mrgsolve: Simulate from ODE-Based Models

Get Started Package Vignette

Kyle T. Baron

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mrgsolve is an R package maintained under the auspices of Metrum Research Group that facilitates simulation from models based on systems of ordinary differential equations (ODE) that are typically employed for understanding pharmacokinetics, pharmacodynamics, and systems biology and pharmacology. mrgsolve consists of computer code written in the R and C++ languages, providing an interface to a C++ translation of the Isoda differential equation solver. This vignette will show you how to get started using mrgsolve.

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1 Big picture

In this section, I want to give you an overhead view of what it is like working with mrgsolve. There are a huge number of little details that you might want to eventually know in order to use mrgsolve effectively; but for now, let's get a handle on the big ticket items.

There are 3 (or 4) main simulation workflows that we want to work up to. We can think about the type of outputs we want and determine what inputs we'll need to create and the functions that need to be called in order to get those outputs back.

First, load the package along with any other helper packages we need for this vignette.

```
library(mrgsolve)
library(dplyr)
```

1.1 You need a model

For every workflow, you need a model. In most cases, is coded in a separate file and read in by mread()

```
mod <- mread("azithro-fixed.mod")</pre>
```

Building azithro-fixed_mod ... done.

mod

```
----- source: azithro-fixed.mod ------
```

project: /Users/kyleb/vig...vignettes/src

shared object: azithro-fixed.mod-so-174474dd47d60

time: start: 0 end: 240 delta: 0.1

add: <none>

compartments: GUT CENT PER2 PER3 [4]

parameters: TVCL TVV1 TVQ2 TVV2 Q3 V3 KA WT [8]

captures: CP [1] omega: 2x2 sigma: 1x1

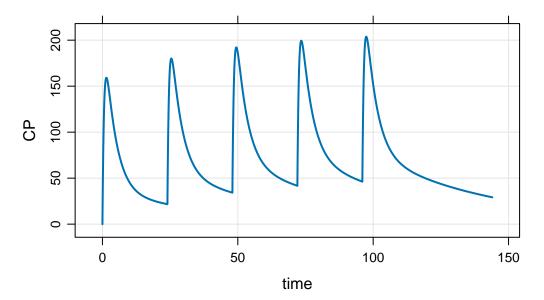
solver: atol: 1e-08 rtol: 1e-08 maxsteps: 20k

In the above example, we created a file called azithro-fixed.mod (azithromycin population PK with fixed effect parameters only) and wrote out the covariate model, differential equations, etc into that file. We point mread() at that file to parse, compile and load that model. More information on using mread() and the model object is found in Section 3. We'll start showing you the model syntax in Section 7.

1.2 Single profile

The first and simplest workflow is to generate a single simulated profile from the model. The quickest way we'll do this is using the model object loaded in the previous section along with an event object

```
mod %>%
  ev(amt = 250, ii = 24, addl = 4) %>%
  mrgsim(end = 144, delta = 0.1) %>%
  plot("CP")
```



The mrgsim() function is called to actually execute the simulation and we've introduced some simulation options (like the simulation end time) by passing those arguments in. More info on mrgsim() can be found in Section 5.

The event object is a quick way to introduce an intervention (like dose administration) into your simulation. More information about event objects is provided in Section 4.

1.3 Population

When we simulate a population, we want to simulate a collection of individuals (or profiles) in a single simulation. Most often, this involves creating an input data set with dosing or other information for each subject in the population.

In this example, we'll load another azithromycin population PK model

```
mod <- mread("azithro.mod")</pre>
```

Building azithro mod ... done.

Rather than using an event object as we did for the single profile, we make a data set.

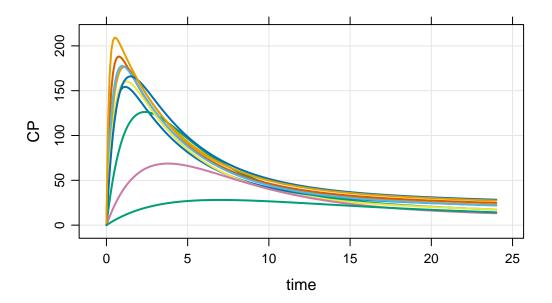
```
set.seed(9876)
data <- expand.ev(amt = 250, WT = runif(10, 50, 100))
data</pre>
```

```
WT
   ID time amt cmt evid
1
    1
          0 250
                  1
                        1 92.33453
2
          0 250
                        1 68.39476
    2
                  1
3
    3
         0 250
                        1 56.19846
                  1
4
    4
         0 250
                        1 78.43937
                  1
5
    5
                        1 71.22273
         0 250
                  1
6
    6
         0 250
                        1 63.88194
                  1
7
    7
         0 250
                  1
                        1 73.15188
8
    8
         0 250
                        1 80.16205
                  1
9
    9
         0 250
                        1 75.37584
                  1
10 10
         0 250
                  1
                        1 59.11208
```

In this data set, we see 10 subjects who are differentiated by their different weights (WT). For this simulation, we'll give every subject 250 mg.

```
set.seed(9876)

mod %>%
   data_set(data) %>%
   mrgsim(end = 24) %>%
   plot("CP")
```



This simulation introduces variability not only through the covariate WT but also through random effects (i.e., ETAs) which are simulated when we call mrgsim().

1.4 Batch

You can also simulate a population (or a batch of subjects) with a data set of parameters and an event object. This workflow is *like* the population simulation, but the inputs are configured in a slightly different way where the population is a set of parameters with a common intervention, rather than and data set with (possibly) different interventions (or different parameters) for each subject in the population. Going back to the azithro-fixed model

```
mod <- mread("azithro-fixed.mod")</pre>
```

Building azithro-fixed_mod ... done.

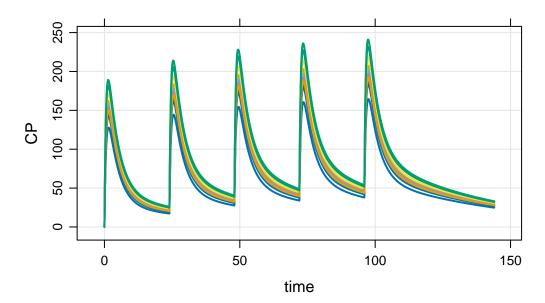
Rather than creating a data set with doses for everyone, we just create their parameters

```
set.seed(9876)
data <- expand.idata(WT = runif(10, 50, 100))
data</pre>
```

```
ID
             WT
1
    1 92.33453
    2 68.39476
2
3
    3 56.19846
4
    4 78.43937
5
    5 71.22273
6
    6 63.88194
7
    7 73.15188
8
    8 80.16205
    9 75.37584
10 10 59.11208
```

Here, we have 10 parameter sets which can also be thought of as 10 people. We can pass this set of parameters as idata, or individual-level data, along with an event object

```
mod %>%
  ev(amt = 250, ii = 24, addl = 4) %>%
  idata_set(data) %>%
  mrgsim(end = 144) %>%
  plot("CP")
```



Here, we get the same output as we got for the population simulation, but a slightly different setup. This setup might be more or less convenient or more or less flexible to use compared to the population setup. Either way, the approach is up to you and the needs of your simulation project.

