

Question 1 - Suppose that the data for analysis includes the attribute age. The age values for the data tuples are (in increasing order) 13, 15, 16, 16, 19, 20, 20, 21, 22, 22, 25, 25, 25, 25, 30, 33, 33, 35, 35, 35, 35, 36, 40, 45, 46, 52, 70.

- Use min-max normalization to transform the values of age to the range [0:1].
- Use z-score normalization to transform the values of age.
- Use normalization by decimal scaling to transform the values of age such that the transformed value is less than 1.

```
In [ ]: Age = np.array([13, 15, 16, 16, 19, 20, 20, 21, 22, 22, 25, 25, 25, 25, 30, 30])
```

(i) Min-Max

```
In [ ]: Age min
```

Out[ ]: 13

```
In [ ]: Age max
```

```
Out[ ]: 70
```

```
In [ ]: Age min max
```

```
Out[ ]: [0.0,
0.03508771929824561,
0.05263157894736842,
0.05263157894736842,
0.10526315789473684,
0.12280701754385964,
0.12280701754385964,
0.14035087719298245,
0.15789473684210525,
0.15789473684210525,
0.21052631578947367,
0.21052631578947367,
0.21052631578947367,
```

```
0.21052631578947367,  
0.2982456140350877,  
0.3508771929824561,  
0.3508771929824561,  
0.38596491228070173,  
0.38596491228070173,  
0.38596491228070173,  
0.38596491228070173,  
0.40350877192982454,  
0.47368421052631576,  
0.5614035087719298,  
0.5789473684210527,  
0.6842105263157895,
```

```
In [ ]: Age_mean = np.mean(Age)  
Age_std = np.std(Age)
```

(ii)Z score

```
In [ ]: Age_mean
```

```
Out[ ]: 29.962962962962962
```

```
In [ ]: Age_std
```

```
Out[ ]: 12.700193878606099
```

```
In [ ]: Age_Zscore = [(i - Age_mean)/Age_std for i in Age]
```

```
In [ ]: Age_Zscore
```

```
Out[ ]: [-1.3356459850221374,  
-1.1781680741243308,  
-1.0994291186754275,  
-1.0994291186754275,  
-0.8632122523287176,  
-0.7844732968798143,  
-0.7844732968798143,  
-0.705734341430911,  
-0.6269953859820077,  
-0.6269953859820077,  
-0.39077851963529775,  
-0.39077851963529775,  
-0.39077851963529775,  
-0.39077851963529775,  
0.0029162576092187234,  
0.23913312395592862,  
0.23913312395592862,  
0.3966110348537352,  
0.3966110348537352,  
0.3966110348537352,  
0.3966110348537352,  
0.4753499903026385,  
0.7903058120982517,  
1.1840005893427683,  
1.2627395447916716,
```

We can see that here that the dataset has at max 2 digit numbers, we can easily realize that  $j = 2$

```
In [ ]: display(Output)
```

	Age	Min-Max	Z-score	Decimal Scale
0	13	0.000000	-1.335646	0.13
1	15	0.035088	-1.178168	0.15
2	16	0.052632	-1.099429	0.16
3	16	0.052632	-1.099429	0.16
4	19	0.105263	-0.863212	0.19
5	20	0.122807	-0.784473	0.20
6	20	0.122807	-0.784473	0.20
7	21	0.140351	-0.705734	0.21
8	22	0.157895	-0.626995	0.22

	Age	Min-Max	Z-score	Decimal Scale
<b>9</b>	22	0.157895	-0.626995	0.22
<b>10</b>	25	0.210526	-0.390779	0.25
<b>11</b>	25	0.210526	-0.390779	0.25
<b>12</b>	25	0.210526	-0.390779	0.25
<b>13</b>	25	0.210526	-0.390779	0.25
<b>14</b>	30	0.298246	0.002916	0.30
<b>15</b>	33	0.350877	0.239133	0.33
<b>16</b>	33	0.350877	0.239133	0.33
<b>17</b>	35	0.385965	0.396611	0.35
<b>18</b>	35	0.385965	0.396611	0.35
<b>19</b>	35	0.385965	0.396611	0.35
<b>20</b>	35	0.385965	0.396611	0.35
<b>21</b>	36	0.403509	0.475350	0.36
<b>22</b>	40	0.473684	0.790306	0.40
<b>23</b>	45	0.561404	1.184001	0.45
<b>24</b>	46	0.578947	1.262740	0.46
<b>25</b>	52	0.684211	1.735173	0.52