

Engineering Secure Software Systems Winter 2020/21

Exercise Sheet 3

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Exercise 3.1, DY closure and derivations (10 Points)

In the lecture, the following lemma was stated (without proof):

If S is a set with $\text{IDs} \cup \{k_a \mid a \in \text{IDs}\} \cup \{\epsilon\} \subseteq S$ and $m \in \text{DY}(S)$, then there is a derivation of m from S : $S = S_0 \rightarrow_{L_0} S_1 \rightarrow_{L_1} \dots S_{n-1} \rightarrow_{L_{n-1}} S_n$ with $m \in S_n$.

1. Prove the above lemma.
2. State and prove an appropriate converse of the lemma.

Note: As in the lecture, you can assume that both S and m do not contain applications of hash functions, message authentication codes (MACs), or signatures.

Exercise 3.2, minimal derivation properties (10 Points)

In the video lecture on the computation of the Dolev-Yao closure, we proved a lemma characterizing shortest derivations.

1. Can you generalize this result to handle signatures, MACs, and hash functions?
2. Which properties does the modeling of cryptographic primitives have to satisfy for an analog of this result to hold?
3. Can you come up with a modeling of cryptographic primitives where this property does not hold?

Exercise 3.3, DY algorithm correctness (10 Points)

Prove that the algorithm for computing the DY closure (in its decisional variant DERIVE) as stated in the lecture is correct and runs in polynomial time. As in the lecture, restrict yourself to terms without applications of hash functions, signatures, or message authentication codes (MACs).