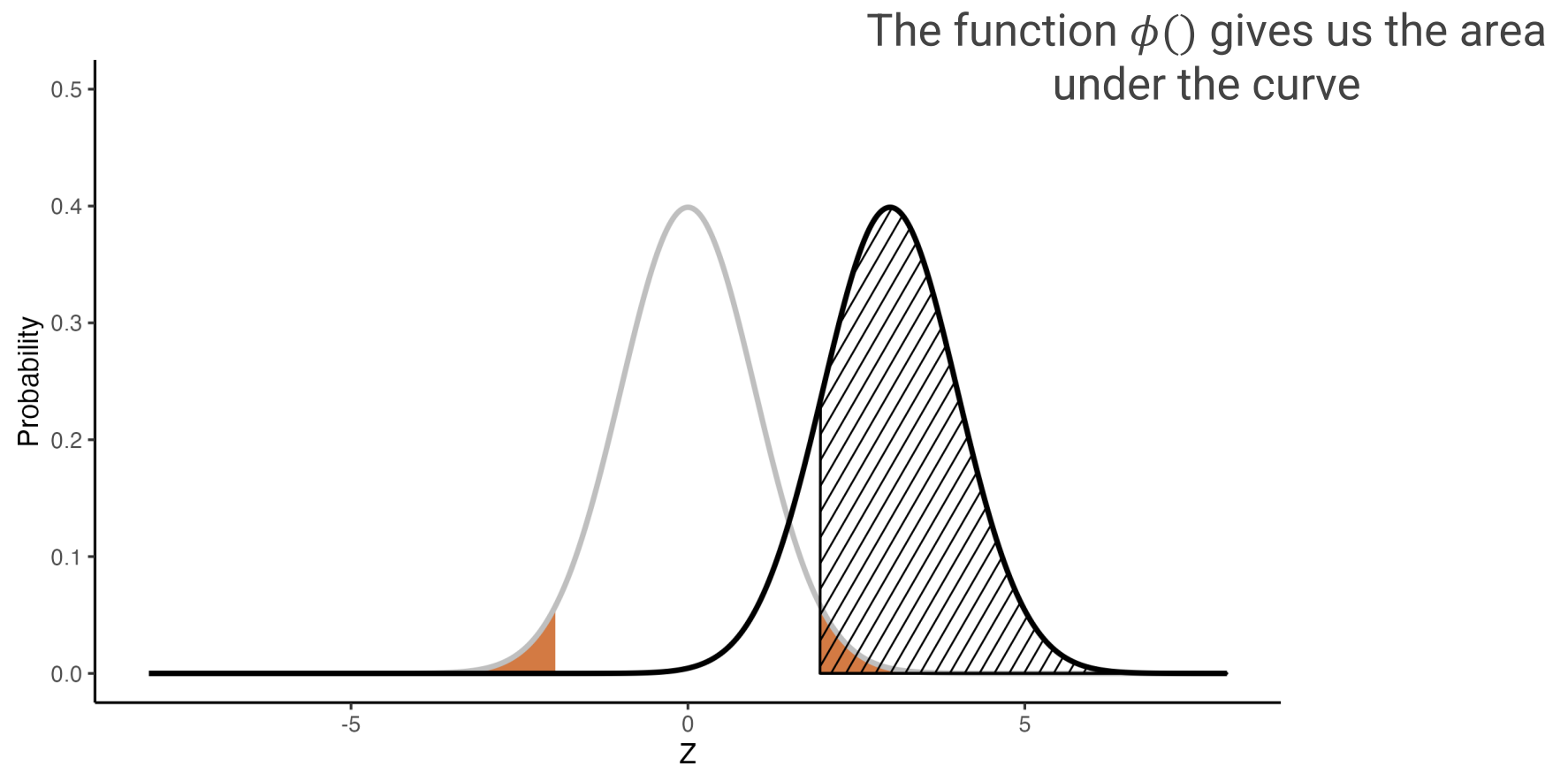
How do we calculate power?



