

Import relevant packages here.

```
In [1]: import matplotlib.pyplot as plt  
import numpy as np  
import pandas as pd  
import math
```

Load the data and verify it is loaded correctly.

- Print it (head, tail, or specific rows, choose a sensible number of rows).
- Compare it to the source file.

```
In [2]: data = pd.read_csv(r"C:\Users\Mischa de Gooijer\OneDrive\Python\Python Projects\  
data.head(5)  
#data = data.iloc[:50]
```

```
Out[2]:      dv      s      a  
0 -0.743240  53.5427  1.242570  
1 -0.557230  53.6120  1.777920  
2 -0.454769  53.6541  0.544107  
3 -0.525396  53.7030 -0.294755  
4 -0.601285  53.7592 -0.290961
```

In the ensuing, you will use `numpy`.

Let's create a grid for the values to plot. But first create **two arrays named `dv` and `s`** using `numpy.linspace` that hold the grid values at the relevant indices in their respective dimension of the grid.

Create a **grid named `a`** with zeros using `numpy.zeros` in to which calculated acceleration values can be stored.

Let the grid span:

- Speed difference `dv` [m/s]
 - From -10 till 10
 - With 41 evenly spaced values
- Headway `s` [m]
 - From 0 till 200
 - With 21 evenly spaced values

```
In [3]: dv = np.linspace(-10, 10, 41)  
s = np.linspace(0, 200, 21)  
a = np.zeros((21, 41))  
print(dv)  
print(s)
```

```

[-10. -9.5 -9. -8.5 -8. -7.5 -7. -6.5 -6. -5.5 -5. -4.5
 -4. -3.5 -3. -2.5 -2. -1.5 -1. -0.5 0. 0.5 1. 1.5
 2. 2.5 3. 3.5 4. 4.5 5. 5.5 6. 6.5 7. 7.5
 8. 8.5 9. 9.5 10. ]
[ 0. 10. 20. 30. 40. 50. 60. 70. 80. 90. 100. 110. 120. 130.
 140. 150. 160. 170. 180. 190. 200.]

```

Create from the imported data 3 separate numpy arrays for each column dv , s and a . (We do this for speed reasons later.)

- Make sure to name them differently from the arrays that belong to the grid as above.
- You can access the data of each column in a DataFrame using data.xxx where xxx is the column name (not as a string).
- Use the method to_numpy() to convert a column to a numpy array.

```
In [4]: DV = data.dv.to_numpy()
S = data.s.to_numpy()
A = data.a.to_numpy()
```

Create an algorithm that calculates all the acceleration values and stores them in the grid. The algorithm is described visually in the last part of the lecture. At each grid point, it calculates a weighted mean of all measurements. The weights are given by an exponential function, based on the 'distance' between the grid point, and the measurement values of dv and s . To get you started, how many for -loops do you need?

For this you will need math .

Use an *upsilon* of 1.5m/s and a *sigma* of 30m.

Warning: This calculation may take some time. So:

- Print a line for each iteration of the outer-most for -loop that shows you the progress.
- Test your code by running it only on the first 50 measurements of the data.

```
In [5]: upsilon = 1.5 #m/s
sigma = 30 #m

for i in range(len(s)):
    for j in range(len(dv)):
        total_weighted_acceleration = 0
        total_weight = 0
        for k in range(len(DV)):
            distance_dv = DV[k] - dv[j]
            distance_s = S[k] - s[i]
            weight = math.exp(-(abs(distance_dv)/upsilon) - (abs(distance_s))/sig
            weighted_acceleration = weight * A[k]
            total_weighted_acceleration += weighted_acceleration
            total_weight += weight
        a[i][j] = total_weighted_acceleration / total_weight
```

```
In [7]: print(a)
```

```
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```