1.5 Replicate

This pattern is just like data set, but we do that in a loop to generate replicate simulations. Sometimes we do a simulation like this when we are doing simulation-based model evaluation or maybe we're simulating across draws from a posterior distribution of parameter estimates.

This simulation might look something like this (code not evaluated in this vignette)

```
sim <- function(i, model, data) {
  mod %>%
    data_set(data) %>%
    mrgsim() %>%
    mutate(irep = i)
}
out <- lapply(1:1000, sim, model = mod, data = data) %>% bind_rows()
```

Here, we create a function that simulates a data set once and call that repeatedly to get replicate simulated data sets.

1.6 The overall pattern

So the overall pattern to working with mrgsolve is

• Code a model

- Load it with mread()
- Set up your intervention and population
- Simulate with mrgsim()
- Plot or process your output

2 Quick start

To quickly get started with mrgsolve, try using the built in model library like this

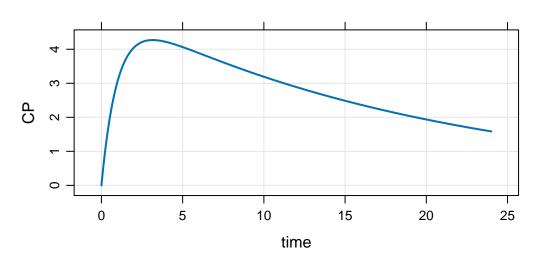
```
mod <- modlib("pk1", delta = 0.1)

out <- mrgsim(mod, events = ev(amt = 100))

out</pre>
```

```
Model:
        pk1
Dim:
        242 \times 5
Time:
        0 to 24
ID:
         1
    ID time
                 {\tt EV}
                      CENT
                                CP
               0.00
1:
     1
        0.0
                     0.000 0.0000
        0.0 100.00
     1
                     0.000 0.0000
3:
        0.1
             90.48
                    9.492 0.4746
     1
        0.2
             81.87 18.034 0.9017
        0.3 74.08 25.715 1.2858
6:
     1
        0.4 67.03 32.619 1.6309
7:
        0.5
             60.65 38.819 1.9409
     1
        0.6 54.88 44.383 2.2191
8:
     1
```

plot(out, "CP")



That was a really simple simulation where we used an event object to initiate a dose into a one-compartment model. See how the plot() method allows us to quickly visualize what happened in the simulation. See the ?modlib help topic for more models you can play around with to get comfortable with mrgsolve. Or keep reading to dig into more of the details.

3 Model object

This chapter introduces the model object.

- The model object contains all information about the model
 - Compartments
 - ODE
 - Algebraic relationships
 - Random effects
 - More
- The model object is what you use in R to
 - Query the model
 - Run simulations

3.1 mread()

Load a model from a model specification file using mread().

- Don't worry for now what is in that file; we'll show you how to create it.
- Your model can have any extension. Traditionally, we've used the .cpp extension because a lot of the code in that file is C++. However, we've moved away from that in recent years because code editors like Rstudio see that .cpp extension and think that all the code is C++ and format the code in ways that aren't what you usually want. So using .mod (or .txt can be helpful just to keep your editor from doing too much.

3.1.1 Syntax to load a model

This section walks you though some of the ways you can use mread() to load a model.

Provide the complete path to the file

```
mod <- mread("model/test.mod")</pre>
```

Provide the directory as an argument

Assumes you are keeping all simulation code in the models directory

```
mod <- mread("test.mod", project = "model")</pre>
```

Set project as an option

All my models are in this directory for this project

```
options(mrgsolve.project = "model")
mod <- mread("test.mod")</pre>
```

Update on load

mrgsolve provides an update() method for updating a model object. mread() will take in arguments and pass them along to update() so you can make these changes at the time the model is loaded.

In this example, we'll

- Set the simulation end time to 240
- Set (increase) ODE solver relative tolerance to 1e-5

```
mod <- mread("model/test.mod", end = 240, rtol = 1e-5)</pre>
```

3.1.2 Read and cache

Use mread_cache() to build and cache the model on disk.

When you load the model the first time, it'll be

```
mod <- mread_cache("test.mod", project = "model")</pre>
```

Building test_mod ... done.

When you load it again, you'll see

```
mod <- mread_cache("test.mod", project = "model")</pre>
```

Loading model from cache.

By default, mrgsolve will store the cached model information in the temporary directory that R sets up every time you start a new R session. This is convenient because you don't have to think about what that directory is, but sometimes you want the cached model to sit in a location that you have a little more control over. Look at the soloc argument; this will let you place the cached model information in a stable location.

3.2 modlib()

Use the modlib() function to load a model from an internal model library.

- Pre-coded models
- Sourced from inside the mrgsolve installation directory
- Great way to get models to experiment with
 - But I rarely use these for production work

This code will load a 1-compartment PK model.

```
mod <- modlib("pk1")</pre>
```

List out the location of he model library

```
modlib()
```

[1] "/Users/kyleb/renv/renv/library/R-4.3/aarch64-apple-darwin20/mrgsolve/models"

So the modlib() function is equivalent to

```
mod <- mread("pk1", project = modlib())</pre>
```

Find out what models are in the library

```
?modlib
```

3.3 Overview

You can print mod to the R console and see what's going on

 ${\tt mod}$

```
----- source: test.mod ------
```

```
project: /Users/kyleb/vig...tes/src/model
shared object: test_mod-so-174473d0621a0
```

time: start: 0 end: 24 delta: 1

add: <none>

compartments: GUT CENT [2] parameters: CL V TVKA [3]

captures: CP [1]

```
omega: 2x2
sigma: 0x0
```

solver: atol: 1e-08 rtol: 1e-08 maxsteps: 20k

or summarize

summary(mod)

```
Model: test_mod
- Parameters: [3]
CL, V, TVKA
- Compartments: [2]
GUT, CENT
- Captured: [1]
CP
- Outputs: [3]
GUT, CENT, CP
```

or see the model code

see(mod)

```
Model file: test.mod
$PARAM CL = 1, V = 20, TVKA = 1.2

$OMEGA 0.1 0.2

$PKMODEL cmt = "GUT CENT", depot = TRUE

$MAIN
double KA = TVKA + ETA(1);

$TABLE
capture CP = CENT/V;
```

3.4 Parameters

Parameters are name=value pairs that are used in your model. You can *change* the value of a parameter in several different ways. Understanding how to do this update is really important if you want to make interesting simulation outputs.