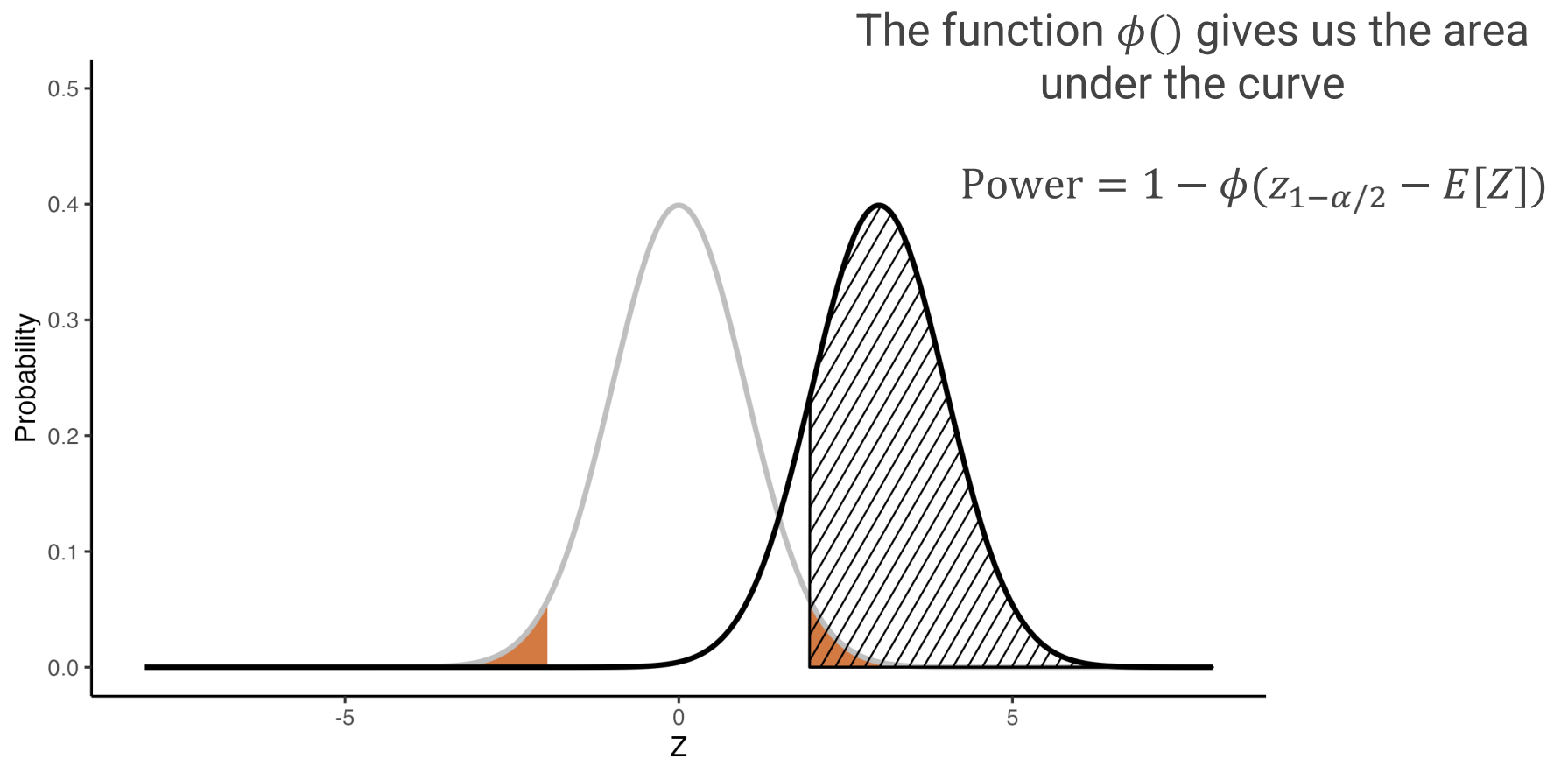
How do we calculate power?