```

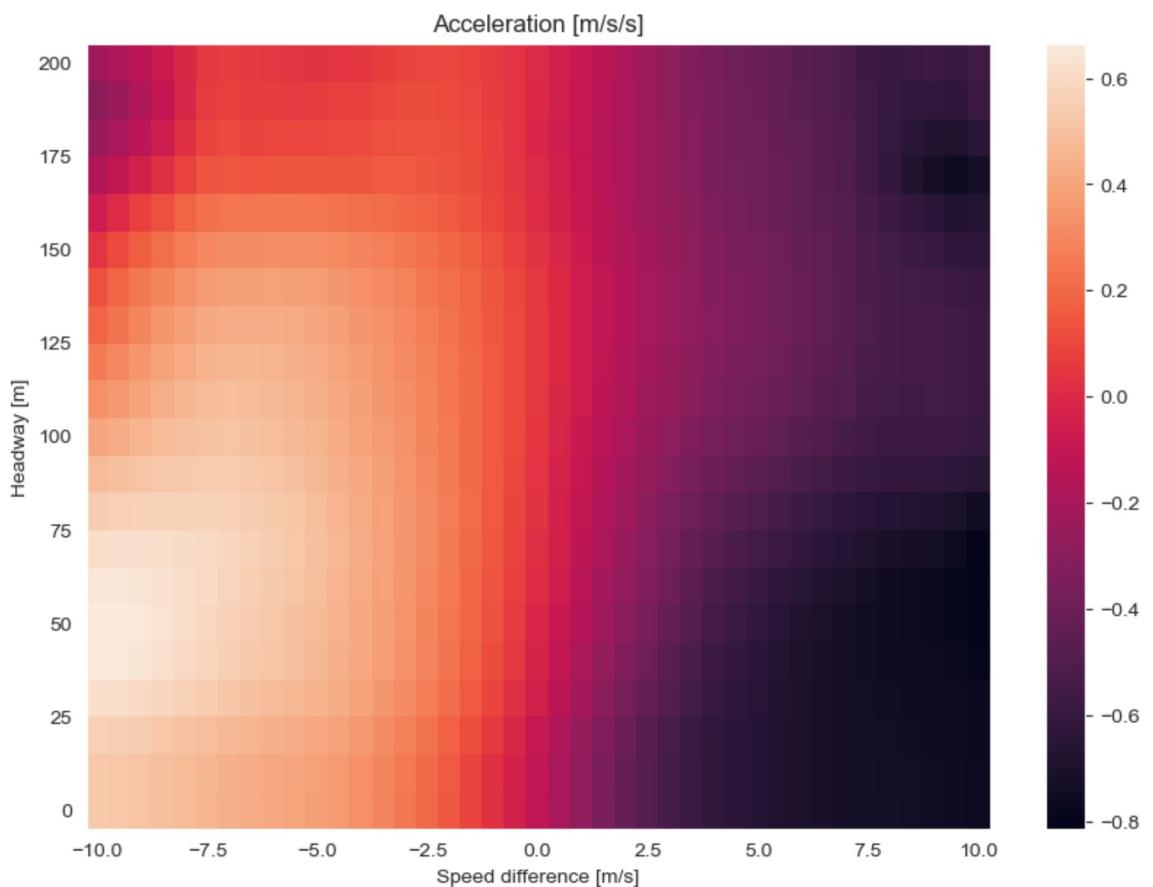
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-5.95710430e-01 -5.82963641e-01 -5.81207817e-01 -5.98363866e-01
-5.68579803e-01]]

```

The following code will plot the data for you. Does it make sense when considering:

- Negative (slower than leader) and positive (faster than leader) speed differences?
- Small and large headways?

```
In [6]: X, Y = np.meshgrid(dv, s)
axs = plt.axes()
p = axs.pcolor(X, Y, a, shading='nearest')
axs.set_title('Acceleration [m/s/s]')
axs.set_xlabel('Speed difference [m/s]')
axs.set_ylabel('Headway [m]')
axs.figure.colorbar(p);
axs.figure.set_size_inches(10, 7)
```



In []: