



# Diagnosing the Porous Structure of Fuel Cell Electrodes

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Steinfeld, September 2020



**RWTH**AACHEN  
UNIVERSITY

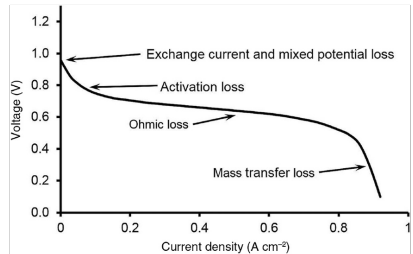
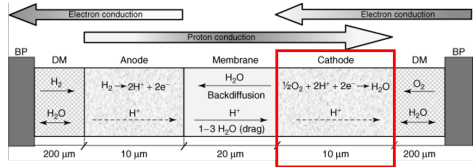
# Diagnosing the Porous Structure of Fuel Cell Electrodes

## Polymer Electrolyte Membrane Fuel Cell (PEMFC) The Challenges

### Performance limitations

### Material degradation

### Diagnosis of state of health



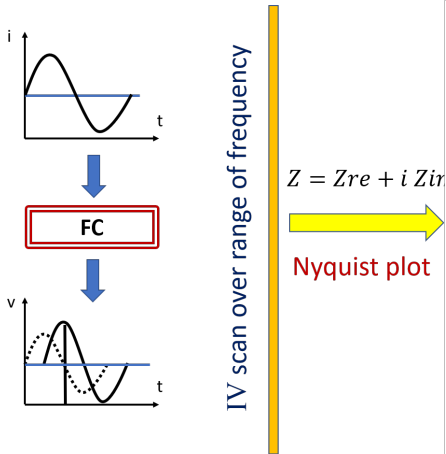
R. Gloukhovski et al. Reviews in Chem. Eng. (2017) 34, 455-479

Tang et al. J Electrochem. Soc. (2006) 153, A2036-43.

Voltage drop caused by charger transfer, membrane and mass transfer resistances at different current densities at 80 °C.

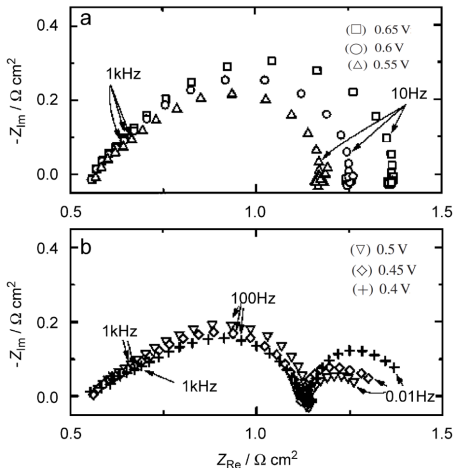
# Diagnosing the Porous Structure of Fuel Cell Electrodes

## Frequency response analysis

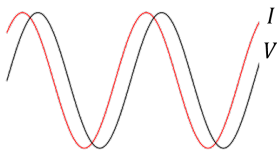


Paganin et al., *Electrochim. Acta* (1998) 43, 3761.

## Electrochemical Impedance Spectra



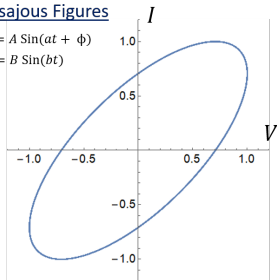
# Diagnosing the Porous Structure of Fuel Cell Electrodes



Lissajous Figures

$$x = A \sin(at + \phi)$$

$$y = B \sin(bt)$$



## Impedance Spectroscopy

IV scan over range of frequency

$$Z = Z_{re} + i Z_{im}$$

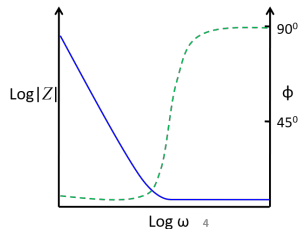
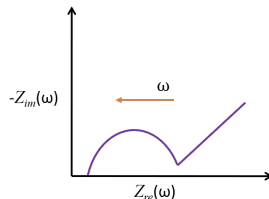
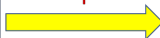
**Nyquist plot**



$$|Z| = \sqrt{Z_{re}^2 + Z_{im}^2}$$

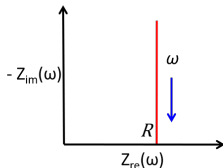
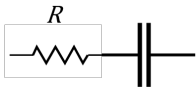
$$\phi = \text{Arctan} \left[ \frac{-Z_{im}}{Z_{re}} \right]$$

**Bode plot**

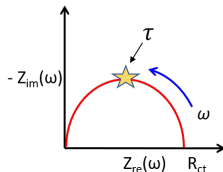
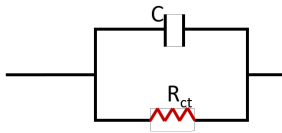


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## Nyquist Plot

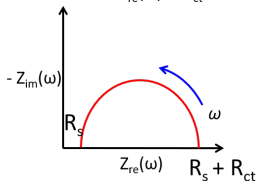
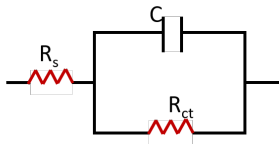


$$Z = R + \frac{1}{i\omega C}$$



$$Z = \left( \frac{1}{R_{ct}} + i\omega C \right)^{-1}$$

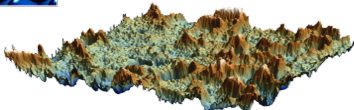
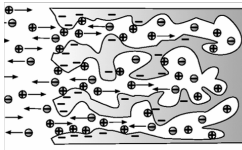
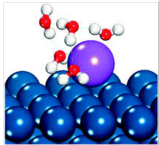
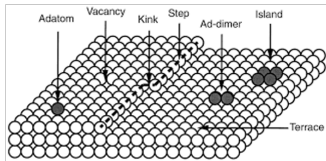
$$R_{ct} = \frac{RT}{nF i_0}$$