Query the parameter list with param()

param(mod)

```
Model parameters (N=3):
name value . name value
CL 1 | V 20
TVKA 1.2 | . .
```

This output shows you there are 3 parameters in the model

- CL, with nominal value 1
- V, with nominal value 20
- KA, with nominal value 1

Note that each parameter has

- A name(e.g. CL)
- A value (must be numeric)

3.5 Compartments

We'll keep working with the model object we loaded in the previous section.

Models also have compartments. Like parameters, compartments have

- A name
- A value

Compartments also have a *number*

Query the compartment list with init()

init(mod)

```
Model initial conditions (N=2): name value . name value CENT (2) 0 | GUT (1) 0
```

Notice that each compartment has a number associated with it. This is mainly used for dosing. But there is a model syntax that allows you to write a model in terms of named compartments (e.g. A(2) or F1).

3.6 Random effects

revar(mod)

\$omega

```
$...
```

[,1] [,2] 1: 0.1 0.0 2: 0.0 0.2

\$sigma

No matrices found

3.7 Update the model object

We frequently want to *change* or *update* the settings in the model object.

Updates can be made through update(). To change the simulation time grid we might use

```
mod <- update(mod, end = 240, delta = 2)</pre>
```

to change the simulation end time to 240 hours and the output time interval to every 2 hours. This results in a new model object with updated settings that will be in place whenever you simulate from mod until you make more changes.

You can also update on model read

```
mod <- mread("model.mod", end = 240, delta = 2)</pre>
```

or at the time of simulation

```
out <- mod %>% mrgsim(end = 240, delta = 2)
```

All of these update mechanisms execute updates to the model object. But only when we save the results back to mod are the updates persistent in the model.

What else can I update?

- Time
 - start, end, delta, add
- Parameters and compartment initial values
- Solver settings
 - atol, rtol
 - hmax, maxsteps, mxhnil, ixpr
 - Usually changing rtol, atol, and maybe hmax

- \$OMEGA, \$SIGMA
- tscale (rescale the output time)
- digits

Parameter update

To update parameters, use param(). More on this in Section 6

```
mod <- param(mod, CL = 2)</pre>
```

3.8 Advanced

Get the value of a parameter or setting

```
mod$CL
```

[1] 1

mod\$end

[1] 240

Extract all parameters as a list

```
as.list(param(mod))
```

\$CL

[1] 1

\$V

[1] 20

\$TVKA

[1] 1.2

Extract the value of one parameter

mod\$CL

[1] 1

Extract everything

You can get the model object contents as a plain list

```
1 <- as.list(mod)</pre>
```

4 Event objects

Event objects are quick ways to generate an intervention or a sequence of interventions to apply to your model. For example, you have a PK model and want to implement a series of doses into the system during the simulation. Event objects function like quick and easy data sets to accomplish this.

4.1 Create and event object

Use ev() and pass NMTRAN data names in lower case.

For example

```
ev(amt = 100, ii = 12, addl = 2)
```

Events:

```
time amt ii addl cmt evid 1 \quad 0 \quad 100 \quad 12 \quad 2 \quad 1 \quad 1
```

You can pass

- time time of the event
- evid event ID
 - -1 for dose
 - 2 for other type
 - 3 for reset
 - 4 for dose and reset
 - 8 for replace
- amt dose amount
- cmt compartment for the intervention
 - usually the compartment number
 - can be character compartment name
- ii inter-dose interval
- addl additional doses (or events)
 - total alternative for total number of doses
- ss advance to steady-state?
 - 0 don't advance to steady-state
 - 1 advance to steady-state
 - 2 irregular steady-state
- rate give the dose zero-order with this rate

- tinf alternative for infusion time

See ?ev for additional details.

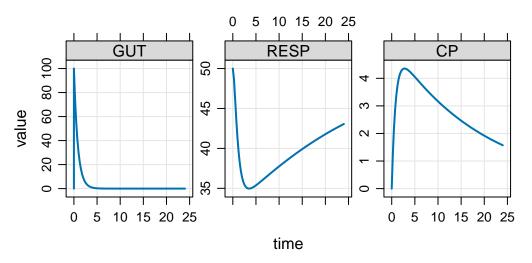
4.2 Invoke event object

There are several ways to create an invoke event objects.

4.2.1 Inline

When the event is simple and can be expressed in a single line, you can pipe the model object to ev() and then simulate.

```
mod <- house(outvars = "GUT,CP,RESP", end = 24)
mod %>% ev(amt = 100) %>% mrgsim() %>% plot()
```



This is a common work flow when exploring a model and an intervention.

4.2.2 As object

You can also save the event object and pass it into the pipeline as we did before with the inline setup.

```
e <- ev(amt = 100)
mod %>% ev(e) %>% mrgsim() %>% plot()
```

Invoking the event object this way is a good idea when you want to create an intervention and apply it to several different simulation scenarios.

Alternatively, you can pass it in as the events argument for mrgsim()

```
mod %>% mrgsim(events = e) %>% plot()
```

This is functionally the same as passing the (saved) event object into the pipeline via ev().

4.3 Combining event objects

We can create more complex interventions from several simpler event objects. mrgsolve provides an interface with helper functions to facilitate this.

4.3.1 Simple combination

Use the c() operator to concatenate several event objects into a single event object.

For 100 mg loading dose followed by 50 mg daily x6

```
load <- ev(amt = 100)
maintenance <- ev(time = 24, amt = 50, ii = 24, addl = 5)
c(load, maintenance)</pre>
```

Events:

```
time amt cmt evid ii addl
1 0 100 1 1 0 0
2 24 50 1 1 24 5
```

4.3.2 Sequence

We can make this simpler by putting these in a sequence using the seq() generic. Here is 100 mg daily for a week, followed by 50 mg daily for the rest of the month

```
a <- ev(amt = 100, ii = 24, total = 7)
b <- ev(amt = 50, ii = 24, total = 21)
seq(a,b)</pre>
```

Events:

```
time amt ii addl cmt evid
1 0 100 24 6 1 1
2 168 50 24 20 1 1
```

The output shows that the **b** event was timed to start once all of the doses from the **a** event were given.

