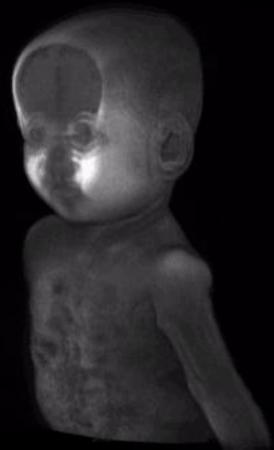


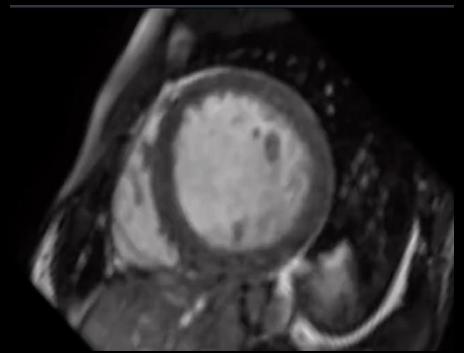
MRI reconstruction methods: Compressed sensing, model-based and machine learning methods

Efrat Shimron

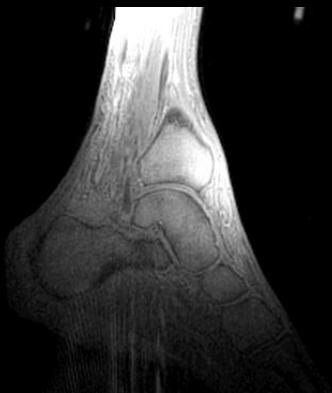
MRI



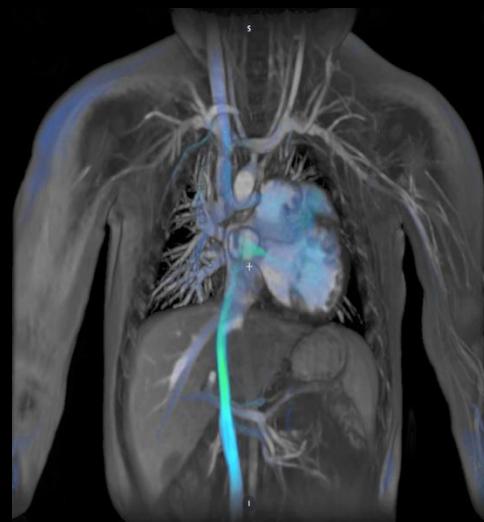
Courtesy of Lustig lab



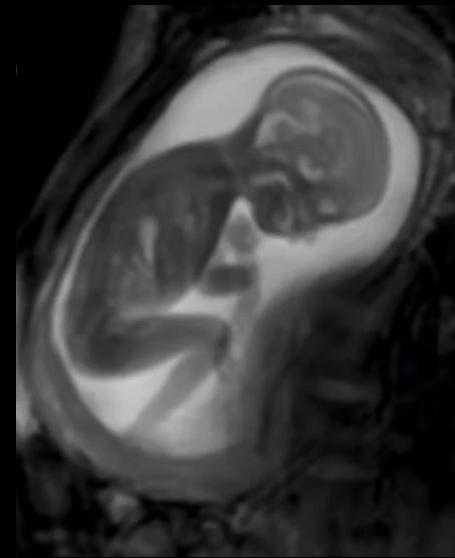
Courtesy of Lustig lab



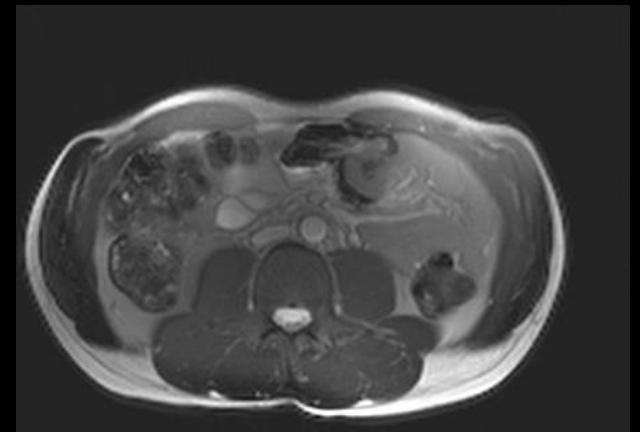
Courtesy of Lustig lab



Courtesy of Joseph Cheng/Stanford

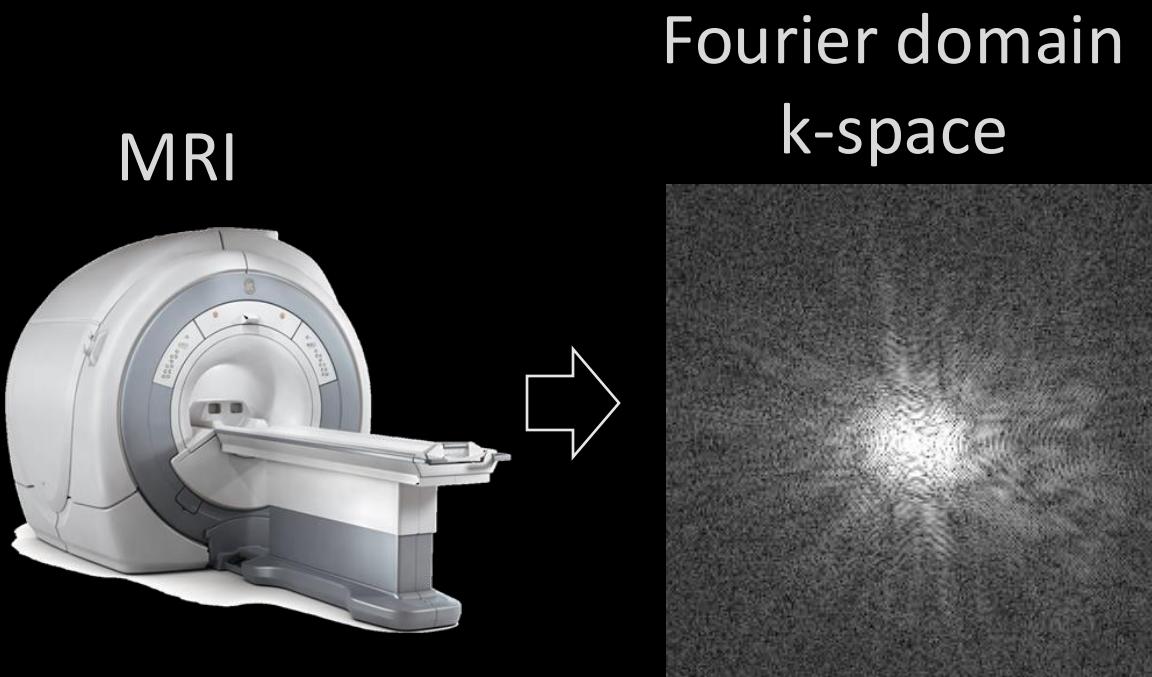


www.youtube.com/user/channelmum

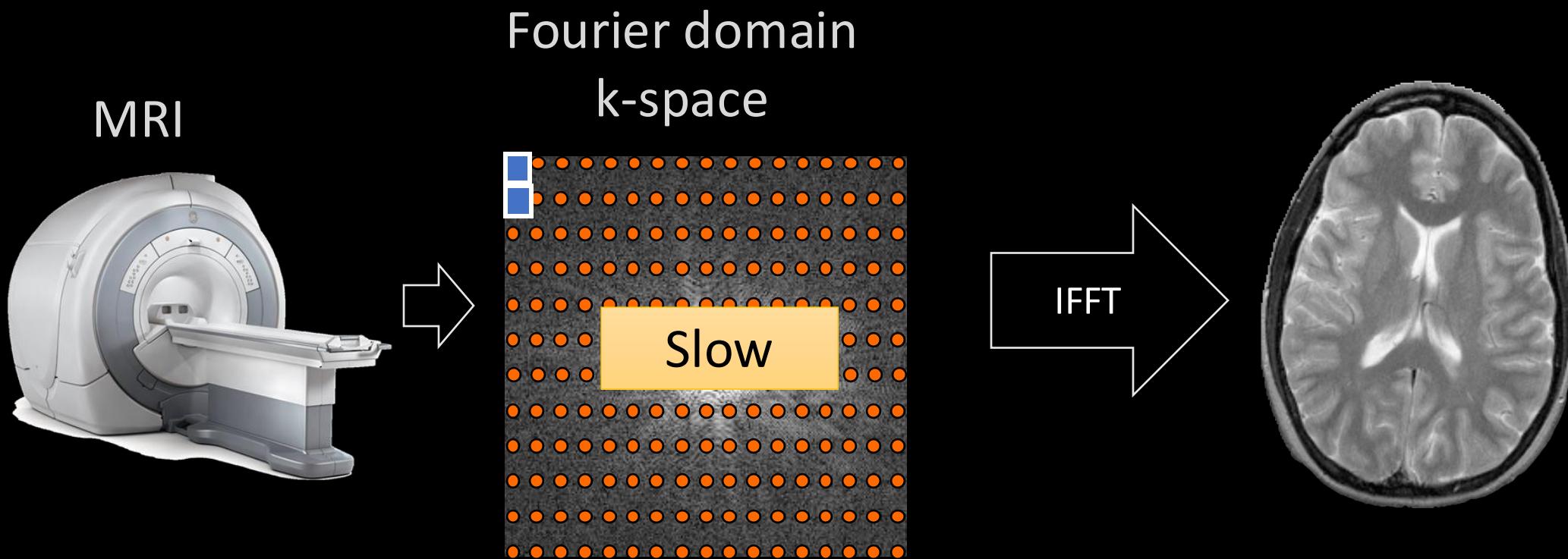


Courtesy of Lustig lab

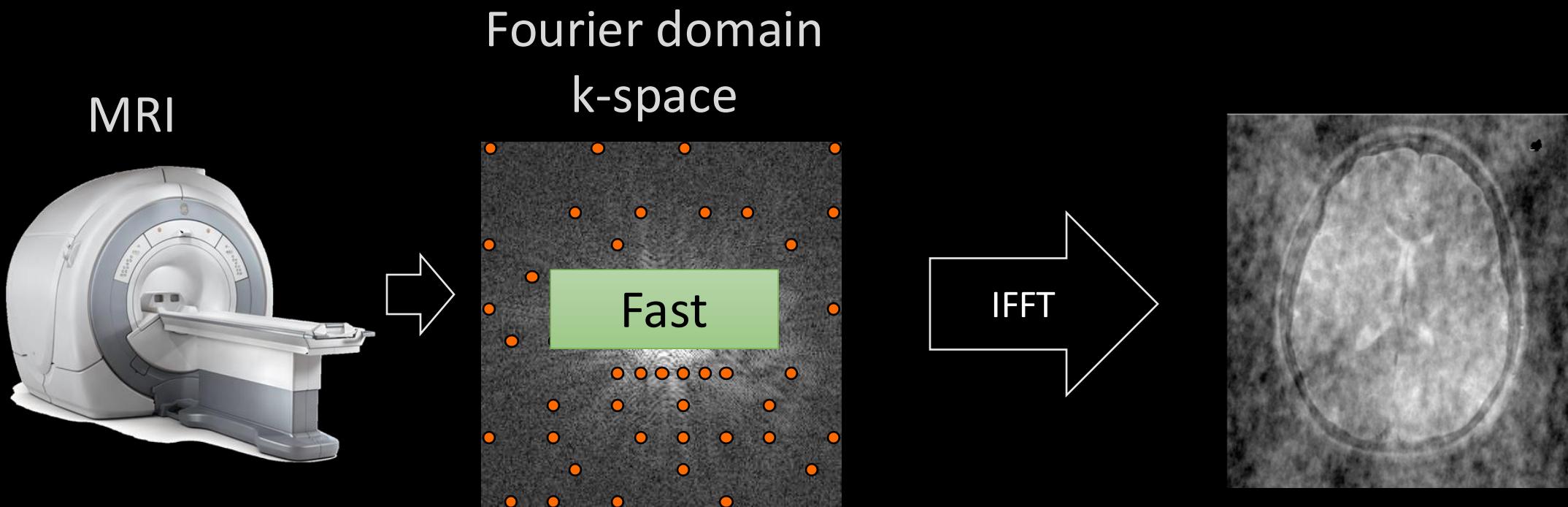
MRI: from sampling to images



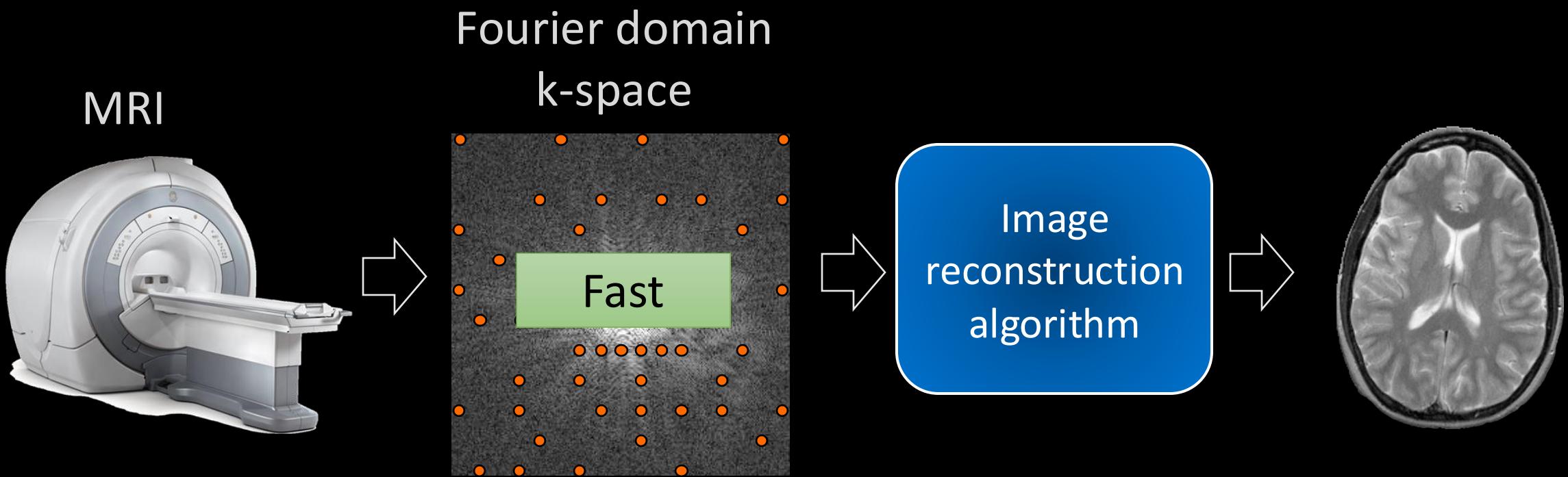
MRI: from sampling to images



MRI: from sampling to images



MRI: from sampling to images



The MRI inverse problem



Measurement model: $y = Ax + n$

acquired data forward operator image (unknown) noise

```
graph LR; A[acquired data] --> y["y = Ax + n"]; B[forward operator] --> y; C[image<br/>(unknown)] --> y; D[noise] --> y;
```

Aim: estimate x from y

Under-sampling → ill-posed problem

The MRI inverse problem



Measurement model: $y = Ax + n$

Image reconstruction - least-squares problem:

$$\min_x \|y - Ax\|_2$$

Closed form solution

$$\hat{x} = (A^H A)^{-1} A^H y$$