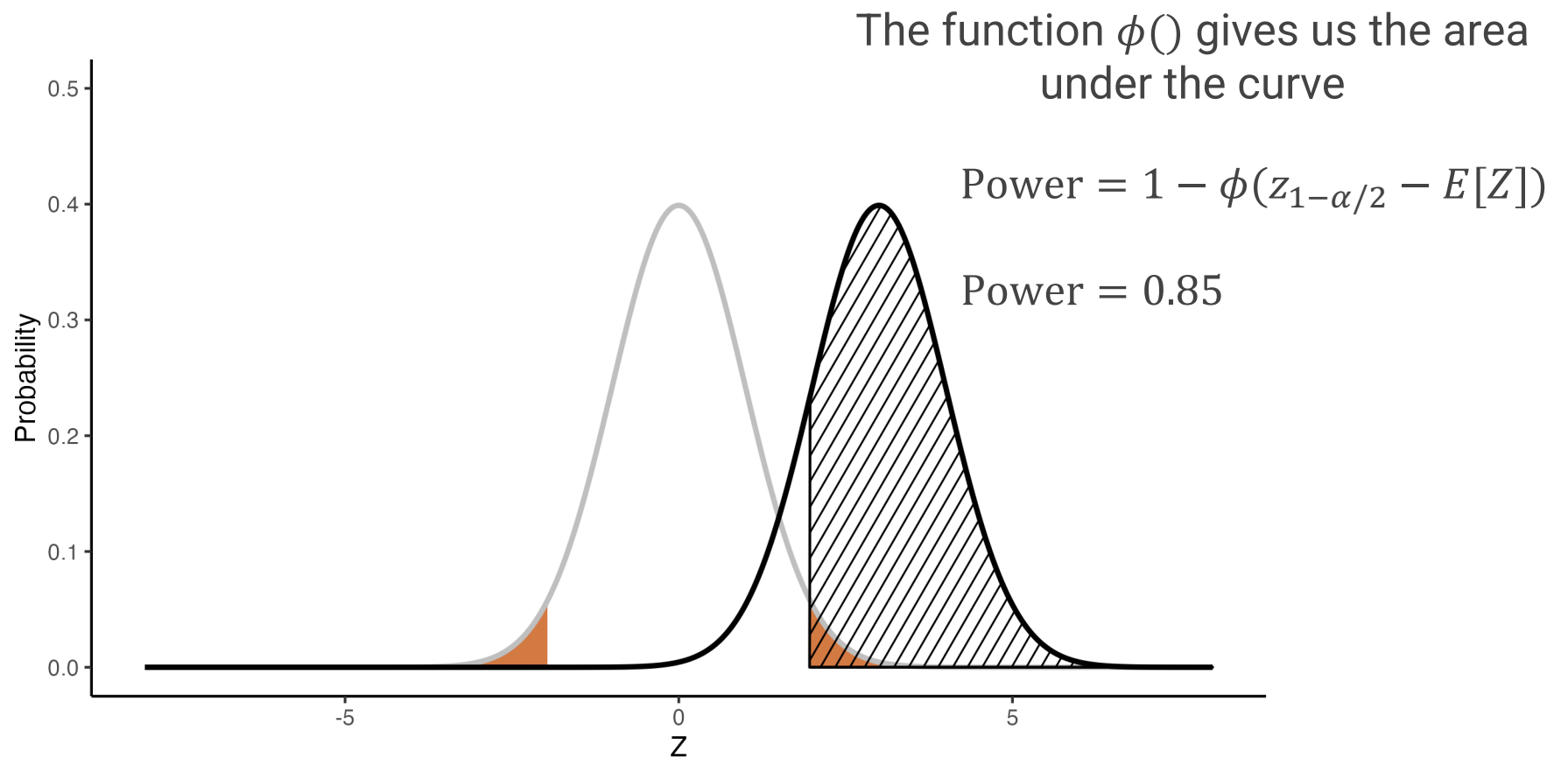
How do we calculate power?



