

3.1.1

we have $f(n)$ & $g(n)$, asymptotically non-negative f^u .

we have to prove

$$\max(f(n), g(n)) = \Theta(f(n) + g(n))$$

$$\begin{aligned} \text{let us take } f(n) &= a_1 x^n + a_2 x^{n-1} + \dots + a_n \\ g(n) &= a_1 x^m + a_2 x^{m-1} + \dots + a_n \end{aligned}$$

Now to find $\max(f(n), g(n))$

let's add $f(n) + g(n)$

$$= a_1(x^m + x^n) + a_2(x^{m-1} + x^{n-1}) + \dots$$

Now the greater among them will be given by

$$\Theta(f(n) + g(n)) = \sum_{\substack{\max \\ a_i}} a_i x^{\max}$$

$$\text{Hence } \max(f(n), g(n)) = \Theta(f(n) + g(n))$$