4.3.3 Expand into multiple subjects

We can take any event object and replicate it into several objects with the ev_rep() function.

```
Events:
   time amt ii addl cmt evid
1   0 100 24   6   1   1
2   168   50   24   20   1   1
```

```
seq(a,b) %>% ev_rep(1:3)
```

```
ID time amt ii addl cmt evid
        0 100 24
                    6
                        1
2
  1
     168
          50 24
                   20
                        1
                             1
3 2
        0 100 24
                    6
                        1
                             1
4 2
     168
          50 24
                   20
                        1
                             1
5 3
        0 100 24
                   6
                        1
                             1
  3
     168
          50 24
                   20
```

4.3.4 Combine into a data set

Use as_data_set with ev_rep() to create a single data set

```
c <- seq(a,b)
as_data_set(
  a %>% ev_rep(1:2),
  b %>% ev_rep(1:2),
  c %>% ev_rep(1:2)
)
```

```
ID time cmt evid amt ii addl
1
        0
            1
                 1 100 24
2
  2
        0
            1
                 1 100 24
                              6
3
 3
        0
            1
                 1
                    50 24
                             20
4 4
        0
            1
                 1 50 24
                             20
5 5
        0
                 1 100 24
            1
                             6
6 5
      168
            1
                    50 24
                             20
7
  6
                 1 100 24
                              6
        0
            1
8 6 168
                 1 50 24
                             20
            1
```

4.4 Modifying event objects

You can use a selection of the tidyverse to modify event objects. For example,

```
single <- ev(amt = 100)
ss <- mutate(single, ii = 24, ss = 1)
ss</pre>
```

Events:

```
time amt ii cmt evid ss
1 0 100 24 1 1 1
```

Available tidyverse verbs include

- mutate()
- select()
- filter()

0 100

1

4.5 Column name case

By default, event objects have lower case names

```
ev(amt = 100) %>% as.data.frame()

time amt cmt evid
1  0 100  1  1
```

You can request upper case names by using the evd() constructor

```
evd(amt = 100) %>% as.data.frame()

TIME AMT CMT EVID
1  0 100  1  1
```

These are the names you will see in the rendered data set and in the simulated output. Note that, when working with event objects, always refer to lower case names

```
e <- evd(amt = 100)
e <- mutate(e, ss = 1)
as.data.frame(e)

TIME AMT CMT EVID SS</pre>
```

1 1

You can change the case of any event object to upper case (uctran()) or to lower case (lctran())

```
evd(amt = 100) %>% lctran() %>% as.data.frame()
```

```
time amt cmt evid
1 0 100 1 1
```

In this example, we created an event object using evd() and then immediately requested lower case names. This step can also be performed on the raw data frame.

4.6 Rx specification

This is an alternate syntax letting you create event objects the same way you might write out a prescription.

```
ev_rx("100 mg x1 then 50 q12h x 10 at 24")
```

Events:

```
time amt ii addl cmt evid
1 0 100 0 0 1 1
2 0 50 12 9 1 1
```

This syntax will cover many common dosing scenarios. But more complicated scenarios might require creating events as usual with ev() and then combining as described above.

5 Simulation and outputs

This section discusses

- Simulation from a model object
- Dealing with simulated output

5.1 mrgsim()

Use the mrgsim() function to actually run the simulation. We always pass in the model object as the first argument.

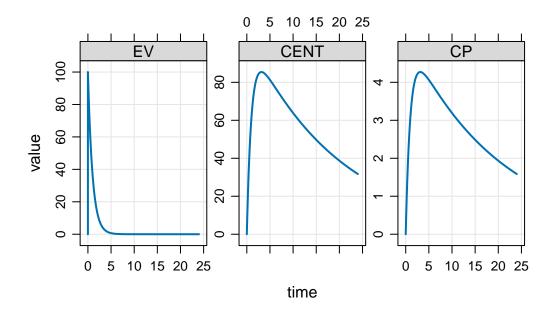
```
mod <- modlib("pk1") %>% ev(amt = 100)
```

mrgsim(mod)

Model: pk1 Dim: 242 x 5 Time: 0 to 24 ID: 1 ID time ΕV CENT CP 0.0 1: 0.00 0.000 0.0000 2: 0.0 100.00 0.000 0.0000 3: 0.1 90.48 9.492 0.4746 4: 0.2 81.87 18.034 0.9017 74.08 25.715 1.2858 5: 1 0.3 6: 0.4 67.03 32.619 1.6309 7: 0.5 60.65 38.819 1.9409 54.88 44.383 2.2191 8: 0.6

Alternatively with the pipe

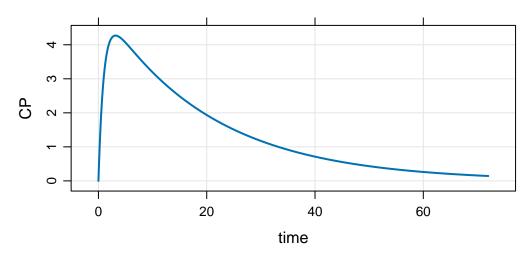
mod %>% mrgsim() %>% plot()



5.1.1 Update

The mrgsim() signature contains ... which are passed to update(). Use this mechanism to customize your simulation or the output on the fly

```
mod %>% mrgsim(outvars = "CP", end = 72, delta = 0.1) %>% plot()
```



In this example, we selected the output variable (CP), ran the simulation to 72 hours (end = 72) and asked for a finer output time grid (delta = 0.1).

5.1.2 Options

There are some options that can *only* be set when you call mrgsim(). These are function arguments. You can see them at?mrgsim'

- carry_out: numeric data columns to copy into the simulated output
- recover: like carry_out but works with any type
- output: pass "df" to get output as a regular data frame
- obsonly: don't return dosing records in the simulated output
- etasrc: should ETAs be simulated? or scraped from the data set
- recsort: how doses and observations having the same time are ordered
- tad: insert time after dose into the output
- ss_n and ss_fixed: settings for finding steady state
- nocb: next observation carry backward; set to FALSE for locf

5.1.3 Variants

Inputs

There are mrgsim() variants which are specific to the types of inputs

- mrgsim_e() just an event object
- mrgsim_d() just a data set
- mrgsim_ei() event + idata set
- mrgsim_di() data set + idata set
- mrgsim_i() just idata set

Outputs

You can also call mrgsim_df(), which is a wrapper for mrgsim() that always returns a data frame.

Quick

Call mrgsim_q() for a quick turnaround simulation, with minimal overhead (and features). Only really useful when you are simulating repeatedly ... like when estimating parameters or doing optimal design.