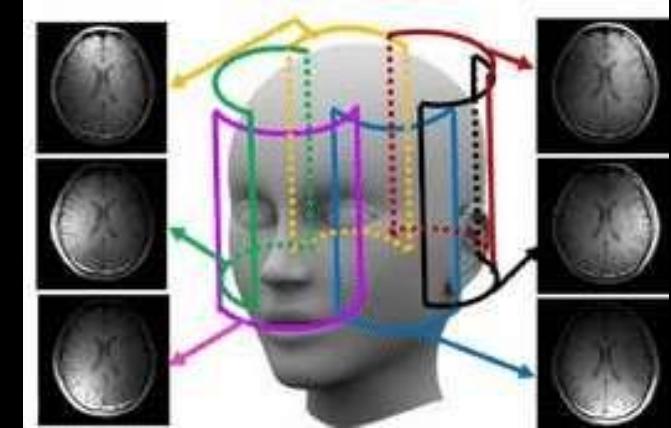
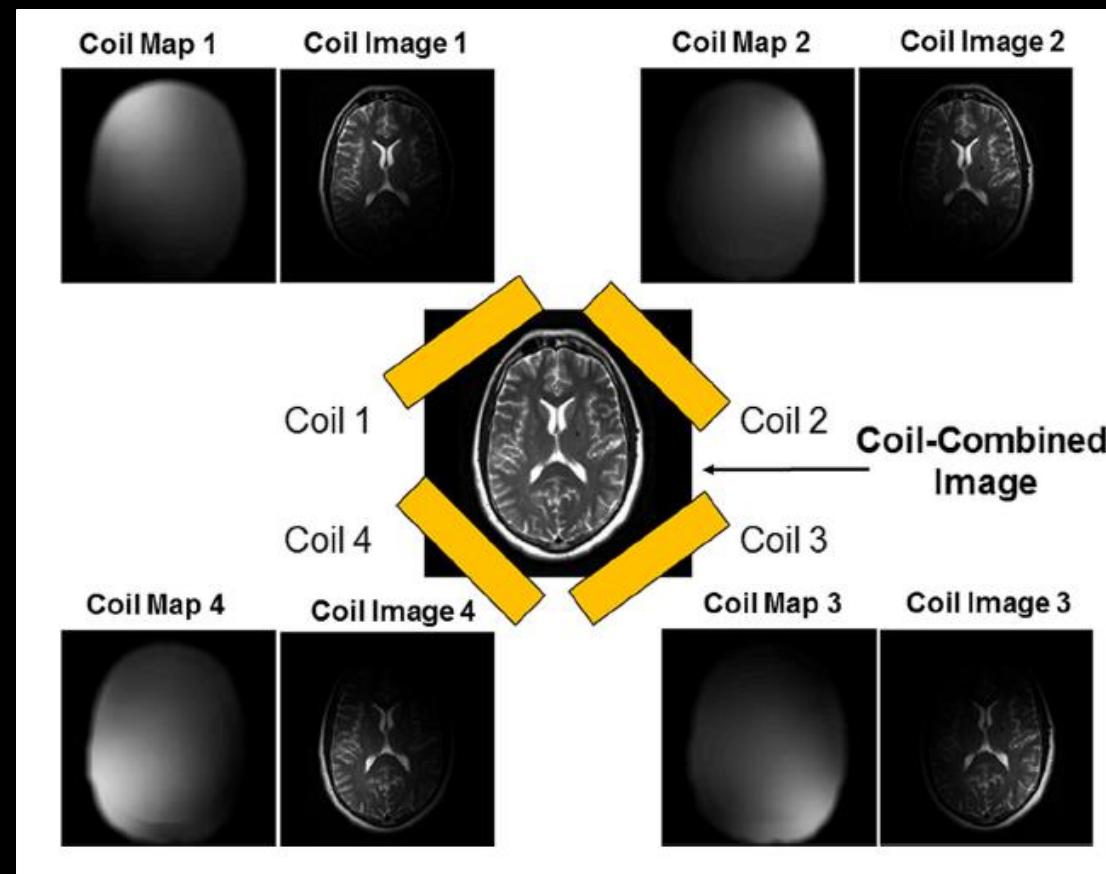
Reviews: Fessler, IEEE Signal Processing 2010

Hammernik et al., "Physics-based deep learning.." IEEE Sig Proc Magazine 2023

Parallel Imaging

Parallel MRI

Imaging with multi-coil arrays



Parallel Imaging Illustration
Mardani et al. arxiv

Pruessman et al., 1999, MRM; Griswold et al., 2002, MRM; Sodickson et al 2000; Hamilton et al. (2017) Prog Nucl Mag Res Sp

Parallel MRI

SENSE

GRAPPA

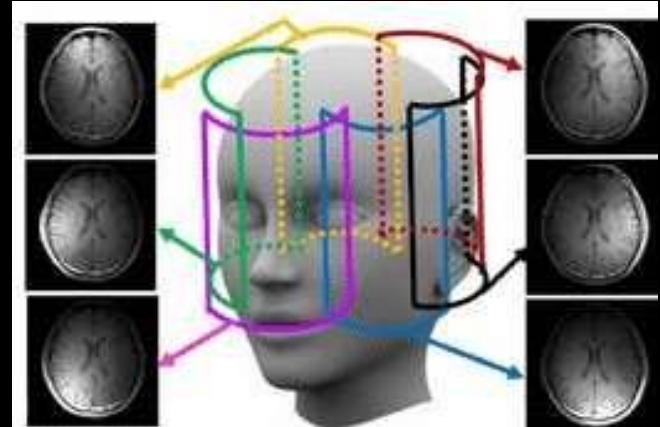
Advantages:

- Linear computations
- High SNR
- Clinical applications

Limitations:

- modest acceleration (2-4)

How can we do better?



Parallel Imaging Illustration
Mardani et al. arxiv

Pruessman et al., 1999, MRM; Griswold et al., 2002, MRM; Sodickson et al 2000; Hamilton et al. (2017) Prog Nucl Mag Res Sp

The MRI inverse problem



A *regularized* least-squares problem:

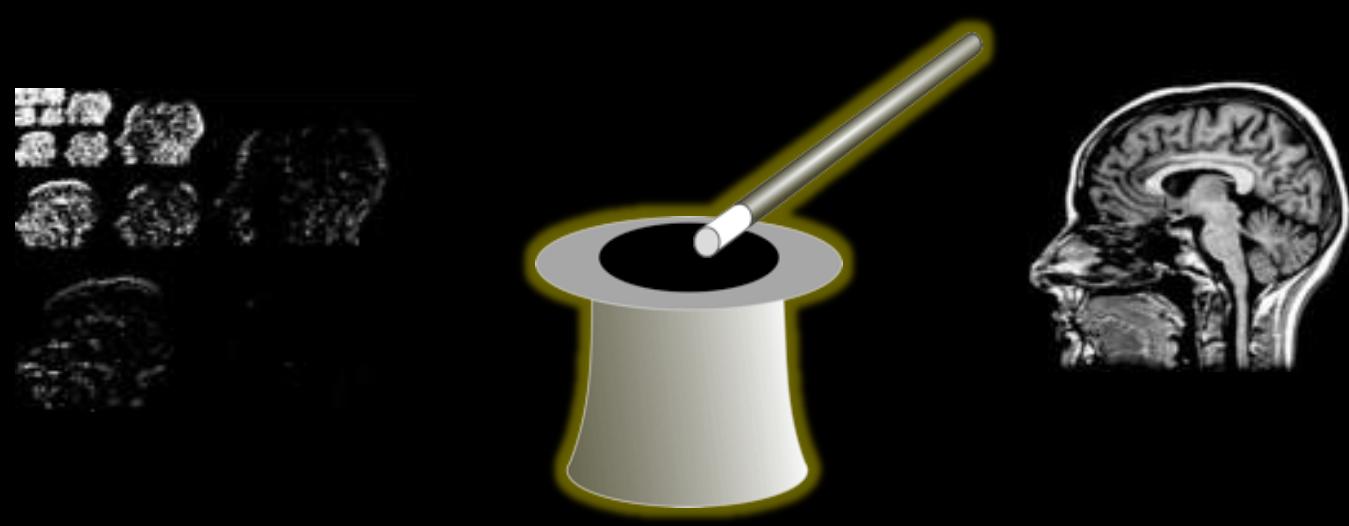
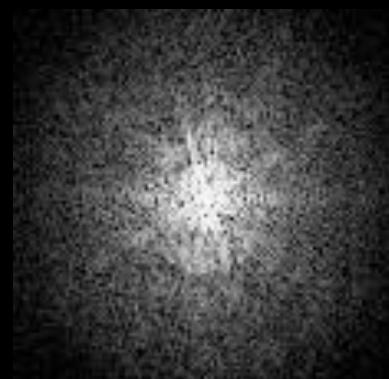
$$\min_x \|y - Ax\|_2 + \lambda R(x)$$

Types of regularization:

- Tikhonov: $R(x) = \|x\|^2$
- Compressed sensing - promotes sparsity

knowledge

Compressed Sensing



Compressed Sensing



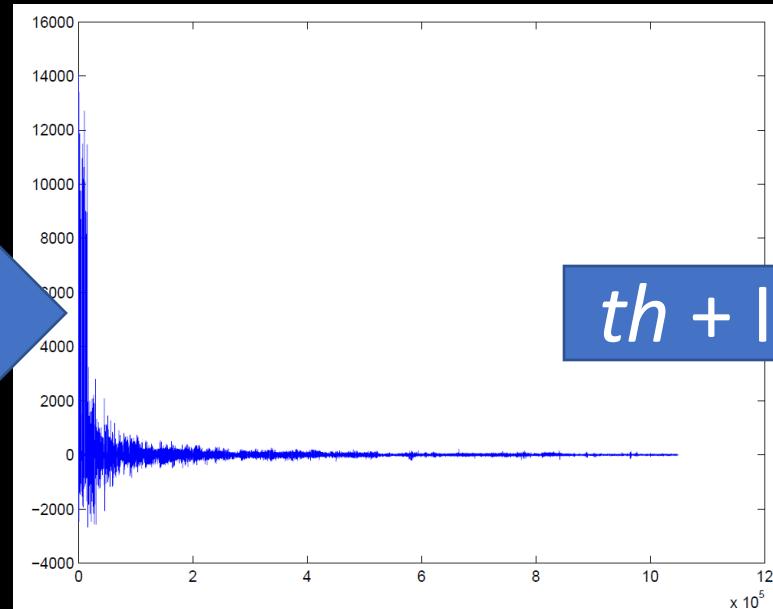
Sparsity

An image is **sparse** if it has very few ‘strong’ coefficients



Full data
100% coeffs.

