

formula to find the critical speed!

$\gamma_R$  can be neglected  $\rightarrow$  because we have a relation that as the  $\tan\alpha$  of the speed! becomes very little!

For  $\rightarrow$  UNDERSTEERING car  $\rightarrow$  no critical speed

$\downarrow$  OVERSTEERING CAR ( $N_B < 0$ )  $\rightarrow$  we have a positive value for  $-N_B mV$

There is a CRITICAL SPEED

slide 29  $\rightarrow$  shows that a OS vehicle increasing the speed improves the ~~reports~~  $\rightarrow$  ability to respond to the change of S faster in control!  $\downarrow$  problem, reach critical speed in a very sensitive zone of the steering wheel!

$\curvearrowleft$  In VS is the opposite, but for average velocity all the vehicles are similar!

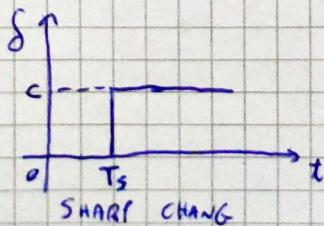
the car starts to turn more of how you expect at a certain speed

### TRANSIENT RESPONSE

before we assumed that the radius of the corner was constant

$\rightarrow$  the only way to go out from an UNSTABLE regime is to correct the trajectory acting on the steering wheel.

Now! what happens with a step-wise change in the steering wheel?



markedly large from  $S=0$  to  $S=c$  we obtain a low/flat transient that lead to our vehicle.

Why happens in the transient region?

{  
Velocity  $\rightarrow$  we see "noise"  
Acceleration  $\rightarrow$  notice that is not a step  
}  $\Rightarrow$  NOT A STEP as the input

$\rightarrow$  at the exam can ask the plot of slide 36, argue for a short time change

{ Time constant of initial velocity ( $T_1$ ) tells that if we set a short  $T_1$  (fast response) we have high value of  $N_p$  and so we need an OS vehicle  
↳ depend also on the mass of the vehicle!

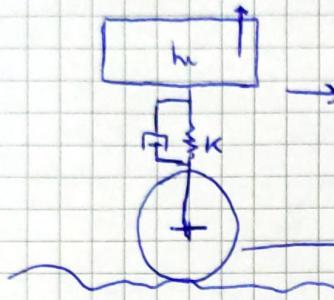
- for larger velocity the  $T_1$  is higher, the response is slower!

{  
↳ depending ratio and how it change the plot increasing it!  
↳ increasing it we try to avoid the overshoot!

## VERTICAL DYNAMICS

- Allow to predict the effect of the road impacting the comfort and the vertical tire contact

→ Road with holes, bump → vehicle must ABSORB all the energy thanks to the suspension



We are interested in the vertical effect

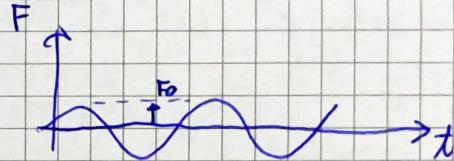
also the tire can be modelled as a



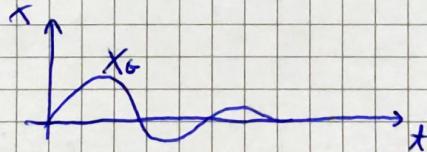
(NB) In the QUARTER CAR MODEL the mass M of the vehicle is =  $\frac{M_{\text{VEHICLE}}}{4}$

## OSCILLATOR THEORY : 1 DOF

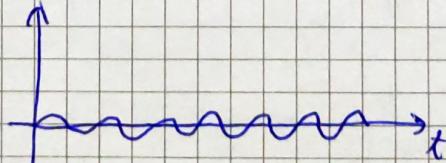
is applied an harmonic load



- GENERAL INTEGRAL  
input for initial  
truncating



- PARTICULAR INTEGRAL



for slide 8 rewrite the plot + the diff equation!

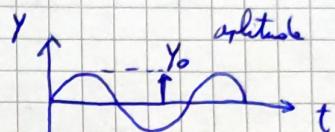
slide 9 → remember the  $X$  formula!  
↓  
amplitude of the oscillation...

slide 12 → invert the TRANSMISSIBILITY

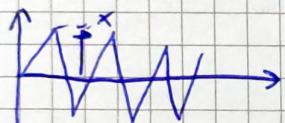
$F_0 \rightarrow$  static force

slide 13 →

influence a displacement on  $y$



the displacement of  $x$  depend on the ratio between  $K, c, m$



slide 14 → remember the plot → for 0 and 2 we have 1,  
for 1 we have Resonance

$\frac{X}{P}$  displacement between ) the car body and the ground  
after 2 is a good behavior

with  $\omega_n > 0 \rightarrow \left(\frac{\omega}{\omega_n}\right)^2 \uparrow$  and we have a very confortable  
car (kinked in the right part of the plot)

car with a very high  $m$ , but we care for longitudinal and  
lateral dynamics.

So the idea is to get a SOFT suspension!

slide 15  $\rightarrow$  the  $K$  of the model is not the  $\text{real } K$  of the real car!

### QUARTER CAR MODEL

Just represent the shock in the front of a vehicle

$\rightarrow$  NB formula to get the 2 masses! (different approach)

slide 19  $\rightarrow$  better to have low damping { but very dangerous  
near in the RESONANCE region

for different frequencies diff situation for the passenger!

slide 22: a real DAMPER is not LINEAR

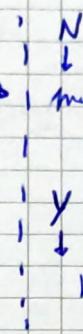
~~With~~ we want low force in bump and high force in rebound to avoid that the wheel ~~will~~ detach from the ground!