5.2 Simulated output

mrgsim() returns an object with class mrgsims; this is essentially a data frame but with some extra features.

```
out <- mrgsim(mod)
class(out)

[1] "mrgsims"
attr(,"package")
[1] "mrgsolve"</pre>
```

head(out)

```
ID time
                 EV
                         CENT
                                     CP
     0.0
            0.00000
                    0.000000 0.0000000
1
     0.0 100.00000
                    0.000000 0.0000000
3
     0.1 90.48374
                    9.492112 0.4746056
     0.2 81.87308 18.033587 0.9016794
          74.08182 25.715128 1.2857564
5
  1
     0.3
     0.4 67.03200 32.618803 1.6309401
```

summary(out)

```
ID
                                     ΕV
                                                          CENT
                  time
Min.
       :1
                    : 0.000
                                         0.00000
                                                    Min.
                                                            : 0.00
            Min.
                               Min.
1st Qu.:1
            1st Qu.: 5.925
                               1st Qu.:
                                         0.00000
                                                    1st Qu.:41.38
Median:1
            Median :11.950
                               Median:
                                         0.00059
                                                    Median :55.09
                                                            :56.50
Mean
       :1
            Mean
                    :11.950
                               Mean
                                         4.34229
                                                    Mean
                               3rd Qu.:
3rd Qu.:1
            3rd Qu.:17.975
                                         0.24198
                                                    3rd Qu.:72.26
            Max.
                               Max.
Max.
       :1
                    :24.000
                                      :100.00000
                                                    Max.
                                                            :85.41
      CP
       :0.000
Min.
1st Qu.:2.069
Median :2.754
       :2.825
Mean
3rd Qu.:3.613
Max.
       :4.270
```

5.2.1 Output scope

- The first column in the output is always ID
- The second column in the output is always time (or TIME)

By default, you get simulated values in all compartments and for every derived output at every time

head(out)

```
ID time
                 ΕV
                         CENT
                                     CP
   1
      0.0
            0.00000
                    0.000000 0.0000000
  1
     0.0 100.00000
                    0.000000 0.0000000
3
                    9.492112 0.4746056
      0.1
          90.48374
4
      0.2
          81.87308 18.033587 0.9016794
          74.08182 25.715128 1.2857564
5
  1
      0.3
          67.03200 32.618803 1.6309401
```

- EV and CENT are compartments
- CP is a derived variable (CENT/V)

```
outvars(mod)
```

```
$cmt
[1] "EV" "CENT"
$capture
[1] "CP"
```

You can control which compartments and derived outputs are returned when you do a simulation run. This is a *really* important feature when the simulations become very large: limiting the outputs to those you actually need can make the difference between a simulation that fits within the available memory and one that doesn't.

To request specific outputs at simulation time, set outvars in the model. In this example, we make the selection on the fly

```
mod %>%
  update(outvars = "CP") %>%
  mrgsim()
```

```
Model: pk1
Dim: 242 x 3
Time: 0 to 24
ID: 1
ID time CP
```

```
0.0 0.0000
1:
       0.0 0.0000
2:
    1
3:
    1 0.1 0.4746
4:
    1 0.2 0.9017
    1 0.3 1.2858
5:
    1 0.4 1.6309
    1 0.5 1.9409
7:
    1 0.6 2.2191
8:
```

Alternatively, we can make the change persistent

```
mod2 <- update(mod, outvars = "CP")
outvars(mod2)

$cmt
character(0)

$capture
[1] "CP"</pre>
```

5.2.2 Copy inputs into output

Input data items can be *copied* into the simulated output without passing through the model code itself.

For most applications, use the recover argument to mrgsim()

```
data <- expand.ev(amt = c(100,300)) %>%
  mutate(dose = amt, arm = "100 mg x1", "300 mg x1")

out <- mrgsim(mod, data, recover = "dose, arm", output = "df")

count(out, dose, arm)</pre>
```

```
dose arm n
1 100 100 mg x1 242
2 300 100 mg x1 242
```

This will let you copy inputs of any type into the output.

If you just want to get numeric inputs into the output, use carry_out

```
data <- expand.ev(amt = c(100,300)) %>% mutate(dose = amt)

out <- mrgsim(mod, data, carry_out = "dose", output = "df")

count(out, dose)</pre>
```

```
dose n
1 100 242
2 300 242
```

5.3 Working with mrgsims object

The mrgsims object can be convenient to work with when the output is small.

```
mod <- modlib("pk1", delta = 0.1)</pre>
```

Loading model from cache.

```
out <- mrgsim(mod, ev(amt = 100))</pre>
```

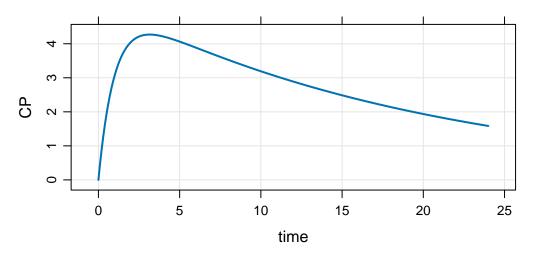
out

```
Model: pk1
        242 \times 5
Dim:
Time:
        0 to 24
ID:
        1
    ID time
                     CENT
                ΕV
        0.0
1:
     1
              0.00
                    0.000 0.0000
        0.0 100.00
                    0.000 0.0000
        0.1 90.48 9.492 0.4746
     1
        0.2 81.87 18.034 0.9017
        0.3 74.08 25.715 1.2858
6:
        0.4 67.03 32.619 1.6309
        0.5 60.65 38.819 1.9409
7:
     1
8:
        0.6 54.88 44.383 2.2191
```

5.3.1 Plot

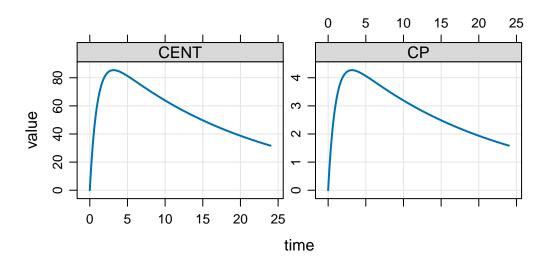
The main benefit from using this object is the ability to easily make plots to see what happened. You can plot a single output

```
plot(out, CP ~ time)
```



or a collection of outputs

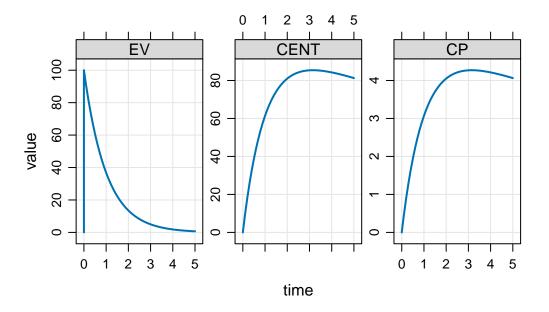




5.3.2 Filter

Use $filter_sims()$ to limit the rows that are retained in the simulated output

```
out2 <- filter_sims(out, time <= 5)
plot(out2)</pre>
```