WT



$th + IWT$



Rec. Image
7% coeffs.

Lustig, Donoho, Pauly (2007); Candés, Romberg, Tao (2006); Donoho (2006)

Compressed Sensing



$$\min_x \underbrace{\|y - Ax\|_2}_\text{Data consistency} + \lambda \underbrace{|\Psi x|_1}_\text{Sparsity promoting regularization}$$

Data consistency

Sparsity promoting regularization

CS methods:

- Recover a **sparse** solution in the Ψ domain
- Introduce non-linearity
- Require *incoherent* undersampling artifacts

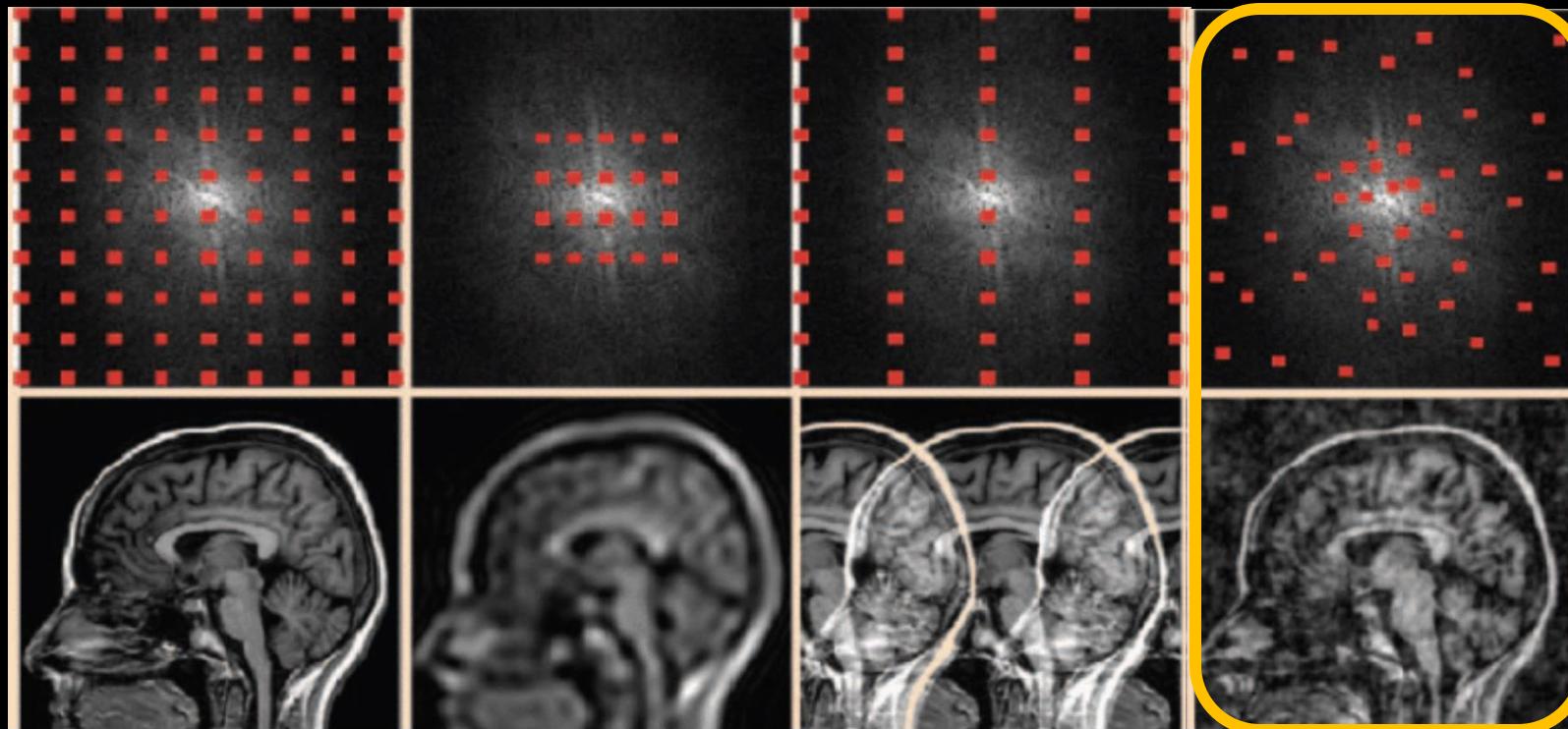
Lustig, Donoho, Pauly (2007); Candés, Romberg, Tao (2006); Donoho (2006)

Compressed Sensing



Ordered sampling

Random sampling



incoherent
“noise-like”
artifacts

Lustig, Donoho, Pauly (2007); IEEE Sig Proc Magazine; Feng et al., JMRI 2016

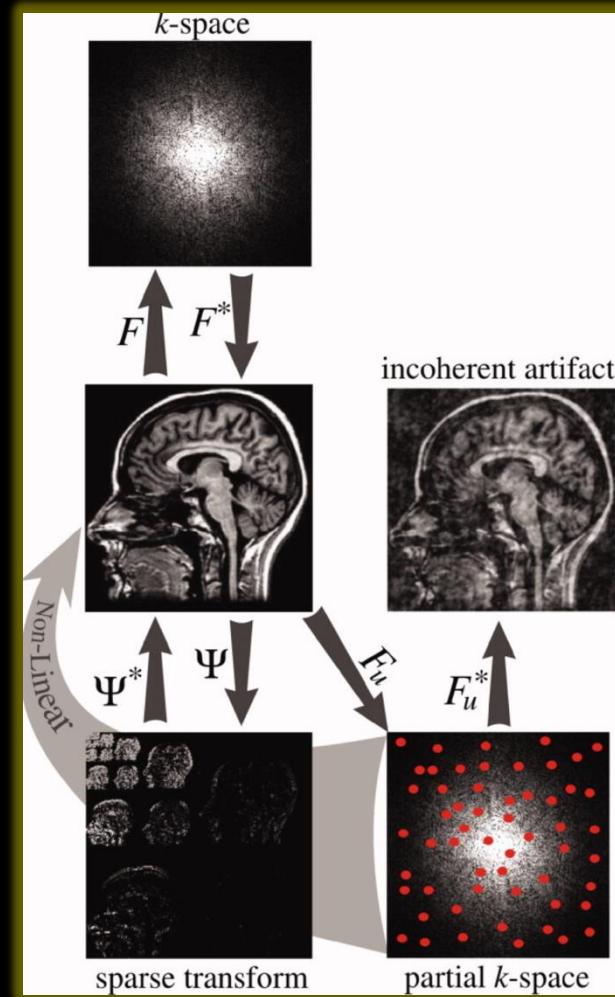
Compressed Sensing



Iterative reconstruction

Optimization algorithms:

- Iterative soft thresholding algorithm (ISTA)
- Proximal methods



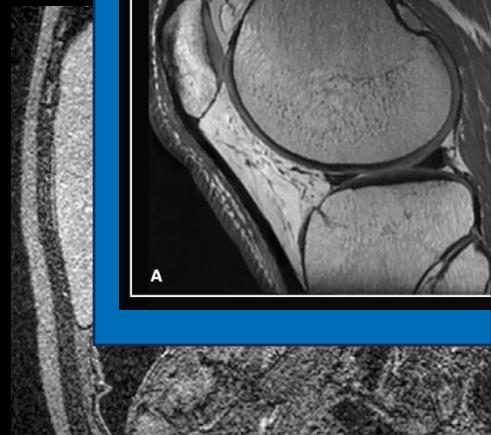
Fessler, J. "Optimization methods for MR image reconstruction" *arXiv* (2019)

Lustig, Donoho, Pauly (2007); IEEE Sig Proc Magazine; Feng et al., JMRI 2016

Compressed Sensing

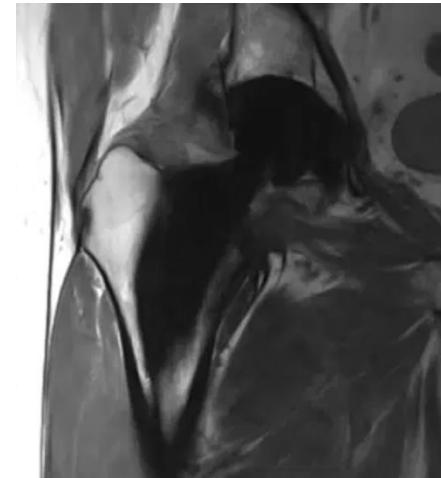


HyperSense



SIEMENS
Healthineers

Compressed Sensing SEMAC



Vasanawala et al., Radiology 2010

PHILIPS

Compressed SENSE

Lustig, Donoho, Pauly (2007); Candès, Romberg, Tao (2006); Donoho (2006)
Feng et al. MRI 2017;

Compressed Sensing



$$\min_x \underbrace{\|y - Ax\|_2}_\text{Data consistency} + \lambda \underbrace{|\Psi x|_1}_\text{Sparsity-promoting Regularization}$$

Data consistency

Sparsity-promoting
Regularization

Advantages:

- High acceleration (R)
- Convex optimization

Limitations:

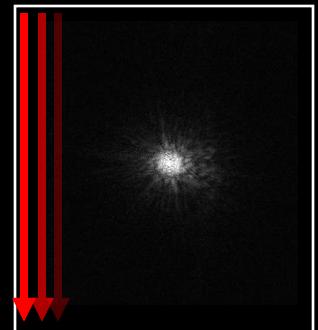
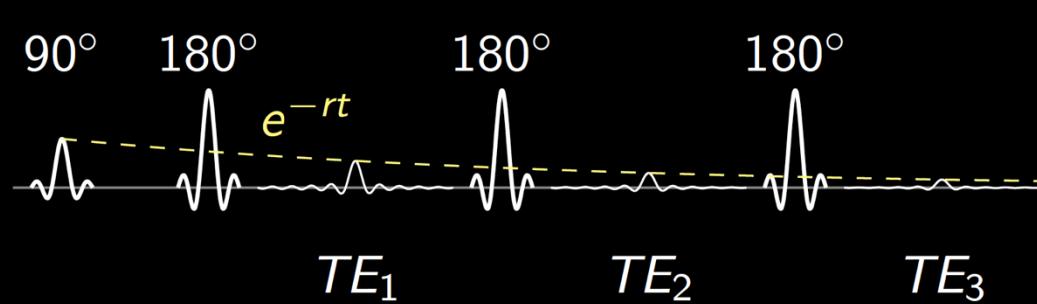
- Heavy iterative computations
- Sensitivity to parameter tuning

Lustig, Donoho, Pauly (2007); Candés, Romberg, Tao (2006); Donoho (2006)

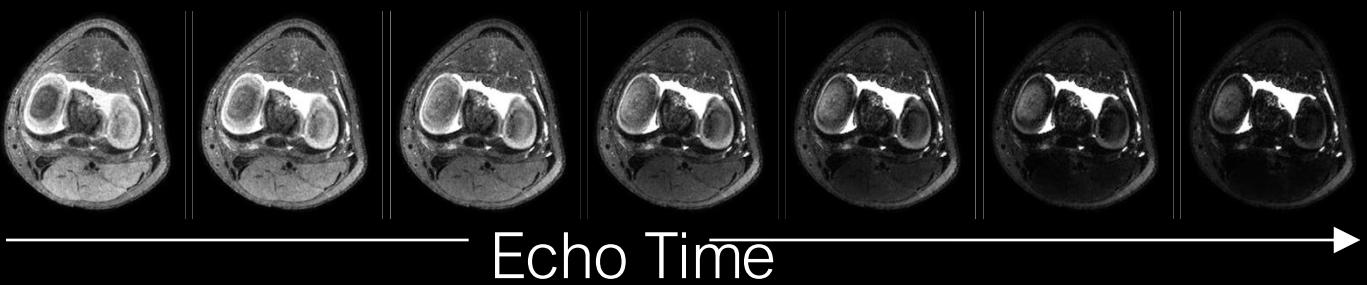
Model-based reconstruction

Adding *physics* to the optimization

Fast Spin-Echo



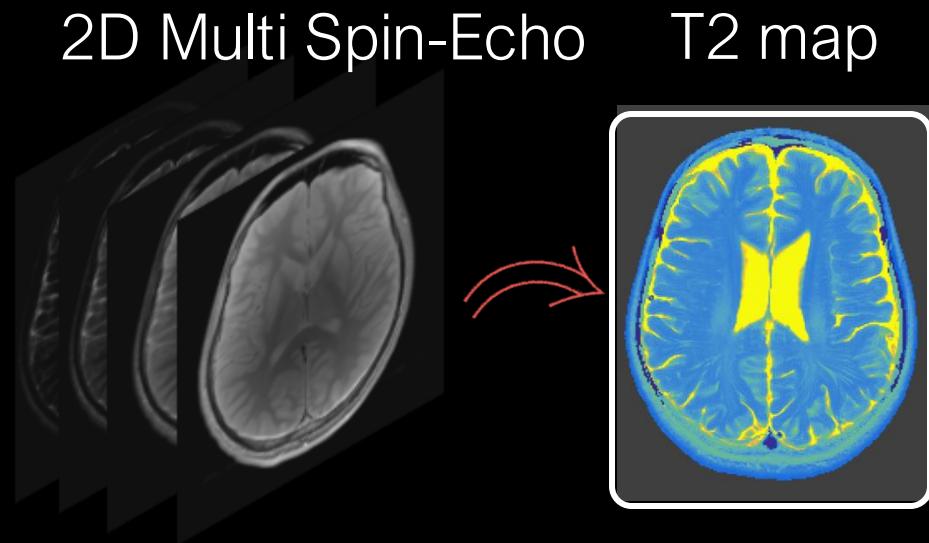
- Fast
- But - T2 blurring effect - the signal decays during sampling