How do we calculate power?



How do we calculate power?



Power as a function of sample size



$$\text{Power} = 1 - \phi(z_{1-\alpha/2} - E[Z])$$

Power as a function of sample size



$$\text{Power} = 1 - \phi \left(z_{1-\alpha/2} - \frac{|p - p_0|}{\sqrt{\frac{p(1-p)}{n}}} \right)$$

Power as a function of sample size



$$\text{Power} = 1 - \phi \left(z_{1-\alpha/2} - \frac{|p - p_0|}{\sqrt{\frac{p(1-p)}{n}}} \right)$$

Power varies as a function of sample size

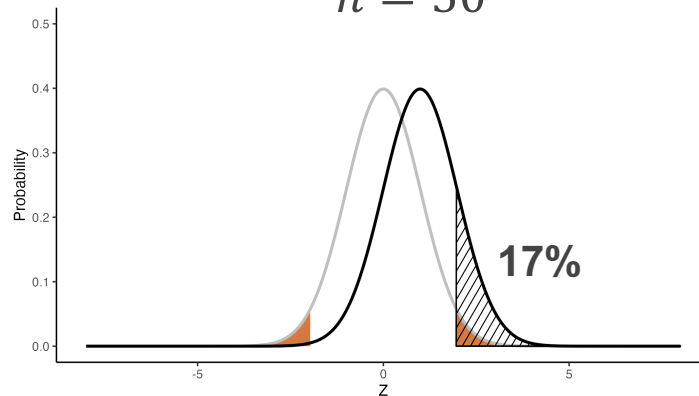
Power as a function of sample size

$$\text{Power} = 1 - \phi \left(z_{1-\alpha/2} - \frac{|p - p_0|}{\sqrt{\frac{p(1-p)}{n}}} \right)$$