5.3.3 Mutate

Use mutate_sims() to alter the columns in the simulated output

```
Model: pk1
```

Dim: 242 x 6 Time: 0 to 24

ID: 1

ID time ΕV CENT CP week 1: 0.0 0.00 0.000 0.0000 0.0000000 2: 0.0 100.00 0.000 0.0000 0.0000000 90.48 9.492 0.4746 0.0005952 3: 1 0.1 4: 1 0.2 81.87 18.034 0.9017 0.0011905 0.3 74.08 25.715 1.2858 0.0017857 5: 1 6: 0.4 67.03 32.619 1.6309 0.0023810 0.5 60.65 38.819 1.9409 0.0029762 7: 8: 0.6 54.88 44.383 2.2191 0.0035714

mutate_sims(out, week = time/168)

5.4 Coerce output

When output is big, the methods mentioned above are less likely to be useful: what we really want is just a simple data frame to work on. In this case, coerce outputs to data.frame or tibble

```
df <- as.data.frame(out)
df <- as_tibble(out)
head(df)</pre>
```

```
# A tibble: 6 x 5
                       CENT
     ID
          time
                   ΕV
                                CP
  <dbl> <dbl> <dbl> <dbl> <dbl> <
1
      1
           0
                  0
                       0
                             0
2
      1
           0
               100
                       0
                             0
3
           0.1
                90.5
                       9.49 0.475
4
      1
           0.2
                81.9 18.0
                             0.902
5
           0.3
                74.1 25.7
                             1.29
      1
6
      1
           0.4
                67.0 32.6
                             1.63
```

Once the output is coerced to data frame, it is like any other R data frame.

Remember that you can get a data frame directly back from mrgsim() with the output argument

```
mrgsim(mod, ev(amt = 100), output = "df") %>% class()
```

[1] "data.frame"

This is what you'll want to do most of the time when doing larger simulations.

5.4.1 dplyr verbs

You can pipe simulated output directly to several dplyr verbs, for example filter() or mutate().

```
mod %>% mrgsim(ev(amt = 100)) %>% mutate(rep = 1)
```

```
# A tibble: 242 x 6
          time
                    EV
                        CENT
                                  CP
                                       rep
   <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
            0
                   0
                         0
 1
        1
                              0
                                          1
 2
            0
                 100
                         0
                                          1
 3
        1
            0.1
                  90.5
                        9.49 0.475
                                          1
 4
        1
            0.2
                 81.9 18.0
                              0.902
                                          1
 5
        1
            0.3
                 74.1 25.7
                              1.29
                                          1
 6
        1
            0.4
                  67.0 32.6
                              1.63
                                          1
 7
        1
                  60.7 38.8
            0.5
                              1.94
                                          1
 8
            0.6
                  54.9 44.4
                              2.22
                                          1
 9
                  49.7 49.4
        1
            0.7
                              2.47
                                          1
                 44.9 53.8 2.69
10
        1
            0.8
                                          1
# i 232 more rows
```

This will first coerce the output object to a data frame and then continue to work on the simulated data according to the functions in the pipeline.

Other verbs you can use include

- group_by()
- mutate()
- filter()
- summarise()
- select()
- slice()
- pull()
- distinct()

6 Model parameters

Model parameters are name / value pairs that are used *inside* your model, but they can be varied *outside* the model.

Understanding how mrgsolve handles model "parameters" particularly important for generating interesting and robust simulations.

Big picture

- mrgsolve maintains a parameter list, including names and values
 - This list is used by default if nothing else is done
 - The parameter values in this list can be updated
- mrgsolve will check input data sets for *columns* which have the same name as a parameter
 - When a match is made between data set and parameter list, mrgsolve will update the value based on what is passed on the data
 - Parameters in idata are checked (and parameter list updated) first; after that, the data set is checked (and parameter list updated)

6.1 Coding model parameters

Traditionally, we've used the \$PARAM block to set parameter names and values

```
$PARAM
WT = 70, SEX = 0, EGFR = 100
```

New in mrgsolve 1.2.0, you can use the \$INPUT block. This is another way to specify parameters, but they will have a special *tag* on them that we can use later.

```
$INPUT
WT = 70, SEX = 0, EGFR = 100
```

It's best if you can set these to sensible values; this is usually the *reference* value in your covariate model or some other value that gives you a sensible *default* output.

6.2 Updating parameter values

You can't change the names or number of parameters after you compile the model, but you can change the values.

You can update parameters either

- prior to simulation or
- during simulation

We will illustrate with this model

```
mod <- mread("parameters.mod")</pre>
```

Building parameters_mod ... done.

```
param(mod)
```

```
Model parameters (N=8):
name value . name value
EGFR 100 | THETA3 0.262
SEX 0 | THETA4 0.331
THETA1 0 | THETA5 -0.211
THETA2 3 | WT 70
```

There parameters are:

- WT
- SEX
- EGFR
- THETA1 ... THETA5

6.2.1 Update prior to simulation

Use param() to update the model object. You can do this in one of two ways.

6.2.1.1 Update with name=value

The first way is to pass the new value with the parameter name you want to change. To change WT

mod\$WT

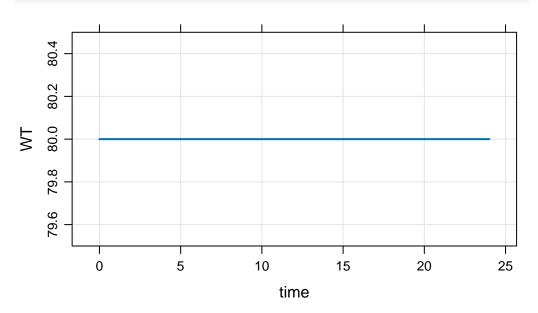
[1] 70

```
mod <- param(mod, WT = 80)
mod$WT</pre>
```

[1] 80

And when we simulate,

```
mrgsim(mod) %>% plot("WT")
```



You can also do this via update()

```
mod <- update(mod, param = list(WT = 60))
mod$WT</pre>
```

[1] 60

Remember that ${\tt mrgsim}()$ passes to ${\tt update}()$ so you can do the same thing with

```
out <- mrgsim(mod, param = list(WT = 70))</pre>
```

This will generate simulated output with \mathtt{WT} set to 70

6.2.2 Update with object

If you have a named object, you can pass that in to the update as well. For example, pass in a named list

```
p <- list(WT = 70.2, F00 = 1)

mod <- param(mod, p)

mod$WT</pre>
```

[1] 70.2

Or a data frame

```
data <- data.frame(WT = c(70, 80.1), BAR = 2)
mod <- param(mod, data[2,])
mod$WT</pre>
```

[1] 80.1

6.3 Update during simulation

In this approach, we'll add a columns to our input data set with the same names as our parameters and let mrgsolve pick up the new values.

