# Adaptative balancing techniques applied to parallel mechanisms

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### **SUMMARY**

#### **KEYWORDS:**

#### 1 Introduction and literature review

- 1.1 Dynamic Models
  - Massa pontual:

$$\begin{cases}
\begin{bmatrix} \dot{x}_i \\ \dot{y}_i \end{bmatrix} = \begin{bmatrix} v_{i,x} \\ v_{i,y} \end{bmatrix} \\
M_i \dot{v}_{i,x} \\
M_i \dot{v}_{i,y} \end{bmatrix} + g \begin{bmatrix} 0 \\ M_i \end{bmatrix} = \begin{bmatrix} F_{i,x} \\ F_{i,y} \end{bmatrix}
\end{cases}$$
(1)

Que pode ser reescrito como:

$$\begin{bmatrix} M_i & \mathbf{0} \\ \mathbf{0} & M_i \end{bmatrix} \begin{bmatrix} \ddot{x}_i \\ \ddot{y}_i \end{bmatrix} + g \begin{bmatrix} \mathbf{0} \\ M_i \end{bmatrix} = \begin{bmatrix} F_{i,x} \\ F_{i,y} \end{bmatrix}$$

• RR:

$$\begin{cases}
\begin{bmatrix} \dot{\theta}_{i,1} \\ \dot{\theta}_{i,2} \end{bmatrix} = \begin{bmatrix} \omega_{0,z1} \\ \omega_{0,z2} - \omega_{0,z1} \end{bmatrix} \\
\begin{bmatrix} 1 & 0 \\ 0 & 1 \\ l_{1}s_{i,2} & 0 \\ l_{1}c_{i,2} & l_{g2} \end{bmatrix}^{T} \begin{bmatrix} 1 & 0 \\ 0 & 1 \\ m_{1}\dot{v}_{i,y1} \\ m_{2}\dot{v}_{i,x2} \\ m_{2}\dot{v}_{i,y2} \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 0 \\ -m_{1}v_{i,y2}\omega_{i,z2} \\ m_{1}v_{i,x2}\omega_{i,z2} \end{bmatrix} + g \begin{bmatrix} 0 \\ 0 \\ m_{1}c_{i,1} \\ m_{2}s_{i,1+2} \\ m_{2}c_{i,1+2} \end{bmatrix} \\
\begin{bmatrix} l_{g1} & 0 & -1 & 0 & 0 \\ l_{1}s_{i,2} & 0 & 0 & -1 & 0 \\ l_{1}c_{i,2} & l_{g2} & 0 & 0 & -1 \end{bmatrix} \begin{bmatrix} \dot{\omega}_{i,z1} \\ \dot{\omega}_{i,z2} \\ \dot{v}_{i,y1} \\ \dot{v}_{i,x2} \\ \dot{v}_{i,y2} \end{bmatrix} = - \begin{bmatrix} 0 \\ l_{1}c_{i,2}\omega_{i,z1}(-\omega_{i,z1} + \omega_{i,z2}) \\ l_{1}s_{i,2}\omega_{i,z1}(\omega_{i,z1} - \omega_{i,z2}) \end{bmatrix}
\end{cases} (2)$$

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Que pode ser reescrito como:

$$\begin{bmatrix} J_{z1} + J_{z2} + m_1 l_{g1}^2 + m_2 (l_1^2 + 2l_1 l_{g2} \mathbf{c}_2 + l_{g2}^2) & J_{z2} + m_2 l_{g2} (l_1 \mathbf{c}_2 + l_{g2}) \end{bmatrix} \begin{bmatrix} \ddot{\theta}_{i,1} \\ \ddot{\theta}_{i,2} \end{bmatrix}$$

$$+ \begin{bmatrix} -m_2 l_1 l_{g2} \mathbf{s}_{i,2} \dot{\theta}_{i,2}^2 - 2m_2 l_1 l_{g2} \mathbf{s}_{i,2} \dot{\theta}_{i,1} \dot{\theta}_{i,2} \\ m_2 l_1 l_{g2} \mathbf{s}_{i,2} \dot{\theta}_{i,1}^2 \end{bmatrix} + g \begin{bmatrix} m_1 l_{g1} \mathbf{c}_{i,1} + m_2 (l_{g2} \mathbf{c}_{i,1+2} + l_1 \mathbf{c}_{i,1}) \\ m_2 l_{g2} \mathbf{c}_{i,1+2} \end{bmatrix} = \begin{bmatrix} \tau_{i,1} \\ \tau_{i,2} \end{bmatrix}$$

• RR (0) com 2 massas acopladas (1 e 2):

$$\begin{cases} \begin{bmatrix} \dot{\theta}_{0,1} \\ \dot{\theta}_{0,2} \\ \dot{x}_1 \\ \dot{y}_1 \\ \dot{x}_2 \\ \dot{y}_2 \end{bmatrix} = \begin{bmatrix} \omega_{0,z1} \\ \omega_{0,z2} - \omega_{0,z1} \\ v_{1,x} \\ v_{1,y} \\ v_{2,x} \\ v_{2,y} \end{bmatrix} \\ \begin{bmatrix} 1 & 0 \\ 0 & 1 \\ l_{1}s_{0,2} & 0 \\ l_{1}c_{0,2} & l_{1}s_{0,2} \\ -L_{1}s_{0,1} & 0 \\ -l_{1}s_{0,1} & -L_{2}s_{0,1} \\ l_{1}c_{0,1} & L_{2}c_{0,1} \end{bmatrix}^{T} \begin{cases} \begin{bmatrix} J_{z1}\dot{\omega}_{0,z1} \\ J_{z2}\dot{\omega}_{0,z2} \\ m_{1}\dot{v}_{0,y1} \\ m_{2}\dot{v}_{0,y2} \\ m_{1}\dot{v}_{1,x} \\ M_{1}\dot{v}_{1,x} \\ M_{2}\dot{v}_{2,x} \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 0 \\ -m_{1}v_{0,y2}\omega_{i,z2} \\ m_{1}v_{0,x2}\omega_{i,z2} \\ 0 \\ 0 \\ 0 \end{bmatrix} + g \begin{bmatrix} 0 \\ 0 \\ m_{1}c_{0,1} \\ m_{2}s_{0,1+2} \\ m_{2}c_{0,1+2} \\ 0 \\ M_{1} \\ 0 \\ M_{2} \end{bmatrix} \end{cases} \\ \begin{bmatrix} l_{g1} & 0 & -1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 \\ -l_{1}s_{0,1} & -L_{2}c_{0,1} \end{bmatrix} \begin{bmatrix} \dot{\omega}_{0,z1} \\ \dot{\omega}_{0,z2} \\ \dot{v}_{0,y1} \\ \dot{v}_{0,z2} \\ \dot{v}_{0,y2} \\ \dot{v}_{1,x} \\ \dot{v}_{1,y} \\ \dot{v}_{2,x} \\ \dot{v}_{2,y} \end{bmatrix} = - \begin{bmatrix} 1 & 0 \\ l_{1}c_{0,2}\omega_{0,z1}(-\omega_{0,z1} + \omega_{0,z2}) \\ l_{1}s_{0,2}\omega_{0,z1}(\omega_{0,z1} - \omega_{0,z2}) \end{bmatrix}$$

## Acknowledgments