Figures from Jonathan Tamir

Fast Spin-Echo

Quantitative imaging, e.g. T2 mapping, requires estimating a series of images – long scans



Figures from Jonathan Tamir

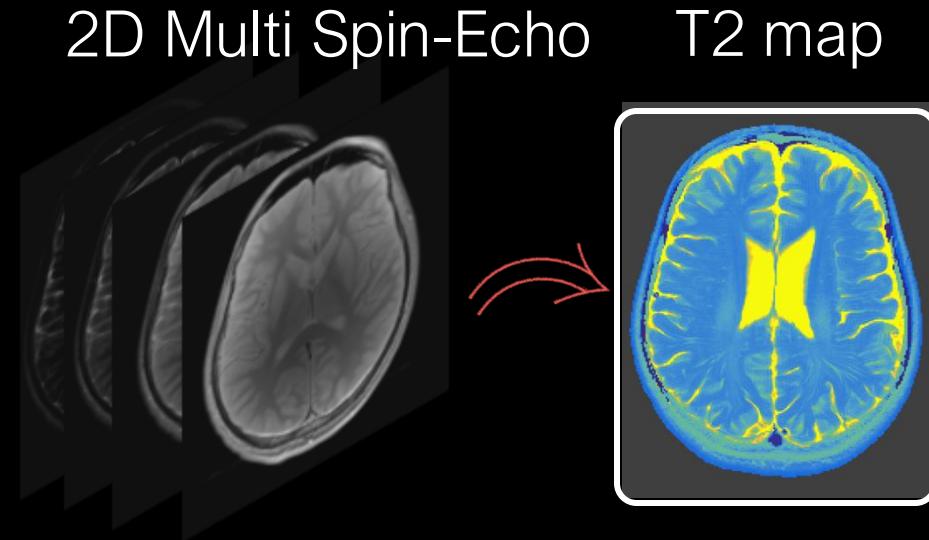
Model-based reconstruction

Signal decay is known – Bloch equations

We solve directly for parameter maps (T2, T1 maps)

Advantages:

- Dimensionality reduction
- We can synthesize images at any time



Figures from Jonathan Tamir

Model-based reconstruction

- The forward model now includes *relaxation* – it's *nonlinear*
- We solve directly for tissue relaxation maps $Q(\vec{x})$ (e.g., T2 map)
- We can also solve for the image simultaneously (ρ , spin density)

$$\min_{\rho, q} \|y - \mathcal{M}(\rho, q)\|_2 + R(x)$$

Forward
model:

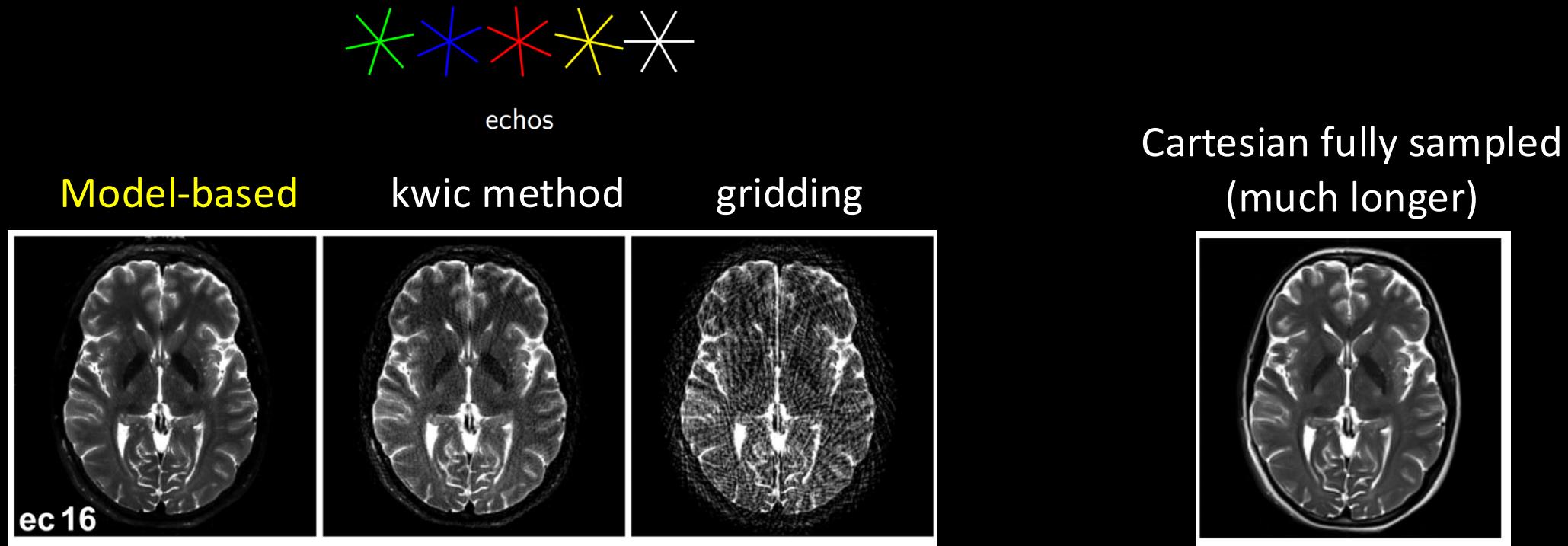
$$\mathcal{M}: (\rho, q) \rightarrow \int d\vec{x} \rho \vec{x} e^{-Q(\vec{x})} e^{-i\vec{k}(t)\vec{x}}$$

Requires algorithms for non-linear optimization, e.g. conjugate gradient

Block et al., IEEE TMI 2009; Fessler, IEEE Sig Proc Mag, 2010; Tamir et al, IEEE Sig Proc Mag 2020;
Wang et al., Philosophical Transactions of the Royal Society 2021

Model-based reconstruction

Example: solve directly for tissue relaxation map and image from radial spokes [Block et al., IEEE TMI 2009]

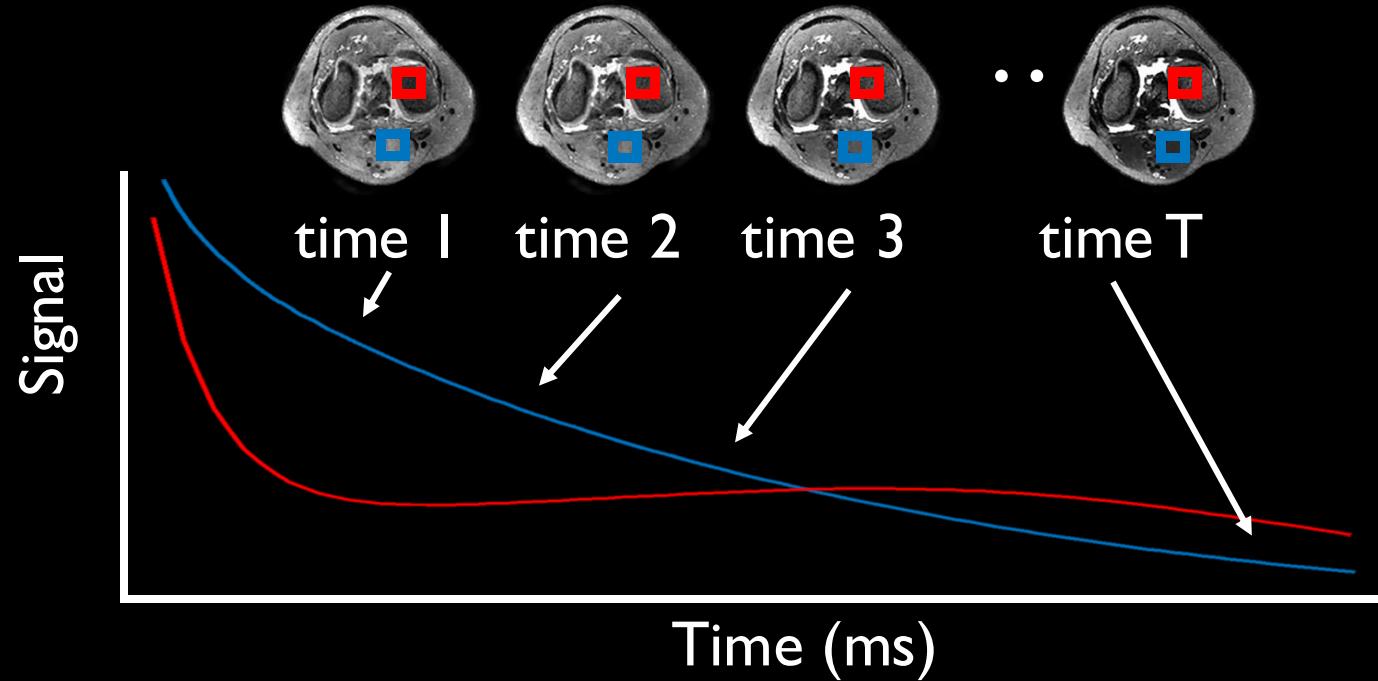


How can we do better?

Block et al., IEEE TMI 2009

Subspace-constrained reconstruction

Relaxation of different tissues is highly correlated
→ lower dimensional space



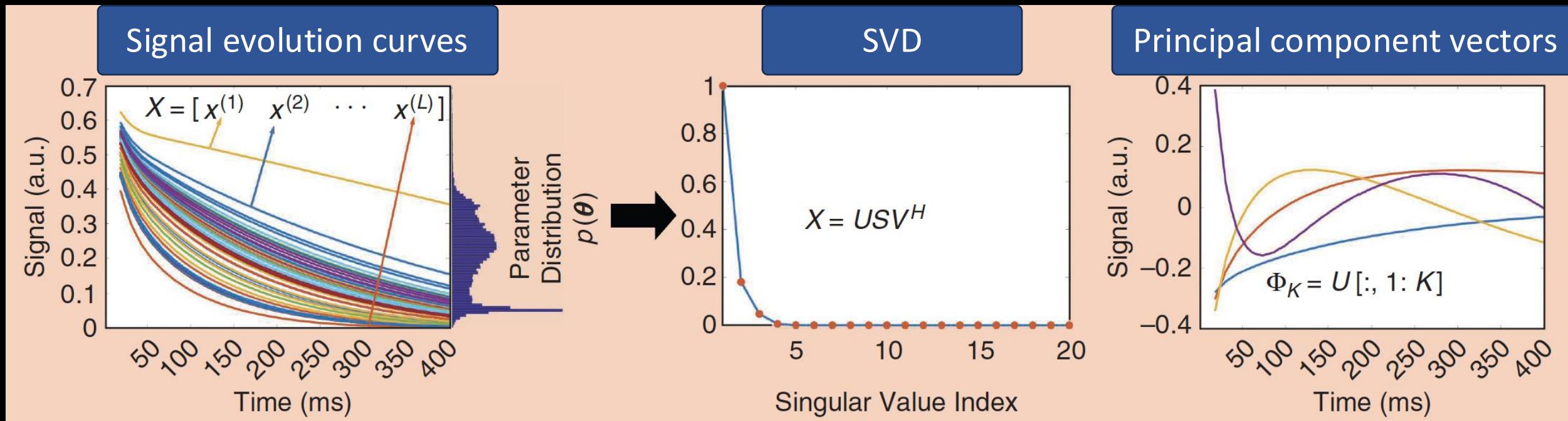
Subspace-constrained recon exploits the lower dimensionality

Figures from Jonathan Tamir

Tamir et al., "T2 shuffling", MRM (2017); Tamir et al, IEEE Sig Proc Mag 2020;

Subspace-constrained reconstruction

Plot signal curves \rightarrow SVD \rightarrow the main components (K largest values)
 \rightarrow use this to regularize the optimization problem



Tamir et al., "T2 shuffling", MRM (2017); Tamir et al, IEEE Sig Proc Mag 2020;

Subspace-constrained reconstruction

Plot signal curves → SVD → the main components (K largest values)
→ use this to regularize the optimization problem

$$\min_x \|y - Ax\|_2 + \lambda_1 \|x - \Phi_K \Phi_K^H\|_2^2 + \lambda_2 R(x)$$

{

Data consistency

{

Subspace-constrained
regularization

{

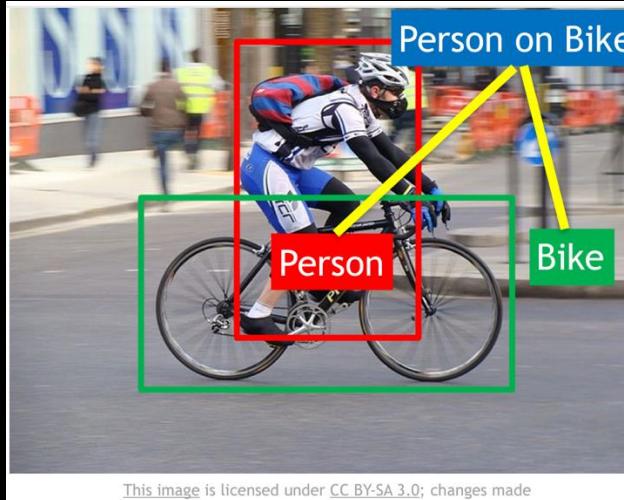
Other
regularization

Implemented in BART!