To illustrate, load a data set from which to simulate

```
data <- read.csv("parameters-data.csv")
data</pre>
```

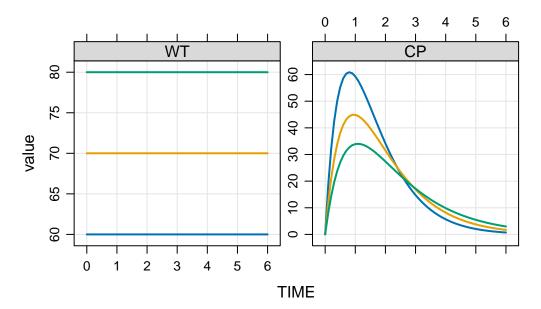
```
ID TIME AMT CMT WT SEX EGFR EVID
1
       0 100 1 60
                      0
                          60
2
 2
       0 100
               1 70
                      0
                          60
                                1
  3
       0 100
               1 80
                          60
                                1
                      0
```

- Subjects 1, 2, and 3 have different (increasing) weight
- All subjects have SEX=0
- All subjects have EGFR=60

When we pass this data frame for simulation and plot

```
out <-
   mod %>%
   data_set(data) %>%
   zero_re() %>%
   mrgsim(delta = 0.1, end = 6)

plot(out, "WT,CP")
```



All of this *only* works if the names in the data set match up with the names in the model.

6.4 Check if the names match

Recall that we coded the model covariates using \$INPUT, rather than \$PARAM? We can see that these parameters have this special tag

param_tags(mod)

```
name tag
1 WT input
2 SEX input
3 EGFR input
```

They have the input tag, which means we expect to find them on the data set when we ask.

We can check this data set against the parameters in the model

```
check_data_names(data, mod)
```

Found all expected parameter names in `data`.

Now, modify the data set so it has eGFR rather than EGFR

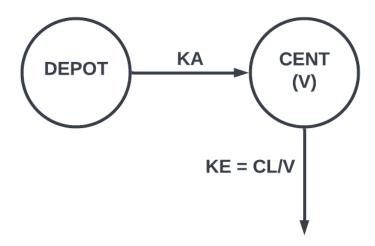
```
data2 <- rename(data, eGFR = EGFR)
check_data_names(data2, mod)</pre>
```

Warning: Could not find the following parameter names in `data`:

- * EGFR (input)
- i Please check names in `data` against names in the parameter list.

7 Model Specification

In this chapter, we'll start by coding up a pharmacokinetic model. The model will be very simple to start, letting us get some concepts in place. Later on, we'll do more compilcated model syntax.



Parameters

- CL
- V
- KA

Compartments

- CENT
- DEPOT

7.1 Where to save your code?

- You can use any file name with any extension
- The extension you use may influence how your editor highlights and indents your code
- I use .mod

7.2 Model specification blocks

Model components are coded into blocks, which are delineated by a specific block syntax. You have a couple of options

NONMEM style

These start with \$ and then the block name (\$PK)

Bracket style

Put the block name in brackets ([ERROR])

Upper or lower case

You can use either:

- \$error
- [pk]
- etc ... they all work

7.2.1 Syntax

The "type" of code you write will vary from block to block. Sometimes it is an R-like syntax and sometimes it is c++ code.

Don't worry if you don't know c++! We have taken a lot of the complexity out and with a handful of exceptions, the code should be pretty natural and similar to what you write in R.

7.3 Base model blocks

7.3.1 Parameters

Use the \$PARAM block header.

```
$PARAM
CL = 1, V = 20, KA = 1.1
```

Parameters have a **name** and a **value**, separated by =.

Parameter names can be upper or lower case. If you want punctuation, use underscore _.

Parameter values must evaluate to numeric.

Parameters can't be functions of other parameters when writing the \$PARAM block. But there is a place where you can do this ...we'll see this later on.

Multiple parameters can go on one line, but separate by comma.

7.3.2 Read it in with mread()

Point mread() at your model file to

- read in the model
- see if it compiles

```
mod <- mread("simple.mod")</pre>
```

Building simple_mod ... done.

We'll learn much more about mread() later on, but for now we need a way to check if our model coding is correct.

7.4 Compartments

```
$PARAM
CL = 1, V = 20, KA = 1.1
$CMT DEPOT CENT
```

Compartments are named

- Upper or lower case
- Punctuation use _

Order doesn't matter, except

- When putting dosing records into the data set
- You want to use the NONMEM-style coding

7.5 Differential equations

Now, we'll write ODE using \$DES (or \$ODE) block.

```
$PARAM
CL = 1, V = 20, KA = 1.1

$CMT DEPOT CENT

$DES
dxdt_DEPOT = -KA * DEPOT;
dxdt_CENT = KA * DEPOT - (CL/V)*CENT;
```

Left hand side is dxdt_<compartment name>.

Right hand side can reference

- Compartments
- Parameters
- Other quantities derived in \$DES or \$PK
- Other internal variables

Unlike \$PARAM and \$CMT, this is c++ code

- Any valid c++ code is allowed
- Each line (statement) should end in semi-colon;

7.6 Derived outputs

Like NONMEM, derived can be calculated in the \$ERROR block.

```
$PARAM
CL = 1, V = 20, KA = 1.1

$CMT DEPOT CENT

$DES
dxdt_DEPOT = -KA * DEPOT;
dxdt_CENT = KA * DEPOT - (CL/V)*CENT;

$ERROR
double CP = CENT/V;
```

Like \$DES, this block must be valid c++ code.

Here we have created a new variable called CP, which is the amount in the central compartment divided by the central volume of distribution.

When we create a new variable, we must declare its type. Use double for a floating point number.

7.7 Capture outputs into the simulated data

mrgsolve has a \$CAPTURE block that works like NONMEM's \$TABLE. Just list the names you want copied into the output.

```
$PARAM
CL = 1, V = 20, KA = 1.1

$CMT DEPOT CENT

$DES
dxdt_DEPOT = -KA * DEPOT;
dxdt_CENT = KA * DEPOT - (CL/V)*CENT;
```

```
$ERROR
double CP = CENT/V;
$CAPTURE CP
```

Rather than putting stuff in \$CAPTURE, try declaring with type capture

```
$ERROR
capture CP = CENT/V;
```

capture is identical to type double, but tells mrgsolve to include this item in the simulated output.

