

# Newton-Euler Equations

System of Particles  
Rigid Body

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Newton's Equations of Motion for a Single  
Particle of mass  $m$

$$\mathbf{F} = m\mathbf{a}$$

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# Newton's Second Law for a System of Particles

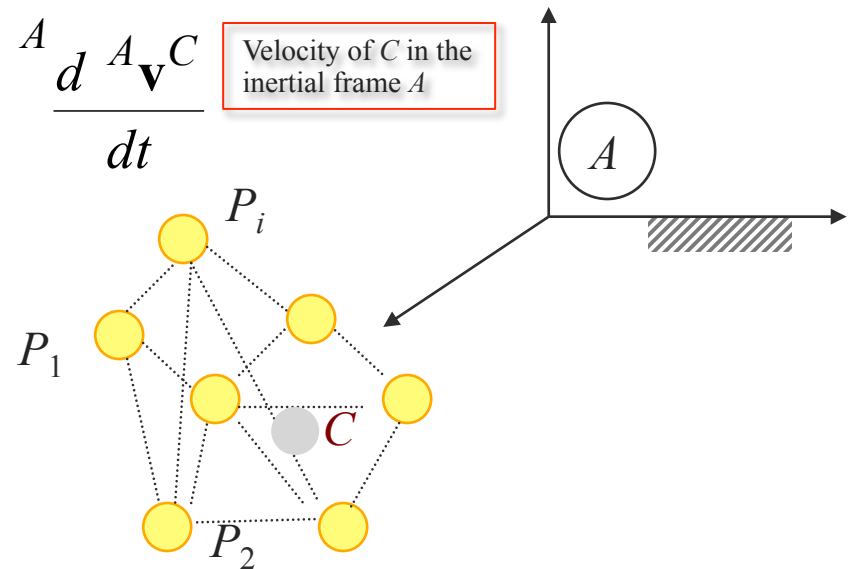
The center of mass for a system of particles,  $S$ , accelerates in an inertial frame ( $A$ ) as if it were a single particle with mass  $m$  (equal to the total mass of the system) acted upon by a force equal to the net external force.

$$\mathbf{F} = \sum_{i=1}^N \mathbf{F}_i = m \frac{d}{dt} {}^A \mathbf{v}^C$$

Velocity of  $C$  in the inertial frame  $A$

Center  
of  
mass

$$\mathbf{r}_c = \frac{1}{m} \sum_{i=1, N} m_i \mathbf{p}_i$$



## Rate of Change of Linear Momentum

Derivative in the inertial frame  $A$

$$\mathbf{F} = \frac{d}{dt} \mathbf{L}$$

Linear momentum of the system of particles in the inertial frame  $A$

*Also true for a rigid body*

# Rotational equations of motion for a rigid body

The rate of change of angular momentum of the rigid body  $B$  relative to  $C$  in  $A$  is equal to the resultant moment of all external forces acting on the body relative to  $C$

Derivative in the inertial frame  $A$

$$\frac{{}^A d {}^A \mathbf{H}_C^S}{dt} = \mathbf{M}_C^S$$

Angular momentum of the rigid body  $B$  with the origin  $C$  in the inertial frame  $A$

*Net moment from all external forces and torques about the reference  $C$*

*Angular momentum*

$${}^A \mathbf{H}_C^S = \mathbf{I}_C \cdot {}^A \boldsymbol{\omega}^B$$

*angular velocity of  $B$  in  $A$*

*inertia tensor with  $C$  as the origin*