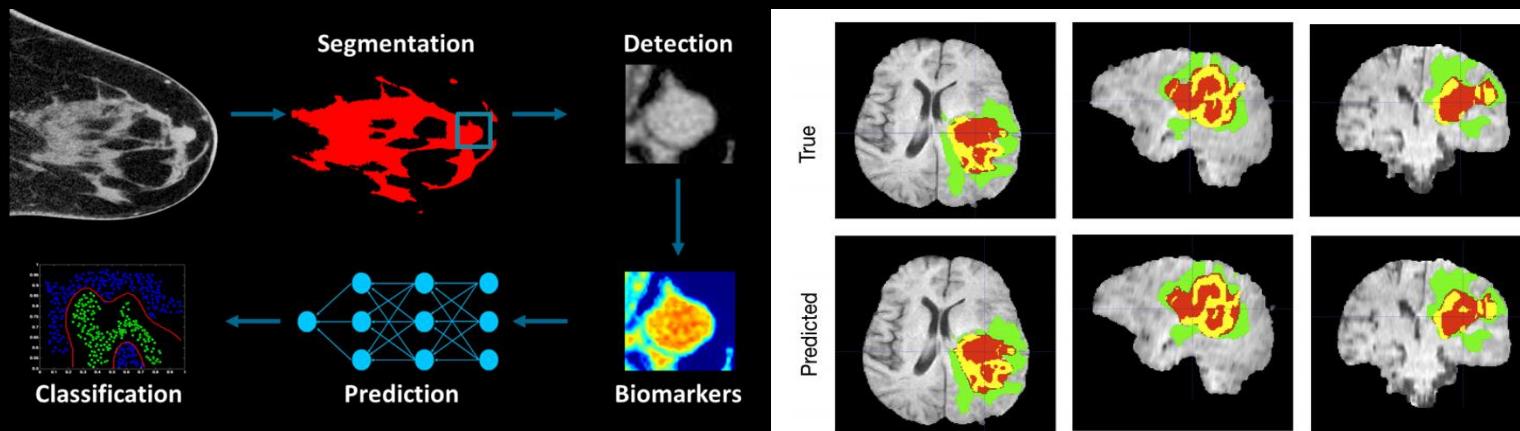
Coming up – hands-on tutorial by Martin's & Julia

Deep learning

Deep Learning



Mindy-support.com



<http://axti.radboudimaging.nl/>

Nvidia.com

Natural language Processing
ChatGPT

Deep Learning

Slides here:



ISMRM & ISMRT
ANNUAL MEETING & EXHIBITION

TORONTO
03-08 JUNE 2023

Berkeley
UNIVERSITY OF CALIFORNIA

BAIR
BERKELEY ARTIFICIAL INTELLIGENCE RESEARCH

Fundamentals of Deep Learning



Efrat Shimron



Review paper here:



Review paper

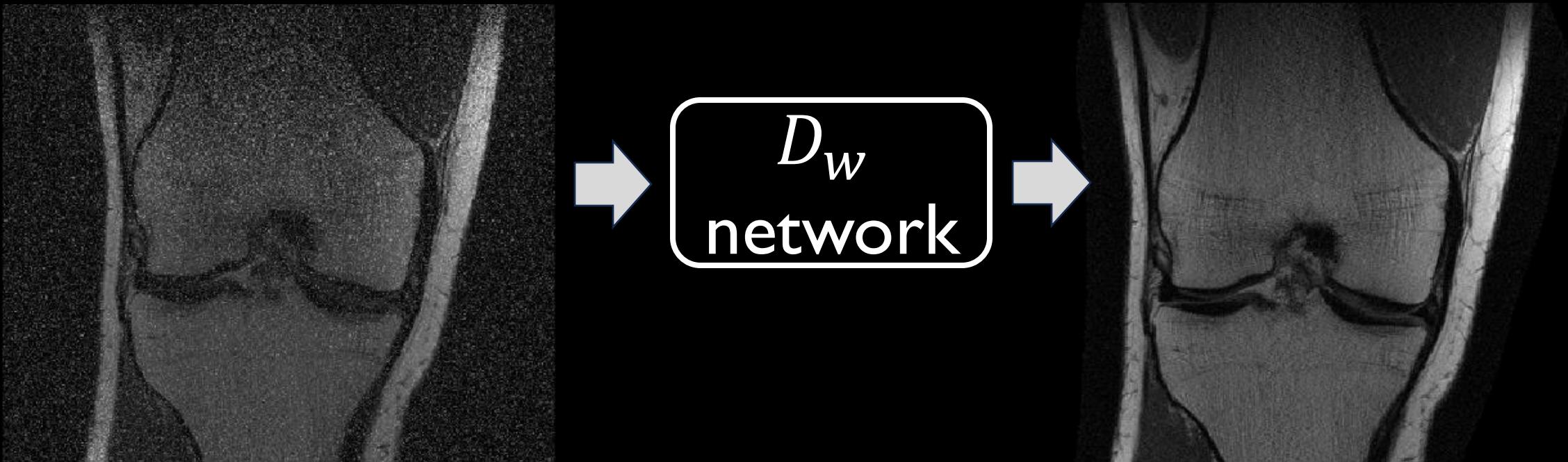
Deep learning for accelerated and robust MRI reconstruction

Reinhard Heckel, Mathews Jacob, Akshay Chaudhari, Or Perlman, Efrat Shimron, (MAGMA 2024)

Deep Learning

$$x_0 = F^{-1}(y)$$

$$\mathbf{x} = D_w(x_0)$$



Figures from Jonathan Tamir

Deep Learning

First deep-learning papers – data driven approach:
Learn the mapping from zero-filled images to reconstructed images

ACCELERATING MAGNETIC RESONANCE IMAGING VIA DEEP LEARNING

*Shanshan Wang¹, Zhenghang Su², Leslie Ying³, Xi Peng¹, Shun Zhu¹
Feng Liang⁴, Dagan Feng⁵ and Dong Liang¹*

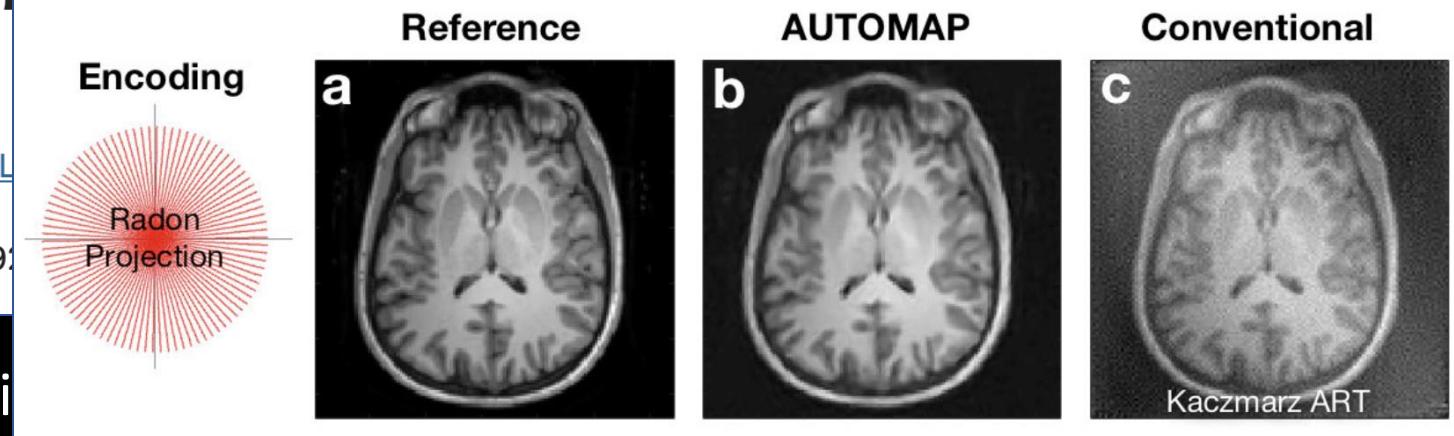
nature

Letter | Published: 22 March 2018

Image reconstruction by domain transform manifold learning

[Bo Zhu, Jeremiah Z. Lin et al.](#)

[Nature 555, 487–491](#)



Figures from Jonathan Tamir

Deep Learning



$$\min_x \|\gamma - Ax\|_2 + \lambda R(x)$$

Diagram illustrating the cost function for a linear inverse problem. The term $\|\gamma - Ax\|_2$ is crossed out with a large yellow X, indicating it is not used. The term $\lambda R(x)$ is circled in yellow and has a grey arrow pointing down to the text "Regularization".

Data consistency Regularization

Early deep learning methods:

$$x = D_w(x_0)$$

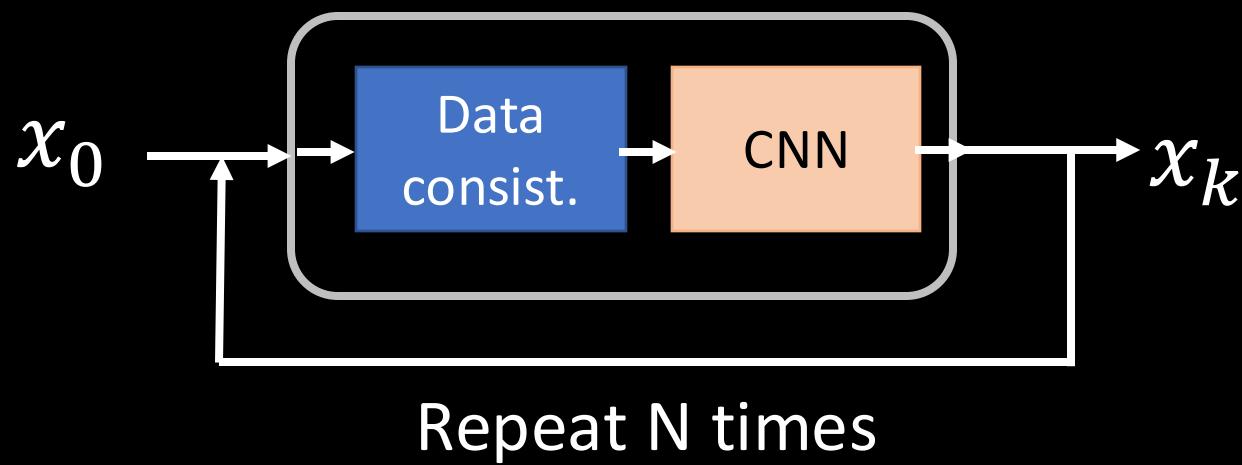
- Data driven
- Replace hand-crafted regularizers with *learned* ones
- No data consistency

Deep Learning

Iterative (unrolled) deep learning - the best of both worlds!