A little-use feature is renaming items in \$CAPTURE

```
$ERROR
double DV = CENT/V;

$CAPTURE CP = DV
```

7.8 Covariate model

Like NONMEM, we can use \$PK (or \$MAIN) to code the covariate model, random effects, F, D, R, and ALAG, and initialize compartments.

```
$PK
double CL = TVCL * pow(WT/70, 0.75) * exp(ETA(1));
```

- Any valid c++ code is allowed
- Each line (statement) should end in semi-colon;

7.9 C++ examples

```
if(a == 2) b = 2;
if(b <= 2) {
    c=3;
} else {
    c=4;
}
d = a==2 ? 50 : 100;
double d = pow(base, exponent);
double e = exp(3);
double f = fabs(-4);
double g = sqrt(5);</pre>
```

```
double h = log(6);
double i = log10(7);
double j = floor(4.2);
double k = ceil(4.2);
```

7.9.1 Integer division

Be careful of dividing two integers; it's usually not what you want to do. When people get bit by this, it's usually when they divide one integer literal by another integer literal in their code. For example, we might *think* the following should evaluate to 0.75

```
double result = 3/4; # 0
```

but it doesn't; here, result will evaluate to 0 because the C++ compiler will do integer division between the 3 and the 4 and you'll get 0.

It is good to get in the habit of putting .0 behind whole numbers.

```
double result = 3.0/4.0; # 0.75
```

Of course, you *might* really want to divide two integers at some point; but for now, please mind this "feature" of C++ when writing your code.

Lots of help with C++ on the web http://en.cppreference.com/w/cpp/numeric/math/tgamma

7.10 Random effects

There are times when you will need to code this manually. When estimating with NONMEM and simulating with mrgsolve, these matrices will frequently be imported automatically via \$NMXML.

7.10.1 Omega / ETA

Diagonal matrix

```
$OMEGA
0.1 0.2 0.3
```

This is a 3x3 matrix with 0.1, 0.2, and 0.3 on the diagonal.

Block matrix

```
$DMEGA @block
0.1 0.002 0.3
```

This is a 2x2 matrix matrix with 0.1 and 0.3 on the diagonal. Sometimes it's easier to see when we code it like this

```
$OMEGA @block
0.1
0.002 0.3
```

Random effects simulated from OMEGA are referred to with ETA(n).

7.10.2 Sigma / EPS

Works just like Omega / ETA, but use \$SIGMA and EPS(n).

For sigma-like theta, code it just as you would in NONMEM.

```
$PARAM THETA12 = 0.025

$SIGMA 1

$ERROR
double W = sqrt(THETA12);
Y = (CENT/V) + W*EPS(1);
```

There is no FIX in mrgsolve; everything in OMEGA and SIGMA is always fixed.

7.11 Import estimates from NONMEM

- Use \$NMEXT or \$NMXML
 - \$NMEXT reads from the .ext file
 - * Can be faster
 - * Doesn't retain \$OMEGA and \$SIGMA structure
 - \$NMXML reads from the .xml file
 - * Can be slower
 - * Does retain OMEGA and SIGMA structure

This is the safest way to call

```
$NMXML
path = "../nonmem/106/106.xml"
root = "cppfile"
```

You might be able to use this run/project approach as well

```
$NMXML
run = 1006
project = "../sim/"
root = "cppfile"
```

7.12 Models in closed form

mrgsolve will solve one- and two-compartment models with first order input in closed form. This usually results in substantial speed up. Use \$PKMODEL.

```
$PKMODEL cmt = "GUT,CENT", depot = TRUE
```

Certain symbols are required to be defined depending on the model. mrgsolve models are always parameterized in terms of clearances and volumes except for absorption, which is in terms of rate constant.

- CL / V
- CL / V / KA
- CL / V2 / Q / V3
- CL / V2 / Q / V3 / KA

These can be defined as a parameter or a derived quantity in \$PK.

Compartment names are user-choice; the only thing mrgsolve cares about is the number of compartments.

7.13 Plugins

7.13.1 autodec

Historically, you have had to *declare* the type of any new variable you want to create.

```
$PK
double KE = CL/V;
```

For most models, the numeric variables you declare are likely to be floating point numbers ... with type double.

We created a plugin that tells mrgsolve to look for new variables and declare them for you.

```
$PLUGIN autodec

$PK
KE = CL/V;
```

7.13.2 nm-vars

mrgsolve historically used

- CENT
- dxdt_CENT
- F_CENT
- D_CENT

etc. When we started mrgsolve, this was a really nice feature because you didn't have to think about compartment *numbers*. However, this made translation of the model more difficult.

When you invoke the nm-vars plugin, you can write in a syntax that is much more like NONMEM.

For example

```
$PK
F2 = THETA(3);
ALAG2 = EXP(THETA(4));
$DES
DADT(1) = - KA * A(1);
```

Other convenience syntax

- LOG() and log()
- EXP() and exp()
- SQRT() and sqrt()

Regardless of whether you have nm-vars invoked or not, you can still use THETA(n) to refer to parameter THETAn.

Try the nm-like model in the model library for an example.

```
mod <- modlib("nm-like")
mod@code</pre>
```

7.13.3 Rcpp (random numbers)

This gives you functions and data structures that you're used to using in R, but they work in c++.

The main use for this is random number generation. Any d/q/p/r function in R will be available; arguments are the same, but omit n (you always get just one draw when calling from c++.

For a draw from U(0,1)

```
$PLUGIN Rcpp

$ERROR
double u = R::runif(0, 1);
```

Note: this will slightly increase compile time.

7.14 Other blocks

- Use \$SETUP to configure the model object on load
 - For example, set the simulation end time
- Use \$ENV to define a set of R objects that might be evaluated in other model blocks
- Use \$PRED for other closed form models
- Use \$PREAMBLE for code that gets run once at the start of a problem NEWIND==0
- Use \$GLOBAL to define variables outside of any other block

7.15 Variables and macros

There is too much syntax to mention it all here. You will find all the syntax here

https://mrgsolve.org/user-guide/

7.16 Modeled event times

To get the model to stop at any time (even if not in the data set) with EVID 2

```
double mt1 = self.mtime(1.23 + ETA(1));
```

To get the model to stop at any time with user-specified EVID (e.g. 33)

```
self.mevent(1.23 + ETA(1), 33);
```