## FORCE MOMENT AND G-G DIAGRAMS

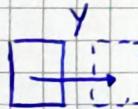
Tools to showing the effect of lateral dynamics of a vehicle!

### FORCE moment Plot

start from  $C_w$   $\Rightarrow$  max torque that you can give in the vertical direction  
 consider to  $w$  (weight)  $\Rightarrow$  how free the vehicle goes in  $y$  direction  
 $\ell$  (wheel base)



$N$  and  $\gamma$  plotted in the  $n\gamma$  plot



$\beta$  is the damping of the body...

slide 6  $\rightarrow$  in point P we have a lot of lateral acceleration but also a small angular acceleration

point T is the next point to continue to rotate

the position of the point P tell me if the vehicle is stable or not stable!

point P below  $\rightarrow$  stable

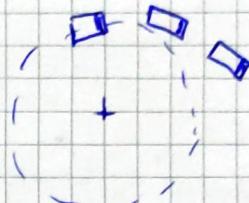
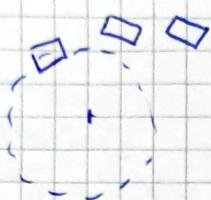
point P above  $\rightarrow$  unstable

TERMINAL DRIFT

SPIN

PLow

(19)



DANGEROUS

### G-G diagrams

helpful to understand the max lateral and longitudinal  
acceleration capabilities!  
(must be plotted for different speed)

can be parameterize with  $\delta$  (steering angle) and  $T_p$  (pressure of  
braking pedal) and  $T_o$  (throttle pedal)

slide 11  $\rightarrow$  plot for a specific velocity!

# SUSPENSION

## KINEMATICS

Represent rotation of body w.r.t. wheel

INSTANTANEOUS CENTER (IC) = body w.r.t. the wheel, the moment  
is on the intersection of the two walls  
in this four bar linkage

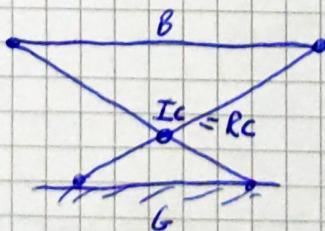
Knowing the IC we can delete the linkage and connect the wheel  
to a single point (IC)

ASSUMPTION  $\rightarrow$  IC stay in the same position for the entire suspension  
movement

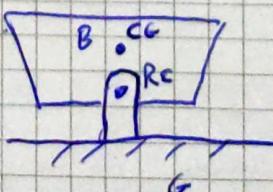
It is common to define two IC  $\xrightarrow{\text{FRONT view}}$  OBTAINED THE  
 $\xrightarrow{\text{SIDE VIEW}}$  INSTANT AXIS

ROLL CENTER HEIGHT (RC) =

RC  $\rightarrow$  instantaneous center of B w.r.t. G  
body ground



glide  $\rightarrow$



$\rightarrow$  Knowing RC and the CG of the vehicle we can understand the tilt  
during curve

higher is the distance between RG and CG  
the higher is the rolling behavior

slide 6 → if the IC is near the wheel the corner will change a lot during the suspension movement

$\text{SCRVB}$  → is the lateral movement of the tire during the suspension movement  
?1

if IC stay at the ground level  $\rightarrow \text{SCRVB} = 0$

### ANTI DIVE - ANTI SQUAT (Anti LIFT)

Considering the IC in the side view, deplacating the position of the IC respect to the center of the tire we have anti dive - anti squat effect

Anti-LIFT  $\rightarrow$  IC higher than the center of the tire!

NB during the brake  $\rightarrow$  no dive in ground

### Front Suspension

interesting parameters due to the steering system!

CASTER ANGLE related to the mechanical trail

 the axis we have the rotation due to the steer our choice!

higher is the mechanical TRAIL and easier the tire will align automatically to the direction of the car!

(8-12°)

KING PIN related to the SERVO



control where the scrub radius is! → obtaining positive or negative value

## CAMBER

angle of the tire respect to the vertical line



TOE OUT → help the handling

TOE IN → help for the stability

## TYPE OF SUSPENSION

MC PHERSON = allows to save space, the shock absorber is the (FRONT SUSPENSION) camber change during the work and the weight

DOUBLE WISHBONE = best possibility! quite expensive!

(A-ARM)  
(Front/rear/rear)

TRAILING ARM = we can't control the camber!  
(REAR SUSPENSION)

SEMI-TRAILING ARM → possibility to manage a little bit the camber but not used anymore

SWING AXLE = NOT USED ANYMORE, camber change a lot during the operation

H-ARM, tri-link front = used in jeep car or trucks

FIVE LINKS = similar to the double wishbone but with a different structure  
↓

but we can move the four hard points where we want!

control the camber, toe in, toe out during the movement of the suspension  
NEED of computer simulation to optimise it!

PANHARD = still used in TRUCKS,

TORQUE TUBE = very simple, used in US car, etc in racing car!  
the diff. goes up and down!

NASCAR type = same that are NOT INDEPENDENT SUSPENSION!

DE DION = it is heavy! the diff. stay fixed!

WIST AXLE = super simplified! NOT USED ANYMORE