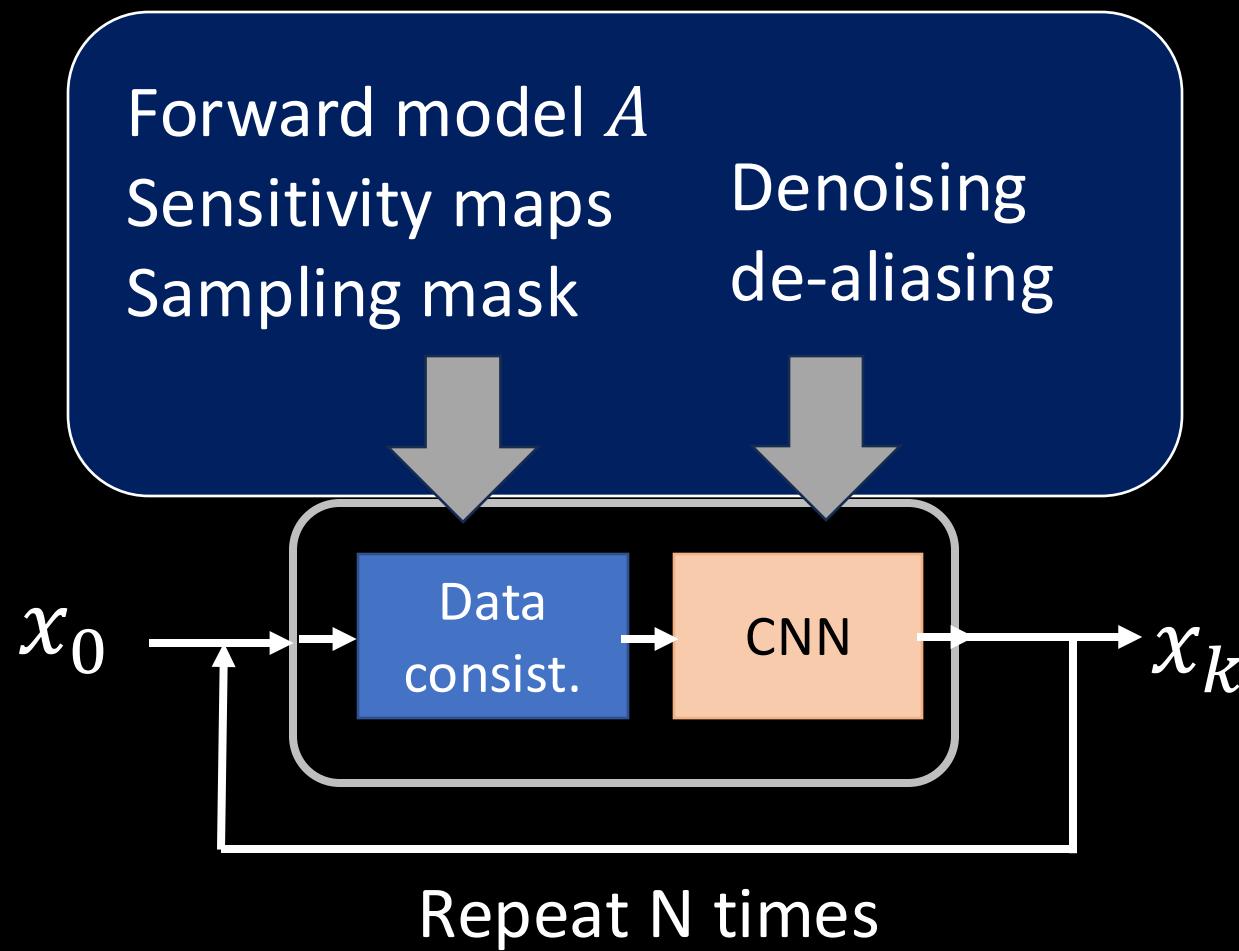
$$\min_x \underbrace{\|y - Ax\|_2}_\text{Data consistency} + \underbrace{D_w(x_0)}_\text{Deep-learning regularization}$$

Data consistency Deep-learning regularization



Deep Learning

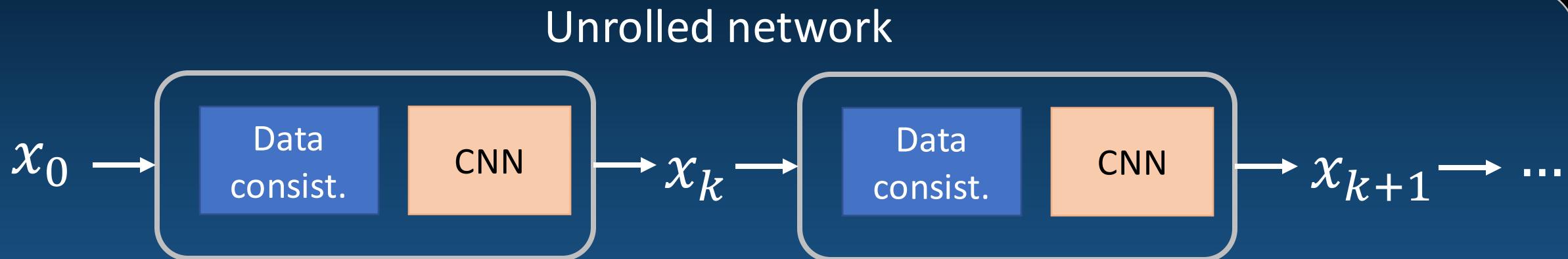
Iterative (unrolled) deep learning - the best of both worlds!



Deep Learning

Iterative deep learning - the best of both worlds!

$$\min_x \underbrace{\|y - Ax\|_2}_\text{Data consistency} + \underbrace{D_w(x_0)}_\text{Deep-learning regularization}$$



Full Paper |  Free Access

Learning a variational network for reconstruction of accelerated MRI data

Kerstin Hammernik , Teresa Klatzer, Erich Kobler, Michael P. Recht, Daniel K. Sodickson, Thomas Pock, Florian Knoll

Journals & Magazines > IEEE Transactions on Medical ... > Volume: 38 Issue: 2 

both worlds!

MoDL: Model-Based Deep Learning Architecture for Inverse Problems

Publisher: IEEE

Cite This

 PDF

Hemant K. Aggarwal ; Merry P. Mani ; Mathews Jacob  All Authors



IEEE TRANSACTIONS ON MEDICAL IMAGING, VOL. 37, NO. 2, FEBRUARY 2018

491

$x_0 \rightarrow$

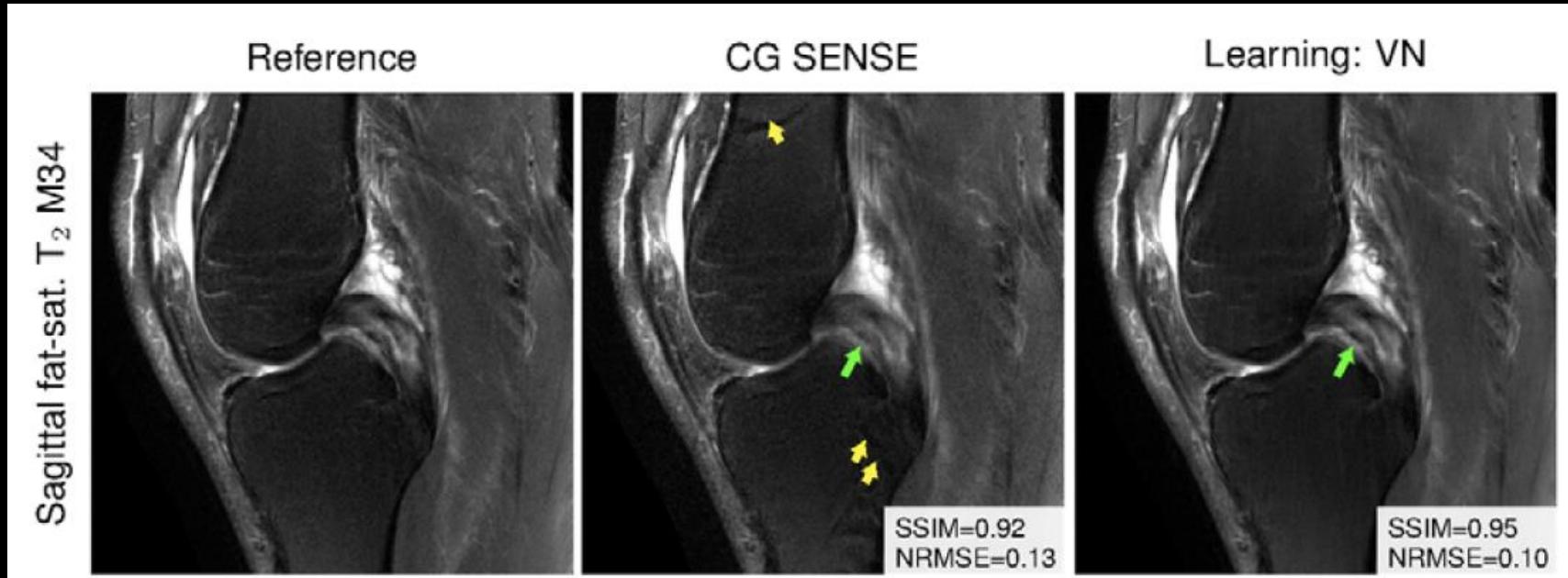
Data
consist.

A Deep Cascade of Convolutional Neural Networks for Dynamic MR Image Reconstruction

Jo Schlemper , Jose Caballero , Joseph V. Hajnal, Anthony N. Price, and Daniel Rueckert, Fellow, IEEE

Deep Learning

Iterative deep learning - the best of both worlds!



Hammernik et al., MRM 2018

Deep Learning

Training - Supervised learning:

Training data?

output target

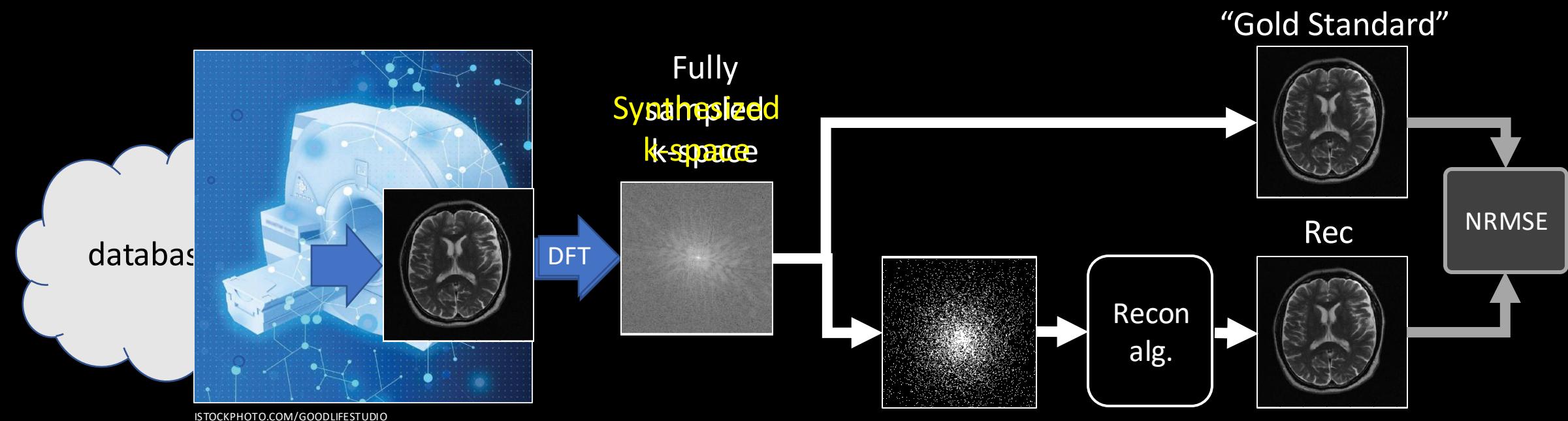
Loss



Data Crimes

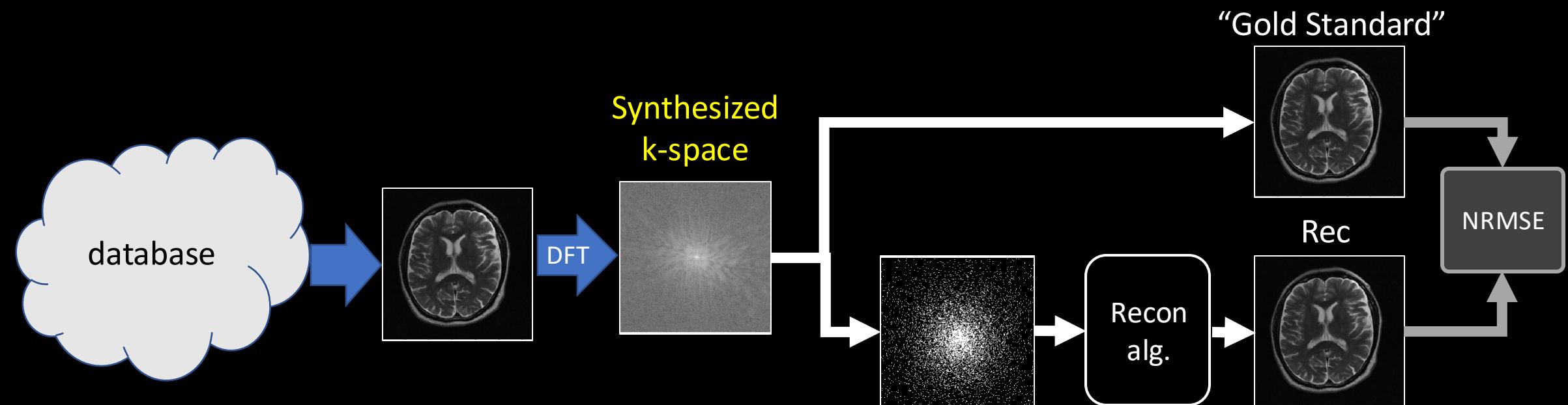


A Common Research Pipeline



Shimron et al., *Implicit data crimes*, PNAS (2022)