Power varies as a function of sample size

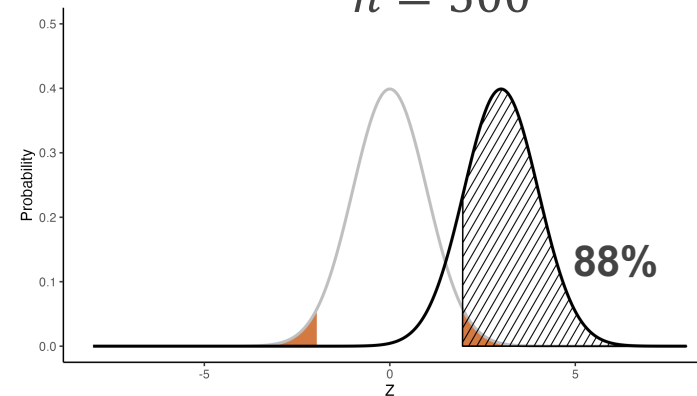
Small sample

$n = 50$

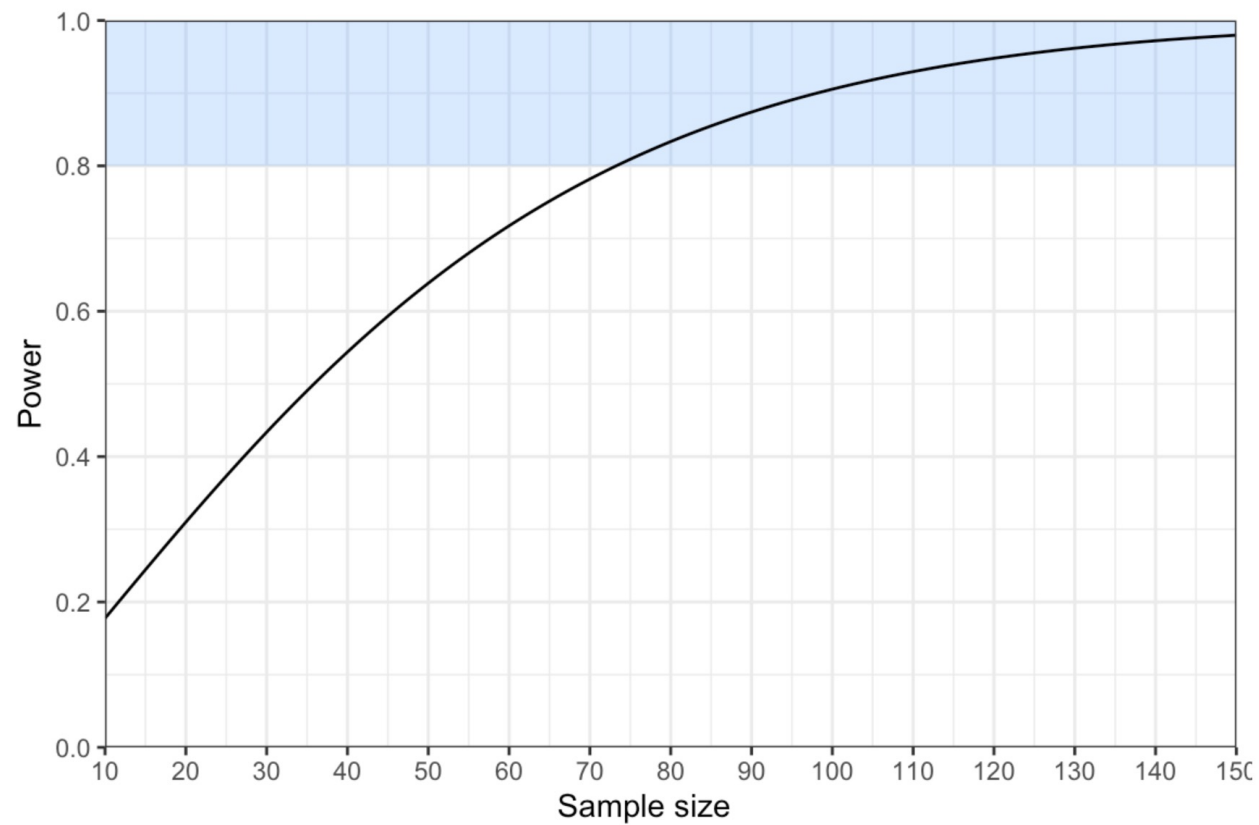


Large sample

$n = 500$

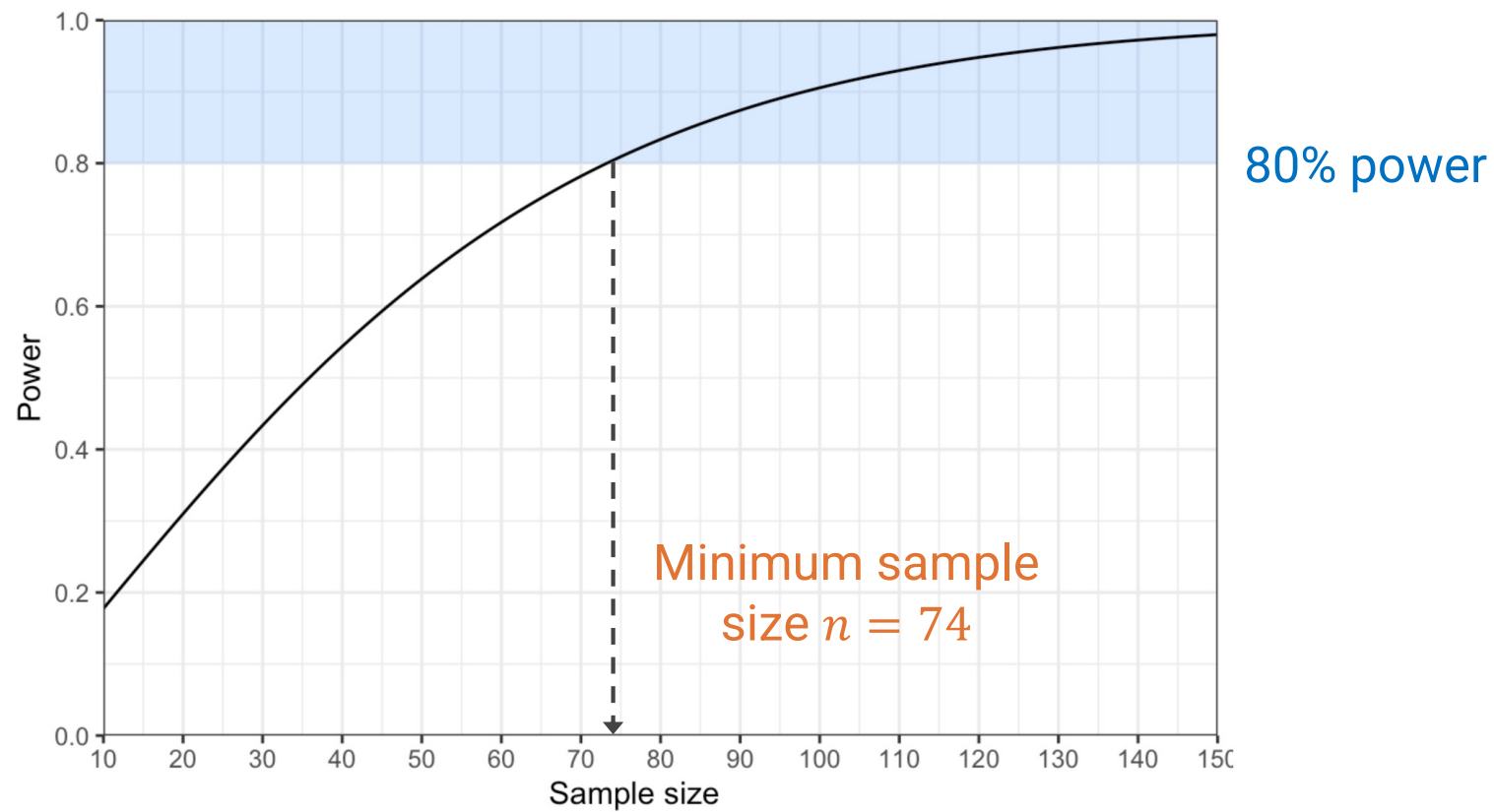


Power curves



80% power

Power curves



Sample size formulae



$$\text{Power} = 1 - \phi \left(z_{1-\alpha/2} - \frac{|p - p_0|}{\sqrt{\frac{p(1-p)}{n}}} \right)$$

Can we reverse-engineer this to find the value of n that achieves a target power?

Sample size formulae



$$\text{Power} = 1 - \phi \left(z_{1-\alpha/2} - \frac{|p - p_0|}{\sqrt{\frac{p(1-p)}{n}}} \right)$$

Can we reverse-engineer this to find the value of n that achieves a target power?

$$n = \left(z_{1-\beta} + z_{1-\frac{\alpha}{2}} \right)^2 \frac{p(1-p)}{(p - p_0)^2}$$

For 80% power, we find $z_{1-\beta} = 0.84$

Summary



- **Power** is the true positive rate. It is the chance of **correctly rejecting the null hypothesis**.
- Power increases with **sample size**. We can use power curves or sample size formulae to choose a value of n

Module 3 activity



Format: Interactive R code, accessed through the web

- Short quiz on hypothesis testing
- Test for change in prevalence
- Test for detection of rare *pfk13* variant



Workshop materials

https://mrc-ide.github.io/MMS-SD_workshop/