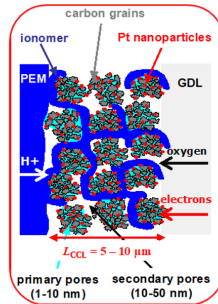
$$Z = R_s + \left( \frac{1}{R_{ct}} + i\omega C \right)^{-1}$$

# Diagnosing the Porous Structure of Fuel Cell Electrodes

## Sensitivity of EIS response and physics based modeling approaches



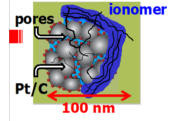
### Porous Cathode Catalyst Layer In PEMFC



Interface model

Macrohomogeneous model

Agglomerate model



M. Eikerling and A. Kulikovsky. Polymer Electrolyte Fuel Cells—Physical Principles of Materials and Operation. CRC Press, 2017. ISBN 9781138077447

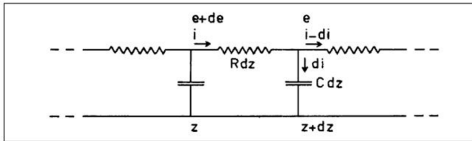
# Diagnosing the Porous Structure of Fuel Cell Electrodes

## Transport in porous electrodes

Electrochimica Acta, 1963, Vol. 8, pp. 751 to 780.

### ON POROUS ELECTRODES IN ELECTROLYTE SOLUTIONS\*

R. DE LEVIE§  
Electrochemistry Laboratory, University of  
Amsterdam, Holland



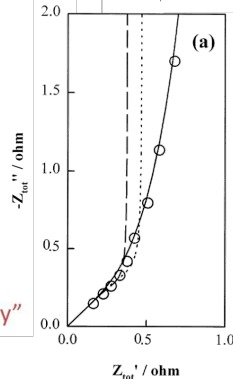
“RC Transmission Line Theory”, or “De Levie Theory”

Song et al. Electrochimica Acta 44 (1999) 3513-3519

M. E. Orazem and Bernard Tribollet. Electrochemical Impedance Spectroscopy. John Wiley & Sons, 2018. DOI:10.1002/9780470381588

## Distributed circuit elements

$$Z(\omega) = \sqrt{\frac{R_{sol}}{i\omega C_{dl}}} \coth \sqrt{R_{sol} i\omega C_{dl}}$$



- Not any random distribution would work.
- **Distributed** time constant, pore size distribution.

# Diagnosing the Porous Structure of Fuel Cell Electrodes

## Frequency Response Analysis

### Transfer Functions

Assume an initially relaxed linear system excited at  $t=0$  by an input  $x(t)$ , and assume that  $y(t)$  is the corresponding output. Let

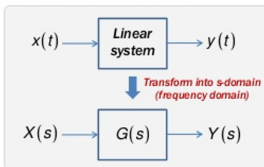
$$X(s) = \mathcal{L}[x(t)]$$

$$Y(s) = \mathcal{L}[y(t)]$$

For a linear system

$$Y(s) = G(s) X(s)$$

where  $G(s) = \frac{Y(s)}{X(s)}$  is called the **transfer function** of the circuit or system, and it provides a direct mathematical relationship between the input and the output for any arbitrary input.



**Transient response function**  
response of a system to a change from an equilibrium or a steady state

**Impedance response probe**  
Small harmonic perturbation  
Linear response

M. E. Orazem and Bernard Tribollet. Electrochemical Impedance Spectroscopy. John Wiley & Sons, 2018. DOI:10.1002/9780470381588

M. Eikerling and A. Kulikovskiy. Polymer Electrolyte Fuel Cells –Physical Principles of Materials and Operation. CRC Press, 2017. ISBN 9781138077447

A. A. Kulikovskiy. Analytical Modeling of Fuel Cells. Second Edition, Elsevier, 2017. ISBN 978-0-444-64222-6



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## MODELING METHODOLOGY

### Conservation equations:

Mass, charge, momentum, energy

$$\frac{\partial c_{H^+}}{\partial t} - D_{H^+} \nabla \cdot \left( \nabla c_{H^+} + \frac{F c_{H^+}}{RT} \nabla \varphi \right) = 0$$

$$\frac{\partial c_{O_2}}{\partial t} - D_{O_2} (\nabla c_{O_2}) = 0$$

For concentration and potential

$$x = \bar{x} + \delta x e^{i\omega t}$$

Linearization in Fourier space

For concentration and potential

$$\delta \varphi, \delta c$$

Electrochemical Impedance response of a pore

$$Z(\omega) = \frac{1}{2\pi R} \cdot \frac{\delta \phi^M(\omega)}{\int_0^L \delta j(\omega, z) dz}$$

Boundary conditions:

- reaction kinetics,
- metal charging,
- surface charge density

Pore size distribution  
Particle size distribution

M. Eikerling, A.A. Kornyshev, J. Electroanal. Chem. 475 (1999) 107–123

K. Chan, M. Eikerling, J. Electrochem. Soc. 159 (2012) B155-B164

A. Kulikovskiy, J. Electrochem. Soc. 164 (2017) F374-F386

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