A Common Research Pipeline



Shimron et al., *Implicit data crimes*, PNAS (2022)



A Common Research Pipeline

Hidden data processing



database

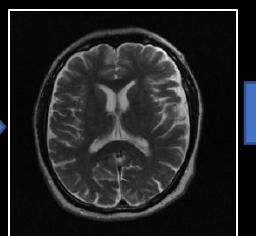


IXI Dataset

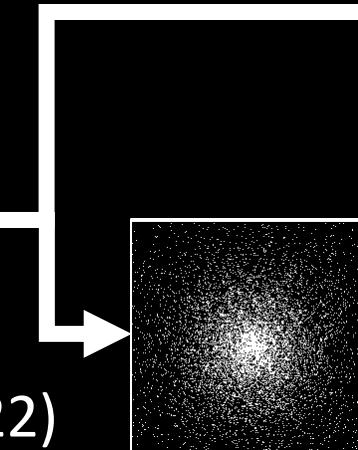
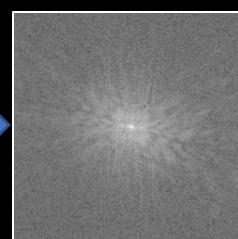
Biased!

download

Synthesized
k-space

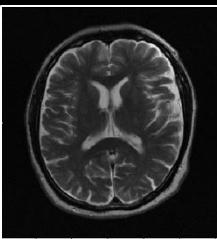


DFT



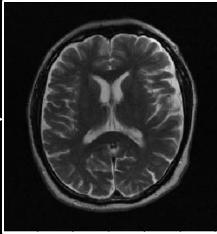
Recon
alg.

→



“Gold Standard”

Rec

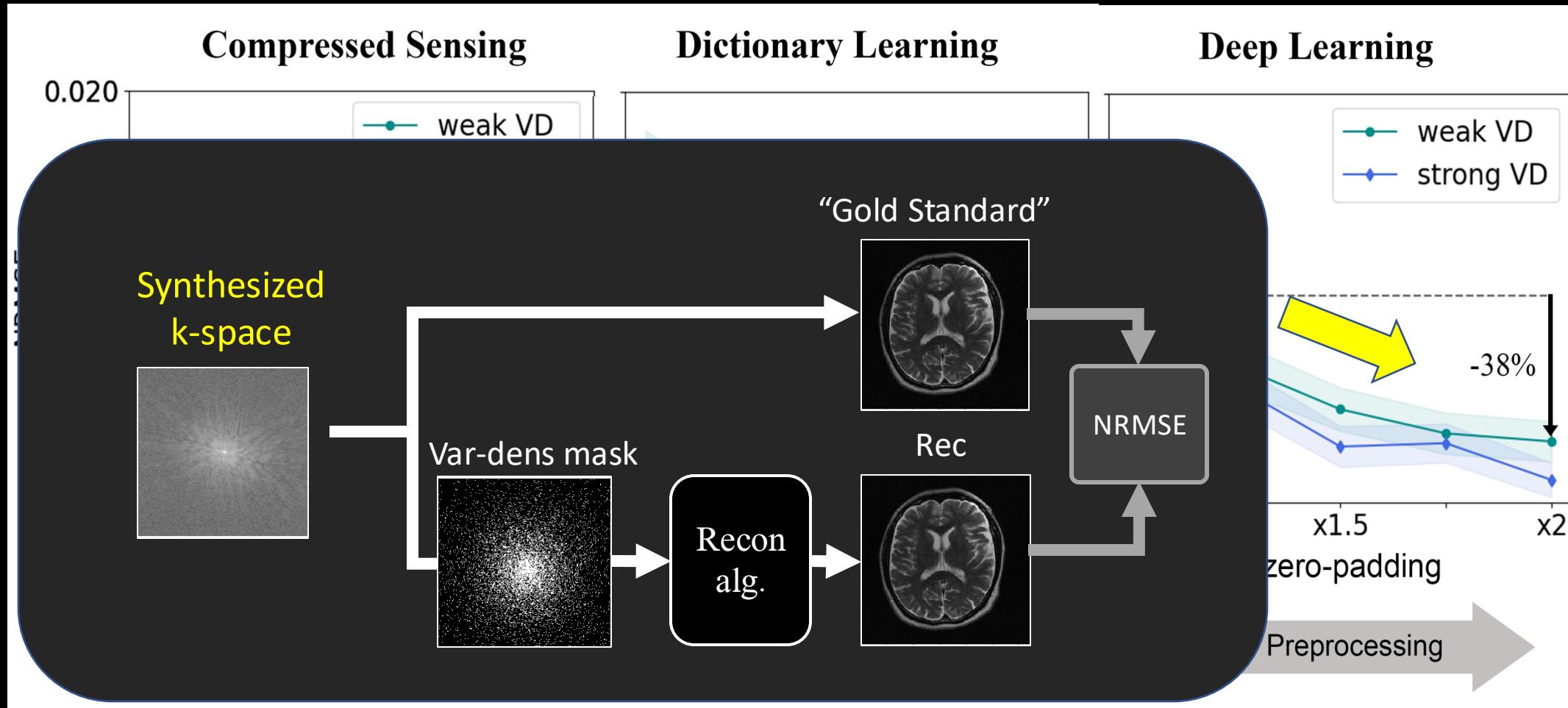


NRMSE

Shimron et al., *Implicit data crimes*, PNAS (2022)

Data Crimes

FastMRI Data

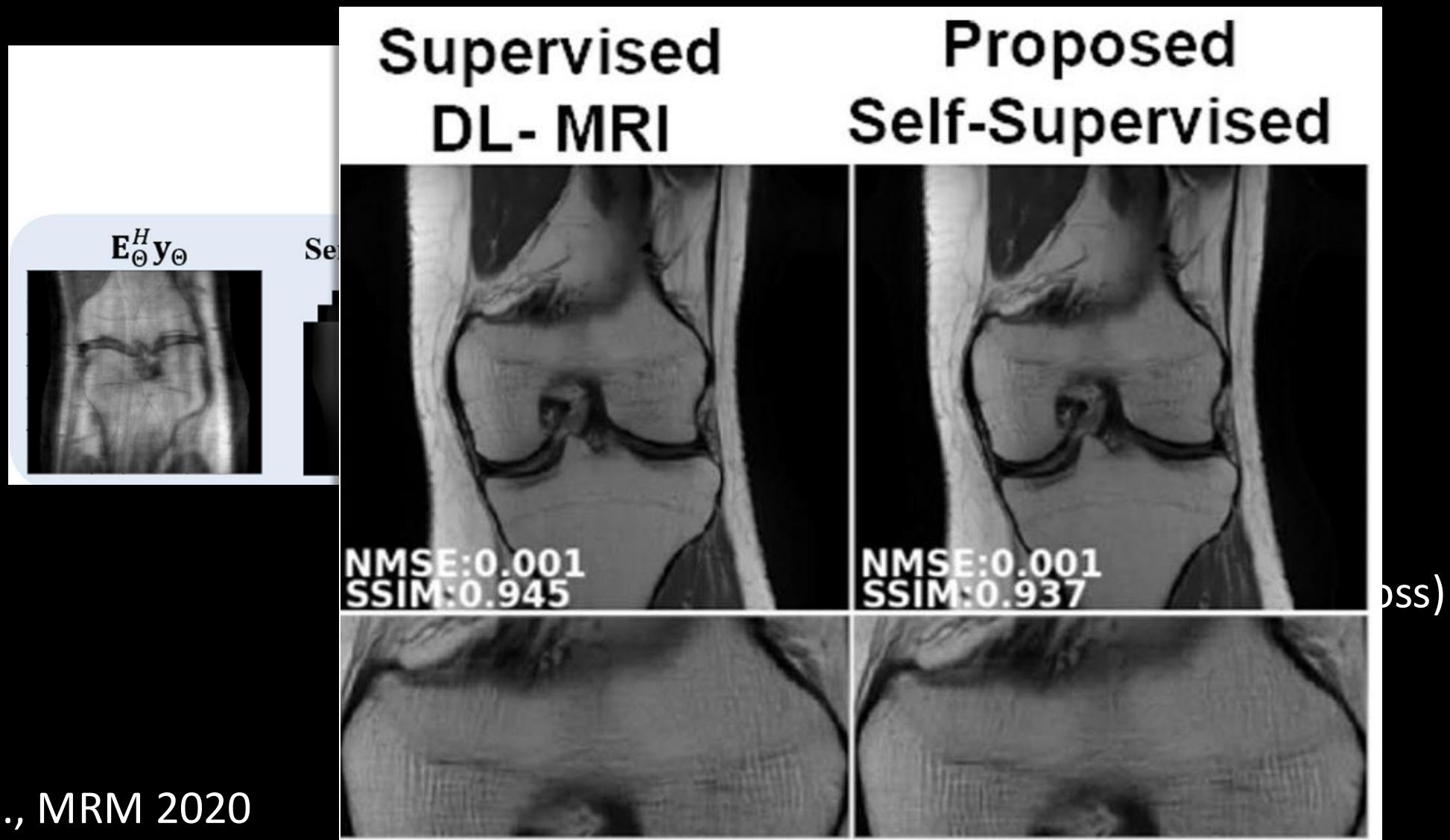


- ✗ Naïve use of Big Data can lead to biased results
- ✗ Error metrics - *blind* to the preprocessing

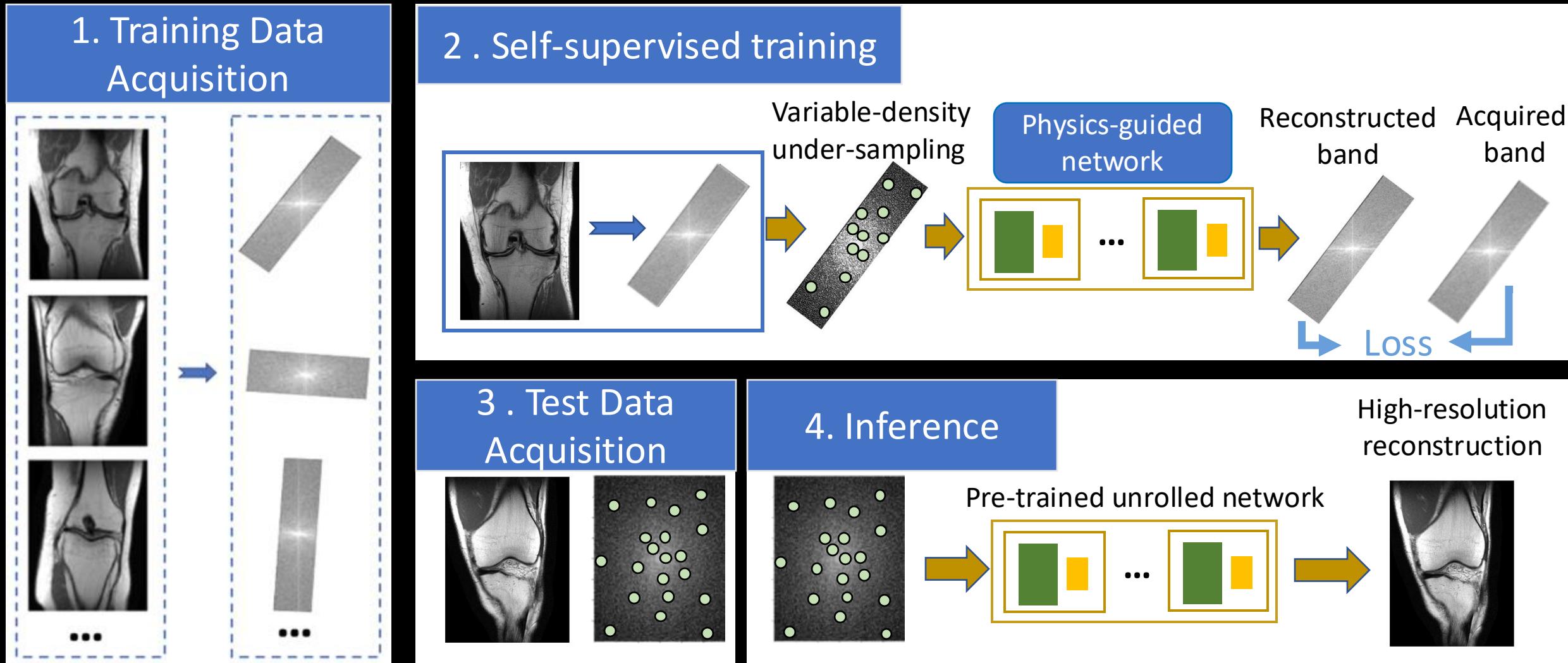
Shimron et al., *Implicit data crimes*, PNAS (2022)

