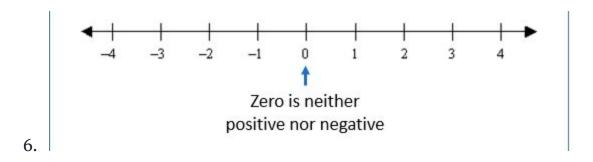
# Negative Number Operations and Fractions

A Study Guide

Some basic rules we must agree upon first:

(We will use the \* symbol for multiplication)

- 1. A negative number is just a number that has been multiplied by -1. i.e. -a = a \* -1 e.g. -2 = 2 \* (-1)
- 2. Subtraction is just the *inverse* of addition. i.e.  $\mathbf{a} \mathbf{b} = \mathbf{a} + (-\mathbf{b})$  e.g.  $\mathbf{2} \mathbf{1} = \mathbf{2} + (-\mathbf{1})$
- 3. Division is the *inverse* of multiplication. i.e.  $\mathbf{a} \div \mathbf{b} = \mathbf{a} * (1/\mathbf{b})$  e.g.  $1 \div 2 = 1 * \frac{1}{2}$
- 4. Converting division and subtraction equations to multiplication and addition is convenient because multiplication and addition are commutative, meaning the order of terms (numbers) does not matter.
- 5. Number lines continue in the positive direction to the right and negative numbers to the left



### Adding Negative Numbers:

When adding negative numbers, move left on the number line toward the negative end. It is basically the same as subtracting.

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#### **Subtracting Negative Numbers:**

Remember that subtraction is the inverse of addition. Using the rule outlined in #2 we can see that when we want to subtract a negative number we first invert the operation (subtraction to addition) and the sign (negative or positive) of the following term.

When we add a negative number, we move toward the negative end of the number line, to the left.

i.e.. If we want to find 10 - (-5), first we invert the subtraction symbol to make it an addition problem, and we have to invert the sign of the following term (5). E.g.

$$10 - (-5) = 10 + (+5) = 15$$
  
 $10 - 5 = 10 + (-5) = 15$ 

#### Multiplying Negative Numbers

When multiplying negative numbers, use rule numbers 1 and 4 to rewrite the equation so that the only negative number is (-1).

i.e. To find the product of the equation 19 \* (-7), first convert the equation to 19 \* 7 \* (-1) and perform the multiplication problem normally.

e.g.

$$19 * (-7) = 19 * 7 * (-1) = 133 * (-1) = -133$$
  
You could also think of this one as =  $(20*7+(-7)) * (-1)$ 

If an odd number of negative numbers is multiplied, the product is negative. If an even number of negative numbers is multiplied, the product is positive. e.g.

$$(-1) * (-1) = 1$$

### **Dividing Negative Numbers**

Use rules 1 and 3 to work out these kinds of problems.

Convert division to multiplication and invert the term to be divided (rule 3), convert the negative number to (-1) \* (n). (rule 1)

e.g. 
$$12 \div (-4) = 12 * (1/4) * (-1) = 3 * (-1) = -3$$

## Negative Number Operations and Fractions

A Study Guide

Working with Mixed Numbers and Fractions

#### Basic rules:

- 1. Fractions are ratios that describe how many parts of a whole are represented.
- 2. All fractions are rational numbers
- 3. Fractions have been reduced completely when the numerator and denominator are coprimes
- 4. A whole number can be represented as the number of 1, or "the number of whole numbers". e.g. n = n/1, or 2 = 2/1
- 5. A common denominator is is a multiple of both denominators in any math problem. (Including the number 1, see rule 4 above)
- 6. Fractions can be defined as a long division problem. e.g.  $\frac{1}{2} = 3 \cdot 2$

Adding/Subtracting: Find a common denominator, convert to addition problem as necessary, solve and reduce.

e.g. 
$$2/3 + 3/4 = (2*4)/(3*4) + (3*3)/(4/3) = 8/12 + 7/12 = 15/12 = 5/4 = 11/4$$
. Why does this work?

In the above example, the number 2/3 was multiplied by 4/4 (or 1), and the second number was multiplied by 3/3 (or 1). The denominator 12 is a common factor of both numbers. In each case, the term was only multiplied by 1 by determining the lowest common denominator with the other term.

Multiplying: Convert mixed number to improper fraction first. Multiply numerators to determine product numerator, and multiply denominators to determine product denominator. Reduce and convert to mixed number.

e.g. 
$$33/8 * 4\% = 27/8 * 14/3 = (27*14) / (8*3) = 378/24 = 63/4 = 153/4$$

Division: First invert the divisor (2 becomes ½, ½ becomes 2) then multiply as above. A ÷ B = A \* 1/B

$$2 \div 1 = 2 * 1/2 = 2/1 * 1/2 = (2*1) / (1*2) = 2/2 = 1$$

The same rules for negative numbers apply to fractions. i.e. Convert the negative number to positive number \* -1, then multiply as normal. Odd number of -1 = negative number, even number of -1 terms = positive.