Self-supervised MRI reconstruction

Deep learning: Self-supervised training



K-band: Fast Acquisition & Self-supervised Reconstruction

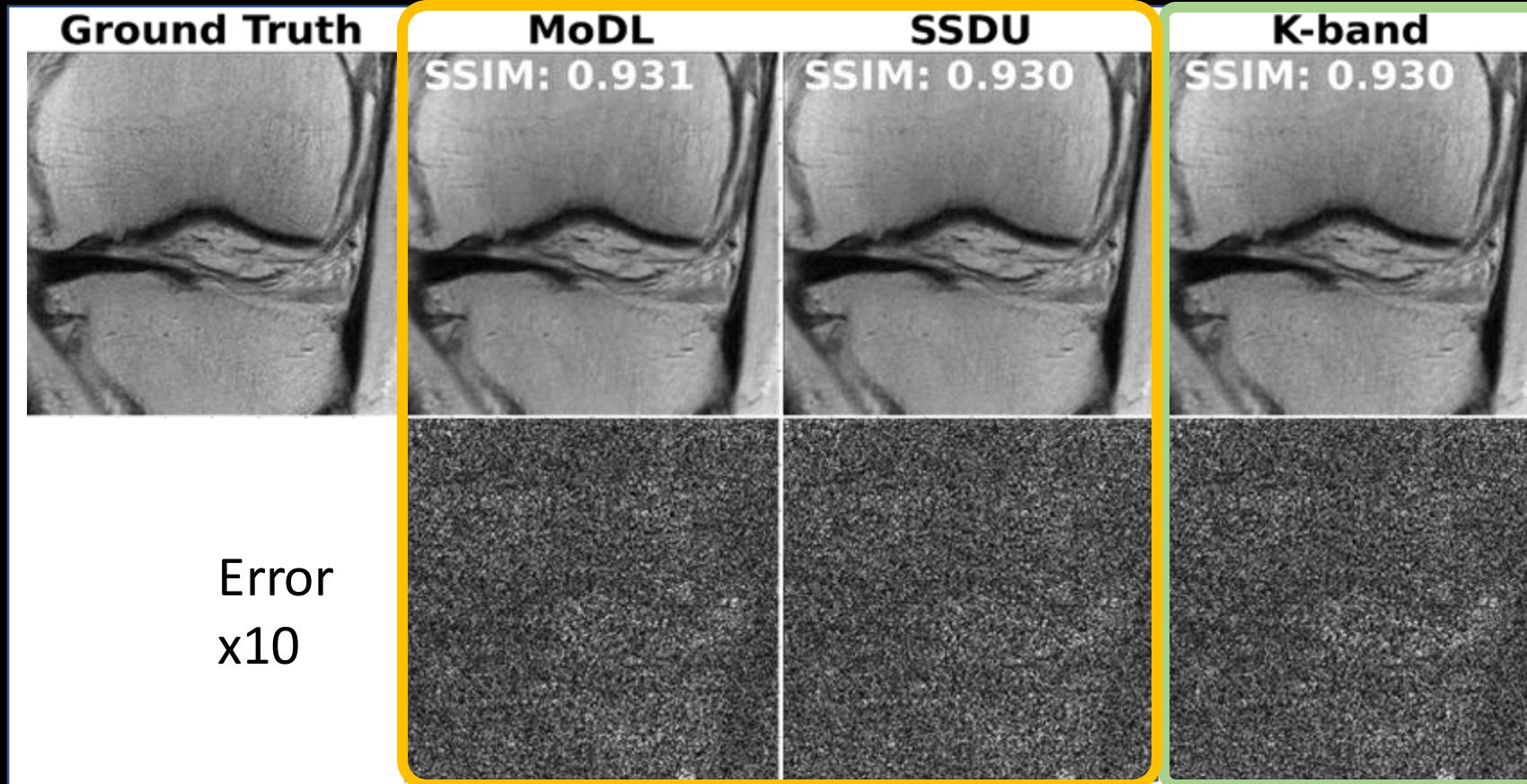


Wang et al., arXiv 2023, “k-band: self-supervised MRI reconstruction”

K-band: Fast Acquisition & Self-supervised Reconstruction

Trained on high-res
data

Trained on data with 4x
lower resolution



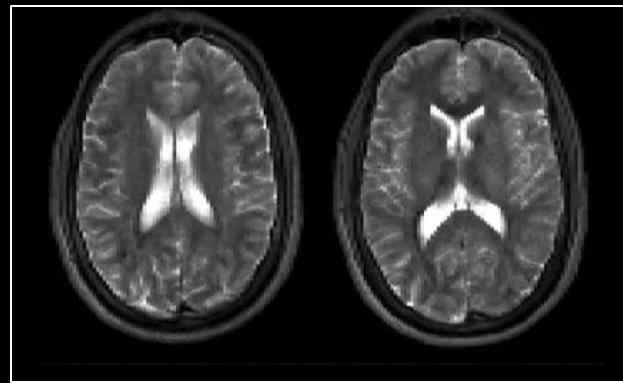
Mathematical convergence proof – in the paper

Wang et al., arXiv 2023, "k-band: self-supervised MRI reconstruction"

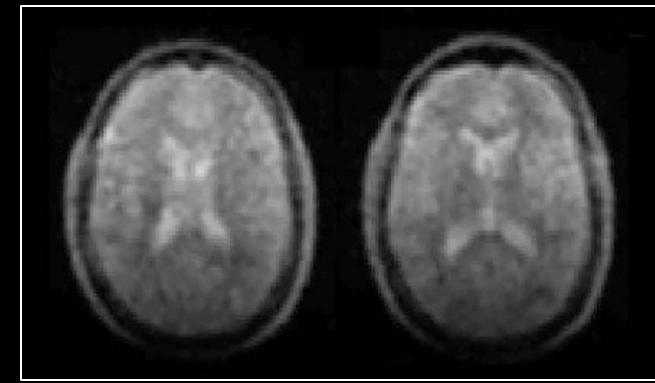
Reconstruction for low-field MRI

Low-field MRI

High-field MRI



Low-field MRI



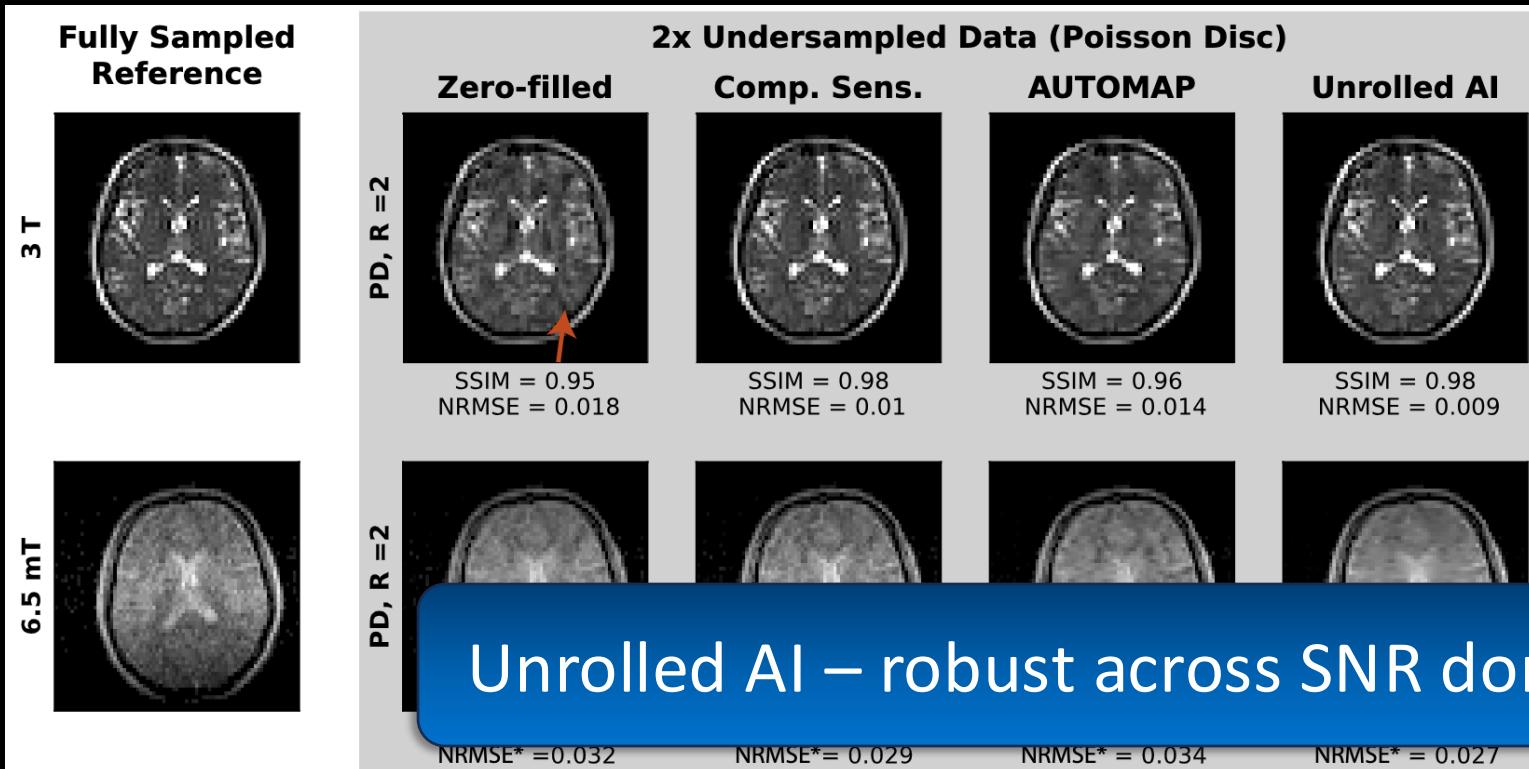
Low SNR

Coming soon
on arXiv

AI for low-field MRI



Unrolled networks provide high-quality recons

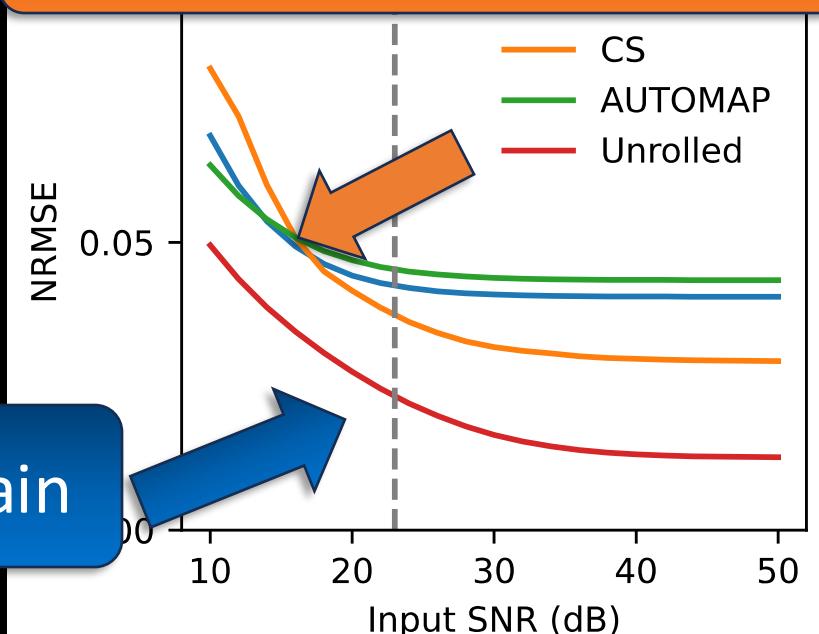


Unrolled AI – robust across SNR domain



David Waddington Matthew Rosen

CS & AUTOMAP switch places



Waddington, Shimron, et al., ISMRM 2023



Open positions - Med AI & MRI lab



Technion



Team



Join us



Thank You